



Figure Q35.10



- areas of the Earth see a total eclipse, other areas see a partial eclipse, and most areas see no eclipse.
17. The display windows of some department stores are slanted slightly inward at the bottom. This is to decrease the glare from streetlights or the Sun, which would make it difficult for shoppers to see the display inside. Sketch a light ray reflecting off such a window to show how this technique works.

18. When two colors of light X and Y are sent through a glass prism, X is bent more than Y. Which color travels more slowly in the prism?
19. Why does the arc of a rainbow appear with red on top and violet on the bottom?
20. Under what conditions is a mirage formed? On a hot day, what are we seeing when we observe “water on the road”?

## PROBLEMS

1, 2, 3 = straightforward, intermediate, challenging ☐ = full solution available in the *Student Solutions Manual and Study Guide*

WEB = solution posted at <http://www.saunderscollege.com/physics/> = Computer useful in solving problem = Interactive Physics

☐ = paired numerical/symbolic problems

### Section 35.1 The Nature of Light

#### Section 35.2 Measurements of the Speed of Light

- The Apollo 11 astronauts set up a highly reflecting panel on the Moon's surface. The speed of light can be found by measuring the time it takes a laser beam to travel from Earth, reflect from the retroreflector, and return to Earth. If this interval is measured to be 2.51 s, what is the measured speed of light? Take the center-to-center distance from the Earth to the Moon to be  $3.84 \times 10^8$  m, and do not neglect the sizes of the Earth and the Moon.
- As a result of his observations, Roemer concluded that eclipses of Io by Jupiter were delayed by 22 min during a six-month period as the Earth moved from the point in its orbit where it is closest to Jupiter to the diametrically opposite point where it is farthest from Jupiter. Using  $1.50 \times 10^8$  km as the average radius of the Earth's orbit around the Sun, calculate the speed of light from these data.
- In an experiment to measure the speed of light using the apparatus of Fizeau (see Fig. 35.2), the distance between light source and mirror was 11.45 km and the wheel had 720 notches. The experimentally determined value of  $c$  was  $2.998 \times 10^8$  m/s. Calculate the minimum angular speed of the wheel for this experiment.
- Figure P35.4 shows an apparatus used to measure the speed distribution of gas molecules. It consists of two slotted rotating disks separated by a distance  $d$ , with the slots displaced by the angle  $\theta$ . Suppose that the speed of light is measured by sending a light beam from the left through this apparatus. (a) Show that a light beam will be seen in the detector (that is, will make it through both slots) only if its speed is given by  $c = \omega d / \theta$ , where  $\omega$  is the angular speed of the disks and  $\theta$  is measured in radians. (b) What is the measured speed of light if the distance between the two slotted rotating disks is 2.50 m, the slot in the second disk is displaced  $1/60$  of  $1^\circ$  from the slot in the first disk, and the disks are rotating at 555 rev/s?

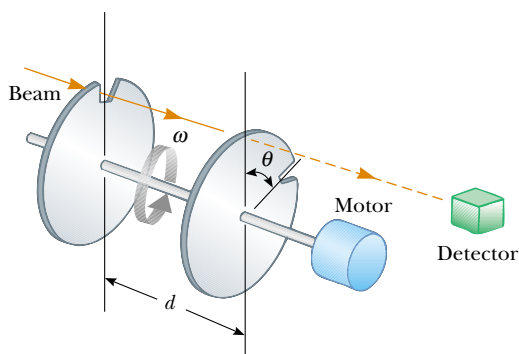


Figure P35.4

**Section 35.3 The Ray Approximation in Geometric Optics****Section 35.4 Reflection****Section 35.5 Refraction****Section 35.6 Huygens's Principle**

*Note:* In this section, if an index of refraction value is not given, refer to Table 35.1.

5. A narrow beam of sodium yellow light, with wavelength 589 nm in vacuum, is incident from air onto a smooth water surface at an angle  $\theta_1 = 35.0^\circ$ . Determine the angle of refraction  $\theta_2$  and the wavelength of the light in water.
6. The wavelength of red helium–neon laser light in air is 632.8 nm. (a) What is its frequency? (b) What is its wavelength in glass that has an index of refraction of 1.50? (c) What is its speed in the glass?
7. An underwater scuba diver sees the Sun at an apparent angle of  $45.0^\circ$  from the vertical. What is the actual direction of the Sun?
8. A laser beam is incident at an angle of  $30.0^\circ$  from the vertical onto a solution of corn syrup in water. If the beam is refracted to  $19.24^\circ$  from the vertical, (a) what is the index of refraction of the syrup solution? Suppose that the light is red, with a vacuum wavelength of 632.8 nm. Find its (b) wavelength, (c) frequency, and (d) speed in the solution.
9. Find the speed of light in (a) flint glass, (b) water, and (c) cubic zirconia.
10. A light ray initially in water enters a transparent substance at an angle of incidence of  $37.0^\circ$ , and the transmitted ray is refracted at an angle of  $25.0^\circ$ . Calculate the speed of light in the transparent substance.
11. A ray of light strikes a flat block of glass ( $n = 1.50$ ) of thickness 2.00 cm at an angle of  $30.0^\circ$  with the normal. Trace the light beam through the glass, and find the angles of incidence and refraction at each surface.
12. Light of wavelength 436 nm in air enters a fishbowl filled with water and then exits through the crown glass wall of the container. What is the wavelength of the light (a) in the water and (b) in the glass?

13. An opaque cylindrical tank with an open top has a diameter of 3.00 m and is completely filled with water. When the setting Sun reaches an angle of  $28.0^\circ$  above the horizon, sunlight ceases to illuminate any part of the bottom of the tank. How deep is the tank?
14. The angle between the two mirrors illustrated in Figure P35.14 is a right angle. The beam of light in the vertical plane  $P$  strikes mirror 1 as shown. (a) Determine the distance that the reflected light beam travels before striking mirror 2. (b) In what direction does the light beam travel after being reflected from mirror 2?

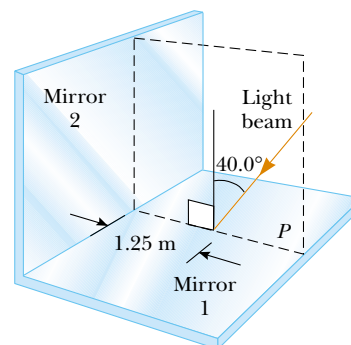


Figure P35.14

15. How many times will the incident beam shown in Figure P35.15 be reflected by each of the parallel mirrors?

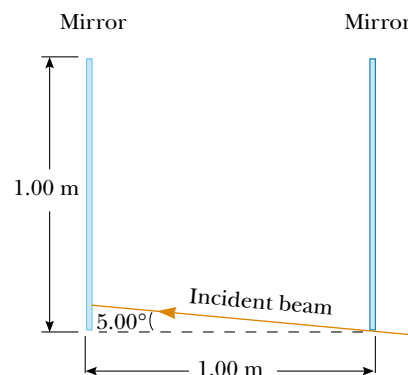
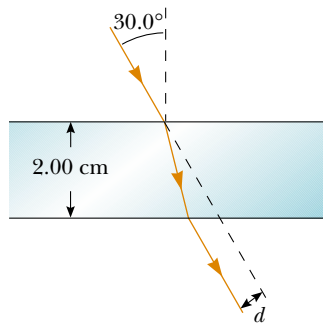
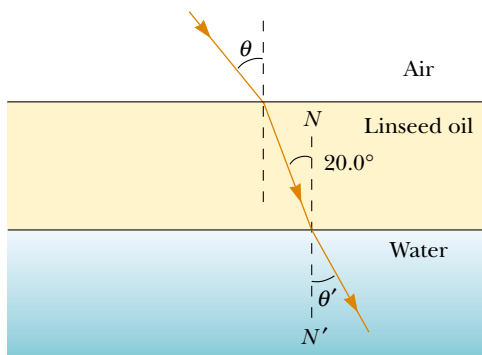


Figure P35.15

16. When the light illustrated in Figure P35.16 passes through the glass block, it is shifted laterally by the distance  $d$ . If  $n = 1.50$ , what is the value of  $d$ ?
17. Find the time required for the light to pass through the glass block described in Problem 16.
18. The light beam shown in Figure P35.18 makes an angle of  $20.0^\circ$  with the normal line  $NN'$  in the linseed oil. Determine the angles  $\theta$  and  $\theta'$ . (The index of refraction for linseed oil is 1.48.)

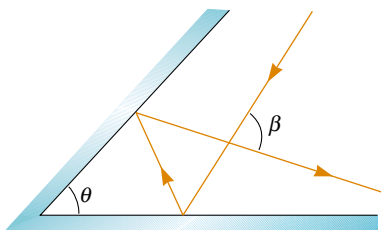


**Figure P35.16** Problems 16 and 17.



**Figure P35.18**

19. Two light pulses are emitted simultaneously from a source. Both pulses travel to a detector, but one first passes through 6.20 m of ice. Determine the difference in the pulses' times of arrival at the detector.
20. When you look through a window, by how much time is the light you see delayed by having to go through glass instead of air? Make an order-of-magnitude estimate on the basis of data you specify. By how many wavelengths is it delayed?
21. Light passes from air into flint glass. (a) What angle of incidence must the light have if the component of its velocity perpendicular to the interface is to remain constant? (b) Can the component of velocity parallel to the interface remain constant during refraction?
22. The reflecting surfaces of two intersecting flat mirrors are at an angle of  $\theta$  ( $0^\circ < \theta < 90^\circ$ ), as shown in Figure



**Figure P35.22**

P35.22. If a light ray strikes the horizontal mirror, show that the emerging ray will intersect the incident ray at an angle of  $\beta = 180^\circ - 2\theta$ .

23. A light ray enters the atmosphere of a planet and descends vertically 20.0 km to the surface. The index of refraction where the light enters the atmosphere is 1.000, and it increases linearly to the surface where it has a value of 1.005. (a) How long does it take the ray to traverse this path? (b) Compare this to the time it takes in the absence of an atmosphere.
24. A light ray enters the atmosphere of a planet and descends vertically to the surface a distance  $h$ . The index of refraction where the light enters the atmosphere is 1.000, and it increases linearly to the surface where it has a value of  $n$ . (a) How long does it take the ray to traverse this path? (b) Compare this to the time it takes in the absence of an atmosphere.

### Section 35.7 Dispersion and Prisms

25. A narrow white light beam is incident on a block of fused quartz at an angle of  $30.0^\circ$ . Find the angular width of the light beam inside the quartz.
26. A ray of light strikes the midpoint of one face of an equiangular glass prism ( $n = 1.50$ ) at an angle of incidence of  $30.0^\circ$ . Trace the path of the light ray through the glass, and find the angles of incidence and refraction at each surface.
27. A prism that has an apex angle of  $50.0^\circ$  is made of cubic zirconia, with  $n = 2.20$ . What is its angle of minimum deviation?
28. Light with a wavelength of 700 nm is incident on the face of a fused quartz prism at an angle of  $75.0^\circ$  (with respect to the normal to the surface). The apex angle of the prism is  $60.0^\circ$ . Using the value of  $n$  from Figure 35.20, calculate the angle (a) of refraction at this first surface, (b) of incidence at the second surface, (c) of refraction at the second surface, and (d) between the incident and emerging rays.
29. The index of refraction for violet light in silica flint glass is 1.66, and that for red light is 1.62. What is the angular dispersion of visible light passing through a prism of apex angle  $60.0^\circ$  if the angle of incidence is  $50.0^\circ$ ? (See Fig. P35.29.)
30. Show that if the apex angle  $\Phi$  of a prism is small, an approximate value for the angle of minimum deviation is  $\delta_{\min} = (n - 1)\Phi$ .
31. A triangular glass prism with an apex angle of  $\Phi = 60.0^\circ$  has an index of refraction  $n = 1.50$  (Fig. P35.31). What is the smallest angle of incidence  $\theta_1$  for which a light ray can emerge from the other side?
32. A triangular glass prism with an apex angle of  $\Phi$  has an index of refraction  $n$  (Fig. P35.31). What is the smallest angle of incidence  $\theta_1$  for which a light ray can emerge from the other side?

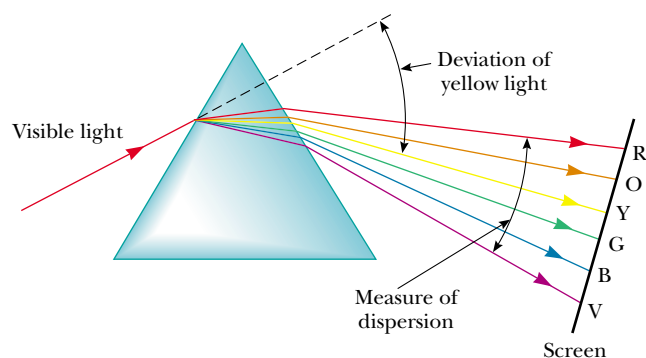


Figure P35.29

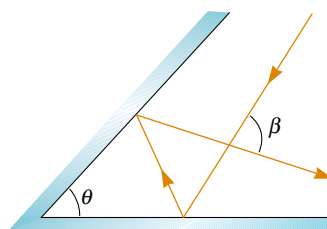


Figure P35.31

33. An experimental apparatus includes a prism made of sodium chloride. The angle of minimum deviation for light of wavelength 589 nm is to be  $10.0^\circ$ . What is the required apex angle of the prism?
34. A triangular glass prism with an apex angle of  $60.0^\circ$  has an index of refraction of 1.50. (a) Show that if its angle of incidence on the first surface is  $\theta_1 = 48.6^\circ$ , light will pass symmetrically through the prism, as shown in Figure 35.26. (b) Find the angle of deviation  $\delta_{\min}$  for  $\theta_1 = 48.6^\circ$ . (c) Find the angle of deviation if the angle of incidence on the first surface is  $45.6^\circ$ . (d) Find the angle of deviation if  $\theta_1 = 51.6^\circ$ .

### Section 35.8 Total Internal Reflection

35. For 589-nm light, calculate the critical angle for the following materials surrounded by air: (a) diamond, (b) flint glass, and (c) ice.
36. Repeat Problem 35 for the situation in which the materials are surrounded by water.
37. Consider a common mirage formed by super-heated air just above a roadway. A truck driver whose eyes are 2.00 m above the road, where  $n = 1.0003$ , looks forward. She perceives the illusion of a patch of water ahead on the road, where her line of sight makes an angle of  $1.20^\circ$  below the horizontal. Find the index of refraction of the air just above the road surface. (*Hint:* Treat this as a problem in total internal reflection.)
38. Determine the maximum angle  $\theta$  for which the light

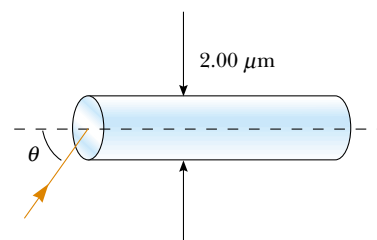


Figure P35.38

- rays incident on the end of the pipe shown in Figure P35.38 are subject to total internal reflection along the walls of the pipe. Assume that the pipe has an index of refraction of 1.36 and the outside medium is air.
39. A glass fiber ( $n = 1.50$ ) is submerged in water ( $n = 1.33$ ). What is the critical angle for light to stay inside the optical fiber?
40. A glass cube is placed on a newspaper, which rests on a table. A person reads all of the words the cube covers, through all of one vertical side. Determine the maximum possible index of refraction of the glass.
41. A large Lucite cube ( $n = 1.59$ ) has a small air bubble (a defect in the casting process) below one surface. When a penny (diameter, 1.90 cm) is placed directly over the bubble on the outside of the cube, one cannot see the bubble by looking down into the cube at any angle. However, when a dime (diameter, 1.75 cm) is placed directly over it, one can see the bubble by looking down into the cube. What is the range of the possible depths of the air bubble beneath the surface?
42. A room contains air in which the speed of sound is 343 m/s. The walls of the room are made of concrete, in which the speed of sound is 1850 m/s. (a) Find the critical angle for total internal reflection of sound at the concrete-air boundary. (b) In which medium must the sound be traveling to undergo total internal reflection? (c) "A bare concrete wall is a highly efficient mirror for sound." Give evidence for or against this statement.
43. In about 1965, engineers at the Toro Company invented a gasoline gauge for small engines, diagrammed in Figure P35.43. The gauge has no moving parts. It consists of a flat slab of transparent plastic fitting vertically into a slot in the cap on the gas tank. None of the plastic has a reflective coating. The plastic projects from the horizontal top down nearly to the bottom of the opaque tank. Its lower edge is cut with facets making angles of  $45^\circ$  with the horizontal. A lawnmower operator looks down from above and sees a boundary between bright and dark on the gauge. The location of the boundary, across the width of the plastic, indicates the quantity of gasoline in the tank. Explain how the gauge works. Explain the design requirements, if any, for the index of refraction of the plastic.

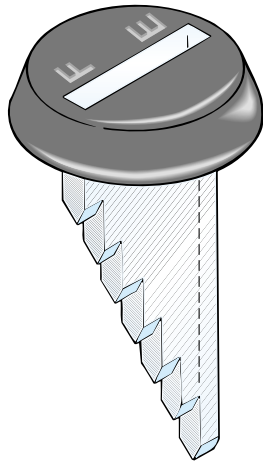


Figure P35.43

(Optional)

**Section 35.9 Fermat's Principle**

44. The shoreline of a lake runs from east to west. A swimmer gets into trouble 20.0 m out from shore and 26.0 m to the east of a lifeguard, whose station is 16.0 m in from the shoreline. The lifeguard takes a negligible amount of time to accelerate. He can run at 7.00 m/s and swim at 1.40 m/s. To reach the swimmer as quickly as possible, in what direction should the lifeguard start running? You will need to solve a transcendental equation numerically.

**ADDITIONAL PROBLEMS**

45. A narrow beam of light is incident from air onto a glass surface with an index of refraction of 1.56. Find the angle of incidence for which the corresponding angle of refraction is one half the angle of incidence. (*Hint:* You might want to use the trigonometric identity  $\sin 2\theta = 2 \sin \theta \cos \theta$ .)
46. (a) Consider a horizontal interface between air above and glass with an index of 1.55 below. Draw a light ray incident from the air at an angle of incidence of  $30.0^\circ$ . Determine the angles of the reflected and refracted rays and show them on the diagram. (b) Suppose instead that the light ray is incident from the glass at an angle of incidence of  $30.0^\circ$ . Determine the angles of the reflected and refracted rays and show all three rays on a new diagram. (c) For rays incident from the air onto the air–glass surface, determine and tabulate the angles of reflection and refraction for all the angles of incidence at  $10.0^\circ$  intervals from  $0$  to  $90.0^\circ$ . (d) Do the same for light rays traveling up to the interface through the glass.
47. A small underwater pool light is 1.00 m below the surface. The light emerging from the water forms a circle
- on the water's surface. What is the diameter of this circle?
48. One technique for measuring the angle of a prism is shown in Figure P35.48. A parallel beam of light is directed on the angle so that the beam reflects from opposite sides. Show that the angular separation of the two beams is given by  $B = 2A$ .
49. The walls of a prison cell are perpendicular to the four cardinal compass directions. On the first day of spring, light from the rising Sun enters a rectangular window in the eastern wall. The light traverses 2.37 m horizontally to shine perpendicularly on the wall opposite the window. A young prisoner observes the patch of light moving across this western wall and for the first time forms his own understanding of the rotation of the Earth. (a) With what speed does the illuminated rectangle move? (b) The prisoner holds a small square mirror flat against the wall at one corner of the rectangle of light. The mirror reflects light back to a spot on the eastern wall close beside the window. How fast does the smaller square of light move across that wall? (c) Seen from a latitude of  $40.0^\circ$  north, the rising Sun moves through the sky along a line making a  $50.0^\circ$  angle with the southeastern horizon. In what direction does the rectangular patch of light on the western wall of the prisoner's cell move? (d) In what direction does the smaller square of light on the eastern wall move?
50. The laws of refraction and reflection are the same for sound as for light. The speed of sound in air is 340 m/s, and that of sound in water is 1 510 m/s. If a sound wave approaches a plane water surface at an angle of incidence of  $12.0^\circ$ , what is the angle of refraction?
51. Cold sodium atoms (near absolute zero) in a state called a *Bose–Einstein condensate* can slow the speed of light from its normally high value to a speed approaching that of an automobile in a city. The speed of light in one such medium was recorded as 61.15 km/h. (a) Find the index of refraction of this medium. (b) What is the critical angle for total internal reflection if the condensate is surrounded by vacuum?
52. A narrow beam of white light is incident at  $25.0^\circ$  onto a slab of heavy flint glass 5.00 cm thick. The indices of

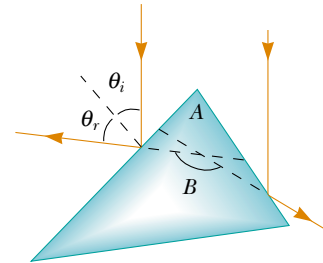


Figure P35.48



refraction of the glass at wavelengths of 400 nm and 700 nm are 1.689 and 1.642, respectively. Find the width of the visible beam as it emerges from the slab.

- 53.** A hiker stands on a mountain peak near sunset and observes a rainbow caused by water droplets in the air 8.00 km away. The valley is 2.00 km below the mountain peak and entirely flat. What fraction of the complete circular arc of the rainbow is visible to the hiker? (See Fig. 35.25.)
- 54.** A fish is at a depth  $d$  under water. Take the index of refraction of water as  $4/3$ . Show that when the fish is viewed at an angle of refraction  $\theta_1$ , the apparent depth  $z$  of the fish is

$$z = \frac{3d \cos \theta_1}{\sqrt{7 + 9 \cos^2 \theta_1}}$$

- WEB 55.** A laser beam strikes one end of a slab of material, as shown in Figure P35.55. The index of refraction of the slab is 1.48. Determine the number of internal reflections of the beam before it emerges from the opposite end of the slab.

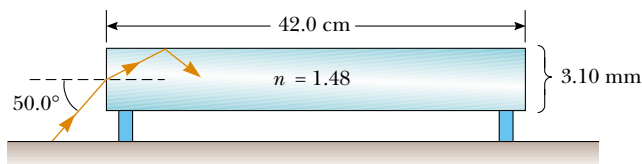


Figure P35.55

- 56.** When light is normally incident on the interface between two transparent optical media, the intensity of the reflected light is given by the expression

$$S'_1 = \left( \frac{n_2 - n_1}{n_2 + n_1} \right)^2 S_1$$

In this equation,  $S_1$  represents the average magnitude of the Poynting vector in the incident light (the incident intensity),  $S'_1$  is the reflected intensity, and  $n_1$  and  $n_2$  are the refractive indices of the two media. (a) What fraction of the incident intensity is reflected for 589-nm light normally incident on an interface between air and crown glass? (b) In part (a), does it matter whether the light is in the air or in the glass as it strikes the interface? (c) A Bose–Einstein condensate (see Problem 51) has an index of refraction of  $1.76 \times 10^7$ . Find the percent reflection for light falling perpendicularly on its surface. What would the condensate look like?

- 57.** Refer to Problem 56 for a description of the reflected intensity of light normally incident on an interface between two transparent media. (a) When light is normally incident on an interface between vacuum and a transparent medium of index  $n$ , show that the intensity  $S_2$  of the transmitted light is given by the expression

$S_2/S_1 = 4n/(n + 1)^2$ . (b) Light travels perpendicularly through a diamond slab, surrounded by air, with parallel surfaces of entry and exit. Apply the transmission fraction in part (a) to find the approximate overall transmission through the slab of diamond as a percentage. Ignore light reflected back and forth within the slab.

- 58.** This problem builds upon the results of Problems 56 and 57. Light travels perpendicularly through a diamond slab, surrounded by air, with parallel surfaces of entry and exit. What fraction of the incident intensity is the intensity of the transmitted light? Include the effects of light reflected back and forth inside the slab.
- 59.** The light beam shown in Figure P35.59 strikes surface 2 at the critical angle. Determine the angle of incidence,  $\theta_1$ .

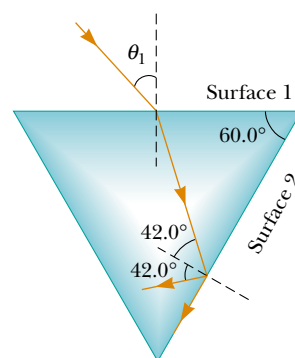


Figure P35.59

- 60.** A 4.00-m-long pole stands vertically in a lake having a depth of 2.00 m. When the Sun is  $40.0^\circ$  above the horizontal, determine the length of the pole's shadow on the bottom of the lake. Take the index of refraction for water to be 1.33.

- WEB 61.** A light ray of wavelength 589 nm is incident at an angle  $\theta$  on the top surface of a block of polystyrene, as shown in Figure P35.61. (a) Find the maximum value of  $\theta$  for which the refracted ray undergoes total internal reflection.

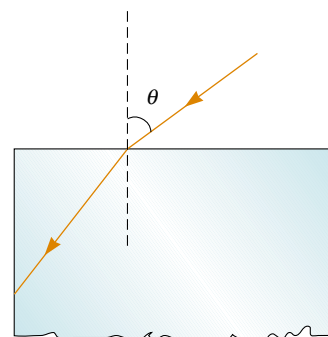


Figure P35.61

tion at the left vertical face of the block. Repeat the calculation for the case in which the polystyrene block is immersed in (b) water and (c) carbon disulfide.

62. A ray of light passes from air into water. For its deviation angle  $\delta = |\theta_1 - \theta_2|$  to be  $10.0^\circ$ , what must be its angle of incidence?

63. A shallow glass dish is 4.00 cm wide at the bottom, as shown in Figure P35.63. When an observer's eye is positioned as shown, the observer sees the edge of the bottom of the empty dish. When this dish is filled with water, the observer sees the center of the bottom of the dish. Find the height of the dish.

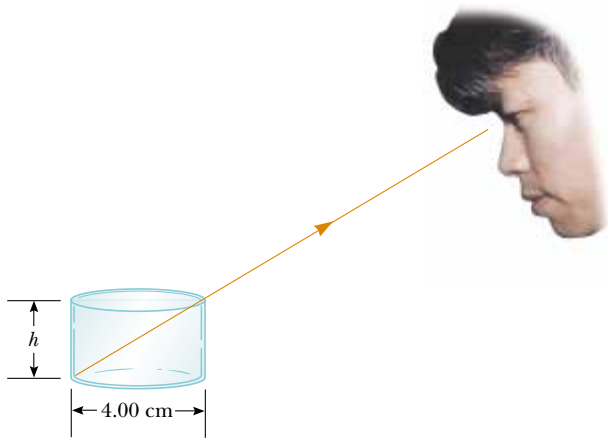


Figure P35.63

64. A material having an index of refraction  $n$  is surrounded by a vacuum and is in the shape of a quarter circle of radius  $R$  (Fig. P35.64). A light ray parallel to the base of the material is incident from the left at a distance of  $L$  above the base and emerges out of the material at the angle  $\theta$ . Determine an expression for  $\theta$ .

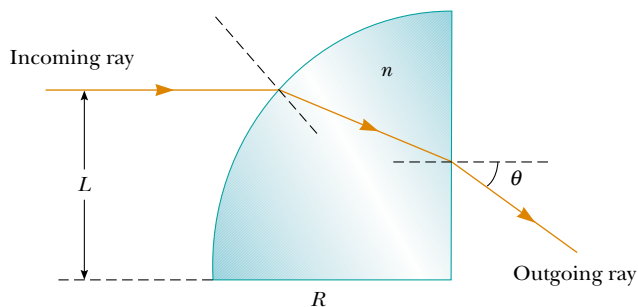


Figure P35.64

65. Derive the law of reflection (Eq. 35.2) from Fermat's principle of least time. (See the procedure outlined in Section 35.9 for the derivation of the law of refraction from Fermat's principle.)

66. A transparent cylinder of radius  $R = 2.00$  m has a mirrored surface on its right half, as shown in Figure P35.66. A light ray traveling in air is incident on the left side of the cylinder. The incident light ray and exiting light ray are parallel and  $d = 2.00$  m. Determine the index of refraction of the material.

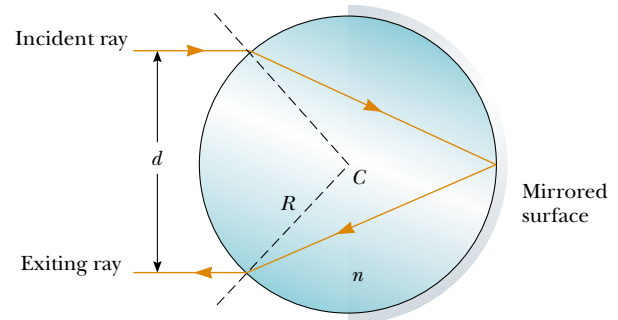


Figure P35.66

67. A. H. Pfund's method for measuring the index of refraction of glass is illustrated in Figure P35.67. One face of a slab of thickness  $t$  is painted white, and a small hole scraped clear at point  $P$  serves as a source of diverging rays when the slab is illuminated from below. Ray  $PBB'$  strikes the clear surface at the critical angle and is totally reflected, as are rays such as  $PCC'$ . Rays such as  $PAA'$  emerge from the clear surface. On the painted surface there appears a dark circle of diameter  $d$ , surrounded by an illuminated region, or halo. (a) Derive a formula for  $n$  in terms of the measured quantities  $d$  and  $t$ . (b) What is the diameter of the dark circle if  $n = 1.52$  for a slab 0.600 cm thick? (c) If white light is used, the critical angle depends on color caused by dispersion. Is the inner edge of the white halo tinged with red light or violet light? Explain.

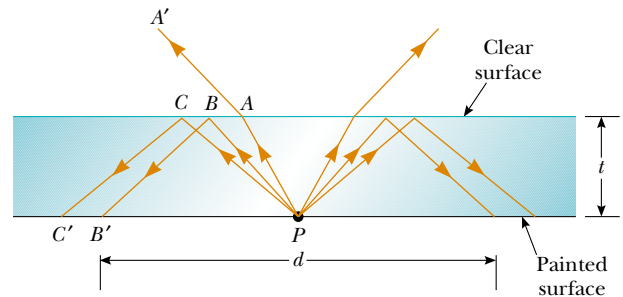


Figure P35.67

68. A light ray traveling in air is incident on one face of a right-angle prism with an index of refraction of  $n = 1.50$ , as shown in Figure P35.68, and the ray follows the path shown in the figure. If  $\theta = 60.0^\circ$  and the base of the prism is mirrored, what is the angle  $\phi$  made by

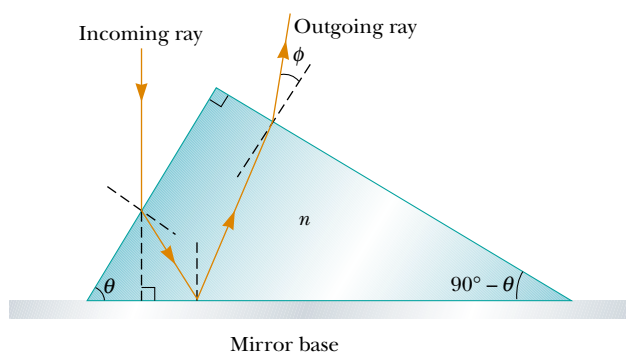


Figure P35.68

the outgoing ray with the normal to the right face of the prism?

69. A light ray enters a rectangular block of plastic at an angle of  $\theta_1 = 45.0^\circ$  and emerges at an angle of  $\theta_2 = 76.0^\circ$ , as shown in Figure P35.69. (a) Determine the index of refraction for the plastic. (b) If the light ray enters the plastic at a point  $L = 50.0$  cm from the bottom edge, how long does it take the light ray to travel through the plastic?
70. Students allow a narrow beam of laser light to strike a water surface. They arrange to measure the angle of refraction for selected angles of incidence and record the data shown in the accompanying table. Use the data to verify Snell's law of refraction by plotting the sine of the angle of incidence versus the sine of the angle of refraction.

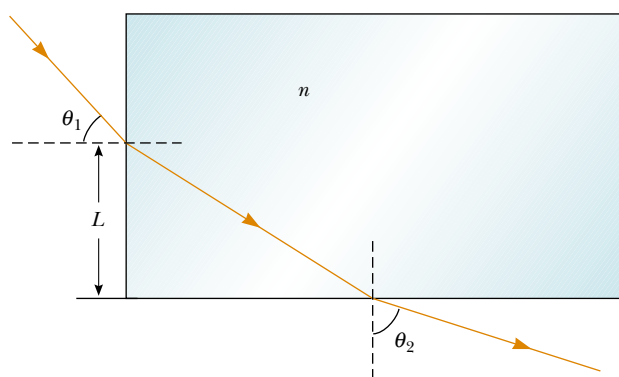


Figure P35.69

tion. Use the resulting plot to deduce the index of refraction of water.

Angle of Incidence (degrees)	Angle of Refraction (degrees)
10.0	7.5
20.0	15.1
30.0	22.3
40.0	28.7
50.0	35.2
60.0	40.3
70.0	45.3
80.0	47.7

## ANSWERS TO QUICK QUIZZES

- 35.1 Beams ② and ④ are reflected; beams ③ and ⑤ are refracted.
- 35.2 Fused quartz. An ideal lens would have an index of refraction that does not vary with wavelength so that all colors would be bent through the same angle by the lens. Of the three choices, fused quartz has the least variation in  $n$  across the visible spectrum. Thus, it is the best choice for a single-element lens.
- 35.3 The two rays on the right result from total internal reflection at the right face of the prism. Because all of the light in these rays is reflected (rather than partly refracted), these two rays are brightest. The light from the other three rays is divided into reflected and refracted parts.