

15. Circumference of a Circle and Area

Exercise 15.1

1. Question

The radius of a circle is 3.5 cm. Find the circumference and area of the circle.

Answer

Given that radius of the circle = 3.5 cm

We know that circumference of the circle = $2\pi r$

$$\Rightarrow \text{Circumference} = 2 \times \frac{22}{7} \times 3.5 = 22 \text{ cm}$$

Also, the area of a circle = πr^2

$$\Rightarrow \text{Area} = \frac{22}{7} \times 3.5 \times 3.5 = 38.5 \text{ cm}^2$$

2. Question

The circumference of a wheel is 44 m. find the area of the circle.

Answer

Given that circumference of the circle = 44 m

We know that circumference of the circle = $2\pi r$

$$\Rightarrow 2 \times \frac{22}{7} \times r = 44$$

$$\Rightarrow r = 7 \text{ m}$$

Also, the area of a circle = πr^2

$$\Rightarrow \text{Area} = \frac{22}{7} \times 7 \times 7 = 154 \text{ m}^2$$

3. Question

The radius of a semicircular plot is 21 m. Find its area and perimeter.

Answer



A semicircle is a half of the circle.

Given that radius of the semicircular plot = 21 m

To find the perimeter of the semicircular plot, we need to find the perimeter of the semicircle and add the diameter of the circle to it.

$$\text{Diameter} = AB = 2 \times \text{radius} = 2 \times 21 = 42 \text{ m}$$

We know that circumference of the circle = $2\pi r$

$$\Rightarrow \text{Perimeter of semicircle} = \pi r$$

$$\Rightarrow \text{Perimeter of semicircle} = \frac{22}{7} \times 21 = 66 \text{ m}$$

$$\text{Total perimeter of the semicircular plot} = 66 + 42 = 108 \text{ m}$$

Also, the area of a circle = πr^2

$$\Rightarrow \text{Area of semicircle} = \pi \frac{r^2}{2}$$

$$\Rightarrow \text{Area of semicircular plot} = \frac{22}{7 \times 2} \times 21 \times 21$$

$$\Rightarrow \text{Area of semicircular plot} = 693 \text{ m}^2$$

4. Question

A scooter wheel makes 100 revolutions in covering a distance of 88 m. Find the radius of the wheel.

Answer

Distance travelled by the wheel of the scooter = 88 m in 100 revolutions

$$\text{Distance travelled in 1 revolution} = \frac{88}{100} \text{ m} = 88 \text{ cm}$$

Distance travelled in 1 revolution of a wheel = circumference of the wheel

We know that circumference of the circle = $2\pi r$

$$\Rightarrow 2 \times \frac{22}{7} \times r = 88$$

$$\Rightarrow r = 14 \text{ cm}$$

5. Question

The area of a circular plate is 154 cm^2 . Find its circumference.

Answer

Given that the area of a circle = 154 cm^2

We know that the area of a circle = πr^2

$$\Rightarrow \frac{22}{7} \times r \times r = 154 \text{ cm}^2$$

$$\Rightarrow r = 7 \text{ cm}$$

Also, the circumference of the circle = $2\pi r$

$$\Rightarrow \text{Circumference} = 2 \times \frac{22}{7} \times 7 = 44 \text{ cm}$$

6. Question

The circumference of a circle is equal to perimeter of a square. If area of the square is 484 m^2 , then find the area of the circle.

Answer

Given area of the square = 484 m^2

We know that area of the square = $(\text{Side})^2$

$$\Rightarrow (\text{Side})^2 = 484$$

$$\Rightarrow \text{side} = 22 \text{ m}$$

Also, given that circumference of a circle = perimeter of a square

We know that circumference of the circle = $2\pi r$

And the perimeter of a square = $4 \times \text{length of the side}$

$$\Rightarrow \text{Perimeter of square} = 4 \times 22 = 88 \text{ m}$$

$$\Rightarrow \text{Circumference of circle} = 88 \text{ m}$$

$$\Rightarrow 2 \times \frac{22}{7} \times r = 88$$

$$\Rightarrow r = 14 \text{ m}$$

Also, the area of a circle = πr^2

$$\Rightarrow \text{Area} = \frac{22}{7} \times 14 \times 14 = 616 \text{ m}^2$$

7. Question

The cost of fencing a circular field at the rate of 24 per metre is 5280. The field is to be ploughed at the rate of 0.50 per m^2 . Find the cost of ploughing the field.

Answer

Given that cost of fencing a circular field at the rate of Rs 24 per meter = Rs 5280

Fencing takes place at the circumference of the circular field.

$$\text{So, the circumference of the field} = \frac{5280}{24} = 220 \text{ m}$$

We know that circumference of the circle = $2\pi r$

$$\Rightarrow 2 \times \frac{22}{7} \times r = 220$$

$$\Rightarrow r = 35 \text{ m (radius of the field)}$$

Also, the area of a circle = πr^2

$$\Rightarrow \text{Area of the field} = \frac{22}{7} \times 35 \times 35 = 3850 \text{ m}^2$$

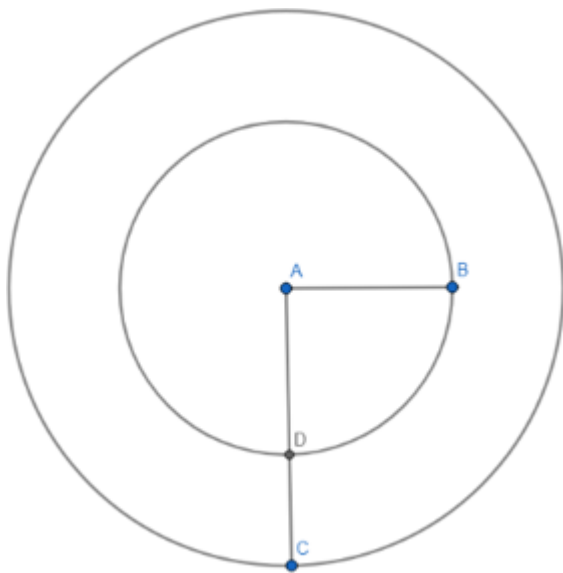
The field is to be ploughed at the rate of 0.50 per m^2 .

$$\text{Cost of ploughing the field} = 3850 \times 0.50 = \text{Rs } 1925$$

8. Question

The radius of a circular grass field is 35 m. There is a 7 m wide path all around it. Find the area of the path.

Answer



Given: Radius of the smaller circle $AB = 35$ m

Also, $CD = 7$ m

$\Rightarrow$ Radius of the larger circle $AC = AD + CD = 35 + 7 = 42$ m

Area of the path = Area of the larger circle - area of the smaller circle

$\because$ The area of a circle $= \pi r^2$

$\Rightarrow$ Area of the path $= \pi R^2 - \pi r^2$

$\Rightarrow$ Area of the path $= \frac{22}{7} (R^2 - r^2)$

$\Rightarrow$ Area of the path $= \frac{22}{7} (42^2 - 35^2)$

Using $(a+b)(a-b) = a^2 - b^2$

$\Rightarrow$ Area of the path $= \frac{22}{7} (42 - 35)(42 + 35)$

$\Rightarrow$ Area of the path $= \frac{22}{7} (7)(77)$

$\Rightarrow$ Area of the path $= 22 \times 77 = 1694 \text{ m}^2$

9. Question

The area enclosed between two concentric circles is:

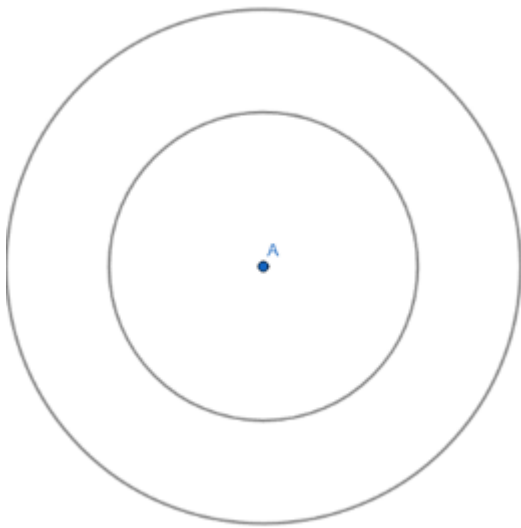
A. πr^2

B. $\pi(R + r)(R - r)$

C. $\pi(R^2 - r)$

D. None of these

Answer



Let the radius of the smaller circle be r and radius of the larger circle be R .

The area enclosed between two concentric circles = Area of the larger circle
– area of the smaller circle

$\therefore$ The area of a circle = πr^2

$\Rightarrow$ Required area = $\pi R^2 - \pi r^2$

$\Rightarrow$ Required area = $\pi (R^2 - r^2)$

Using $(a+b)(a-b) = a^2 - b^2$

$\Rightarrow$ Required area = $\pi (R+r)(R-r)$

10. Question

The radii of two concentric circles are 4 cm and 3 cm respectively. The area enclosed by the two circles is:

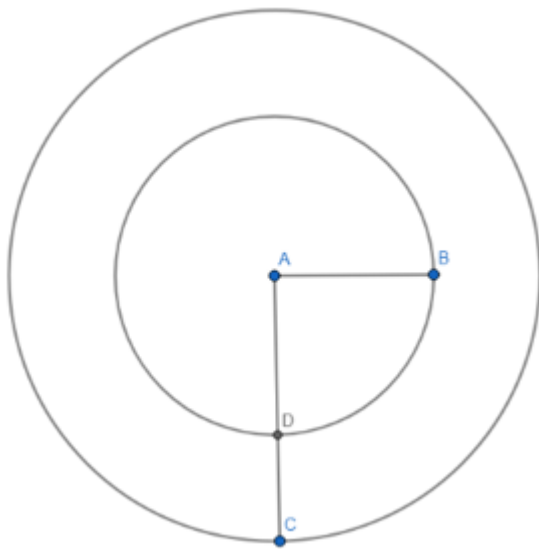
A. 22 cm^2

B. 12 cm^2

C. 32 cm^2

D. 18 cm^2

Answer



The radius of the smaller circle $AB = 3 \text{ cm}$

And radius of the larger circle $AC = 4 \text{ cm}$

The area enclosed between two concentric circles = Area of the larger circle
– area of the smaller circle

$\therefore$ The area of a circle $= \pi r^2$

$\Rightarrow$ Required area $= \pi R^2 - \pi r^2$

$\Rightarrow$ Required area $= \pi (R^2 - r^2)$

Using $(a+b)(a-b) = a^2 - b^2$

$\Rightarrow$ Required area $= \pi (R+r)(R-r)$

$\Rightarrow$ Required area $= \frac{22}{7} \times (4 + 3)(4 - 3) = 22 \text{ cm}^2$

Exercise 15.2

1. Question

In a circle of radius 7 cm, an arc subtends an angle of 60° at the centre. Find the length of the arc.

Answer

Given: Radius of the circle = 7 cm and angle subtended by the arc = 60°

We know that the length of the arc $= \frac{\theta}{360^\circ} \times (2\pi r)$

$\Rightarrow$ Length of the arc $= \frac{60^\circ}{360^\circ} \times 2 \times \frac{22}{7} \times 7 = 7.3 \text{ cm}$

2. Question

A sector of a circle of radius 10.5 cm contains an angle of 45° . Find the area of the minor sector. $\left(\pi = \frac{22}{7}\right)$

Answer

Given: Radius of the circle = 10.5 cm and angle subtended by the arc = 45°

We know that the area of the minor sector = $\frac{\theta}{360^\circ} \times (\pi r^2)$

$$\Rightarrow \text{Area of the minor sector} = \frac{45^\circ}{360^\circ} \times \frac{22}{7} \times 10.5 \times 10.5$$

$$\Rightarrow \text{Area of the minor sector} = 43.3125 \text{ cm}^2$$

3. Question

The length of an arc of a circle of radius 7 cm is 12 cm. Find the area of the minor sector.

Answer

Given: Radius of the circle = 7 cm and length of an arc = 12 cm

We know that the length of the arc = $\frac{\theta}{360^\circ} \times (2\pi r)$

$$\Rightarrow \frac{\theta}{360^\circ} \times 2 \times \frac{22}{7} \times 7 = 12$$

$$\Rightarrow \theta = \frac{12 \times 360^\circ}{44} = 98.18^\circ$$

We know that the area of the minor sector = $\frac{\theta}{360^\circ} \times (\pi r^2)$

$$\Rightarrow \text{Area of the minor sector} = \frac{98.18^\circ}{360^\circ} \times \frac{22}{7} \times 7 \times 7$$

$$\Rightarrow \text{Area of the minor sector} = 42 \text{ cm}^2$$

4. Question

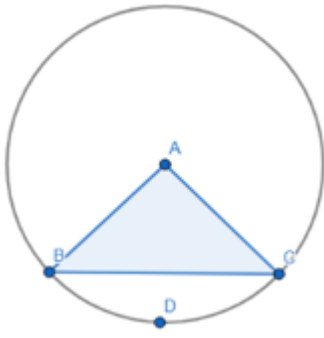
In a circle of radius 21 cm, an arc subtends an angle of 60° at the centre. Find:

(i) The length of the arc.

(ii) Area of the sector formed by the arc.

(iii) Area of the segment formed by the corresponding chord.

Answer



Given: Radius of the circle = 21 cm and angle subtended by the arc = 60°

(i) We know that the length of the arc = $\frac{\theta}{360^\circ} \times (2\pi r)$

$$\Rightarrow \text{Length of BDC} = \frac{60^\circ}{360^\circ} \times 2 \times \frac{22}{7} \times 21 = 22\text{cm}$$

(ii) We know that the area of the minor sector = $\frac{\theta}{360^\circ} \times (\pi r^2)$

$$\Rightarrow \text{Area of ABDC} = \frac{60^\circ}{360^\circ} \times \frac{22}{7} \times 21 \times 21$$

$$\Rightarrow \text{Area of ABDC} = 231\text{cm}^2$$

(iii) Area of the segment BDC = area of sector ABDC – area of triangle ABC

In $\triangle ABC$,

$$\angle A = 60^\circ, AB = AC = 21 \text{ cm \{radius of the circle\}}$$

$$\Rightarrow \angle ABC = \angle ACB \text{ \{angles opposite to equal sides are equal\}}$$

By the angle sum property of the triangle,

$$\angle ABC + \angle ACB + \angle A = 180^\circ$$

$$\Rightarrow 2\angle ABC = 180^\circ - 60^\circ$$

$$\Rightarrow \angle ABC = 60^\circ$$

Hence, $\triangle ABC$ is an equilateral triangle.

Area of a equilateral triangle = $\frac{\sqrt{3}}{4} a^2$, where a is the side of it.

$$\text{Area of } \triangle ABC = \frac{\sqrt{3}}{4} (21)^2$$

$$\Rightarrow \text{Area of } \triangle ABC = 190.95\text{cm}^2$$

$\therefore$ Area of the segment BDC = area of sector ABDC – area of triangle ABC

$$\Rightarrow \text{Area of the segment BDC} = 231 - 190.95$$

$$\Rightarrow \text{Area of the segment BDC} = 40.05\text{cm}^2$$

5. Question

The length of the minute hand of a clock is 10.5 cm. Find area of the sector formed by the minute hand in 10 minutes. $\left(\pi = \frac{22}{7}\right)$

Answer

Let us consider clock as a circle with radius 10.5 cm.

Also, the 60 minutes of the clock constitute the 360° angle of the circle.

$$\text{So, the angle formed by the minute hand in 10 minutes} = \frac{10}{60} \times 360^\circ = 60^\circ$$

$$\text{We know that the area of the minor sector} = \frac{\theta}{360^\circ} \times (\pi r^2)$$

$$\Rightarrow \text{Area of the minor sector} = \frac{60^\circ}{360^\circ} \times \frac{22}{7} \times 10.5 \times 10.5$$

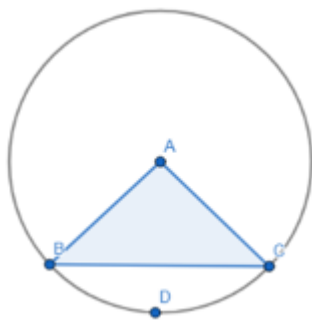
$$\Rightarrow \text{Area of the minor sector} = 57.75\text{cm}^2$$

6. Question

A chord of a circle of radius 3.5 cm subtends an angle of 90° at the centre.

Find the area of the minor segment of the circle. $\left(\pi = \frac{22}{7}\right)$

Answer



Given: Radius of the circle = 3.5 cm and angle subtended by the arc = 90°

Area of the segment BDC = area of sector ABDC – area of triangle ABC

$$\text{We know that the area of the minor sector} = \frac{\theta}{360^\circ} \times (\pi r^2)$$

$$\Rightarrow \text{Area of ABDC} = \frac{90^\circ}{360^\circ} \times \frac{22}{7} \times 3.5 \times 3.5$$

$$\Rightarrow \text{Area of ABDC} = 9.625\text{cm}^2$$

In $\triangle ABC$,

$\angle A = 90^\circ$, $AB = AC = 3.5$ cm {radius of the circle}

$\therefore \triangle ABC$ is a right angled triangle.

$$\text{Area of } \triangle ABC = \frac{1}{2} \times \text{base} \times \text{height}$$

$$\Rightarrow \text{Area of } \triangle ABC = \frac{1}{2} \times 3.5 \times 3.5$$

$$\Rightarrow \text{Area of } \triangle ABC = 6.125\text{cm}^2$$

$\therefore$ Area of the segment BDC = area of sector ABDC – area of triangle ABC

$$\Rightarrow \text{Area of the segment BDC} = 9.625 - 6.125$$

$$\Rightarrow \text{Area of the segment BDC} = 3.5\text{cm}^2$$

7. Question

Find the area of a quadrant of a circle whose circumference is 22 cm.

Answer

Given that circumference of the circle = 22 cm

We know that circumference of the circle = $2\pi r$

$$\Rightarrow 2 \times \frac{22}{7} \times r = 22$$

$$\Rightarrow r = 3.5\text{cm}$$

Quadrant of a circle is the one fourth part of a circle.

Also, the area of a circle = πr^2

$$\Rightarrow \text{Area} = \frac{22}{7} \times 3.5 \times 3.5 = 38.5\text{ cm}^2$$

$$\text{Area of a quadrant} = \frac{38.5}{4} = 9.625\text{cm}^2$$

8. Question

The hour hand of a clock is 5 cm long. Find the area of the sector formed by the hour hand in 7 minutes.

Answer

Let us consider clock as a circle with radius 5 cm.

Also, the hour hand of the clock makes 360° when takes 12 hours.

So let us convert 7 minutes to degrees.

There are 12×60 minutes in 12 hours.

So, the angle formed by the hour in 7 minutes $= \frac{7}{12 \times 60} \times 360^\circ = 3.49^\circ$

We know that the area of the minor sector $= \frac{\theta}{360^\circ} \times (\pi r^2)$

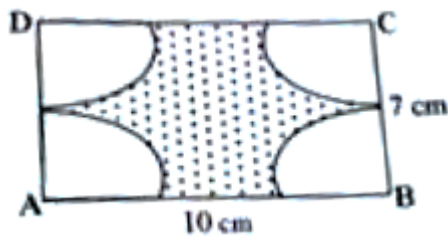
$$\Rightarrow \text{Area of the minor sector} = \frac{3.49^\circ}{360^\circ} \times \frac{22}{7} \times 5 \times 5$$

$$\Rightarrow \text{Area of the minor sector} = 0.7638 \text{ cm}^2$$

9. Question

In figure, ABCD is a rectangle. The side AB = 10 cm and BC = 7 cm. From each vertex of the rectangle, arcs of radii 3.5 cm are drawn. Find the shaded region.

$$\left(\pi = \frac{22}{7} \right)$$



Answer

Given: AB = 10 cm, BC = 7 cm, Radius of the quadrants = 3.5 cm

In the given figure, the four quadrants together form a circle of radius 3.5 cm

$\therefore$ Area of the shaded region = Area of the rectangle – Area of the circle formed by the 4 quadrants

$$\text{Area of rectangle} = \text{Length} \times \text{breadth} = 10 \times 7 = 70 \text{ cm}^2$$

$$\text{Area of a circle} = \pi r^2$$

$$\Rightarrow \text{Area} = \frac{22}{7} \times 3.5 \times 3.5 = 38.5 \text{ cm}^2$$

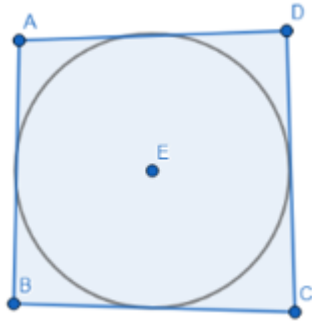
$$\text{Area of the shaded region} = 70 - 38.5 = 31.5 \text{ cm}^2$$

Exercise 15.3

1. Question

Find the circumference of the incircle of a square of side 14 cm

Answer



Let ABCD be the square with side 14 cm.

$$\Rightarrow BC = 14 \text{ cm}$$

Let the circle centered at E be the incircle of the ABCD.

$$BC = \text{diameter of the circle} = 14 \text{ cm}$$

$$\Rightarrow \text{Radius of the circle} = 7 \text{ cm}$$

$$\text{Given that radius of the circle} = 7 \text{ cm}$$

$$\text{We know that circumference of the circle} = 2\pi r$$

$$\Rightarrow \text{Circumference} = 2 \times \frac{22}{7} \times 7 = 44 \text{ cm}$$

2. Question

Difference between the circumference and radius of a circle is 74 cm. Find the area of the circle.

Answer

$$\text{Given that difference between the circumference of the circle and radius of it} = 74 \text{ cm}$$

$$\text{We know that circumference of the circle} = 2\pi r$$

$$\Rightarrow 2\pi r - r = 74$$

$$\Rightarrow 2 \times \frac{22}{7} r - r = 74$$

$$\Rightarrow r(2 \times \frac{22}{7} - 1) = 74$$

$$\Rightarrow r \times \frac{37}{7}$$

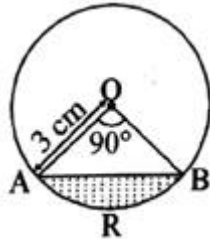
$$\Rightarrow r = \frac{74 \times 7}{37} = 14 \text{ cm}$$

$$\text{Area of a circle} = \pi r^2$$

$$\Rightarrow \text{Area} = \frac{22}{7} \times 14 \times 14 = 616 \text{ cm}^2$$

3. Question

In the given figure, O is the centre of the circle. $\angle AOB = 90^\circ$ and $OA = 3 \text{ cm}$. Find the area of the shaded region.



Answer

Given: Radius of the circle = 3 cm and angle subtended by the arc = 90°

Area of the segment ARB = area of sector OARB – area of triangle OAB

We know that the area of the minor sector = $\frac{\theta}{360^\circ} \times (\pi r^2)$

$$\Rightarrow \text{Area of ABDC} = \frac{90^\circ}{360^\circ} \times \frac{22}{7} \times 3 \times 3$$

$$\Rightarrow \text{Area of ABDC} = 7.071428 \text{ cm}^2$$

In $\triangle ABC$,

$\angle A = 90^\circ$, $AB = AC = 3 \text{ cm}$ {radius of the circle}

$\therefore \triangle ABC$ is a right angled triangle.

$$\text{Area of } \triangle ABC = \frac{1}{2} \times \text{base} \times \text{height}$$

$$\Rightarrow \text{Area of } \triangle ABC = \frac{1}{2} \times 3 \times 3$$

$$\Rightarrow \text{Area of } \triangle ABC = 4.5 \text{ cm}^2$$

$\therefore$ Area of the segment BDC = area of sector ABDC – area of triangle ABC

$$\Rightarrow \text{Area of the segment BDC} = 7.071428 - 4.5$$

$$\Rightarrow \text{Area of the segment BDC} = 2.57 \text{ cm}^2$$

4. Question

The circumference of a circle is equal to the perimeter of a square. Find the ratio of their areas.

Answer

Given the circumference of a circle is equal to the perimeter of a square. We know that circumference of the circle = $2\pi r$ and the perimeter of a square = $4 \times \text{length of the side}$.

$$\Rightarrow 2\pi r = 4 \times \text{side}$$

$$\Rightarrow \frac{r}{\text{side}} = \frac{2}{\pi} \dots (i)$$

We know that area of the square = $(\text{Side})^2$

Also, the area of a circle = πr^2

$$\Rightarrow \text{Ratio of their areas} = \frac{\pi r^2}{\text{side}^2}$$

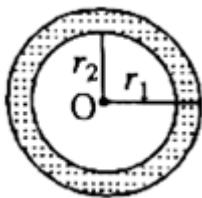
$$\Rightarrow \text{Ratio of their areas} = \pi \times \left(\frac{2}{\pi}\right)^2$$

$$\Rightarrow \text{Ratio of their areas} = \frac{4}{\pi}$$

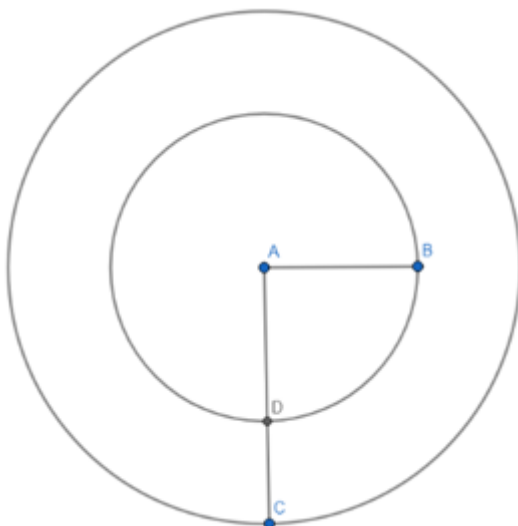
$$\Rightarrow \text{Ratio of their areas} = \frac{4 \times 7}{22} = \frac{14}{11}$$

5. Question

The radius of a circular park is 3.5 m. A 1.4 m wide footpath is made all round the circular park. Find the area of the footpath.



Answer



Given: Radius of the smaller circle $AB = 3.5$ m

Also, $CD = 1.4$ m

$\Rightarrow$ Radius of the larger circle $AC = AD + CD = 3.5 + 1.4 = 4.9$ m

Area of the path = Area of the larger circle - area of the smaller circle

$\because$ The area of a circle $= \pi r^2$

$\Rightarrow$ Area of the path $= \pi R^2 - \pi r^2$

$\Rightarrow$ Area of the path $= \frac{22}{7} (R^2 - r^2)$

$\Rightarrow$ Area of the path $= \frac{22}{7} (4.9^2 - 3.5^2)$

Using $(a+b)(a-b) = a^2 - b^2$

$\Rightarrow$ Area of the path $= \frac{22}{7} (4.9 - 3.5)(4.9 + 3.5)$

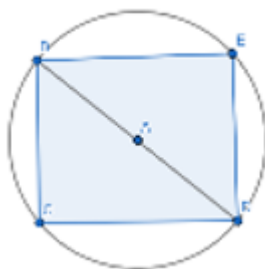
$\Rightarrow$ Area of the path $= \frac{22}{7} (1.4)(8.4)$

$\Rightarrow$ Area of the path $= 36.96 \text{ m}^2$

6. Question

Find the area of the largest square that can be drawn inside a circle of radius 8 cm.

Answer



Given: Radius of the circle = 8 cm

Diameter of the circle = 16 cm

For the largest square inscribed in it i.e. BCDE,

Diagonal of the square = diameter of the circle

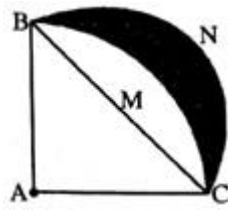
$\Rightarrow BD = 16$ cm

Area of a square $= \frac{\text{Diagonal}^2}{2}$

$\Rightarrow$ Area of BCDE $= \frac{16 \times 16}{2} = 128 \text{ cm}^2$

7. Question

In the given figure, ABMC is a quadrant of a circle of radius 14 cm and a semicircle is drawn with BC as diameter. Find the area of the shaded region.



Answer

Given: ABMC is a quadrant of radius 14 cm.

In $\triangle ABC$,

$$\angle A = 90^\circ, AB = AC = 14 \text{ cm}$$

By Pythagoras theorem,

$$BC^2 = AB^2 + AC^2$$

$$\Rightarrow BC^2 = 2 \times 14 \times 14$$

$$\Rightarrow BC = 14\sqrt{2} \text{ cm}$$

$$\text{Now, Area of } \triangle ABC = \frac{1}{2} \times \text{base} \times \text{height}$$

$$\Rightarrow \text{Area of } \triangle ABC = \frac{1}{2} \times 14 \times 14$$

$$\Rightarrow \text{Area of } \triangle ABC = 98 \text{ cm}^2$$

$$\text{We know that the area of the minor sector} = \frac{\theta}{360^\circ} \times (\pi r^2)$$

$$\Rightarrow \text{Area of ABMC} = \frac{90^\circ}{360^\circ} \times \frac{22}{7} \times 14 \times 14$$

$$\Rightarrow \text{Area of ABMC} = 154 \text{ cm}^2$$

$$\text{So, area of ABMC} = \text{area of } \triangle ABC + \text{area of BCM}$$

$$\Rightarrow \text{Area of BCM} = \text{area of ABMC} - \text{area of } \triangle ABC$$

$$\Rightarrow \text{Area of BCM} = 154 - 98 = 56 \text{ cm}^2$$

Also, we have a semicircle made at BC in the figure.

$$\text{Diameter of the semicircle} = BC = 14\sqrt{2} \text{ cm}$$

$$\Rightarrow \text{Radius of the semicircle} = 7\sqrt{2} \text{ cm}$$

$$\text{Area of semicircle} = \pi \frac{r^2}{2}$$

$$\Rightarrow \text{Area of semicircular plot} = \frac{22}{7 \times 2} \times 7\sqrt{2} \times 7\sqrt{2}$$

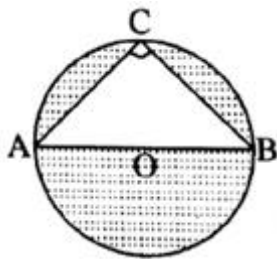
$$\Rightarrow \text{Area of semicircular plot} = 154 \text{ cm}^2$$

$$\text{Area of the shaded region} = \text{Area of the semicircle} - \text{Area of BCM}$$

$$\Rightarrow \text{Area of the shaded region} = 154 - 56 = 98 \text{ cm}^2$$

8. Question

In the given figure, AB is a diameter, AC = 6 cm, BC = 8 cm. Find the shaded region.



Answer

Given:

In $\triangle ABC$,

$$AC = 6 \text{ cm}, BC = 8 \text{ cm}$$

Also, $\angle C = 90^\circ$ because angle subtended by the diameter is 90° and AB is the diameter.

By Pythagoras theorem,

$$BA^2 = CB^2 + AC^2$$

$$\Rightarrow BC^2 = 36 + 64$$

$$\Rightarrow BC = 10 \text{ cm}$$

$$\text{Area of } \triangle ABC = \frac{1}{2} \times \text{base} \times \text{height}$$

$$\Rightarrow \text{Area of } \triangle ABC = \frac{1}{2} \times 6 \times 8$$

$$\Rightarrow \text{Area of } \triangle ABC = 24 \text{ cm}^2$$

$$\text{Radius of the circle} = 5 \text{ cm}$$

$$\text{Area of a circle} = \pi r^2$$

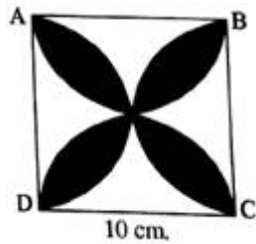
$$\Rightarrow \text{Area} = \frac{22}{7} \times 5 \times 5 = 78.57 \text{ cm}^2$$

Area of the shaded region = Area of circle - Area of the triangle

$$\Rightarrow \text{Area of the shaded region} = 78.57 - 24 = 54.57 \text{ cm}^2$$

9. Question

Find the area of the shaded design in the figure, where ABCD is a square of side 10 cm and semicircles are drawn with each side of the square as diameter (use $\pi = 3.14$).



Answer

Given side of the square ABCD = 10 cm

Area of the square = side $\times$ side

$$\Rightarrow \text{Area of ABCD} = 10 \times 10 = 100 \text{ cm}^2$$

Also given that semicircles are drawn with each side of the square as diameter

Diameter = 10 cm

Radius = 5 cm

Let us mark the four unshaded areas as I, II, III and IV.

Area of I + Area III

= Area of square - Area of two semi-circles

$$= 100 - 2 \times \frac{1}{2} \pi \times 25 = 100 - 3.14 \times 25$$

$$= 21.5 \text{ cm}^2$$

Similarly, Area of II + Area of IV = 21.5 cm²

So, area of shaded region = ar of ABCD - ar (I + II + III + IV)

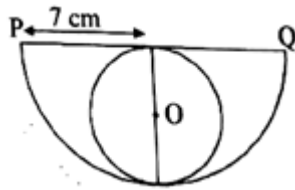
$$= (100 - 2 \times 21.5) \text{ cm}^2$$

$$= 100 - 43$$

$$= 57 \text{ cm}^2$$

10. Question

In the given figure, radius of the semicircle is 7 cm. Find the area of the circle drawn inside the semicircle.



Answer

In the given figure the radius of the semicircle = 7 cm

The diameter of the circle inscribed in the semicircle = 7 cm

$\Rightarrow$ Radius of the circle = 3.5 cm

Area of a circle = πr^2

$$\Rightarrow \text{Area} = \frac{22}{7} \times 3.5 \times 3.5 = 38.5 \text{ cm}^2$$

11. Question

If the sum of circumferences of two circles of radii R_1 and R_2 is equal to the circumference of a circle of radius R , then which of the following choices is correct?

A. $R_1 + R_2 = R$

B. $R_1 + R_2 > R$

C. $R_1 + R_2 < R$

D. Nothing can be said with certainty.

Answer

Given: The sum of circumferences of two circles of radii R_1 and R_2 is equal to the circumference of a circle of radius R .

We know that circumference of the circle = $2\pi r$

$$\Rightarrow 2\pi R_1 + 2\pi R_2 = 2\pi R$$

$$\Rightarrow 2\pi (R_1 + R_2) = 2\pi R$$

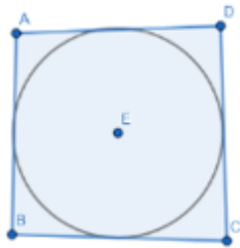
$$\Rightarrow R_1 + R_2 = R$$

12. Question

The circumference of the incircle of a square of side 14 cm is—

- A. 22 cm
- B. 44 cm
- C. 33 cm
- D. 55 cm

Answer



Let ABCD be the square with side 14 cm.

$$\Rightarrow BC = 14 \text{ cm}$$

Let the circle centered at E be the incircle of the ABCD.

$$BC = \text{diameter of the circle} = 14 \text{ cm}$$

$$\Rightarrow \text{Radius of the circle} = 7 \text{ cm}$$

Given that radius of the circle = 7 cm

We know that circumference of the circle = $2\pi r$

$$\Rightarrow \text{Circumference} = 2 \times \frac{22}{7} \times 7 = 44 \text{ cm}$$