CBSE Sample Paper-05 Mathematics Class - XII

Time allowed: 3 hours Maximum Marks: 100

General Instructions:

- a) All questions are compulsory.
- b) The question paper consists of 26 questions divided into three sections A, B and C. Section A comprises of 6 questions of one mark each, Section B comprises of 13 questions of four marks each and Section C comprises of 7 questions of six marks each.
- c) All questions in Section A are to be answered in one word, one sentence or as per the exact requirement of the question.
- d) Use of calculators is not permitted.

Section A

- 1. Is R defined on the set $A=\{1,2,3,.....14,15\}$ defined as $R=\{(x,y):3x-y=0\}$ reflexive?
- 2. Find the angle between the vectors $\vec{a} = 4i + 4j$ and $\vec{b} = 4i 2j$.
- 3. Evaluate $\sin^{-1}\left(\frac{1}{6}\right) + \cos^{-1}\left(\frac{1}{6}\right)$?
- 4. If a matrix has 12 elements, what are the possible orders it can have?
- 5. Prove that A-A' is skew symmetric.
- 6. Find the values of x,y,z s.t $\begin{bmatrix} x-y & 0 & 0 \\ z & 6 & 0 \\ 0 & 0 & 2y \end{bmatrix}$ is a scalar matrix?

Section B

- 7. Solve: $3\sin^{-1}\left(\frac{2x}{1+x^2}\right) 4\cos^{-1}\left(\frac{1-x^2}{1+x^2}\right) + 2\tan^{-1}\left(\frac{2x}{1-x^2}\right) = \frac{\pi}{3}$
- 8. Find a unit vector perpendicular to each of the vectors $(\vec{a} \vec{b})$ and $(\vec{a} + \vec{b})$ where $\vec{a} = i + j + k$ and $\vec{b} = i + 2j + 3k$.
- 9. If A and B are independent events such that P(AUB)=0.6, P(A)=0.2. Find P(B)

$$y = \frac{3x(x+7)}{x+5} + 5$$
. Prove that the marginal cost continuously falls as output increases.

11. Solve
$$\frac{dy}{dx} + \frac{2y}{3} = \frac{x}{\sqrt{y}}$$

12. If
$$A = \begin{bmatrix} 0 & -\tan \alpha / 2 \\ \tan \alpha / 2 & 0 \end{bmatrix}$$
 and I is the identity matrix of order 2, show that
$$I + A = (I - A) \begin{bmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix}$$

13. Find the equations of the tangent and the normal to the curve
$$x = \cos t$$
, $y = \sin t$ at $t = \frac{\pi}{4}$.

14. Show that the relation R in the set \mathbb{Z} of integers given by R={(a,b):7 divides a-b} is an equivalence relation.

15. If
$$y = \sqrt{\log x + \sqrt{\log x + \sqrt{\log x + \cdots}}}$$
 prove that $(2y - 1)\frac{dy}{dx} = \frac{1}{x}$.

16. For any two vectors
$$\vec{a}$$
 and \vec{b} , prove that $|\vec{a} + \vec{b}| \le |\vec{a}| + |\vec{b}|$.

17. Integrate
$$\int \frac{e^x}{e^{2x}-4} dx$$
. Write ant points for promoting national integration.

Find the vector equation of the plane passing through the intersection of the planes
$$\vec{r} \cdot (2i+2j-3k) = 7, \vec{r} \cdot (2i+5j+3k) = 9$$
 and the point $(2,1,3)$.

19. Find the equation of the plane passing through the line
$$\frac{x+1}{-3} = \frac{y-3}{2} = \frac{z+2}{1}$$
 and the point (0, 7,-7).

Show that the line
$$x = \frac{7 - y}{3} = \frac{z + 7}{2}$$
 lies on the plane.

Section C

20. In answering a question on a multiple choice test, a student either knows the answer or guesses. Let ³/₄ be the probability that he knows the answer and ¹/₄ be the probability that he guesses. Assume that a student who guesses the answer would answer correctly with probability 1/4. What is the probability that a student knows the answer, given that he has answered it correctly.

21. Differentiate
$$\tan^{-1} \left(\frac{\sqrt{1+x^2}-1}{x} \right) w.r.t. \sin^{-1} \left(\frac{2x}{1+x^2} \right)$$

22. Integrate
$$\int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \cos 2x \log(\sin x) dx.$$

- 23. Prove that the volume of the largest cone that can be inscribed in a sphere of radius a is 8/27 of the volume of the sphere.
- 24. Solve the following system of equations using matrix method

$$\frac{2}{x} + \frac{3}{y} + \frac{10}{z} = 4$$

$$\frac{4}{x} - \frac{6}{y} + \frac{5}{z} = 1$$

$$\frac{6}{x} + \frac{9}{y} - \frac{20}{z} = 2$$

- 25. A dietician wishes to mix two types of foods in such a way that the vitamin contents of the mixture contain at least 8 units of vitamin A and 10 units of vitamin C. Food 1 contains 2 units per kg of vitamin A and 1 unit per kg of vitamin C. Food 2 contains 1 unit per kg of vitamin A and 2 unit per kg of vitamin C. Food 1 costs Rs.50 per kg and Food 2 costs Rs.70 per kg. Using linear programming, find the minimum cost of such a mixture.
- 26. Draw a rough sketch of the region $\{(x, y): y^2 < 4x, 4x^2 + 4y^2 \le 9\}$ and find the area enclosed.

CBSE Sample Paper-05 Mathematics Class - XII

Time allowed: 3 hours

ANSWERS

Maximum Marks: 100

Section A

1. Solution: NO. Let $1 \in A$, $3(1)-1=2 \neq 0$

Thus, $(1,1) \notin R$

2. Solution:

$$\vec{a} = 4i + 4j \text{ and } \vec{b} = 4i - 2j$$

$$\cos \theta = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}| |\vec{b}|} = \frac{16 - 8}{\left(4\sqrt{2}\right) 2\sqrt{5}} = \frac{8}{8\sqrt{10}} \Rightarrow \theta = \cos^{-1}\left(\frac{8}{8\sqrt{10}}\right)$$

- 3. Solution: $\frac{\pi}{2}$
- 4. Solution: (1,12),(2,6),(3,4),(4,3),(6,2),(12,1)
- 5. Solution:

$$(A-A')' = A'-(A')' = A'-A = -(A-A')$$

Thus, A-A' is skew symmetric.

6. Solution: A scalar matrix is a diagonal matrix with equal diagonal elements.

$$\therefore z = 0, 2y = 6, x - y = 6$$
$$\Rightarrow x = 9, y = 3, z = 0$$

Section B

$$3\sin^{-1}\left(\frac{2x}{1+x^2}\right) - 4\cos^{-1}\left(\frac{1-x^2}{1+x^2}\right) + 2\tan^{-1}\left(\frac{2x}{1-x^2}\right) = \frac{\pi}{3}$$
$$3(2\tan^{-1}x) - 4(2\tan^{-1}x) + 2(2\tan^{-1}x) = \frac{\pi}{3}$$

$$2\tan^{-1}x = \frac{\pi}{3}$$

$$\tan^{-1} x = \frac{\pi}{6}$$

$$x = \tan \frac{\pi}{6} = \frac{1}{\sqrt{3}}$$

$$\vec{a} = i + j + k$$
, $\vec{b} = i + 2j + 3k$

$$\vec{a} + \vec{b} = 2i + 3j + 4k, \vec{a} - \vec{b} = -j - 2k$$

Vector
$$\perp$$
 to $\vec{a} + \vec{b}$, $\vec{a} - \vec{b}$ is $(\vec{a} + \vec{b}) \times (\vec{a} - \vec{b})$

$$(\vec{a} + \vec{b}) \times (\vec{a} - \vec{b}) = \begin{vmatrix} i & j & k \\ 2 & 3 & 4 \\ 0 & -1 & -2 \end{vmatrix} = -2i + 4j - 2k = \vec{c}$$

$$\therefore |\vec{c}| = 2\sqrt{6}$$

$$Unit\ vector = \frac{-2i + 4j - 2k}{2\sqrt{6}}$$

9. Solution:

Since A and B are independent events $P(A \cap B) = P(A)P(B)$

$$\therefore P(A \cup B) = P(A) + P(B) - P(A \cap B) = 0$$

$$\Rightarrow$$
 0.6 = 0.2 + $P(B)$ - .2 $P(B)$

$$\Rightarrow P(B) = \frac{.4}{8} = \frac{1}{2}$$

10. Solution:

$$Cost = y = y = \frac{3x(x+7)}{x+5} + 5 = \frac{3x^2 + 21}{x+5} + 5$$

$$\therefore MC = \frac{dy}{dx} = \frac{(x+5)(6x) - (3x^2 + 21) \cdot 1}{(x+5)^2} = \frac{3x^2 + 30x + 105}{(x+5)^2} = 3 + \frac{30}{(x+5)^2}$$

$$\frac{d}{dx}(MC) = \frac{-60}{\left(x+5\right)^2} < 0$$

Thus, marginal cost is a decreasing function of output(x).

$$\frac{dy}{dx} + \frac{2y}{3} = \frac{x}{\sqrt{y}}$$

$$\sqrt{y} \frac{dy}{dx} + \frac{2y^{3/2}}{3} = x$$

$$Let \ z = y^{3/2} \Rightarrow \frac{dz}{dx} = \frac{3}{2} \sqrt{y} \frac{dy}{dx}$$

$$\Rightarrow \frac{2}{3} \frac{dz}{dx} + \frac{2}{3} z = x$$

$$\Rightarrow \frac{dz}{dx} + z = \frac{3}{2} x$$

$$\therefore P = 1, Q = \frac{3}{2} x$$

$$\therefore I.F = e^{\int Pdx} = e^x$$
Solution is:
$$ze^x = \int \frac{3}{2} xe^x dx$$

$$\Rightarrow y^{3/2} e^x = \frac{3}{2} xe^x - e^x + c$$

$$\Rightarrow y^{3/2} = \frac{3}{2} (x - 1) + Ce^{-x}$$

$$\begin{split} I - A &= \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} - \begin{bmatrix} 0 & -\tan \alpha/2 \\ \tan \alpha/2 & 0 \end{bmatrix} = \begin{bmatrix} 1 & \tan \alpha/2 \\ -\tan \alpha/2 & 1 \end{bmatrix} \\ (I - A) \begin{bmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix} = \begin{bmatrix} 1 & \tan \alpha/2 \\ -\tan \alpha/2 & 1 \end{bmatrix} \begin{bmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix} \\ &= \begin{bmatrix} \cos \alpha + (\tan \alpha/2) \sin \alpha & -\sin \alpha + (\tan \alpha/2) \cos \alpha \\ \sin \alpha - (\tan \alpha/2) \cos \alpha & \cos \alpha + (\tan \alpha/2) \sin \alpha \end{bmatrix} \\ &= \begin{bmatrix} (2\cos^2 \alpha/2 - 1) + (\tan \alpha/2)(2\sin \alpha/2\cos \alpha/2) & -(2\sin \alpha/2\cos \alpha/2) + (\tan \alpha/2)(2\cos^2 \alpha/2 - 1) \\ (2\sin \alpha/2\cos \alpha/2) - (\tan \alpha/2)(2\cos^2 \alpha/2 - 1) & (2\cos^2 \alpha/2 - 1) + (\tan \alpha/2)(2\sin \alpha/2\cos \alpha/2) \end{bmatrix} \\ &= \begin{bmatrix} 1 & -\tan \alpha/2 \\ \tan \alpha/2 & 1 \end{bmatrix} = I + A \end{split}$$

When
$$t = \frac{\pi}{4}$$
, $x = \frac{1}{\sqrt{2}}$, $y = \frac{1}{\sqrt{2}}$

$$\therefore po \text{ int of } contact \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$

$$y = \sin t \Rightarrow \frac{dy}{dt} = \cos t, x = \cos t \Rightarrow \frac{dx}{dt} = -\sin t$$

$$\therefore \frac{dy}{dx} = \frac{dy/dt}{dx/dt} = \frac{\cos t}{-\sin t} = -\cot t$$

$$\therefore slope \ at \ t = \frac{\pi}{4} = -\cot\frac{\pi}{4} = -1$$

$$\therefore equation \ of \ \tan gent = (y - \frac{1}{\sqrt{2}}) = -1(x - \frac{1}{\sqrt{2}}) \Rightarrow x + y - \sqrt{2} = 0$$

Slope of normal =
$$m, m(-1) = -1 \Rightarrow m = 1$$

$$\therefore equation of normal = (y - \frac{1}{\sqrt{2}}) = 1(x - \frac{1}{\sqrt{2}}) \Rightarrow x - y = 0$$

Reflexive:

Let $a \in \mathbb{Z}$

a-a=0, 7 divides 0.

$$\therefore (a,a) \in R \forall a \in \mathbb{Z}$$

Hence, R is reflexive.

Symmetric:

Suppose
$$(a,b) \in R \Rightarrow 7/a-b \Rightarrow a-b=7k \ f.s. \ k \in \mathbb{Z}$$

 $\Rightarrow b-a=-7k=7k' \ f.s. \ k' \in \mathbb{Z}$

$$\therefore (b,a) \in \mathbb{Z}$$

Transitive:

Suppose
$$(a,b),(b,c) \in R$$

$$\Rightarrow b-a=7m \ f.s. \ m \in \mathbb{Z}, c-b=7n \ f.s. \ n \in \mathbb{Z}$$

$$\therefore c-a=c-b+b-a=7(n-m)$$
, where $n-m\in\mathbb{Z}$

$$\therefore (a,c) \in R$$

Hence the above relation is an equivalence relation.

$$y = \sqrt{\log x + \sqrt{\log x + \sqrt{\log x} + \dots}}$$

$$\Rightarrow y = \sqrt{\log x + y}$$

$$\Rightarrow y^2 = \log x + y$$

Differentiating both sides w.r.t x, we get

$$2y\frac{dy}{dx} = \frac{1}{x} + \frac{dy}{dx} \Rightarrow (2y - 1)\frac{dy}{dx} = \frac{1}{x}$$

16. Solution:

$$\begin{aligned} |\vec{a} + \vec{b}|^2 &= (\vec{a} + \vec{b}) \cdot (\vec{a} + \vec{b}) \\ &= \vec{a} \cdot \vec{a} + \vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{a} + \vec{b} \cdot \vec{b} \\ &= |\vec{a}|^2 + 2\vec{a} \cdot \vec{b} + |\vec{b}|^2 \le |\vec{a}|^2 + 2|\vec{a} \cdot \vec{b}| + |\vec{b}|^2 \le |\vec{a}|^2 + 2|\vec{a}||\vec{b}| + |\vec{b}|^2 \\ &= (|\vec{a}| + |\vec{b}|)^2 \\ &\therefore |\vec{a} + \vec{b}| \le |\vec{a}| + |\vec{b}| \end{aligned}$$

$$I = \int \frac{e^x}{e^{2x} - 4} dx$$

$$Let \ e^x = t \Rightarrow e^x dx = dt$$

$$I = \int \frac{1}{t^2 - 4} dt = \int \frac{1}{(t - 2)(t + 2)} dt$$

$$= \frac{1}{4} \int \left(\frac{1}{t - 2} - \frac{1}{t + 2} \right) dt$$

$$= \frac{1}{4} (\log|t - 2| - \log|t + 2|) + c$$

$$= \frac{1}{4} \log\left| \frac{t - 2}{t + 2} \right| + c$$

$$= \frac{1}{4} \log\left| \frac{e^x - 2}{e^x + 2} \right| + c$$

- 1.We should not judge people by their religion.
- 2. Women should be empowered by educating them.
- 18 Solution:

$$\overrightarrow{n_1} = 2i + 2j - 3k, d_1 = 7$$

 $\overrightarrow{n_2} = 2i + 5j + 3k, d_2 = 9$

Equation of plane:

$$\vec{r}.(\vec{n_1} + \lambda \vec{n_2}) = d_1 + \lambda d_2$$

$$\vec{r}.(2i + 2j - 3k + \lambda (2i + 5j + 3k)) = 7 + 9\lambda$$
Let $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$

$$\therefore x(2 + 2\lambda) + y(2 + 5\lambda) + z(-3 + 3\lambda) = 7 + 9\lambda$$
Putting $(x, y, z) = (2, 1, 3)$ we get $\lambda = \frac{10}{9}$
Substituting the value of λ we get, $\vec{r}.(38i + 68j + 3k) = 153$

19. Solution:

Equation of any plane containing the given line is:

$$A(x+1)+B(y-3)+C(z+2)=0$$
, where $-3A+2B+C=0$

Since, plane passes through (0,7,-7) we have,

$$A(1)+B(4)+C(-5)=0$$
, i.eA+4B-5C=0

Solving the above equations for A, B,C we have

$$\frac{A}{-10-4} = \frac{B}{1-15} = \frac{C}{-12-2} \Rightarrow \frac{A}{1} = \frac{B}{1} = \frac{C}{1} = k$$

Thus, substituting the value of A, B,C we get the equation of the plane as x+y+z=0

Now, the line $x = \frac{7-y}{3} = \frac{z+7}{2}$ or $\frac{x}{1} = \frac{y-7}{-3} = \frac{z+7}{2}$ lies on the plane if it is parallel to the plane and any point on it lies on the plane.

Since, $1(1)+-3(1)+2(1)=0 \Rightarrow$ line is parallel to the plane.

Again as (0,7,-7) lies on the plane, we conclude the line lies on the plane.

Section C

20. Solution:

Let E be the event that the student answered correctly.

Let E_1 denote the event that the student knows the answer. Let E_2 denote the event that the student guesses the answer.

$$P(E_1/E) = ?$$

$$P(E_1)=3/4$$
, $P(E_2)=1/4$

$$P(E/E_1)=1$$
, $P(E/E_2)=1/4$

Thus, by Baye's Theorem

$$P(E_1 / E) = \frac{P(E_1)P(E / E_1)}{P(E_1)P(E / E_1) + P(E_2)P(E / E_2)}$$
$$= \frac{(3/4)(1)}{(3/4)1 + (1/4)(1/4)} = \frac{12}{13}$$

21. Solution:

Let
$$y = \tan^{-1} \left(\frac{\sqrt{1 + x^2} - 1}{x} \right)$$
, $z = \sin^{-1} \left(\frac{2x}{1 + x^2} \right)$

Put in $g x = \tan \theta$,

$$y = \tan^{-1} \left(\frac{\sqrt{1 + \tan^2 \theta} - 1}{\tan \theta} \right) = \tan^{-1} \left(\frac{\sec \theta - 1}{\tan \theta} \right) = \tan^{-1} \left(\frac{1 - \cos \theta}{\sin \theta} \right)$$
$$= \tan^{-1} \left(\frac{2 \sin^2 \theta / 2}{2 \sin \theta / 2 \cos \theta / 2} \right) = \tan^{-1} (\tan \theta / 2) = \theta / 2$$
$$z = \sin^{-1} \left(\frac{2 \tan \theta}{1 + \tan^2 \theta} \right) = \sin^{-1} (\sin 2\theta) = 2\theta$$

$$\therefore \theta = 7/2$$

$$\therefore y = \frac{1}{2} \left(\frac{z}{2} \right) = \frac{z}{4}$$

$$\frac{dy}{dz} = \frac{1}{4}$$

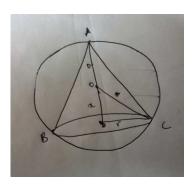
$$I = \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \cos 2x \log(\sin x) dx.$$

$$= \log(\sin x) \cdot \frac{\sin 2x}{2} \Big|_{\frac{\pi}{4}}^{\frac{\pi}{2}} - \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \frac{1}{\sin x} \cos x \cdot \frac{\sin 2x}{2} dx$$

$$= 0 - \log\left(\frac{1}{\sqrt{2}}\right) \frac{1}{2} - \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \frac{1}{\sin x} \cos x \cdot \frac{2 \sin x \cos x}{2} dx$$

$$= -\frac{1}{2} \log\left(\frac{1}{\sqrt{2}}\right) - \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \frac{1 + \cos 2x}{2} dx = -\frac{1}{2} \log\left(\frac{1}{\sqrt{2}}\right) - \frac{\pi}{8} + \frac{1}{4}$$

Consider a sphere of radius a with center O s.t. OD=x and DC=r.



Let h be the height of the cone.

Then, h=OA+x=a+x

Also, for
$$\triangle ODC$$
, $x^2 + r^2 = a^2$

Let V be the volume of the cone.

$$\therefore V = \frac{1}{3}\pi r^2 h$$

$$\Rightarrow V(x) = \frac{1}{3}\pi(a^2 - x^2)(a+x)$$

$$\therefore V'(x) = \frac{1}{3}\pi \Big[(a^2 - x^2) + (a + x)(-2x) \Big] = \frac{\pi}{3} (a + x)(a - 3x)$$

Also, V''(x) =
$$\frac{\pi}{3}$$
[(a+x)(-3x)+(a-3x)1]

$$V'(x) = 0 \Rightarrow x = -a, \frac{a}{3}$$

Neglecting x = -a,

$$V"\left(\frac{a}{3}\right) = \frac{-4\pi a}{3} < 0$$

 \therefore volume is max imum when x = a/3.

$$\therefore h = a + \frac{a}{3} = \frac{4a}{3}$$

$$r^2 = a^2 - \frac{a^2}{9} = \frac{8a^2}{9}$$

:. Volume =
$$\frac{1}{3}\pi r^2 h = \frac{1}{3}\pi \left(\frac{8a^2}{9}\right) \left(\frac{4a}{3}\right) = \frac{8}{27} \left(\frac{4}{3}\pi a^3\right)$$

Let
$$\frac{1}{x} = u, \frac{1}{y} = v, \frac{1}{z} = w$$

: the system of equations becomes,

$$2u + 3v + 10w = 4$$

$$4u - 6v + 5w = 1$$

$$6u + 9v - 20w = 2$$

$$Let A = \begin{bmatrix} 2 & 3 & 10 \\ 4 & -6 & 5 \\ 6 & 9 & -20 \end{bmatrix}, b = \begin{bmatrix} 4 \\ 1 \\ 2 \end{bmatrix}$$

$$\begin{vmatrix} 6 & 9 & -20 \end{vmatrix} \quad \begin{bmatrix} 2 \\ 2 \end{bmatrix}$$

$$|A| = 1200 \neq 0, A^{-1} = \frac{1}{1200} \begin{bmatrix} 75 & 150 & 75 \\ 110 & -100 & 30 \\ 72 & 0 & -24 \end{bmatrix}, U = A^{-1}b = \frac{1}{1200} \begin{bmatrix} 75 & 150 & 75 \\ 110 & -100 & 30 \\ 72 & 0 & -24 \end{bmatrix} \begin{bmatrix} 4 \\ 1 \\ 2 \end{bmatrix} = \begin{bmatrix} 1/2 \\ 1/3 \\ 1/5 \end{bmatrix}$$

$$\therefore u = 1/2 \Rightarrow x = 2, v = 1/3 \Rightarrow y = 3, w = 1/5 \Rightarrow z = 5$$

25. Solution:

Suppose the mixture contains x kg of food 1 and y kgs of food2.

Then, Cost
$$Z=50x + 70y$$

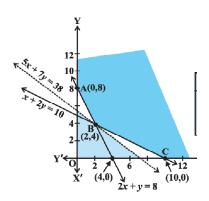
The mathematical formulation of the problem is as follows:

$$Min Z=50x+70y$$

$$2x + y \ge 8$$
 (requirement of VitA)

$$x+2y \ge 10$$
 (requirement of VitC) s.t

$$x \ge 0, y \ge 0$$



We graph the above inequalities. The feasible region as shown in the figure is unbounded. The corner points are A,B and C. The co-ordinates of the corner points are (0,8), (2,4),(10,0).

Corner Point	Z=50x +70y
(0,8)	560
(2,4)	<u>380</u>
(10,0)	500

Thus cost is minimized by mixing 2 units of food $\overline{1}$ and 4 units of food 2 and minimum cost is 380.

26. Solution:

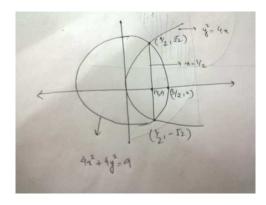
The point of intersection of the curves $y^2=4x$, $4x^2+4y^2=9$:

$$4x^2 + 4(4x) = 9 \Rightarrow 4x^2 - 16x - 9 = 0 \Rightarrow (2x - 1)(2x + 9) = 0$$

 $\Rightarrow x = 1/2, -9/2$

but
$$x = -9/2$$
 is not a possible solution(: $y^2 = -18$, not possible)

$$\therefore x = 1/2 \Rightarrow y = \pm \sqrt{2}$$



The shaded area is the required area.

$$Area = 2 \left[\int_{0}^{1/2} 2\sqrt{x} dx + \int_{1/2}^{3/2} \sqrt{\left(\frac{3}{2}\right)^{2} - x^{2}} dx \right]$$

$$= 2 \left[\frac{2x^{3/2}}{3/2} \Big|_{0}^{1/2} + \left(\frac{x}{2} \sqrt{\left(\frac{9}{4}\right) - x^{2}} + \frac{9}{8} \sin^{-1} \left(\frac{x}{3/2}\right) \right) \Big|_{1/2}^{3/2} \right] = \frac{9}{8} \pi - \frac{9}{4} \sin^{-1} \left(\frac{1}{3}\right) + \frac{5}{6\sqrt{2}}$$