

**NATIONAL TALENT SEARCH EXAMINATION-2019-20, UTTAR PRADESH**  
**SCHOLASTIC APTITUDE TEST (SAT) PAPER & HINTS & SOLUTION**

**PHYSICS**

101. Unit of momentum is  
 (1) meter/second      (2) Newton × meter      (3) kg-meter/second      (4)  $\text{kg}^{-1}$  meter second<sup>-1</sup>

**Ans. (3)**

**Sol.** kg-meter/second

SINCE, MOMENTUM (p) = mass (m) × velocity (v)

Then, unit of 'p' = kg meter/second

102. Which one of the following physical quantity is constant in simple harmonic motion?  
 (1) Restoring force      (2) Kinetic energy      (3) Potential energy      (4) Total energy

**Ans. (4)**

**Sol.** as during simple harmonic motion there is continuous interchange of kinetic energy and potential energy, so total mechanical energy (KE + PE) is conserved.

103. A ray of light passes from glass ( $\mu = \frac{3}{2}$ ) to water ( $\mu = \frac{4}{3}$ ). The value of critical angle will be

- (1)  $\sin^{-1}\left(\frac{1}{2}\right)$       (2)  $\sin^{-1}\left(\sqrt{\frac{8}{9}}\right)$       (3)  $\sin^{-1}\left(\frac{8}{9}\right)$       (4)  $\sin^{-1}\left(\frac{5}{7}\right)$

**Ans. (3)**

**Sol.** As we have refractive index ( $\mu$ ) formula in terms of critical angle (c) as,

$$\mu_1 / \mu_2 = 1/\sin c$$

so, we can write

$$(3/2) / (4/3) = 1/\sin c$$

$$\sin c = 8/9$$

$$c = \sin^{-1}(8/9)$$

$$\text{here, } \mu_1 = \mu_{\text{glass}} = 3/2$$

$$\mu_2 = \mu_{\text{water}} = 4/3$$

104. The value of acceleration due to gravity (g) on the earth will be maximum at  
 (1) surface      (2) poles      (3) equator      (4) center

**Ans. (2)**

**Sol.** since radius of earth at poles are minimum and at equator is maximum

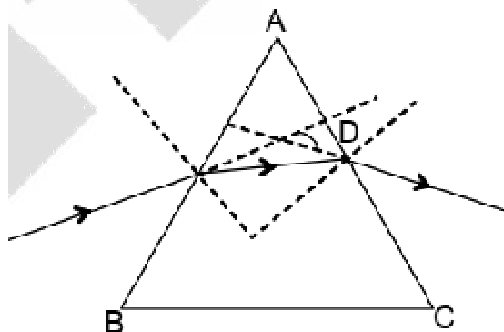
Therefore, acceleration due to gravity increases when we move from equator to poles

105. Which one of the following is an example of Biomass Energy source.  
 (1) Nuclear Energy      (2) Sun energy      (3) Gobar Gas      (4) Wind energy

**Ans. (3)**

**Sol.** since gober gas or bio gas is obtained from decomposition of biomass

106. The refraction of light by a prism is shown in the following figure. Then Angle  $\angle D$  is:



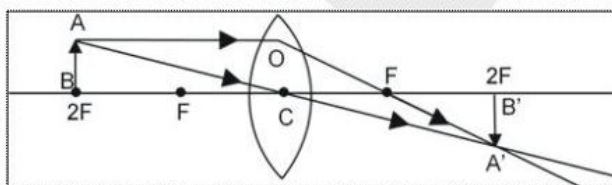
- (1) Angle of prism      (2) Angle of refraction      (3) Angle of emergent      (4) Angle of deviation  
**Ans. (4)**  
**Sol.** since angle of deviation is the angle made between incident ray and emergent ray from the prism.

107. The unit of power of a lens is dioptre. Then one dioptre (1 dioptre) is equal to  
 (1)  $100 \text{ cm}^{-1}$       (2)  $1 \text{ meter}^{-1}$       (3) 1 meter      (4) 100 cm

- Ans. (2)**  
**Sol.** AS S.I. UNIT OF POWER OF LENS IS dioptre (D).  
 FORMULA OF POWER OF LENS ( $P$ ) =  $1/\text{FOCAL LENGTH (in meters)}$   
 $P = 1/f$  (in meters)  
 So,  
 $1 \text{ dioptre} = 1/(\text{meter}) = 1 \text{ meter}^{-1}$

108. If  $F$  be the focal length of a convex lens, then the nature of image of an object placed at a distance of  $2F$  will be  
 (1) Real, inverted and same size      (2) Virtual, erect and small  
 (3) Real, erect and same size      (4) Virtual, inverted and same size

- Ans. (1)**  
**Sol.** When the object is placed at  $2F$



When the object is placed at the centre of curvature of a lens then a ray of light  $AO$  which is parallel to the principal axis after refraction pass through the focus  $F$  along the direction  $OF$ . While the other ray  $AC$  pass through the optical centre  $C$  and goes straight without any deviation. These two refracted light rays intersect each other at point  $A'$ , on the other side of the lens at the centre of curvature  $2F$ . So, the image  $A'B'$  formed in this case is at the centre of curvature, of same size as the object, real and inverted.

109. The power of a plane mirror is  
 (1) Zero      (2)  $+1$       (3)  $-1$       (4) Infinity ( $\infty$ )

- Ans. (1)**  
**Sol.** The power of a mirror is the reciprocal of its focal length. As the focal length of a plane mirror is infinite, its power is zero.  
 $P = 1/f$   
 $P = (1/\infty) = 0$

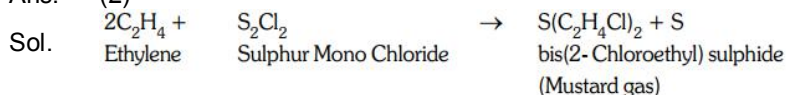
110. The resistance of a wire is  $4\Omega$ . If length of wire is made double and area of cross section is made half, then the new resistance will be  
 (1)  $1\Omega$  (2)  $6\Omega$  (3)  $4\Omega$  (4)  $12\Omega$   
 Ans. (2)  
 Sol. As given in question that old resistance of a wire is = 4 ohm  
 Resistance = Resistivity  $\times$  length/area  
 When the wire is stretched to double the length, the area of cross section gets reduced to half.  
 So  
 New Resistance = Resistivity  $\times$  (2 length) / (area/2)  
 New resistance = (Resistivity  $\times$  length/area)  $\times$  4  
 New resistance = Resistance  $\times$  4  
 So, New resistance =  $4 \times 4 = 16$  ohm
111. Which one of the following alternating current is supplied in our house hold circuits?  
 (1) 110 V and 50 Hz (2) 220 V and 60 Hz (3) 110 V and 60 Hz (4) 220 V and 50 Hz  
 Ans. (4)  
 Sol. In INDIA we work on 50 Hz frequency and 220 V supply in house hold circuits.
112. How much time will be taken by a 100 watt bulb to consume one unit of energy:  
 (1) 1 hour (2) 10 hour (3) 100 hour (4) 1000 hour  
 Ans. (2)  
 Sol. given , power (P) = 100 watt  
 and Energy (E) = 1 unit = 1 kWh = 1000 Wh  
 To find , time(t) = ?  
 energy = power  $\times$  time  
 $E = P \times t$   
 so,  $t = E/P$   $t = 1000/100 = 10$  hour
113. Which one of the following is not a conventional source of energy?  
 (1) Coal (2) Petroleum (3) Hydro (4) Solar energy  
 Ans. (4)  
 Sol. as only solar energy is non conventional as well as renewable source of energy.

## CHEMISTRY

114. Which of the following element is more electro positive?  
 (1) Br (2) F (3) Cl (4) I  
 Ans. (4)  
 Sol. On moving down to the group electropositive character increases because ionization energy decreases as size of atom increases. So in halogens, iodine is the most electropositive element.
115. The name of metal which decomposes water in cold is  
 (1) Cu (2) Pt (3) Ag (4) Na  
 Ans. (4)  
 Sol. According to metal reactivity series Na is more reactive than hydrogen and Pt, Cu and Ag are less reactive than  
 hydrogen.  
 $2\text{Na} + 2\text{H}_2\text{O} \rightarrow 2\text{NaOH} + \text{H}_2$
116. On heating camphor in a porcelain dish it got mixed in air without melting. This phenomenon is known as  
 (1) Condensation (2) Sublimation (3) Suspension (4) Evaporation  
 Ans. (2)  
 Sol. Camphor is an example of sublime substance which upon heating gets converted from solid state into gaseous state without undergoing into liquid state.

117. Ethylene and Sulphur monochloride on heating gives  
 (1) Chloroethane (2) Ethylene chloride (3) Mustard Gas (4) Ethylene glycol

Ans. (2)



118. The  $\text{H}^+$  ion concentration of a solution is  $2 \times 10^{-8} \text{ mol L}^{-1}$ . The pH value of the solution is  
 (1) 7.699 (2) 7.599 (3) 7.799 (4) 7.899

Ans. (1)

Here  $[\text{H}^+]$  of given solution is very less so  $[\text{H}^+]$  from water has to be considered.

$$\begin{aligned} [\text{H}^+]_{\text{total}} &= [\text{H}^+]_{\text{solution}} + [\text{H}^+]_{\text{water}} \\ &= 2 \times 10^{-8} + 10^{-7} \\ &= 10^{-8} (2 + 0.1) \\ [\text{H}^+]_{\text{total}} &= 2.01 \times 10^{-8} \\ \text{pH} &= -\log_{10} [\text{H}^+] \\ &= -\log_{10} (2.01 \times 10^{-8}) \\ &= -\log_{10} 2.01 + (-\log_{10} 10^{-8}) \\ &= -0.3010 + -(-8) \\ &= -0.3010 + 8 \end{aligned}$$

Sol. pH = 7.699

119. Which of the following elements exhibit variable valency?  
 (1) Normal element (2) Typical element (3) Transitional element (4) None of these

Ans. (3)

Sol. The transition elements have their valence electrons into different sets of orbitals i.e.  $(n-1)d$  and  $ns$ . As there is very little difference in the energies of these orbitals. Both energy levels can be used for bond formation. So, transition elements show variable valencies

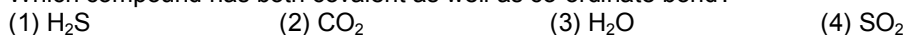
120. Which one is addition reaction?



Ans. (3)

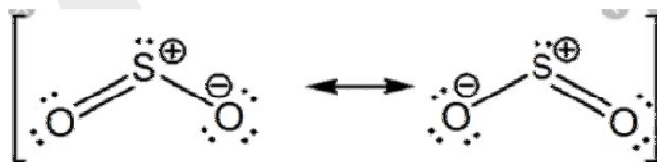
Sol. When two or more reactants combine together to form a product known as addition reaction.

121. Which compound has both covalent as well as co-ordinate bond?



Ans. (4)

Sol. Central sulphur atom is connected to one oxygen by a double bond and to the other by a co-ordinate bond due to presence of lone pair of electron on sulphur atom.



122. Complex salt is



Ans. (4)

Sol. A compound composed of central metal atom having coordinate bonds and with ligands around it, is

123. Calamine is the ore of metal  
 (1) Copper (2) Aluminium (3) Zinc (4) Iron  
 Ans. (3)  
 Sol. The formula of calamine is  $\text{ZnCO}_3$  or it is also known as zinc carbonate
124. Acid used in Lead Batteries is  
 (1) HCl (2)  $\text{H}_2\text{SO}_4$  (3)  $\text{HNO}_3$  (4)  $\text{H}_2\text{CO}_3$   
 Ans. (2)  
 Sol. Sulphuric acid is used in Lead - Acid storage batteries.
125. Which type of ores are concentrated by Froth floatation process?  
 (1) Oxide ores (2) Sulphide ores (3) Carbonate ores (4) Nitrate ores  
 Ans. (2)  
 Sol. Only sulphide ores are concentrated by froth floatation process because pine oil selectively wets the sulphide ores and hence brings it to froth.
126. Which of the following is amphoteric oxide?  
 (1)  $\text{Na}_2\text{O}$  (2)  $\text{SO}_2$  (3)  $\text{Al}_2\text{O}_3$  (4)  $\text{CaO}$   
 Ans. (3)  
 Sol. Aluminium Oxide is amphoteric oxide because it can react with acids as well as base.  
 $\text{Al}_2\text{O}_3 + \text{HCl} \rightarrow \text{AlCl}_3 + \text{H}_2\text{O}$   
 $\text{Al}_2\text{O}_3 + \text{NaOH} \rightarrow \text{NaAlO}_2 + \text{H}_2\text{O}$

## BIOLOGY

127. In human body temperature control centre is  
 (1) Epithalamus (2) Hypothalamus (3) Thalamus (4) Medula oblongata  
 Ans. (2)  
 Sol. Hypothalamus  
 Brain is contral center of our body. Its different part control different function & hypothalamus is control the body temperature.
128. Which factor is responsible for Green House Effect?  
 (1)  $\text{H}_2\text{O}$  (2)  $\text{CO}$  (3)  $\text{SO}_2$  (4)  $\text{CO}_2$   
 Ans. (4)  
 Sol.  $\text{CO}_2$   
 $\text{CO}_2$  trap the UV rays & UV rays donot move out complete to the space & temperature of earth increase. This is green house effect.
129. Which one of the following element is essential for synthesis of Thyroxin Hormones?  
 (1) Zinc (2) Iodine (3) Boron (4) Nitrogen  
 Ans. (2)  
 Sol. Iodine  
 Self explanatory.
130. Smallest unit of classification is  
 (1) Species (2) Class (3) Order (4) Kingdom  
 Ans. (1)  
 Sol. Species
- Kingdome  
 Phylum  
 Class  
 order  
 family  
 Genus  
 Species

TAXONOMIC Classification
131. Which of the following is not a part of the female reproductive system in human beings?  
 (1) Ovary (2) Uterus (3) Fallopian tube (4) Vas defereus

- Ans. (4)  
**Sol.** Vas deferens  
 Vas deferens is part of male reproductive system. which carry sperm
132. Most powerful digestive enzyme occurs in which cell organelles.  
 (1) Mitochondria (2) Chloroplast (3) Golgi body (4) Lysosome  
 Ans. (4)  
**Sol.** Lysosome  
 Lysosome is digestive body of cell & its function to digest unwanted particle of cell & dead cell organelle with help of digestive enzyme so it contain most powerful enzyme.
133. Causative agent of Kala azar (Black fever) is  
 (1) Bacteria (2) Virus (3) Protozoan (4) Fungi  
 Ans. (4)  
**Sol.** Protozoan  
 Kala azar or Black fever is caused by leishmania which is member of protozoa group
134. Unisexual flowers occur in which of the following plants  
 (1) Mustard (2) Tomato (3) Pea (4) Watermelon  
 Ans. (4)  
**Sol.** Watermelon  
 Tomato, mustard, Pea contain male & female reproductive parts in their flower so they are known as bisexual flower.  
 But in watermelon contain either male or female reproductive part so it is known as unisexual flower
135. Biotic components of ecosystem are  
 (1) Producers (2) Consumers (3) Decomposers (4) All of above  
 Ans. (4)  
**Sol.** All of these  
 Producer, consumers, decomposers are living so they all are known as biotic component of ecosystem
136. Which one of the following substance is changed into amino acid after digestion  
 (1) Protein (2) Carbohydrate (3) Fat (4) Nucleic acid  
 Ans. (1)  
**Sol.** Protein is polymer of amino acid  

$$\text{Protein} \xrightarrow{\text{pepsin}} \text{peptides} \xrightarrow{\text{peptidase}} \text{Amino acid.}$$
137. Source of Penicillin antibiotic is  
 (1) Bacteria (2) Fungi (3) Virus (4) Algae  
 Ans. (2)  
**Sol.** Fungi  
 Penicillium is obtain from Penicillium notatum which is a fungi
138. Testosterone Hormone is produced in  
 (1) Leyding cell (2) Kupffer cell (3) Granulosa cell (4) None of above  
 Ans. (1)  
**Sol.** Leyding cells  
 Leyding cells are present in side the testis & they are responsible for secretion of testosterone & This hormone is responsible for secondary sexual character in male. Testis is part of male reproductive system.
139. Number of sex chromosomes in human beings are  
 (1) 23 (2) 46 (3) 1 (4) 2  
 Ans. (4)  
**Sol.** 2  
 Human contain 46 number of chromosome in which 44 are autosomal chromosome & 2 are sex chromosome which are xx in female & xy in male.

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140. Which of the following is known as the 'suicide bag' of the cell?  
(1) Plastid (2) Mitochondria (3) Ribosome (4) Lysosome  
**Ans.** (4)  
**Sol.** Lysosome  
because lysosome contain hydrolytic enzymes & when programming of cell is disturbed then digestive enzymes come out in cytoplasm of cell & it digests its own cell

## **SOCIAL SCIENCE**

141. The Harappan Civilization was discovered in the year  
(1) 1910 (2) 1921 (3) 1935 (4) 1942  
**Ans.** (2)  
**Sol.** It was discovered in 1921 by Rakhal Das Banerjee
142. The First Literary Source is  
(1) Rigveda (2) Samveda (3) Yajurved (4) Atharvaved  
**Ans.** (1)  
**Sol.** As per ancient history first literacy source is Rig veda
143. During whose reign Megasthenes visited to India?  
(1) Ashoka (2) Harsh Vardhan (3) Chandragupta Maurya (4) Kumar Gupta  
**Ans.** (2)  
**Sol.** During the reign of Chandra Gupta Maurya Megasthenes visited India.
144. Which dynasty was ruling over North India at the time of Alexander's invasion?  
(1) Nand (2) Maurya (3) Shunga (4) Kanva  
**Ans.** (2)  
**Sol.** Mauryan Empire was ruling over North India
145. The name of Shershah in childhood was  
(1) Hasan (2) Farid (3) Sher Khan (4) None of the above  
**Ans.** (2)  
**Sol.** Farid was his childhood name of Shershah Suri
146. Which sultan of Delhi has also been called 'A mixture of opposites'?  
(1) Balban (2) Alauddin Khilji  
(3) Mohammad Tughlaq (4) Ibrahim Lodhi  
**Ans.** (3)  
**Sol.** Mohammad Tughlaq was called as opposite of mixture because of his insensible decisions
147. The Emperor was called 'Kalandar'  
(1) Babar (2) Humayun (3) Akbar (4) Shahjahan  
**Ans.** (1)  
**Sol.** Kalandar means honesty (Babar)
148. Famous 'Peacock Throne' was taken away out of India by  
(1) Ahmad Shah Abdali (2) Taimur (3) Dalhousie (4) Nadir Shah  
**Ans.** (4)  
**Sol.** Nadir Shah took away Peacock Throne
149. 'Subsidiary Alliance' was implemented during period of  
(1) Lord Cornwallis (2) Lord Wellesley (3) Sir John Shore (4) Lord Auckland  
**Ans.** (2)  
**Sol.** Lord Wellesley initiated Subsidiary Alliance
150. Which one of the following writing is Not related to Mahatma Gandhi?  
(1) My Experiments with truth (2) Harijan  
(3) Das Capital (4) Hind Swaraj  
**Ans.** (3)

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- Sol.** Das Capital was written by Karl Marx
151. Name the founder of 'Gadar Party'  
 (1) Lal Hardayal (2) Subhash Chandra Bose  
 (3) Madam Cama (4) Madan Lal Dhingra  
**Ans.** (1)  
**Sol.** Lala Hardayal started the 'Gadar Party'
152. Who among the following was not known as Moderate in the Indian National Movement?  
 (1) Bal Gangadhar Tilak (2) Dadabhai Naoroji  
 (3) M.G. Ranade (4) Gopal Krishna Gokhale  
**Ans.** (1)  
**Sol.** Bal Gangadhar Tilak was a moderate while others were extremists
153. The Himalayan mountain range is an example of  
 (1) Block mountain (2) Folding mountain (3) Volcanic mountain (4) Residual mountain  
**Ans.** (2)  
**Sol.** Himalayan mountains are called as Young fold mountains
154. The forest of Ganga-Brahmaputra-delta is known as  
 (1) Evergreen Forest (2) Monsoon Forest (3) Sundar Ban (4) Deciduous Forest  
**Ans.** (3)  
**Sol.** Sundar Ban being the most fertile land are called as deltas where river Ganga and Brahmaputra meet
155. How many districts are in Uttar Pradesh?  
 (1) 70 (2) 75 (3) 80 (4) 85  
**Ans.** (2)  
**Sol.** 75 Districts are there in UP
156. In which continent the Sahara desert is situated  
 (1) South America (2) Africa (3) Asia (4) North America  
**Ans.** (2)  
**Sol.** Sahara desert is situated in Africa
157. The Blue Revolution is related with  
 (1) Food Grain (2) Fish Production (3) Milk Production (4) Oil seed Production  
**Ans.** (2)  
**Sol.** Fish production is called blue rebellion
158. The Oil and Natural Gas Commission (ONGC) was set up in  
 (1) 1956 (2) 1957 (3) 1959 (4) 1961  
**Ans.** (1)  
**Sol.** ONGC was set up in 1956
159. What is the name of Mid Latitude grass land in South America?  
 (1) Prairie (2) Pampas (3) Veld (4) Steppes  
**Ans.** (2)  
**Sol.** Pampas are the name given to Mid Latitude grass land in South America
160. Where Thar Desert is located?  
 (1) Pakistan (2) China (3) India (4) United State of America  
**Ans.** (3)  
**Sol.** Thar desert is located in India
161. Where Gobind Sagar reservoir is situated?  
 (1) Uttar Pradesh (2) Haryana (3) Himanchal Pradesh (4) Punjab  
**Ans.** (3)  
**Sol.** Gobind Sagar reservoir is situated in Punjab



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162. When Tourism day is celebrated?  
(1) 5 January (2) 10 December (3) 5 June (4) 27 September  
**Ans. (4)**  
**Sol.** 27<sup>th</sup> September is celebrated as Tourism day
163. According to Census 2011 the population of U.P. is  
(1) 18.8 Crores (2) 19.98 Crores (3) 24.70 Crores (4) 30.00 Crores  
**Ans. (2)**  
**Sol.** The population of UP according to 2011 report was 19.98 crores
164. I.M.F. was established by the recommendations of which Committee?  
(1) Bretton woods committee (2) Goswami committee  
(3) Narsingham committee (4) None of them  
**Ans. (1)**  
**Sol.** Bretton woods Committee was recommended by International monetary fund during world war II (1944)
165. In which year India devalued its currency for the first time  
(1) 1949 (2) 1966 (3) 1991 (4) None of them  
**Ans. (2)**  
**Sol.** The currency of India was devalued for the first time in the year 1966
166. The least Population State in India is  
(1) Sikkim (2) Mizoram (3) Uttar Pradesh (4) Bihar  
**Ans. (1)**  
**Sol.** Sikkim is the least populated state
167. Where is situated the Headquarter of World Bank?  
(1) Texas (2) Canada (3) Washington (4) Geneva  
**Ans. (3)**  
**Sol.** World Bank is situated in Washington (USA)
168. Who has first developed the theory of Rent?  
(1) Recardo (2) Adam Smith (3) Marshall (4) None of them  
**Ans. (1)**  
**Sol.** David Ricardo developed the theory of Rent
169. Which Canal is largest in the world?  
(1) Panama Canal (2) Ram Ganga Canal (3) Kra Canal (4) Suez Canal  
**Ans. (4)**  
**Sol.** Suez canal is the largest canal which is 193.5 km
170. 'Chipko Movement' was basically against  
(1) Water Pollution (2) Noise Pollution (3) Soil Pollution (4) Deforestation  
**Ans. (4)**  
**Sol.** Deforestation give rise to 'Chipko Movement' against cutting of trees.
171. The President's Rule in a state means that the state is ruled by  
(1) The President (2) The Chief Minister  
(3) The Governor of The State (4) The Prime Minister State  
**Ans. (1)**  
**Sol.** During President's rule in the state, the state is ruled by The President
172. In which year "The Right to Information Act" was passed  
(1) 2001 (2) 2003 (3) 2005 (4) 2007  
**Ans. (3)**  
**Sol.** The Right to Information Act was passed in 2005 by central government

173. The Constitution of India primarily did not include in its preamble  
 (1) Sovereign (2) Socialist (3) Democratic (4) Republic  
**Ans. (2)**  
**Sol.** Socialist was the word which was included in the 42nd Amendment Act 1976
174. Article – 370 was associated with  
 (1) Uttar Pradesh (2) Nagaland (3) Jammu & Kashmir (4) Telangana  
**Ans. (3)**  
**Sol.** Article 370 is related to the state Jammu and Kashmir
175. Who presided over the first meeting of the Indian Constituent Assembly?  
 (1) Sachchidanand Sinha (2) Dr. Rajendra Prasad  
 (3) Dr. B.R. Ambedkar (4) H.V. Kamath  
**Ans. (1)**  
**Sol.** Sachchidanand Sinha presided over the 1st meeting of the Indian Constituent Assembly
176. Who appoints the Chairman of Union Public Service Commission?  
 (1) President (2) Prime Minister (3) Chief Justice of India (4) Vice President  
**Ans. (1)**  
**Sol.** The President of the country appoints the chairman of union Public service commission
177. Which of the following appointments is not made by the President of India?  
 (1) Speaker of The Lok Sabha (2) Chief Justice of India  
 (3) Chief of Army (4) Prime Minister  
**Ans. (1)**  
**Sol.** The Speaker of the Lok Sabha is not appointed by the President of India but he/she elected by the majority in the Lok Sabha
178. The first female speaker of Lok Sabha is  
 (1) Vijay Laxmi Pandit (2) Sucheta Kriplani  
 (3) Tarkeshwari Sinha (4) Meira Kumar  
**Ans. (4)**  
**Sol.** Meira Kumar was the first female speaker in Lok Sabha
179. The state in which Panchayati Raj was introduced first  
 (1) Uttar Pradesh (2) Bihar (3) Rajasthan (4) Gujarat  
**Ans. (3)**  
**Sol.** Rajasthan was the first state in which Panchayati Raj was introduced in 2nd Oct. 1959
180. Who was the first Muslim President in India?  
 (1) Fakhruddin Ali Ahmed (2) Dr. Zakir Hussain  
 (3) Salman Khursheid (4) Dr. Abdul Kalam Azad  
**Ans. (2)**  
**Sol.** Dr. Zakir Hussain was first Muslim president of India

## **MATHEMATICS**

181. Which of the following statement is true?
- (1)  $\left(\frac{1}{2}\right)^{\frac{1}{2}} = \left(\frac{1}{3}\right)^{\frac{1}{3}}$  (2)  $\left(\frac{1}{2}\right)^{\frac{1}{2}} < \left(\frac{1}{3}\right)^{\frac{1}{3}}$
- (3)  $\left(\frac{1}{2}\right)^{\frac{1}{2}} > \left(\frac{1}{3}\right)^{\frac{1}{3}}$  (4)  $\left(\frac{1}{2}\right)^{\frac{1}{2}}$  and  $\left(\frac{1}{3}\right)^{\frac{1}{3}}$  are rational numbers
- Ans. (3)**

**Sol.**  $\left(\frac{1}{2}\right)^{\frac{1}{2}} = \left(\frac{1}{2^3}\right)^{\frac{1}{6}} = \left(\frac{1}{8}\right)^{\frac{1}{6}}$

$$\left(\frac{1}{3}\right)^{\frac{1}{3}} = \left(\frac{1}{3^2}\right)^{\frac{1}{6}} = \left(\frac{1}{9}\right)^{\frac{1}{6}}$$

As  $\frac{1}{8} > \frac{1}{9}$

$$\therefore \left(\frac{1}{8}\right)^{\frac{1}{6}} > \left(\frac{1}{9}\right)^{\frac{1}{6}}$$

So  $\left(\frac{1}{2}\right)^{\frac{1}{2}} > \left(\frac{1}{3}\right)^{\frac{1}{3}}$

- 182.** The mean of 15 observations written in some order is 50. If the mean of first eight observations and last eight observations are 48 and 53 respectively then the eighth observation is

(1) 35 (2) 80 (3) 72 (4) 58

**Ans.** (4)

**Sol.** Mean of 15 observations = 50

Mean of first eight observations = 48

Mean of last eight observations = 53

$\therefore$  Sum of 15 observations =  $15 \times 50 = 750$

Sum of first eight observations =  $8 \times 48 = 384$

Sum of last eight observation =  $8 \times 53 = 424$

$\therefore$  8th observation =  $384 + 424 - 750 = 808 - 750 = 58$

- 183.** The point on the y-axis, which is equidistant from points A(6, 5) and B(-4, 3) is

(1) (9, 0) (2) (0, 9) (3) (0, 4) (4) (0, 3)

**Ans.** (2)

**Sol.** Let the point Y axis is P(0,y)

PA = PB

$$\sqrt{(0-6)^2 + (y-5)^2} = \sqrt{(0+4)^2 + (y-3)^2}$$

$$36 + y^2 - 10y + 25 = 16 + y^2 - 6y + 9$$

$$61 - 25 = 4y$$

$$36 = 4y$$

$$y = 9$$

$\therefore$  Coordinate of point P (0, 9)

- 184.** If  $(\sec \theta - \tan \theta) = k$  where  $k \neq 0$  then the value of  $(\sec \theta + \tan \theta)$  is

(1)  $1 - \frac{1}{k}$  (2)  $1 - k$  (3)  $1 + k$  (4)  $\frac{1}{k}$

**Ans.** (4)

**Sol.** We know  $\sec^2 \theta - \tan^2 \theta = 1$

$$(\sec \theta - \tan \theta)(\sec \theta + \tan \theta) = 1$$

$$k(\sec \theta + \tan \theta) = 1$$

$$\frac{1}{k}$$

**185.** The value of k for which the system of linear equation  $x + 2y = 5$  and  $3x + ky = 15$  has no solution, is

(1) 6

(2) - 6

(3)  $\frac{3}{2}$

(4)  $\frac{2}{3}$

**Ans.** Bouns

$$x + 2y = 5$$

$$3x + ky = 15$$

For no solutions

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

$$\frac{1}{3} = \frac{2}{k} \neq \frac{5}{15}$$

$$\frac{1}{3} = \frac{2}{k} \text{ and } \frac{2}{k} \neq \frac{5}{15}$$

$$k = 6 \text{ and } k \neq 6$$

**OR**

**Sol.** System of linear equations  $x + 2y = 5$  and  $3x + ky = 15$  has no solution

By using condition of no solution

$$\Rightarrow \frac{1}{3} = \frac{2}{k} \neq \frac{-5}{-15}$$

$$\left( \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2} \right)$$

$$\Rightarrow \frac{1}{3} = \frac{2}{k} \neq \frac{1}{3}$$

$$\Rightarrow \frac{1}{3} = \frac{2}{k} \text{ and } \frac{2}{k} \neq \frac{1}{3}$$

$$\Rightarrow k = 6 \text{ and } k \neq 6$$

Hence contradiction.

$\therefore$  None of the options is correct.

**186.** If  $x = 1$  is a common root of the equations  $ax^2 + ax + 3 = 0$  and  $x^2 + x + b = 0$  then the value of ab is

(1) 3

(2) 3.5

(3) 6

(4) - 3

**Ans.** (1)

**Sol.** Given,  $x = 1$  is a common root of the equations  $ax^2 + ax + 3 = 0$  and  $x^2 + x + b = 0$

$$\therefore ax^2 + ax + 3 = 0$$

$$a(1)^2 + a(1) + 3 = 0$$

$$a + a + 3 = 0$$

$$2a + 3 = 0$$

$$a = \frac{-3}{2}$$

$$\text{and } x^2 + x + b = 0$$

$$1^2 + 1 + b = 0$$

$$1 + 1 + b = 0$$

$$2 + b = 0$$

$$b = -2$$

$$\therefore ab = \left( \frac{-3}{2} \right)(2) = 3$$

**187.** If points  $(a, 0)$ ,  $(0, b)$  and  $(1, 1)$  are collinear, then the value of  $\left( \frac{1}{a} + \frac{1}{b} \right)$  is

(1) 1

(2) 2

(3) 0

(4) - 1

**Ans.** (1)

**Sol.** As the point (a, 0), (0, b) and (1, 1) are collinear.

$$\therefore \Delta = 0$$

$$\frac{1}{2} |a(b-1) + 0(1-0) + 1(0-b)| = 0$$

$$|ab - a + 0 - b| = 0$$

$$ab = a + b$$

$$1 = \frac{a+b}{ab}$$

$$1 = \frac{1}{a} + \frac{1}{b}$$

**188.** If the centroid of the triangle formed by points (a, b), (b, c) and (c, a) is at the origin, then  $a^3 + b^3 + c^3$  is equal to

(1) abc

(2) 0

(3)  $a + b + c$

(4) 3abc

**Ans.** (4)

**Sol.** Given ; Coordinates of vertices of triangle are

A(a, b), B(b, c) and C(c, a)

$$\therefore \text{Coordinates of centroid } G\left(\frac{a+b+c}{3}, \frac{b+c+a}{3}\right)$$

since centroid is at the origin

$$\text{Therefore, } G\left(\frac{a+b+c}{3}, \frac{b+c+a}{3}\right) = (0, 0)$$

$$\therefore \frac{a+b+c}{3} = 0$$

$$\Rightarrow a + b + c = 0$$

$$\Rightarrow a + b = -c$$

$$\Rightarrow (a + b)^3 = (-c)^3$$

$$\Rightarrow a^3 + b^3 + 3ab(a + b) = -c^3$$

$$\Rightarrow a^3 + b^3 + 3ab(-c) = -c^3$$

$$\Rightarrow a^3 + b^3 - 3abc = -c^3$$

$$\Rightarrow a^3 + b^3 + c^3 = 3abc$$

**189.** The distance between the points  $(\cos \theta, \sin \theta)$  and  $(\sin \theta, -\cos \theta)$  is

(1)  $\sqrt{3}$

(2)  $\sqrt{2}$

(3) 2

(4) 1

**Ans.** (2)

$$\text{Sol. } AB = \sqrt{(\cos \theta + \sin \theta)^2 + (\sin \theta + \cos \theta)^2}$$

$$= \sqrt{\cos^2 \theta + \sin^2 \theta - 2\sin \theta \cos \theta + \sin^2 \theta + \cos^2 \theta + 2\sin \theta \cos \theta} = \sqrt{1+1} = \sqrt{2}$$

**190.** If 35% of income of A is equal to 25% of income of B then the ratio of incomes of A and B is

(1) 4:3

(2) 5:7

(3) 7:5

(4) 4:3

**Ans.** (2)

**Sol.** 35% of income of A = 25% of income of B

$$\frac{35}{100} \times I_A = \frac{25}{100} \times I_B$$

$$\frac{I_A}{I_B} = \frac{25}{100} \times \frac{100}{35} = \frac{5}{7}$$

**191.** If the ratio of volumes of two cubes is 27:64 then the ratio of their surface area is

(1) 3:4

(2) 4:3

(3) 9:16

(4) 16:9

**Ans.** (3)

**Sol.** Given, Ratio of volumes of two cubes = 27 : 64

$\therefore$  Ratio of volumes = (Ratio of sides of two cubes)<sup>3</sup>

$$27 : 64 = (\text{Ratio of sides of two cubes})^3$$

$\therefore$  Ratio of sides of two cubes = 3 : 4

Now, Ratio of surface area = (Ratio of sides)<sup>2</sup>

$$= \left(\frac{3}{4}\right)^2 = \frac{9}{16} = 9 : 16$$

**192.** If the base of a triangle is decrease by 30% and its height is increased by 25% then percentage decrease in area of triangle is

(1) 20%

(2) 15%

(3) 22.5%

(4) 12.5%

**Ans.** (4)

**Sol.** Let the base and height of triangle are b and h respectively

$$\text{Original Area} = \frac{1}{2}bh$$

Now, base is decreased by 30% and height is increased by 25%

$$\therefore \text{New Area} = \frac{1}{2}\left(b - \frac{30}{100}b\right)\left(h + \frac{25}{100}h\right) = \frac{1}{2}\left(\frac{70}{100}b\right)\left(\frac{125}{100}h\right) = \frac{1}{2} \times \frac{7}{10} \times \frac{5}{4}bh = \frac{7}{16}bh$$

$$\% \text{ Change} = \frac{\text{Change in area}}{\text{original area}} \times 100$$

$$= \frac{\frac{1}{2}bh - \frac{7}{16}bh}{\frac{1}{2}bh} \times 100 = \frac{\frac{1}{2} - \frac{7}{16}}{\frac{1}{2}} \times 100 = \frac{\frac{8-7}{16}}{\frac{1}{2}} \times 100 = \frac{\frac{1}{16}}{\frac{1}{2}} \times 100 = \frac{1}{8} \times 100 = 12.5\%$$

**193.** The equation of the base of an equilateral triangle is  $x + y - 2 = 0$ . If one its vertex is (2, -1) then area of triangle is

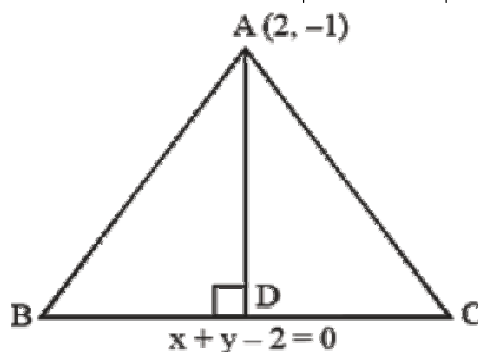
(1)  $\frac{1}{2\sqrt{3}}$  sq. unit

(2)  $\frac{\sqrt{3}}{12}$  sq. unit

(3)  $\frac{2}{3}$  sq. unit

(4)  $\frac{3\sqrt{3}}{4}$  sq. unit

**Sol.** Length of  $l^r$  distance from  $(x_1, y_1)$  to  $ax + by + c = 0$  is  $\left| \frac{ax_1 + by_1 + c}{\sqrt{a^2 + b^2}} \right|$



$$\therefore AD = \left| \frac{2(1) + (-1)(1) - 2}{\sqrt{1^2 + 1^2}} \right| = \frac{1}{\sqrt{2}}$$

$$(\text{AD}) \text{ Altitude of equilateral } \Delta = \frac{\sqrt{3}}{2} \text{ side} = \frac{1}{\sqrt{2}}$$

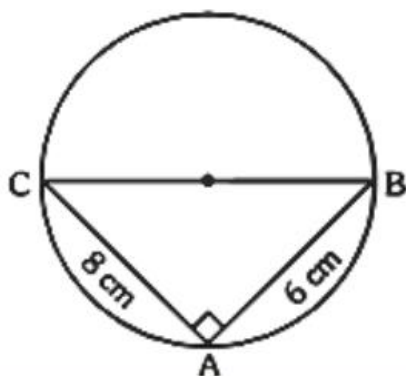
$$\text{side} = \sqrt{\frac{2}{3}}$$

$$\Rightarrow \text{Ar. eq. } \Delta = \sqrt{\frac{3}{4}} \text{side}^2 = \frac{\sqrt{3}}{4} \left( \frac{\sqrt{2}}{\sqrt{3}} \right)^2 = \frac{1}{2\sqrt{3}}$$

194. The lengths of chords AB and AC of a circle are 6 cm and 8 cm respectively. If  $\angle BAC = 90^\circ$  then the radius of the circle is

- (1) 2.5 cm                      (2) 3 cm                      (3) 4 cm                      (4) 5 cm
- Ans. (4)**

**Sol.**



In  $\triangle ABC$

$$AB^2 + AC^2 = BC^2 \text{ (Pythagoras Theorem)}$$

$$6^2 + 8^2 = BC^2$$

$$10^2 = BC^2$$

$$10 \text{ cm} = BC$$

$$BC = 10 \text{ cm}$$

It is given that  $\angle BAC = 90^\circ$

BC is diameter of circle. ( $\because$  Angle in semicircle is  $90^\circ$ )

Therefore radius is 5 cm

195. If  $\cos 43^\circ = \frac{x}{\sqrt{x^2 + y^2}}$  then the value of  $\tan 47^\circ$  is

(1)  $\frac{y}{x}$

(2)  $\frac{y}{\sqrt{x^2 + y^2}}$

(3)  $\frac{x}{y}$

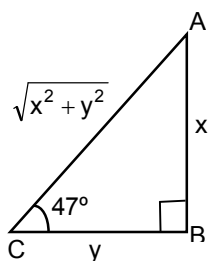
(4)  $\frac{x}{\sqrt{x^2 + y^2}}$

**Ans. (3)**

**Sol.**  $\cos 43^\circ = \frac{x}{\sqrt{x^2 + y^2}}$

We know  $\cos 43 = \sin (90 - 43)$

$$\frac{x}{\sqrt{x^2 + y^2}} = \sin 47^\circ$$



$$AC = \sqrt{x^2 + y^2}$$

$$AB = x$$

$$\therefore CB = \sqrt{AC^2 - AB^2} = y$$

$$\therefore \tan 47^\circ = \frac{AB}{BC} = \frac{x}{y}$$

- 196.** If the quadratic equations  $2x^2 + 4x + (a + 5) = 0$  have equal roots and  $(a + 4)x^2 + ax - 3b = 0$  have distinct real roots then which of the following is true:

- (1)  $a = -3, b < \frac{3}{4}$       (2)  $a = 3, b > \frac{3}{4}$       (3)  $a = -3, b > \frac{3}{4}$       (4)  $a = 3, b < \frac{3}{4}$

**Ans.** (3)

**Sol.** Equation  $2x^2 + 4x + (a + 5) = 0$  have equal roots

$$\therefore B^2 - 4AC = 0$$

$$4^2 - 4(2)(a+5) = 0$$

$$16 - 8(a + 5) = 0$$

$$8(2 - a - 5) = 0$$

$$8(-3 - a) = 0$$

$$-3 - a = 0$$

$$a = -3$$

Equation  $(a + 4)x^2 + ax - 3b = 0$  have real and distinct roots

$$B^2 - 4AC > 0$$

$$a^2 - 4 \times (a + 4) \times (-3b) > 0$$

$$a^2 + 12(a + 4)b > 0$$

$$(-3)^2 + 12(-3 + 4)b > 0$$

$$9 + 12b > 0$$

$$b > \frac{-9}{12}$$

$$b > \frac{-3}{4}$$

$$a = -3 \text{ and } b > \frac{-3}{4}$$

- 197.** The value of  $\tan 1^\circ \tan 2^\circ \dots \tan 89^\circ$  is:

- (1) 0      (2) 1      (3)  $\frac{1}{\sqrt{3}}$       (4) not defined

**Ans.** (2)

**Sol.**  $\tan(90^\circ - \theta) = \cot \theta$

$$\Rightarrow \tan 89^\circ \tan 90^\circ - 1^\circ$$

$$\tan 89^\circ = \cot 1^\circ$$

$$\Rightarrow \tan 88^\circ \tan (90^\circ - 2^\circ)$$

$$\tan 88^\circ \cot 2^\circ$$

$$\tan 1^\circ \tan 2^\circ \dots \tan 44^\circ \tan 45^\circ \tan 46^\circ \dots \tan 88^\circ \tan 89^\circ$$



$$= \tan 1^\circ \tan 2^\circ \dots \tan 44^\circ \tan 45^\circ \cot 44^\circ \dots \cot 2^\circ \cot 1^\circ$$

$$= \tan 1^\circ \tan 2^\circ \dots \tan 44^\circ \times 1 \times \frac{1}{\tan 44^\circ} \times \dots \times \frac{1}{\tan 2^\circ} \times \frac{1}{\tan 1^\circ} = 1$$

198. The digit at the unit place in  $(3157)^{2020}$  is

- (1) 1 (2) 3 (3) 7 (4) 9

Ans. (1)

Sol. Unit place digit is depend on powers of unit digit

$$= \text{unit digit of } (3157)^{2020}$$

$$= \text{unit digit of } 7^{2020}$$

$$= \text{unit digit of } 7^{4 \times 505}$$

$$= \text{unit digit of } (7^4)^{505} \quad (\text{Cyclicity of 7 is 4})$$

$$= \text{unit digit of } (2401)^{505}$$

$$= \text{unit digit of } (1)^{505}$$

$$\therefore \text{Unit place digit is 1}$$

199. A metallic cuboid of dimension 9 cm × 11 cm × 12 cm is melted and recasted into spherical balls of diameter 0.3 cm. The number of balls will be

- (1) 84000 (2) 10500 (3) 78000 (4) 86000

Ans. (1)

Sol. Volume of cuboid = N × Volume of sphere

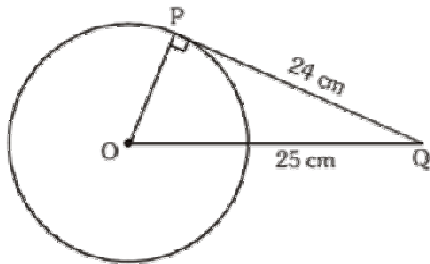
$$9 \times 11 \times 12 = N \times \frac{4}{3} \times \frac{22}{7} \times \frac{3}{20} \times \frac{3}{20} \times \frac{3}{20}$$

$$(\text{No of balls}) N = 84000$$

200. The length of tangent drawn from a point Q to a circle is 24 cm and distance from Q from the centre of circle is 25 cm. The radius of circle is

- (1) 7 cm (2) 12 cm (3) 15 cm (4) 24.5 cm

Ans. (1)



Sol.

$OP \perp PQ$   
In  $\triangle OPQ$

$$OP = \sqrt{OQ^2 - PQ^2} = \sqrt{25^2 - 24^2} = 7$$