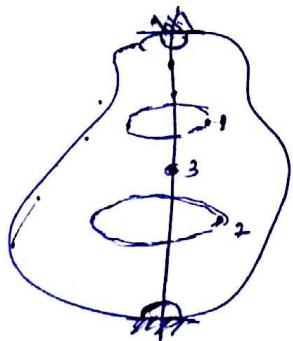


Rotation:-

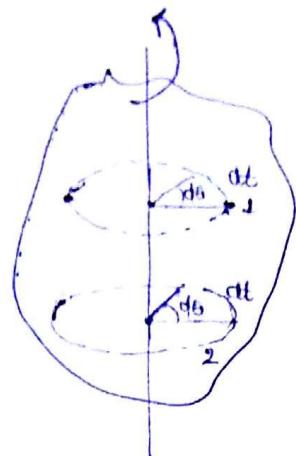


Particle on ~~axis~~ -at rest  
Other- rotation

$$\vec{v} = 0; \vec{a} = 0$$

In rotation, all the particles are in circular motion ~~with~~ [except which are lying on axis of rot"] and their centers will lie on a line which should remain fixed called axis of rotation.

## kinematic :-



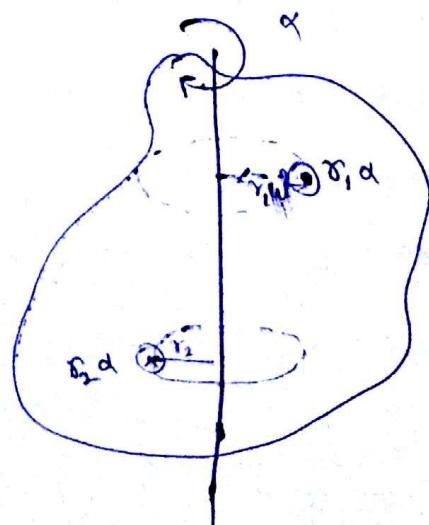
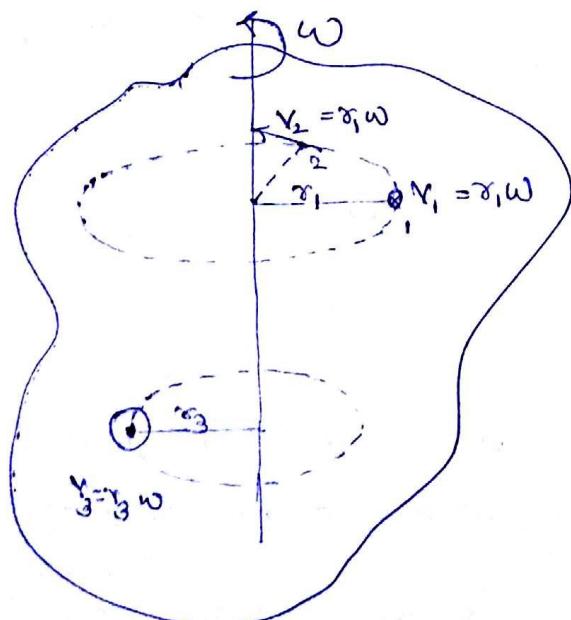
$$\vec{\omega}_1 = \vec{\omega}_2 = \vec{\omega}_3 = \vec{\omega}$$

$$\vec{\alpha}_1 = \vec{\alpha}_2 = \vec{\alpha}_3 = \cancel{\vec{\alpha}} \vec{\alpha}$$

Dir<sup>n</sup> of  $\vec{\omega}$  &  $\vec{\alpha}$  will be along axis of rotation & will be decided by right hand thumb rule.

In rotation  $\vec{\omega}$  &  $\vec{\alpha}$  will be same for each and every particle.

$\vec{v}$  &  $\vec{a}$

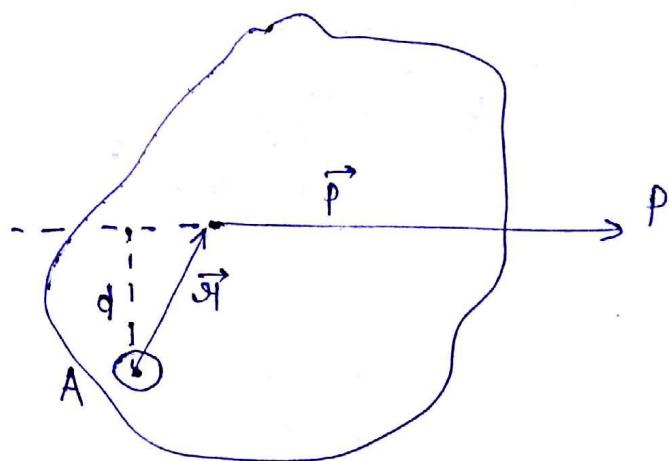


Velocity vector and acc<sup>n</sup> vector of each and every particle are dependent on their location from their ~~position~~ ~~from axis~~ axis of rotation and can be calculated by considering their circular motion

Angular Momentum ( $\vec{L}$ ) : — (Moment of momentum)

$$\vec{L} = \vec{\omega} \times \vec{P}$$

$$\vec{P} = m \vec{V}_{cm}$$

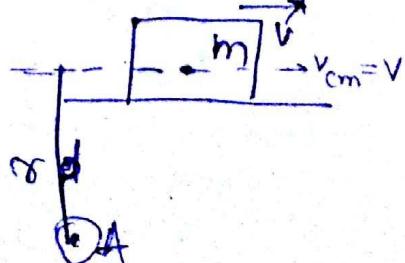


$$\boxed{\vec{L}_A = \vec{\omega} \times \vec{P}}$$

$$\boxed{|\vec{L}_A| = Pd = mV_{cm}d}$$

$\vec{D}_{cm} \rightarrow \perp$  inward.

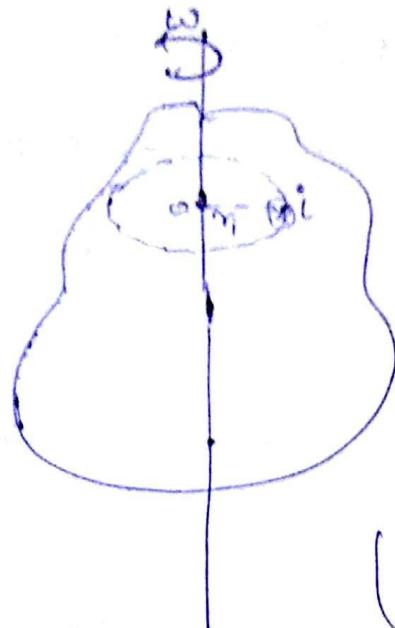
Case-1 Rectilinearly translating body



$$\boxed{L_A = mV_{cm}\vec{\omega} = mV\vec{\omega}}$$

Case-2

Pure rotation



$$\vec{P}_i = m \vec{V}_i$$

$$\vec{V}_i = \vec{\omega} \times \vec{r}_i$$

$$(\vec{L}_i)_0 = \vec{\omega}_i \times \vec{P}_i$$

$$(\vec{L}_i)_0 = \vec{\omega}_i \cdot \vec{P}_i$$

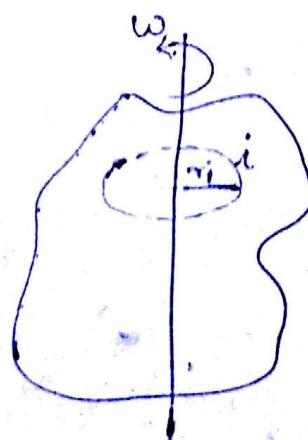
$$\sum_{i=1}^N (\vec{L}_i)_0 = (\vec{L})_{\text{Axis of rotation}} = \sum_{i=1}^N \vec{\omega}_i \cdot \vec{r}_i \times \vec{r}_i \cdot \vec{\omega}$$

$$= \vec{\omega} \sum_{i=1}^N M_i r_i^2$$

$$(\vec{L})_{\text{A.o.r.}} = I_{\text{Axis}} \vec{\omega}$$

$$\vec{L} = I \vec{\omega}$$

Kinetic Energy :-



$$(K.E.)_i = \frac{1}{2} m_i v_i^2 = \frac{1}{2} m_i (\omega_i r_i)^2$$

$$K.E. = \frac{1}{2} \omega^2 \sum_{i=1}^N m_i r_i^2 = \frac{1}{2} I \omega^2$$

$$\boxed{K.E. = \frac{1}{2} I \omega^2}$$

Similarly

$$\boxed{\text{Torque, } T = I \alpha}$$

$$\boxed{\text{work done} = T d\theta}$$

$$\boxed{\text{Power} = \frac{T d\theta}{dt} = T \omega}$$

Power = Rate of doing work

$$\text{Power} = \frac{\vec{F} \cdot \vec{dS}}{dt}$$

$$\boxed{\text{Power} = \vec{F} \cdot \vec{V}}$$

Rate of change of angular momentum.  $\rightarrow$

$$\boxed{\vec{\tau} = \frac{d\vec{L}}{dt}}$$

## Conservation of Angular Momentum ( $\vec{L}$ )

$$\vec{L} \rightarrow \text{Const.}$$

$$\Rightarrow \vec{d}\vec{L} = 0, \text{ when } \vec{T} = 0$$

If the net torque on a system about a point or line is zero, then angular momentum will remain conserved about the point or line.

$$\frac{d\vec{L}}{dt} = \vec{T}$$

$$\underbrace{\vec{T} dt}_{\text{angular impulse}} = \underbrace{d\vec{L}}_{\text{change in momentum}}$$

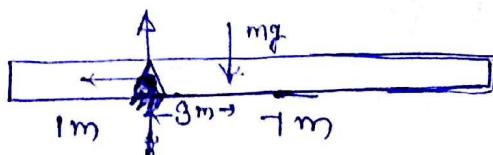
Angular impulse. change in momentum

Q.2.11

P.g. 72

$$m=3\text{kg}$$

$$l=8\text{m}$$



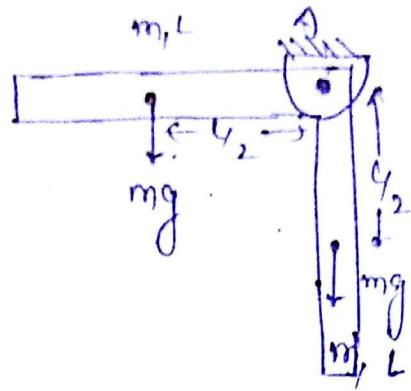
$$T_A = I_A \alpha$$

$$mg \times 3 = [I_{cm} + m \times 3^2] \times \alpha$$

$$8 \times 9.81 \times 3 = \left[ \frac{3 \times 8^2}{12} + 3^2 \right] \times \alpha$$

$$\alpha = 2.05 \text{ rad/sec}^2$$

Prob.



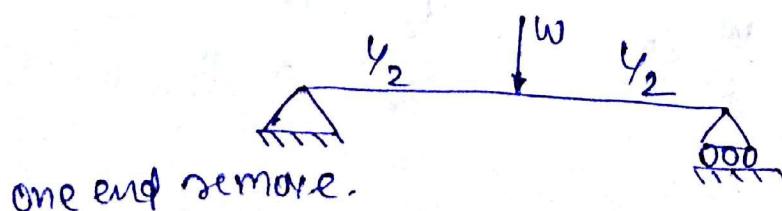
$$T = mg \frac{\theta_2}{L} = I_B \alpha$$

$$mg \frac{\theta_2}{L} = \left[ \frac{ml^2}{3} + \frac{ml^2}{3} \right] \alpha$$

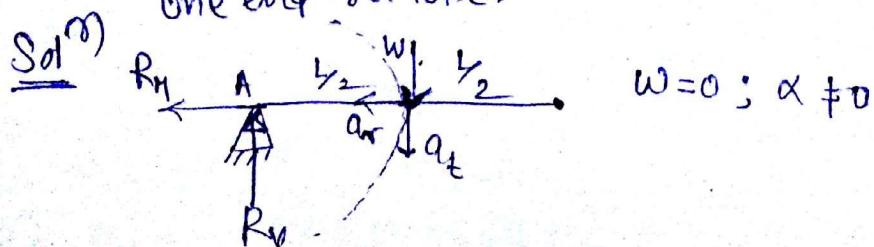
$$\frac{mg}{2} = \frac{2}{3} ml \alpha$$

$$\alpha = \frac{3g}{4l}$$

Quest A uniform beam of weight  $w$  and length  $L$  is simply supported at its both ends if one of the support is suddenly removed then the reaction at other support at the instance of removal is?



one end remove.



$$T_x = I_n \alpha$$

$$w \times \frac{L}{2} = \frac{w L^3}{g \times 3} \times \alpha$$

$$\alpha = \frac{3g}{2L}$$

$$\Rightarrow w - R_v \neq 0$$

$$w - R_v = \frac{w}{g} (a_{cm}) \xrightarrow[-g]{\text{dis}}$$

$$w - R_v = \frac{w}{g} \times \frac{L}{2} \times \frac{3g}{2L} \quad a_t = \frac{L}{2} \alpha$$

$$R_v = \frac{w}{4} \quad \underline{\text{Ans}}$$

$$R_H = \frac{w}{g} (a_{cm}) \xrightarrow[-x]$$

$$R_H = \frac{w}{g} (a_{cm})_x$$

$$R_H = \frac{w}{g} [0]$$

$$Q_H = \gamma w^2$$

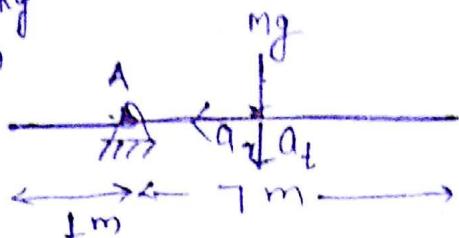
$$Q_H = 0 \quad \text{Bcz } w = 0.$$

$$R_H = 0$$

Prob

$$m = 3 \text{ kg}$$

$$L = 8 \text{ m}$$



Find the reaction at the support for the instant shown in fig taking  $\omega = 2 \text{ rad/s}$

$$T = I \alpha$$

$$\cancel{mg} = mg \times 3 = \left( \frac{mL^2}{3} + m(3)^2 \right) \alpha$$

$$3 \times 9.81 \times 3 = \left( \frac{3 \times 8^2}{3} + 3 \times 3^2 \right) \alpha$$

$$\alpha = 2.05 \text{ rad/s}^2$$

$$(mg - R_V) = m(a_{cm})_t = m\tau \alpha$$

$$3 \times 9.81 - R_V = 3 \times 3 \times 2.05$$

$$R_V = 10.98 \text{ N}$$

$$R_H = m(a_{cm})_r = m\tau\omega^2$$

$$R_H = 3 \times 3 \times 2^2$$

$$R_H = 36 \text{ N}$$