

DPP No. 29

Total Marks: 33

Max. Time : 33 min.

Topics :	Continuity & Derivability, Straight Line, Application of Derivatives, Method of Differentiation
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Type of Questions			M.M., Min.	
Single choice Objective (no negative marking) Q.1,2	(3 marks, 3 min.)	[6,	6]	
Multiple choice objective (no negative marking) Q.3,4,5	(5 marks, 4 min.)	[15,	12]	
Subjective Questions (no negative marking) Q.6,7,8	(4 marks, 5 min.)	[12,	15]	

**1.** Let f(x) be defined as follows :

$$f(x) = \begin{cases} (\cos x - \sin x)^{\cos e c x} &, & -\frac{\pi}{2} < x < 0 \\ a &, & x = 0 \\ \frac{e^{1/x} + e^{2/x} + e^{3/x}}{ae^{2/x} + be^{3/x}} &, & 0 < x < \frac{\pi}{2} \end{cases}$$

If f(x) is continuous at x = 0, then (a, b) =

(A)  $\left( e, \frac{1}{e} \right)$  (B)  $\left( \frac{1}{e}, e \right)$  (C) (e, e) (D)  $(e^{-1}, e^{-1})$ 

2. If  $ax^2 + bx + c = 0$  has imaginary roots and a - b + c > 0, then the set of points (x, y) satisfying the equation

$$\left| a\left(x^{2}+\frac{y}{a}\right)+(b+1)x+c \right| = |ax^{2}+bx+c|+|x+y|$$

consists of the region in the xy-plane which is

(A) on or above the bisector of I and III quadrant (B) on or above the bisector of II and IV quadrant (C) on or below the bisector of I and III quadrant (D) on or below the bisector of II and IV quadrant the bisector of II and IV quadrant (D) on or below the bisector of II and IV quadrant the bisector of II and IV quadrant (D) on or below the bisector of II and IV quadrant the bisector of II and IV quadrant (D) on or below the bisector of II and IV quadrant the bisector of II and IV quadrant (D) on or below the bisector of II and IV quadrant the bisector of II and IV quadrant (D) on or below the bisector of II and IV quadrant the bisecto

- 3. Equation of a tangent to the curve y cot  $x = y^3 \tan x$  at the point where the abscissa is  $\pi/4$ , is: (A)  $4x + 2y = \pi + 2$ (B)  $4x - 2y = \pi + 2$ (C) x = 0(D) y = 0
- 4. If the tangent to the curve  $2y^3 = ax^2 + x^3$  at the point (a, a) cuts off intercepts  $\alpha$ ,  $\beta$  on co-ordinate axes, where  $\alpha^2 + \beta^2 = 61$ , then the value of 'a' is equal to : (A) 20 (B) 25 (C) 30 (D) - 30
- 5. The equation of tangents to the curve  $y = \cos (x + y)$ ,  $-2\pi \le x \le 2\pi$ , that are parallel to the line x + 2y = 0 is/are : (A)  $x + 2y = \pi/2$  (B)  $x + 2y = -3\pi/2$  (C)  $x - 2y = \pi/2$  (D)  $x - 2y = -3\pi/2$

6. If 
$$\left(\frac{x+b}{2}\right) = a \tan^{-1} (a \ln y), a > 0$$
, then prove that  $yy'' - yy' \ln y = (y')^2$ 

- 7. Find the equation of the normal to the curve  $y = (1 + x)^{y} + \sin^{-1}(\sin^{2} x)$  at x = 0
- 8. If x = a(t + sin t), y = a(1 cost), then find

(i) 
$$\frac{dy}{dx}$$
 (ii)  $\frac{d^2y}{dx^2}$  (iii)  $\frac{d^3y}{dx^3}$ 

## **Answers Key**

- (B)
  (B)
  (A)(B)(D)
  (C)(D)
  (A)(B)
  y + x 1 = 0
- 8. If(i)  $\tan \frac{t}{2}$  (ii)  $\frac{1}{2a} \sec^4\left(\frac{t}{2}\right)$ (iii)  $\frac{1}{a^2} \sec^6\left(\frac{t}{2}\right) \tan\left(\frac{t}{2}\right)$