

Solution

1.

(b) distributive property

Explanation: Distributive property

2.

(b) Option (b)

Explanation: By options,

a. $-5 + 3 = -2$ and $3 + (-5) = -2$, which are equal.

b. $\frac{-8}{12} = \frac{10}{-15} \Rightarrow \frac{-2}{3} = \frac{-2}{3}$, which are equal.

c. 2 is not natural number.

d. 17 is not prime number.

3. **(a)** 8

Explanation: $\frac{x-5}{3} = \frac{x-3}{5}$

by cross multiplication

or, $5(x - 5) = 3(x - 3)$

or, $5x - 25 = 3x - 9$

by transposing

or, $5x - 3x = -9 + 25$

or, $2x = 16$

or, $x = \frac{16}{2}$

or, $x = 8$

4.

(d) $\frac{5}{7}$

Explanation: Given equation is

$$\frac{1}{2}(3y + 1) - \frac{-1}{3}(5y + 2) = y - 1$$

To remove fractions, we multiply the equation on both sides by LCM of 2 & 3 i.e

$$6\left[\frac{1}{2}(3y + 1) - \frac{-1}{3}(5y + 2)\right] = 6(y - 1)$$

$$\Rightarrow 3(3y + 1) - 2(5y + 2) = 6y - 6$$

$$\Rightarrow 9y + 3 - 10y - 4 = 6y - 6$$

$$\Rightarrow 9y - 10y - 6y = -6 + 4 - 3$$

$$\Rightarrow -7y = -5$$

$$\Rightarrow y = \frac{5}{7}$$

5.

(d) $30^\circ, 150^\circ, 30^\circ, 150^\circ$

Explanation: Let the adjacent angles of a parallelogram be x and $5x$, respectively.

Then, $x + 5x = 180^\circ$ [\because adjacent angles of a parallelogram are supplementary]

$$\Rightarrow 6x = 180^\circ$$

$$\Rightarrow x = 30^\circ$$

\therefore The adjacent angles are 30° and 150° .

Hence, the angles are $30^\circ, 150^\circ, 30^\circ, 150^\circ$ [\because opposite angles are equal]

6.

(b) trapezium

Explanation: In $\triangle BAD$,

$$\angle BDA = \angle BAD = 57^\circ \text{ (isos. } \triangle \text{ property) In } \triangle BDC,$$

$$\angle BCD = \angle BDC = 66^\circ \text{ (isos } \triangle \text{ property)}$$

$$\therefore \angle D = 57^\circ + 66^\circ = 123^\circ = 180^\circ$$

$$\angle A + \angle D + \angle C = 123^\circ + 66^\circ = 189^\circ$$

$$\text{Also, } \angle D + \angle C = 123^\circ + 66^\circ = 189^\circ$$

Hence, by the property that co-int. angles are supplementary therefore lines are parallel, we have

AB || DC and AD not || BC

Hence, ABCD is a trapezium.

7.

(b) $\frac{1}{26}$

Explanation: There are 2 red king out of 52 cards. So the probability that the card is drawn is a red king $\frac{2}{52} = \frac{1}{26}$

8. (a) 1521

Explanation: $39^2 = 39 \times 39 = 1521$

9. (a) 1.3824×10^7 cu. cm

Explanation: Side of cubical box = 2.4 m

$$\therefore \text{Volume} = (\text{side})^3 = (2.4 \text{ m})^3$$

$$= 13.824 \text{ m}^3 = 13.824 \times 10^6 \text{ cm}^3$$

$$= 1.3824 \times 10^7 \text{ cm}^3$$

10.

(c) $\frac{-7}{11}$

Explanation: $\sqrt[3]{\frac{-343}{1331}} = \frac{\sqrt[3]{-343}}{\sqrt[3]{1331}} = \frac{\sqrt[3]{-7 \times -7 \times -7}}{\sqrt[3]{11 \times 11 \times 11}} = \frac{-7}{11}$

11.

(c) ₹ 85,400

Explanation: Value of the vehicle after 3 years

$$= 1,75,000 \times \left(1 - \frac{20}{100}\right)^3$$

$$= 1,75,000 \times \frac{4}{5} \times \frac{4}{5} \times \frac{4}{5} = ₹ 89,600$$

$$\therefore \text{Total depreciation} = 1,75,000 - 89,600$$

$$= ₹ 85,400$$

12.

(c) 25

Explanation: Let the total matches be = x

According to question,

$$x \times \frac{40}{100} = 10$$

$$\text{or, } x = \frac{10}{40} \times 100$$

$$\text{or, } x = 25 \text{ matches}$$

13.

(b) $(r - 7)(r - 3)$

Explanation: We have, $r^2 - 10r + 21$

$= r^2 - 7r - 3r + 21 = r(r - 7) - 3(r - 7)$ [by splitting the middle term, so that the product of their numerical coefficients is equal constant term]

$$= (r - 7)(r - 3) [\because x^2 + (a + b)x + ab = (x + a)(x + b)]$$

14.

(b) 1.25 m

Explanation: Let r and h be the radius and depth of well respectively.

Volume of earth dug out = $\pi r^2 h$

$$= \frac{22}{7} \times \frac{3.5}{2} \times \frac{3.5}{2} \times 12 = 115.5 \text{ m}^2$$

Let x be the height of platform.

Now, volume of platform = volume of earth dug out
 $\Rightarrow 10.5 \times 8.8 \times x = 115.5 \Rightarrow x = \frac{115.5}{10.5 \times 8.8} = 1.25 \text{ m}$

15.

(b) 130 ft^2

Explanation: length = 8 ft. , breadth = 5 ft. and height = 5 ft.

The surface area of the four walls of the water tank = $2 \times \text{height}(\text{length} + \text{breadth})$

$$S = 2 \times 5(8 + 5)$$

$$S = 10(13) = 130 \text{ ft}^2$$

The surface area of four walls of the water tank is 130 ft^2 .

16. (a) $\left(-\frac{7}{5}\right)^5$

Explanation: Using law of exponents, $a^{-m} = \frac{1}{a^m}$ [\because a is non-zero integer]

$$\therefore \left(\frac{-5}{7}\right)^{-5} = \frac{1}{\left(\frac{-5}{7}\right)^5} = \left(-\frac{7}{5}\right)^5$$

17.

(c) 14

Explanation: We have, $\left(\frac{7}{9}\right)^{-8} \times \left(\frac{9}{7}\right)^6 = \left(\frac{9}{7}\right)^x$

$$\Rightarrow \left(\frac{9}{7}\right)^8 \times \left(\frac{9}{7}\right)^6 = \left(\frac{9}{7}\right)^x \Rightarrow \left(\frac{9}{7}\right)^{8+6} = \left(\frac{9}{7}\right)^x$$

$$\Rightarrow x = 8 + 6 = 14$$

18.

(d) 21

Explanation: Since, more persons can reap a field in lesser days.

Hence, number of persons and number of days to reap a field are in inverse proportion.

Let number of persons = n and number of days = d

Here, $n_1 = 30$, $d_1 = 17$, $d_2 = 10$ and $n_2 = ?$

In case of inverse proportion,

$$n_1 d_1 = n_2 d_2$$

$$\Rightarrow 30 \times 17 = n_2 \times 10$$

$$\Rightarrow n_2 = \frac{30 \times 17}{10} = 51$$

Hence, number of more persons which should be engaged = $51 - 30 = 21$

19.

(b) 4

Explanation: Since x and y vary inversely as each other, therefore the product xy always remains constant.

$$\therefore 10 \times 6 = 15 \times y$$

$$\Rightarrow 60 = 15y$$

$$\Rightarrow \frac{60}{15} = y$$

$$\Rightarrow y = 4$$

20.

(d) $(x + 25)(x - 6)$

Explanation: $x^2 + 19x - 150$

$$= x^2 + 25x - 6x - 150 \text{ [By splitting the middle term]}$$

$$= x(x + 25) - 6(x + 25)$$

$$= (x - 6)(x + 25)$$

21. We have, $729 = 3 \times 3 \times 3 \times 3 \times 3$

Since the prime factors appear in triplets.

So, 729 is a perfect cube.

22. Volume of each brick = $22 \text{ cm} \times 10 \text{ cm} \times 7 \text{ cm}$

$$= 1540 \text{ cm}^3 = 0.00154 \text{ m}^3$$

Volume of wall = $l \times b \times h = 11 \text{ m} \times 3.5 \text{ m} \times \frac{40}{100} \text{ m}$ [\because 1 m = 100 cm]

$$= 11 \times 3.5 \times 0.4 = 15.4 \text{ m}^3$$

If 1/10th part of the wall used in cement and sand, then part of wall used by cement and sand = $\frac{15.4}{10} \text{ m}^3 = 1.54 \text{ m}^3$

$$\text{Remaining part} = 15.4 - 1.54 = 13.86 \text{ m}^3$$

$$\text{Number of bricks} = \frac{\text{Volume of wall to be construct}}{\text{Volume of each brick}} = \frac{13.86}{0.00154} = 9000$$

23. Surface area of the figure = TSA of upper block + TSA of lower block - area of contacted part

$$\text{Surface area of the figure} = 2 [3 \times 1 + 1 \times 1 + 3 \times 1] + 2 [4 \times 1 + 1 \times 1 + 4 \times 1] - [1 \times 1 + 1 \times 1]$$

$$= 2 [3 + 1 + 3] + 2[4 + 1 + 4] - [1 + 1]$$

$$= 2 [7] + 2 [9] - [2]$$

$$= 14 + 18 - 2$$

$$= 32 - 2$$

$$= 30 \text{ cm}^2$$

$$24. (-2)^{-3} \times (-2)^{-4}$$

$$= (-2)^{(-3) + (-4)}$$

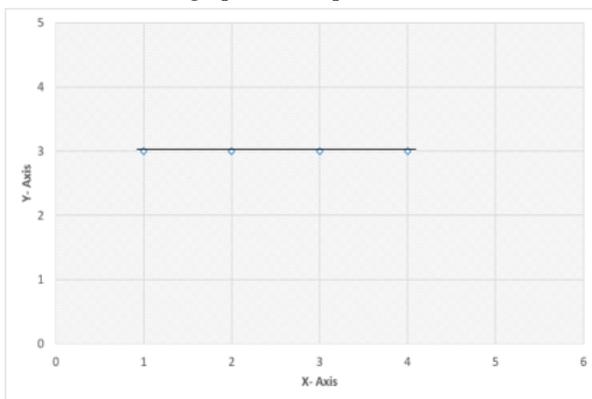
$$= (-2)^{-7}$$

$$25. y^2 - 7y + 12 = y^2 - 3y - 4y + 12$$

$$= y(y-3) - 4(y-3) = (y-3)(y-4)$$

Thus, the factors are $(y-3)$ and $(y-4)$.

26. Its clear from the graph that all points lie on the same line.



$$27. \frac{2}{5} \times \left(-\frac{3}{7}\right) - \frac{1}{6} \times \frac{3}{2} + \frac{1}{4} \times \frac{2}{5}$$

$$= \frac{2}{5} \times \left(-\frac{3}{7}\right) - \frac{1}{6} \times \frac{3}{2} + \frac{2}{5} \times \frac{1}{14} \dots \text{[By commutativity]}$$

$$= \frac{2}{5} \times \left(-\frac{3}{7}\right) + \frac{2}{5} \times \frac{1}{14} - \frac{1}{6} \times \frac{3}{2} \dots \text{[By associativity]}$$

$$= \frac{2}{5} \times \left\{ \left(-\frac{3}{7}\right) + \frac{1}{14} \right\} - \frac{1}{6} \times \frac{3}{2} \dots \text{[By distributivity]}$$

$$= \frac{2}{5} \times \left\{ \frac{(-6)+1}{14} \right\} - \frac{1}{6} \times \frac{3}{2}$$

$$= \frac{2}{5} \times \left\{ \frac{-5}{14} \right\} - \frac{1}{6} \times \frac{3}{2} = \frac{-1}{7} - \frac{1}{4}$$

$$= \frac{-4-7}{28} = \frac{-11}{28}$$

$$28. \frac{x-5}{3} = \frac{x-3}{5}$$

It is a linear equation since it involves linear expressions only.

$$\therefore \frac{x}{3} - \frac{5}{3} = \frac{x}{5} - \frac{3}{5}$$

$$\therefore \frac{x}{3} - \frac{x}{5} = \frac{3}{5} + \frac{5}{3} \dots \text{[Transposing } \frac{x}{5} \text{ to L.H.S. and } \frac{-5}{3} \text{ to R.H.S.]}$$

$$\therefore \frac{5x-3x}{15} = \frac{25-9}{15}$$

$$\therefore \frac{2x}{5} = \frac{16}{15}$$

$$\therefore x = \frac{16}{15} \times \frac{15}{2} \dots \text{[Multiplying both sides by } \frac{15}{2}]$$

$$\therefore x = 8$$

this is the required solution.

Verification,

$$\text{L.H.S.} = \frac{8-5}{3} = \frac{3}{3} = 1$$

$$\text{R.H.S.} = \frac{8-3}{5} = \frac{5}{5} = 1$$

Therefore, L.H.S. = R.H.S.

29. Since, the adjacent angles of a parallelogram are supplementary.

$$\therefore (2x - 4)^\circ + (3x - 1)^\circ = 180^\circ$$

$$\Rightarrow 5x - 5^\circ = 180^\circ$$

$$\Rightarrow 5x = 185^\circ$$

$$\Rightarrow x = \frac{185^\circ}{5} \Rightarrow x = 37^\circ$$

Thus, the adjacent angles are

$$x = 37^\circ$$

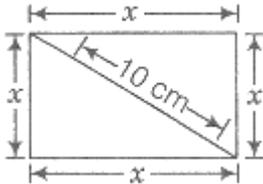
$$2x - 4 = 2 \times 37^\circ - 4 = 74 - 4 = 70^\circ$$

$$\text{and } 3x - 1 = 3 \times 37^\circ - 1 = 111 - 1 = 110^\circ$$

Hence, the angles are $70^\circ, 110^\circ, 70^\circ, 110^\circ$

[\because opposite angles in a parallelogram are equal]

30. Given, length of diagonal = 10 cm Suppose, the length of side of a square is x cm . By using Pythagoras theorem,



$$(10)^2 = x^2 + x^2$$

$$\Rightarrow 100 = 2x^2$$

$$\Rightarrow x^2 = 50$$

$$\Rightarrow x = \sqrt{50} \text{ [taking square root on both sides]}$$

$$\therefore x = 5\sqrt{2} \text{ cm}$$

Hence, the length of the side of square is $\sqrt{50}$ or $5\sqrt{2}$ cm.

31. $P = 54000$

$R = 5\%$ p.a.

$n = 2$ years

$$\therefore A = P \left(1 + \frac{R}{100}\right)^n = 54000 \left(1 + \frac{5}{100}\right)^2$$

$$= 54000 \left(1 + \frac{1}{20}\right)^2 = 54000 \left(1 + \frac{21}{20}\right)^2$$

$$= 54000 \times \frac{21}{20} \times \frac{21}{20} = 59535$$

Hence, the population in 2005 would be 59535.

32. Let the number added is x ,

$$(2m^2 - 3mn + 3n^2) + x = (5m^2 + 2mn + 7n^2)$$

$$x = (5m^2 + 2mn + 7n^2) - (2m^2 - 3mn + 3n^2)$$

$$x = 5m^2 + 2mn + 7n^2 - 2m^2 + 3mn - 3n^2$$

$$x = 3m^2 + 5mn + 4n^2$$

So, the number is $3m^2 + 5mn + 4n^2$.

33. We have given that,

The cost price of the article = ₹ 600

Gain% = 20%

$$\therefore \text{Total Gain} = \frac{600 \times 20}{100} = ₹ 120$$

$$\therefore \text{SP} = \text{Gain} + \text{CP} = ₹ 600 + ₹ 120 = ₹ 720$$

Let marked price be ₹ x .

Now shopkeeper allows a discount of 10%

According to the question, $x - 10\%$ of $x = ₹ 720$

$$\Rightarrow x - \frac{10 \times x}{100} = 720$$

$$\Rightarrow \frac{100x - 10x}{100} = 720$$

$$\Rightarrow \frac{90x}{100} = 720$$

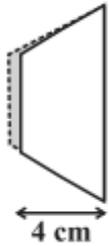
$$\Rightarrow x = \frac{720 \times 100}{90}$$

$$x = ₹ 800$$

Hence, the required marked price is ₹ 800.

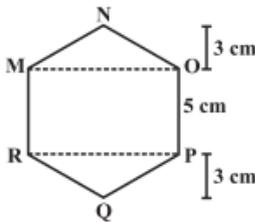
$$\begin{aligned}
34. & x(2x - 1) + 5 \\
& = x(2x) - x(1) + 5 \\
& = 2x^2 - x + 5 \\
& \text{If } x = -4 \\
& 2x^2 - x + 5 \\
& = 2(-4)^2 - (-4) + 5 \\
& = 2(16) + 4 + 5 \\
& = 32 + 9 \\
& = 41
\end{aligned}$$

35. **Aman's method:** Since it is a hexagon so, NQ divides the hexagon into two congruent trapeziums. We can verify it by paper folding (Fig.)



$$\begin{aligned}
\text{Now area of trapezium MNQR} & = 4 \times \frac{(11+5)}{2} \\
& = 32\text{cm}^2 \\
\text{So, the area of hexagon MNOPQR} & = 2 \times 32 \\
& = 64\text{cm}^2.
\end{aligned}$$

Ridhima's method: $\triangle MNO$ and $\triangle RPQ$ are congruent triangles with altitude 3 cm (Fig.)



We can verify this by cutting off these two triangles and placing them on one another.

$$\begin{aligned}
\text{Area of } \triangle MNO & = \frac{1}{2} \times 8 \times 3 \\
& = 12\text{ cm}^2 \\
\text{So, Area of } \triangle RPQ & = 12\text{ cm}^2 \\
\text{Area of rectangle MOPR} & = 8 \times 5 \\
& = 40\text{ cm}^2 \\
\text{Now, area of hexagon MNOPQR} & = 40 + 12 + 12 \\
& = 64\text{ cm}^2
\end{aligned}$$

36. Let the height of the vertical pole be x m and the length of the shadow by y m.

As the height of the vertical pole increases, the length of the shadow also increases in the same ratio, It is a case of direct proportion.

We make use of the relation of the type $\frac{x_1}{y_1} = \frac{x_2}{y_2}$.

Here,

$$x_1 = 5 \text{ m } 60 \text{ cm} = 5.60\text{m}$$

$$y_1 = 3 \text{ m } 20 \text{ cm} = 3.20\text{m}$$

$$x_2 = 10 \text{ m } 50 \text{ cm} = 10.50\text{m}$$

Therefore, $\frac{x_1}{y_1} = \frac{x_2}{y_2}$ gives

$$\frac{5.6}{3.2} = \frac{10.5}{y_2}$$

$$\therefore 5.6y_2 = 3.2 \times 10.5$$

$$\therefore y_2 = \frac{3.2 \times 10.5}{5.6}$$

$$\therefore y_2 = 6$$

Hence, the length of the shadow is 6m.

37. we have $a^2 - 1 + 2x - x^2$

$$= a^2 - (1 - 2x + x^2)$$

$$= a^2 - (1^2 - 2 \times 1 \times x + (x)^2)$$

$$= a^2 - (1 - x)^2$$

$$= \{a - (1 - x)\}^2$$

$$= \{a - (1 - x)\} \{a + (1 - x)\}$$

$$= (a - 1 + x)(a + 1 - x)$$

38. **(b)** 432

Explanation: 432

39. **(c)** 3 : 4

Explanation: 3 : 4

40. **(d)** 289 : 225

Explanation: 289 : 225

41. **(b)** 97 : 29

Explanation: 97 : 29

42. **(a)** 79 : 100

Explanation: 79 : 100

43. **(d)** 2004

Explanation: 2004 \rightarrow 500

44. **(d)** 2006

Explanation: 2006 \rightarrow 100

45. **(b)** 200

Explanation: No. of the labourers 2002 = 300

Number of the labourers 2003 = 500

Difference of the number of labourers in year 2002 and 2003 = 500 - 300 = 200

46. **(d)** 400

Explanation: Number of the labourers 2001 = 200

Number of labourers in 2004 = 600

Rise in the labourers from 2001 to 2004 = 600 - 200 = 400

47. **(c)** 700

Explanation: Number of labourers in 2004 = 600

Number of labourers in 2006 = 100

Sum of the number of labourers in 2004 and 2006 600 + 100 = 700