

**CBSE Test Paper 03**  
**Chapter 2 Polynomials**

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1. If the polynomial  $3x^3 - 4x^2 - 17x - k$  is exactly divisible by  $x - 3$ , then the value of 'k' is **(1)**
  - a. 6
  - b. 5
  - c. -5
  - d. -6
2. The number of zeroes that the polynomial  $f(x) = (x - 2)^2 + 4$  can have is **(1)**
  - a. 0
  - b. 2
  - c. 3
  - d. 1
3. If '2' is the zero of both the polynomials  $3x^2 + mx - 14$  and  $2x^3 + nx^2 + x - 2$ , then the value of  $m - 2n$  is **(1)**
  - a. 5
  - b. -1
  - c. 9
  - d. -9
4. If one of the zeroes of the cubic polynomial  $x^3 + ax^2 + bx + c$  is  $-1$ , then the product of the other two zeroes is **(1)**
  - a.  $b - a + 1$
  - b.  $b + a + 1$
  - c.  $b + a - 1$
  - d.  $b - a - 1$
5. A quadratic polynomial with zeroes  $\frac{1}{4}$  and  $-1$  is **(1)**
  - a.  $4x^2 + 3x - 1$
  - b.  $4x^2 - 3x - 1$
  - c.  $4x^2 - 3x + 1$
  - d.  $4x^2 + 3x + 1$
6. If  $(a-b)$ ,  $a$  and  $(a+b)$  are zeros of the polynomial  $2x^3 - 6x^2 + 5x - 7$ , write the value of  $a$ . **(1)**

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7. The sum of the zeros and the product of zeros of a quadratic polynomial are  $\frac{-1}{2}$  and -3 respectively. Write the polynomial. **(1)**
  8. Find the quadratic polynomial whose zeroes are  $\sqrt{3} + \sqrt{5}$  and  $\sqrt{5} - \sqrt{3}$  **(1)**
  9. Sum and product of zeroes of quadratic polynomial are 5 and 17 respectively. Find the polynomial. **(1)**
  10. Find a quadratic polynomial whose one zero is -8 and sum of zeroes is 0. **(1)**
  11. Find the zeros of the quadratic polynomial  $f(x) = abx^2 + (b^2 - ac)x - bc$ , and verify the relationship between the zeros and its coefficients. **(2)**
  12. Find the zeros of the following quadratic polynomials and verify the relationship between the zeros and the coefficients:  $8x^2 - 4$  **(2)**
  13. Find a quadratic polynomial whose zeroes are  $5 + \sqrt{2}$  and  $5 - \sqrt{2}$ . **(2)**
  14. Find a quadratic polynomial of the given number as the sum and product of its zeroes respectively. 0,  $\sqrt{7}$  **(3)**
  15. Find all the zeroes of  $p(x) = x^3 - 9x^2 - 12x + 20$  if  $x + 2$  is a factor of  $p(x)$ . **(3)**
  16. If  $\alpha$  and  $\beta$  are the zeroes of the quadratic polynomial  $f(x) = 6x^2 + x - 2$ , then, find the value of  $\frac{\alpha}{\beta} + \frac{\beta}{\alpha}$ . **(3)**
  17. Can  $(x - 2)$  be the remainder on division of a polynomial  $p(x)$  by  $(2x + 3)$ ? Justify your answer. **(3)**
  18.  $\alpha, \beta$  and  $\gamma$  are zeroes of the polynomial  $x^3 + px^2 + qx + 2$  such that  $\alpha \cdot \beta + 1 = 0$ . Find the value of  $2p + q + 5$ . **(4)**
  19. Obtain all other zeroes of the polynomial  $x^4 + 6x^3 + x^2 - 24x - 20$ , if two of its zeroes are + 2 and - 5. **(4)**
  20. When a polynomial  $f(x)$  is divided by  $x^2 - 5$ , the quotient is  $x^2 - 2x - 3$  and remainder is zero. Find the polynomial and all its zeroes. **(4)**

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**Solution**

1. d. -6

**Explanation:** If the polynomial  $3x^3 - 4x^2 - 17x - k$  is exactly divisible by  $x - 3$ , then

$$p(3) = 0 \text{ (By factor theorem)}$$

$$\Rightarrow 3(3)^3 - 4(3)^2 - 17 \times 3 - k = 0$$

$$\Rightarrow 81 - 36 - 51 - k = 0$$

$$\Rightarrow -6 - k = 0$$

$$\Rightarrow k = -6$$

2. b. 2

**Explanation:**  $f(x) = (x - 2)^2 + 4 = x^2 - 4x + 4 + 4 = x^2 - 4x + 8$

Here the largest exponent of variable is 2,

therefore number of zeroes of the given polynomial is 2.

3. c. 9

**Explanation:** According to the question,  $p(2) = 3x^2 + mx - 14 = 0$

$$\Rightarrow 3(2)^2 + m \times 2 - 14 = 0$$

$$\Rightarrow 12 + 2m - 14 = 0 \Rightarrow m = 1$$

Also  $p(2) = 2x^3 + nx^2 + x - 2 = 0$

$$\Rightarrow 2 \times (2)^3 + n \times (2)^2 + 2 - 2 = 0$$

$$\Rightarrow 16 + 4n = 0$$

$$\Rightarrow n = -4$$

$$\therefore m - 2n = 1 - 2 \times (-4) = 1 + 8 = 9$$

4. a.  $b - a + 1$

**Explanation:** Let  $\alpha, \beta, \gamma$  are the zeroes of the given polynomial. Given:  $\alpha = 1$   
and To find :  $\beta\gamma$  Since,  $\alpha + \beta + \gamma = \frac{-b}{a} \Rightarrow -1 + \beta + \gamma = \frac{-a}{1} \Rightarrow$

$$\beta + \gamma = -a + 1 \text{ .....(i)}$$

$$\text{Also } \alpha\beta + \beta\gamma + \gamma\alpha = \frac{c}{a} \Rightarrow (-1)\beta + \beta\gamma + (-1)\gamma = \frac{b}{1}$$

$$\Rightarrow -\beta + \beta\gamma - \gamma = b \Rightarrow \beta\gamma - (\beta + \gamma) = b \Rightarrow \beta\gamma - (-a + 1) = b \text{ [From eq. (i)]}$$

$$\Rightarrow \beta\gamma = b - a + 1$$

5. a.  $4x^2 + 3x - 1$

**Explanation:**  $x^2 - (\alpha + \beta)x + (\alpha\beta) = 0$

Here  $\alpha + \beta = \frac{1}{4} + (-1) = \frac{1-4}{4} = \frac{-3}{4}$  And  $\alpha\beta = \frac{1}{4} \times (-1) = \frac{-1}{4} = \frac{c}{a}$

$$x^2 - \left(\frac{-3}{4}\right)x + \left(\frac{-1}{4}\right) = 0$$

$$x^2 + \frac{3}{4}x - \frac{1}{4} = 0$$

$$\frac{4x^2 + 3x - 1}{4} = 0 \text{ (By L.C.M)}$$

$$4x^2 + 3x - 1 = 0$$

6. Given polynomial is  $p(x) = 2x^3 - 6x^2 + 5x - 7$

Let  $\alpha = (a - b)$ ,  $\beta = a$  and  $\gamma = (a + b)$

$$\text{Now, } \alpha + \beta + \gamma = -\frac{(-6)}{2} = 3$$

$$\Rightarrow (a - b) + a + (a + b) = 3$$

$$\Rightarrow a - b + a + a + b = 3$$

$$\Rightarrow 3a = 3$$

$$\Rightarrow a = 3/3$$

$$\Rightarrow a = 1$$

So the value of a in given polynomial is 1.

7. Let  $\alpha$  and  $\beta$  be the zeros of the required quadratic polynomial.

As per given condition the sum of the zeros and the product of zeros of a quadratic polynomial are  $\frac{-1}{2}$  and -3 respectively.

Then, we have

$$\alpha + \beta = -\frac{1}{2} \text{ and } \alpha\beta = -3$$

Now, a quadratic polynomial whose zeros are  $\alpha$  and  $\beta$  is given by

$$p(x) = x^2 - (\alpha + \beta)x + \alpha\beta$$

$\therefore$  Required quadratic polynomial,

$$p(x) = x^2 - \left(-\frac{1}{2}\right)x + (-3)$$

$$= x^2 + \frac{1}{2}x - 3$$

Hence the given polynomial is  $x^2 + \frac{1}{2}x - 3$ .

8. Sum of zeroes =  $\sqrt{3} + \sqrt{5} + \sqrt{5} - \sqrt{3} = 2\sqrt{5}$

$$\begin{aligned} \text{Product of zeroes} &= (\sqrt{3} + \sqrt{5})(\sqrt{5} - \sqrt{3}) = \sqrt{15} - \sqrt{9} + \sqrt{25} - \sqrt{15} \\ &= \sqrt{15} - 3 + 5 - \sqrt{15} \end{aligned}$$

$$= -3 + 5 = 2$$

Quadratic polynomial is  $x^2 - (\text{sum of zeroes})x + \text{product of zeroes}$   
 $= x^2 - 2\sqrt{5}x + 2$

9. Sum of zeroes = 5

Product of zeroes = 17

Quadratic Polynomial =  $x^2 - (\text{sum of zeroes})x + \text{product of zeroes} = x^2 - 5x + 17$

10. It is given that One zero = - 8

and Sum of zeroes = 0

Since sum of zeroes =  $\alpha + \beta$

$\therefore$  Other zero =  $0 - (-8) = 8$

Product of zeroes =  $8 \times (-8) = -64$

Hence, Polynomial  $p(x) = x^2 - (S)x + P$   
 $= x^2 - 64$

11. We have,

$$f(x) = abx^2 + (b^2 - ac)x - bc$$

$$= abx^2 + b^2x - acx - bc$$

$$= bx(ax + b) - c(ax + b)$$

$$= (ax + b)(bx - c)$$

Now  $r(x)=0$  if

$$ax+b=0 \text{ or } bx-c=0$$

$$i.e. X = -\frac{b}{a} \text{ or } X = \frac{c}{b}$$

Thus, the zeroes of  $f(x)$  are :

$$\alpha = -\frac{b}{a} \text{ and } \beta = \frac{c}{b}$$

$$\alpha + \beta = -\frac{b}{a} + \frac{c}{b} = \frac{-b^2+ac}{ab} = -\frac{(b^2-ac)}{ab} \quad (1)$$

$$\alpha\beta = \frac{b}{a} \times -\frac{c}{b} = -\frac{c}{a} \dots (2)$$

Now for  $f(x) = abx^2 + (b^2 - ac)x - bc$

$$A = ab, B = b^2 - ac, C = -bc$$

$$-\frac{B}{A} = -\frac{b^2-ac}{ab} \quad (3)$$

$$\frac{C}{A} = \frac{-bc}{ab} = -\frac{c}{a} \quad (4)$$

From (1) & (3) and (2) & (4) we conclude:

$$\alpha + \beta = -\frac{B}{A}$$

$$\alpha\beta = \frac{C}{A}$$

12.  $f(x) = 8x^2 - 4$

$$= 4(2x^2 - 1)$$

$$= 4[(\sqrt{2}x)^2 - 1^2]$$

$$= 4(\sqrt{2}x - 1)(\sqrt{2}x + 1)$$

$$f(x) = 0 \Rightarrow (\sqrt{2}x - 1)(\sqrt{2}x + 1) = 0$$

$$\therefore \sqrt{2}x - 1 = 0 \text{ or } \sqrt{2}x + 1 = 0$$

$$\therefore x = \frac{1}{\sqrt{2}} \text{ or } x = -\frac{1}{\sqrt{2}}$$

$$\text{So, the zeros of } f(x) \text{ are } \frac{1}{\sqrt{2}} \text{ and } -\frac{1}{\sqrt{2}}$$

$$\text{Sum of zeros} = \left(\frac{1}{\sqrt{2}}\right) + \left(-\frac{1}{\sqrt{2}}\right) = 0 = \frac{0}{8} = \frac{\text{Coeff. of } x}{\text{coeff. of } x^2}$$

$$\text{Product of zeros} = \left(\frac{1}{\sqrt{2}}\right) \times \left(-\frac{1}{\sqrt{2}}\right) = -\frac{1}{2} = \frac{-4}{8}$$

$$= \frac{\text{constant term}}{\text{Coeff. of } x^2}$$

13. Let  $\alpha, \beta$  are zeroes of quadratic polynomial  $p(x)$ .

$$\therefore p(x) = x^2 - (\alpha + \beta)x + \alpha\beta$$

$$\text{Here, } \alpha = 5 + \sqrt{2}, \beta = 5 - \sqrt{2}$$

$$\therefore \alpha + \beta = 5 + \sqrt{2} + 5 - \sqrt{2} = 10$$

$$\text{and } \alpha\beta = (5 + \sqrt{2})(5 - \sqrt{2}) = 25 - 2 = 23$$

$$\text{Hence the polynomial is } p(x) = x^2 - 10x + 23.$$

14.  $0, \sqrt{7}$

$$\text{Let the quadratic polynomial be } ax^2 + bx + c$$

$$\text{and its zeroes be } \alpha \text{ and } \beta,$$

$$\text{Then, } \alpha + \beta = 0 = -\frac{b}{a} \text{ and, } \alpha\beta = \sqrt{3} = \frac{c}{a}$$

$$\text{If } a = 1, \text{ then } b = 0 \text{ and } c = \sqrt{7}$$

$$\text{So, one quadratic polynomial which fits}$$

$$\text{the given conditions is } x^2 + \sqrt{7}$$

15. Given polynomial is  $p(x) = x^3 - 9x^2 - 12x + 20$  and  $x + 2$  is a factor of  $p(x)$ .

$$\begin{array}{r}
 x^2 - 11x + 10 \\
 x + 2 \overline{) \begin{array}{r} x^3 - 9x^2 - 12x + 20 \\ x^3 + 2x^2 \\ \hline -11x^2 - 12x \\ -11x^2 - 22x \\ \hline 10x + 20 \\ 10x + 20 \\ \hline 0 \end{array}} \\
 \hline
 \end{array}$$

dividend = divisor  $\times$  quotient + remainder

$$\therefore p(x) = (x + 2)(x^2 - 11x + 10)$$

$$= (x + 2)(x^2 - 10x - x + 10)$$

$$= (x + 2)[x(x - 10) - 1(x - 10)]$$

$$= (x + 2)(x - 1)(x - 10)$$

$\therefore$  Zeroes of  $p(x)$  are -2, 1, 10.

16.  $f(x) = 6x^2 + x - 2$

$a = 6, b = 1, c = -2$

Let zeroes be  $\alpha$  and  $\beta$ . Then

$$\text{Sum of zeroes} = \alpha + \beta = -\frac{b}{a} = -\frac{1}{6}$$

$$\text{Product of zeroes } \alpha \times \beta = \frac{c}{a} = \frac{-2}{6} = -\frac{1}{3}$$

$$\begin{aligned}
 \frac{\alpha}{\beta} + \frac{\beta}{\alpha} &= \frac{\alpha^2 + \beta^2}{\alpha\beta} \\
 &= \frac{(\alpha + \beta)^2 - 2\alpha\beta}{\alpha\beta} \left[ \because (\alpha + \beta)^2 = \alpha^2 + \beta^2 + 2\alpha\beta \right] \\
 &= \frac{\left[-\frac{1}{6}\right]^2 - 2\left[-\frac{1}{3}\right]}{\left[-\frac{1}{3}\right]} \\
 &= \frac{\frac{1}{36} + \frac{2}{3}}{-\frac{1}{3}} \\
 &= \frac{\frac{1+24}{36}}{-\frac{1}{3}} \\
 &= \frac{25}{36} \times \frac{-3}{1} \\
 &= \frac{-25}{12}
 \end{aligned}$$

17. No,  $(x - 2)$  cannot be remainder on division of polynomial  $p(x)$  by  $(2x + 3)$  because the degree of remainder is either 0 or its degree is less than the degree of the divisor.

18.  $P(x) = x^3 + px^2 + qx + 2$

Here,  $a = 1, b = p, c = q, d = 2$

Now,  $\alpha + \beta + \gamma = \frac{-b}{a} = -p \dots\dots (i)$

$\alpha\beta + \beta\gamma + \alpha\gamma = \frac{c}{a} = q$

$\Rightarrow \alpha\beta + \gamma(\beta + \alpha) = q \dots\dots\dots (ii)$

and  $\alpha \cdot \beta \cdot \gamma = \frac{-d}{a} = -2$

$\Rightarrow \alpha \cdot \beta \cdot \gamma = -2 \dots\dots\dots (iii)$

Also,  $\alpha\beta + 1 = 0 \Rightarrow \alpha\beta = -1$

Therefore, (iii) becomes  $-1 \times \gamma = -2 \Rightarrow \gamma = 2$

Substituting in (i), we get

$\alpha + \beta + 2 = -p \Rightarrow \alpha + \beta = -p - 2$

Substituting these value in (ii), we get

$-1 + 2(-p - 2) = q$

$\Rightarrow -1 - 2p - 4 = q$

$\Rightarrow 2p + q + 5 = 0$

19. As  $x = 2$  and  $-5$  are the zeroes of  $x^4 + 6x^3 + x^2 - 24x - 20$ .

$\Rightarrow (x - 2)$  and  $(x + 5)$  are two factors of  $x^4 + 6x^3 + x^2 - 24x - 20$

$\Rightarrow$  product of factors is  $(x - 2)(x + 5) = x^2 + 3x - 10$

Dividing  $x^4 + 6x^3 + x^2 - 24x - 20$  by  $x^2 + 3x - 10$

$$\begin{array}{r}
 \phantom{x^2 + 3x - 10)} \overline{x^2 + 3x + 2} \\
 x^2 + 3x - 10 \overline{) x^4 + 6x^3 + x^2 - 24x - 20} \\
 \underline{x^4 + 3x^3 - 10x^2} \phantom{- 24x - 20} \\
 \phantom{x^4 + } 3x^3 + 11x^2 - 24x - 20 \\
 \underline{3x^3 + 9x^2 - 30x} \phantom{- 20} \\
 \phantom{x^4 + } \phantom{3x^3 + } 2x^2 + 6x - 20 \\
 \underline{2x^2 + 6x - 20} \\
 \phantom{x^4 + } \phantom{3x^3 + } \phantom{2x^2 + } 0
 \end{array}$$

Dividend = divisor  $\times$  quotient + remainder

$\Rightarrow x^4 + 6x^3 + x^2 - 24x - 20 = (x^2 + 3x - 10)(x^2 + 3x + 2)$

$= (x - 2)(x + 5)(x + 2)(x + 1)$

Hence, other two zeroes are  $-2$  and  $-1$ .

20.  $g(x) = x^2 - 5$

$q(x) = x^2 - 2x - 3$

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$$r(x) = 0$$

By division algorithm for polynomials, we have

$$f(x) = q(x) \cdot g(x) + r(x)$$

$$f(x) = (x^2 - 5)(x^2 - 2x - 3) + 0$$

$$f(x) = x^4 - 2x^3 - 3x^2 - 5x^2 + 10x + 15$$

$$f(x) = x^4 - 2x^3 - 8x^2 + 10x + 15$$

So, the required polynomial is  $f(x) = x^4 - 2x^3 - 8x^2 + 10x + 15$

Now,

$q(x)$  and  $g(x)$  will be factors of  $f(x)$

$$x^2 - 5 = 0 \text{ and } x^2 - 2x - 3 = 0$$

$$x^2 - (\sqrt{5})^2 = 0 \text{ and } x^2 + x - 3x - 3 = 0$$

$$(x - \sqrt{5})(x + \sqrt{5}) = 0 \text{ and } (x + 1)(x - 3) = 0$$

$$x = \sqrt{5}, x = -\sqrt{5}, x = -1 \text{ and } x = 3$$

So, the zeroes are  $\alpha = \sqrt{5}, \beta = -\sqrt{5}, \gamma = -1$  and  $\delta = 3$ .