

CONTROL SYSTEMS TEST I

Number of Questions 35

Time: 60 min.

Directions for questions 1 to 35: Select the correct alternative from the given choices.

1. A system has a damping ratio of 1.25, a natural frequency of 400rad/sec and DC gain of 1. The response of the system to a unit step input is

(A) $1 + \frac{800}{3}(e^{-800t} - e^{-200t})$

(B) $1 - \frac{800}{3}(e^{-200t} + e^{-800t})$

(C) $1 - \frac{800}{3}(e^{-200t} - e^{-800t})$

(D) $1 + \frac{800}{3}(e^{-200t} - e^{-800t})$

2. Gain margin is the amount of gain to make the system

- (A) Oscillatory (B) Stable
(C) Exponential (D) Unstable

3. A system with gain margin close to unity or a phase margin close to zero is

- (A) relatively stable (B) highly stable
(C) oscillatory (D) none

4. The unit step response of a particular control system is $c(t) = 1 - 5e^{-t}$, then the transfer function is

(A) $\frac{1+4s}{(s+1)s}$ (B) $\frac{-(1+4s)}{s+1}$

(C) $\frac{1-4s}{(s+1)}$ (D) $\frac{-1+4s}{(s+1)s}$

5. A phase – lead compensator will

- (A) Improve the speed of the response
(B) Increases Bandwidth
(C) Reduces the amount of overshoot
(D) All the above

6. There are three poles and two zeros of $G(s) H(s)$. there will be

- (A) One root locus (B) Two root loci
(C) Three root loci (D) Five root loci

7. A control system has $G(s)$

$$H(s) = \frac{K}{s(s+3)(s^2 + 4s + 20)}, \text{ for } (0 < K < \infty).$$

Then the number of break away points occurs in the root locus are

- (A) One (B) Two
(C) Three (D) Four

8. The output of a given system settles within $\pm 5\%$ for a unit step input. Then the settling time is

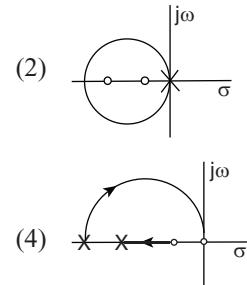
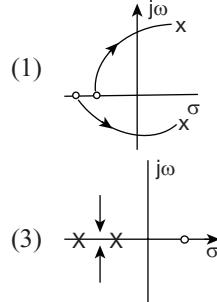
$$G(s) = \frac{s+4}{s^2 + 6s + 36}$$

- (A) 0.5 (B) 0.75
(C) 0.9 (D) 1

9. Which one of the following is correct when a pole is added to a forward path transfer function.

- (A) System becomes less stable
(B) Bandwidth of system Decreases
(C) Stability improves
(D) Both A and B

10. Consider the sketch shown below



The root locus can be

- (A) 1 and 3 (B) 2 and 4
(C) 1, 2 and 4 (D) None of the above

11. Consider a feedback control system with loop transfer function $G(S) H(S) = \frac{K}{s(1+s)(1+2s)}$ then order of the

given system is

- (A) 1 (B) 3
(C) 2 (D) 4

12. A minimum phase unity feedback system has a Bode plot with a constant slope of 0dB/decade for all frequencies. What is the value of the maximum phase margin for the system?

- (A) 180° (B) 90°
(C) -90° (D) 0°

13. The intersection of Asymptotes of root loci of a system with open loop transfer function

$$G(s)H(s) = \frac{K(s+2)}{s(s+1)(s+3)}$$

- is
(A) -2 (B) -1
(C) -0.67 (D) 1

14. Which one of the following characteristic equations of results in the stable operation of feedback system

- (A) $s^3 + 7s^2 + 5s - 6 = 0$
(B) $s^3 + 2s^2 + 3s + 7 = 0$
(C) $s^3 + 4s^2 + 10s + 11 = 0$
(D) $s^4 + s^3 - 3s^2 + 5s + 6 = 0$

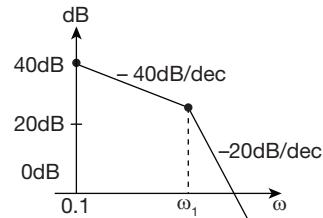
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15. Transfer function of a lag compensator is given by $G(s)$

$H(s) = \frac{s+0.2}{s+0.026}$ then the frequency corresponding to maximum phase lead angle is

- (A) 7.69 rad/sec
- (B) 4.9 rad/sec
- (C) 2.77 rad/sec
- (D) 0.072 rad/sec

16. Find the Transfer function for the given bode plot of a unit feedback system



- (A) $\frac{0.33}{s(s+0.316)^2}$
- (B) $\frac{0.331}{s^2(s+0.316)}$
- (C) $\frac{1}{s^2(1+0.3165)}$
- (D) $\frac{1}{s(1+0.3165)^2}$

17. What should be the value of λ in order to the given system is controllable

- $\dot{x}_1 = x_2 + \mu; \dot{x}_2 = \lambda x_2 - 6x_1 - 2\mu$
- (A) $\lambda = -5$
- (B) $\lambda \neq -5$
- (C) $\lambda = -6$
- (D) $\lambda \neq -6$

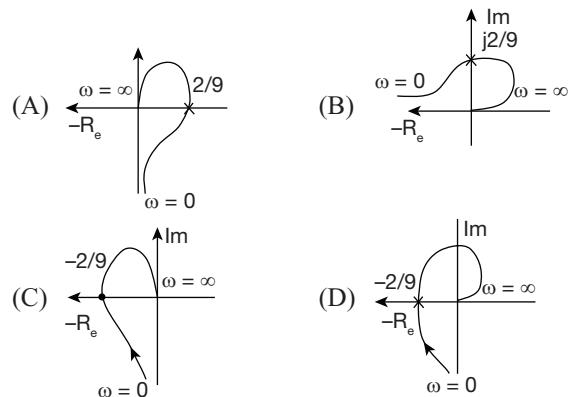
18. For a given transfer function choose the state variable

$$\text{matrix } \frac{C(s)}{R(s)} = \frac{30}{s^3 + 8s^2 + 7s + 30}$$

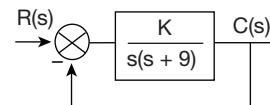
- (A) $\dot{\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -30 & -7 & -8 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 30 \end{bmatrix} r$
- (B) $\dot{\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 30 & 7 & 8 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 30 \end{bmatrix} r$
- (C) $\dot{\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ -8 & -7 & -30 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 30 \end{bmatrix} r$
- (D) $\dot{\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -8 & -7 & -30 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 30 \end{bmatrix} r$

19. A unity feed back has open – loop transfer function

$$G(s) = \frac{1}{s(4s+1)(s+2)}$$



20. The unity feedback system $R(s)$ has

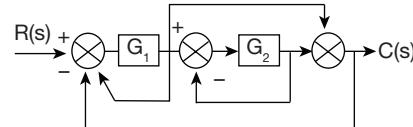


- (A) Steady state velocity error of $k/9$ units
- (B) Steady state position error of $K/9$ units
- (C) Zero steady state velocity error
- (D) Zero steady state position error

21. If maximum peak overshoot is 16.3% then the resonant peak is

- (A) 0.5
- (B) 0.15
- (C) 1.15
- (D) 0.086

22. Determine Transfer function of given system



- (A) $\frac{G_1 G_2 + G_1}{1 + G_1 + G_2 + G_1 G_2}$
- (B) $\frac{2G_1 G_2 + G_1}{1 + 2G_1 + G_2 + G_1 G_2}$
- (C) $\frac{G_1 G_2 + G_1}{1 + 2G_1 + G_2 + 3G_1 G_2}$
- (D) $\frac{2G_1 G_2 + G_1}{1 + 2G_1 + G_2 + 3G_1 G_2}$

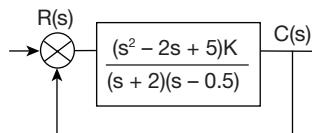
23. The radius of M and N circles are $\sqrt{2}$, 1 respectively then the values of M and N respectively are

- (A) $\sqrt{2}, 1$
- (B) $\sqrt{2}, 1/\sqrt{3}$
- (C) $1/\sqrt{3}, \sqrt{2}$
- (D) $\infty, 0$

24. Maximum peak overshoot in the unit step response is 0.4 and peak time is 2sec. Then settling time for 5% error is

- (A) 0.65
- (B) 0.57
- (C) 0.75
- (D) 0.4564

25. Find Angle of arrival for given system



- (A) 160.355° (B) 109.65°
 (C) 199.645° (D) 189.7°

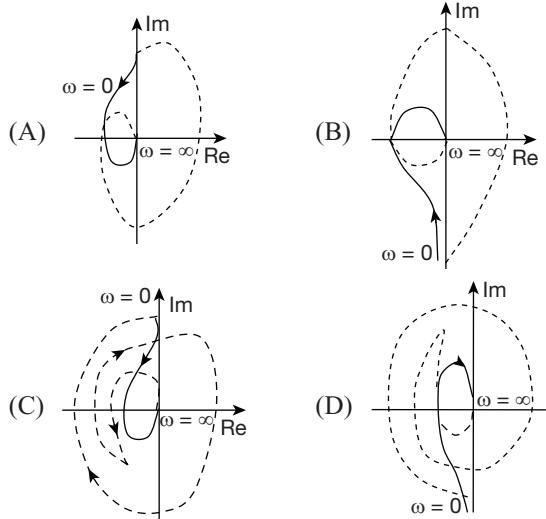
26. Find the phase margin of a system with open loop transfer function $G(S) = \frac{1}{s(1+s)}$

- (A) -141.78° (B) 38.21°
 (C) -38° (D) 180°

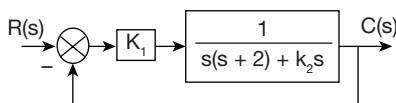
27. The open loop transfer function of a feedback control system is given by $GH(s) = \frac{K(s+2)}{s(1+as)(1+5s)}$, then find

error due to unit parabolic input if $K = 9$ and $a = 3$
 (A) ∞ (B) 0
 (C) 9 (D) 3

28. The open loop transfer function of a system is $GH(s) = \frac{A(1+s)^2}{s^3}$, then Nyquist plot for given system is



29. The system has damping ratio 0.8 and a frequency of damped oscillations of 10 rad/sec. Then the value of K_2



- (A) 16.7 (B) 26.7
 (C) 24.7 (D) 5.16

30. Forward path transfer function of a unity, feedback system is given by

$$G(s)H(s) = \frac{125}{(s+1)(s+2)(s+3)(0.25s+1)},$$

then the system is

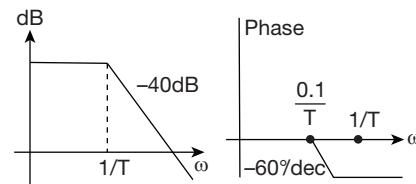
- (A) Stable
 (B) Unstable
 (C) Marginally stable
 (D) More information is required

31. For a second order system overshoot is 20% and settling time is 0.6 seconds then characteristic equation roots are.

- (A) $-6.6576 \pm j13$ (B) $-6.6576 \pm j14.6$
 (C) $13 \pm j14.6$ (D) $14.6 \pm j13$

Common Data for Questions 32 and 33:

The Bode plot of the transfer function $\frac{b_0}{(1+s\tau)}$ is given in below figures.



32. The error in phase angle at $\omega = \frac{0.5}{T}$ is

- (A) 3.44° (B) 26.56°
 (C) 60° (D) 30°

33. The error in gain at $\omega = \frac{0.5}{T}$ is

- (A) -40 dB (B) -30 dB
 (C) 0 dB (D) 0.97 dB

Linked Answer Questions 34 and 35:

The open loop transfer function of a unity feedback control system is given by

$$G(S) = \frac{K}{(s+3)(s+1)(s^2 + 6s + 25)}$$

34. Find the values of K which will cause sustained oscillations in the closed – looped system?

- (A) 3993.6 (B) -75
 (C) -118 (D) 399.36

35. Find the oscillating frequency?

- (A) 11.8 rad/sec
 (B) 3.43 rad/sec
 (C) 0.547 rad/sec
 (D) 1.8 rad/sec

ANSWER KEYS

- | | | | | | | | | | |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1. D | 2. D | 3. C | 4. C | 5. D | 6. C | 7. C | 8. D | 9. D | 10. D |
| 11. B | 12. A | 13. B | 14. C | 15. D | 16. B | 17. B | 18. A | 19. C | 20. D |
| 21. C | 22. D | 23. B | 24. D | 25. C | 26. B | 27. A | 28. C | 29. C | 30. B |
| 31. A | 32. A | 33. D | 34. D | 35. B | | | | | |

HINTS AND EXPLANATIONS

$$1. T(S) = \frac{\omega_n^2}{s^2 + 2\xi\omega_n s + \omega_n^2} \quad \text{Ans}$$

$$= \frac{160000}{s^2 + 2 \times 1.25 \times 400s + (400)^2}$$

$$= \frac{160000}{s^2 + 1000s + 160000}$$

$$C(S) = \frac{160000}{s(s^2 + 1000s + 160000)}$$

$$= \frac{1}{s} + \frac{1600}{6(s+200)} - \frac{1600}{6(s+800)}$$

$$C(t) = 1 + \frac{800}{3}e^{-200t} - \frac{800}{3}e^{-800t}$$

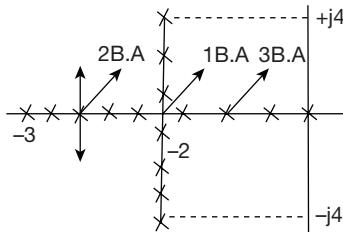
Choice (D)

$$4. C(S) = \frac{1}{s} - \frac{5}{s+1} = \frac{s+1-5s}{s(s+1)} = \frac{1-4s}{s(s+1)}$$

Choice (C)

$$T(S) = \frac{1-4s}{s(s+1)} = \frac{1-4s}{s+1}$$

7.



Choice (C)

8. On 5% basis the setting time for a system is given by

$$t_s = \frac{3}{\xi\omega_n} = \frac{3}{\frac{6}{2}} = 1$$

Choice (D)

10. Root locus path should starts from pole to zero so none of the given diagram root locus starts from pole.

Choice (D)

$$11. GH(S) = \frac{K}{s(1+s)(1+2s)} = \frac{K}{2s^3 + 3s^2 + s}$$

So order is 3.

Choice (B)

$$13. \text{Intersection of asymptotes i.e., centroid}$$

$$= \frac{\sum \text{real parts of poles} - \sum \text{real part of zeros}}{\text{number of poles} - \text{number of zeros}}$$

$$= \frac{-1-3-(-2)}{3-1} = \frac{-4+2}{2} = -1$$

Choice (B)

14. For stable operation, all co-efficient of the characteristic equation should be real & have the same sign and none of the co-efficient should be zero. Choice (C)

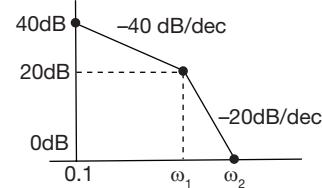
$$15. \text{Transfer function of a lag compensator } G(S) = \frac{\frac{s+1}{s+1}}{\frac{T}{\beta T}}$$

$$\frac{1}{T} = 0.2; \frac{1}{\beta T} = 0.026 \Rightarrow \beta = 7.69$$

$$\omega_m = \frac{1}{T\sqrt{\beta}} = \frac{0.2}{\sqrt{7.69}} = 0.072 \text{ rad/sec}$$

Choice (D)

16.



$$40 - 20 = -40(\log(0.1) - \log\omega_1)$$

$$\Rightarrow \omega_1 = 0.316 \text{ rad/sec}$$

$$20 = -20(1\log 0.316 - \log\omega_2)$$

$$\omega_2 = 3.16$$

$$40 = 20 \left(\log \frac{K}{(0.1)^2 (0.316)} \right)$$

$$K = 0.331$$

Transfer function of system

$$= \frac{0.331}{s^2 (s + 0.316)}$$

Choice (B)

$$17. \dot{x} = \begin{bmatrix} 0 & 1 \\ -6 & \lambda \end{bmatrix} X + \begin{bmatrix} 1 \\ -2 \end{bmatrix} U$$

$$\text{From above } A = \begin{bmatrix} 0 & 1 \\ -6 & \lambda \end{bmatrix} \text{ and } B = \begin{bmatrix} 1 \\ -2 \end{bmatrix}$$

Controllability $Q_c = [B : AB]$

$$AB = \begin{bmatrix} 0 & 1 \\ -6 & \lambda \end{bmatrix} \begin{bmatrix} 1 \\ -2 \end{bmatrix} = \begin{bmatrix} -2 \\ -6-2\lambda \end{bmatrix}$$

$$Q_c = \begin{bmatrix} 1 & -2 \\ -2 & -6-2\lambda \end{bmatrix}$$

If $|Q_c| \neq 0$ then system is said to be controllable

$$-6-2\lambda-4=0$$

$$\Rightarrow 2\lambda=-10$$

$$\lambda=-5$$

$$\lambda \neq -5$$

For the system to be controllable

Choice (B)

$$18. \frac{C(s)}{R(s)} = \frac{b_0}{s^3 + a_2 s^2 a_1 s + a_0}$$

$$\Rightarrow (s^3 + a_2 s^2 + a_1 s + a_0) C(s) = R(s) b_0$$

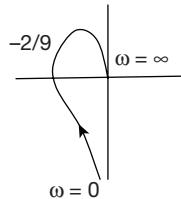
$$\dot{x} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -a_0 & -a_1 & -a_2 \end{bmatrix} X + \begin{bmatrix} 0 \\ 0 \\ b_0 \end{bmatrix} r$$

$$\Rightarrow \dot{x} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -30 & -7 & -8 \end{bmatrix} X + \begin{bmatrix} 0 \\ 0 \\ 30 \end{bmatrix} r$$

Choice (A)

$$19. \text{ Given system is } \frac{1}{s(4s+1)(s+2)}$$

$$\phi = -90^\circ - \tan^{-1}(4\omega) - \tan^{-1}(\omega/2)$$



Transfer function cuts the real axis when imaginary part is equal to zero.

$$-180 = -90 - \tan^{-1}(4\omega) - \tan^{-1}\omega/2$$

$$90 = \tan^{-1}4\omega + \tan^{-1}\omega/2$$

$$1 - 4\omega \times \omega/2 = 0$$

$$2\omega^2 = 1$$

$$\omega = \frac{1}{\sqrt{2}}$$

Magnitude Nyquist plot can be real axis is

$$= \frac{1}{\omega\sqrt{16\omega^2+1}\sqrt{\omega^2+4}} = \frac{1}{1/\sqrt{2}\sqrt{16\times 1/2+1}\sqrt{1/2+4}}$$

$$= 2/9$$

Choice (C)

$$20. \text{ For unit step i/p the steady state error is } \frac{A}{1+K_p}$$

$$K_p = Lt_{s \rightarrow 0} GH(s)$$

$$= Lt_{s \rightarrow 0} \frac{K}{s(s+9)} = \infty$$

$$e_{ss} = \frac{A}{1+\infty} = \frac{A}{\infty} = 0$$

$$\Rightarrow \text{ for unit ramp input } e_{ss} = \frac{A}{K_V}$$

$$K_V = Lt_{s \rightarrow 0} s \frac{K}{s(s+9)} = K/9$$

$$e_{ss} = 9/K$$

Hence steady state error is $9/K$ for ramp input.

Choice (D)

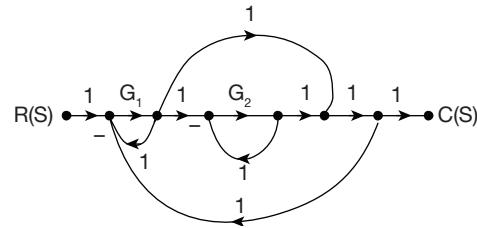
$$21. M_p = e^{-\pi\xi/\sqrt{1-\xi^2}} = 0.163$$

$$\Rightarrow \xi = 0.5$$

$$M_r = \frac{1}{2\xi\sqrt{1-\xi^2}} = 1.15$$

Choice (C)

22. Draw signal flow graph



$$T/F = \frac{G_1 G_2 + G_1 (1+G_2)}{1+G_2 + G_1 + G_1 G_2 + G_1 + G_1 G_2 + G_1 G_2}$$

$$= \frac{2G_1 G_2 + G_1}{1+2G_1 + G_2 + 3G_1 G_2}$$

Choice (D)

$$23. \text{ radius of } M \text{ circle} = \sqrt{\frac{M^2}{(M^2-1)^2}} = \sqrt{2}$$

$$\frac{M}{M^2-1} = \sqrt{2}$$

$$\Rightarrow M = \sqrt{2}$$

$$\text{Radius of } N \text{ circle} = \sqrt{\frac{1}{4} + \frac{1}{(2N)^2}}$$

$$1 = \frac{1}{4} + \frac{1}{(2N)^2} \Rightarrow \frac{3}{4} = \frac{1}{(2N)^2}$$

$$\Rightarrow \frac{1}{2N} = \frac{\sqrt{3}}{2} \Rightarrow N = \frac{1}{\sqrt{3}}$$

Choice (B)

$$24. M_p = e^{-\xi\pi/\sqrt{1-\xi^2}} = 0.4$$

$$\Rightarrow \xi = 0.28$$

$$t_p = 2\sec = \frac{\pi}{\omega_n \sqrt{1-\xi^2}}$$

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$$\Rightarrow \omega_n = \frac{3.14}{2\sqrt{1-(0.28)^2}} = 1.63 \text{ rad/sec}$$

$$T_s = \frac{3}{\xi\omega_n} = \frac{3}{0.28 \times 1.63} = 0.4564$$

Choice (D)

$$25. \frac{C(s)}{R(s)} = \frac{(s^2 - 2s + 5)K}{(s+2)(s-0.5)}$$

$$= \frac{K(s-1-2j)(s-1+2j)}{(s+2)(s-0.5)}$$

$$\angle GH(S) = \frac{K(1+2j-1+2j)}{(1+2j+2)(1+2j-0.5)} \text{ at } s = 1+2j$$

$$= \frac{K(4j)}{(3+2j)(0.5+2j)}$$

$$\angle GH(S) = 90^\circ - \tan^{-1} 2/3 - \tan^{-1} 2/0.5 \\ = -19.645^\circ$$

$$\phi_A = 180 - \phi = 199.645^\circ$$

Choice (C)

26. Given that $G(S) = \frac{1}{s(1+s)}$. At gain cross over frequency ω_{gc} the magnitude of $G(j\omega)$ is unity.

$$\text{At } \omega = \omega_{gc}$$

$$\Rightarrow |G(j\omega)| = \frac{1}{\omega_{gc}^2 \sqrt{1+\omega_{gc}^2}} = 1$$

$$\Rightarrow \omega_{gc} \sqrt{1+\omega_{gc}^2} = 1$$

$$\Rightarrow \omega_{gc}^2 (1 + \omega_{gc}^2) = 1$$

$$\omega_{gc}^4 - \omega_{gc}^2 - 1 = 0$$

$$\omega_{gc}^2 = 1.27$$

$$\phi_{jc} = -90^\circ - \tan^{-1} \omega_{gc} \\ = -141.78^\circ$$

$$\text{Phase margin} = 180^\circ + \phi_{jc} = 38.21^\circ \quad \text{Choice (B)}$$

27. Given system

$$G(S) H(S) = \frac{9(s+2)}{s(1+3s)(1+5s)}$$

Error due to Ramp input is $= 1/K_a$

$$\text{Where } K_a = \lim_{s \rightarrow 0} s^2 G(S) = 0$$

Unit parabolic i/p $= 1/K_a$

$$= \frac{1}{0} = \infty$$

Choice (A)

$$28. GH(j\omega) = \frac{K(1+j\omega)^2}{(j\omega)^3}$$

$$\Rightarrow |GH| = \frac{K(1+\omega^2)}{\omega^3}$$

$$\angle GH(j\omega) = -270^\circ + 2\tan^{-1}\omega$$

As ω increases from 0 to ∞ , phase -270° to -90° .

Due to S^3 term there will be 3 infinite semicircles.

Choice (C)

$$29. \frac{C(s)}{R(s)} = \frac{K_1}{s^2 + (2+K_2)s + K_1}$$

$$\omega_d = \omega_n \sqrt{1-\xi^2}$$

$$10 = \omega_n \sqrt{1-(0.8)^2}$$

$$\omega_n = \frac{10}{0.6} = 16.66$$

$$\Rightarrow 2 + K_2 = 2\xi\omega_n$$

$$2 + k_2 = 2 \times 0.8 \times 16.7$$

$$\Rightarrow K_2 = 24.66$$

Choice (C)

30. Closed loop transfer function

$$= \frac{125 \times 4}{(s^2 + 3s + 2)(s+3)(s+4) + 125 \times 4}$$

$$= \frac{500}{(s^2 + 3s + 2)(s^2 + 7s + 12) + 500}$$

Characteristic equation

$$= (s^2 + 3s + 2)(s^2 + 7s + 12) + 500$$

$$\Rightarrow s^4 + 10s^3 + 35s^2 + 50s + 524 = 0$$

S^4	1	35	524
S^3	10	50	0
S^2	30	524	
S^1	-124.7	0	
S^0	524		

There are two sign changes so it unstable.

Choice (B)

$$31. M_p = e^{-\xi\pi/\sqrt{1-\xi^2}} = 0.2$$

$$\Rightarrow \xi = 0.456$$

$$T_s = \frac{4}{\xi\omega_n}$$

$$\Rightarrow \omega_n = \frac{4}{\xi T_s} = \frac{4}{0.456 \times 0.6} = 14.6$$

$$\text{Then poles are } -\xi\omega_n \pm j\omega_n \sqrt{1-\xi^2}$$

$$= -14.6 \times 0.456 \pm j14.6\sqrt{1-(0.456)^2}$$

$$= -6.6576 \pm j13$$

Choice (A)

$$32. \omega = \frac{0.5}{T}$$

$$\angle G\left(\omega = \frac{0.5}{T}\right) = -\tan^{-1} \omega T$$

$$= -\tan^{-1} 0.5 = -26.56^\circ$$

From the phase plot at $\omega = \frac{0.5}{T}$

$$\angle GH(S) = -30^\circ$$

$$\text{Error} = -26.56^\circ + 30^\circ = 3.44^\circ$$

33. At $\omega = \frac{0.5}{T}$

$$|GH| = \left| \frac{K}{1 + jT \frac{0.5}{T}} \right| = \frac{K}{\sqrt{1.25}}$$

$$20 \log |GH| = 20 \log K - 10 \log 1.25$$

$$= 20 \log K - 0.97$$

$$\text{From the plot at } \omega = \frac{0.5}{T} = 20 \log K$$

$$\text{So error in gain} = 0.97 \text{ dB}$$

Choice (A)

$$\begin{array}{c|ccc} S^4 & 1 & 52 & 75+K \\ S^3 & 10 & 118 & 0 \\ S^2 & 40.2 & 75+1C & \\ S^1 & 3993.6 - 10K & & \\ \hline S^0 & 40.2 & & \\ & 75+K & & \end{array}$$

$$\Rightarrow 75 + K > 0$$

$$K > -75$$

$$\Rightarrow 3993.6 - 10K > 0$$

$$\Rightarrow K < 399.36$$

\Rightarrow The range of K for the system to be stable
 $0 < K < 399.36$

[$\therefore K$ range starts from zero]

\Rightarrow For $K = 399.36$ system will oscillate Choice (D)

34. Given system is open loop transfer function

$$G(S) = \frac{K}{(s+3)(s+1)(s^2 + 6s + 25) + K}$$

\Rightarrow Characteristic equation is

$$(s^2 + 4s + 3)(s^2 + 6s + 25) + K = 0$$

$$s^4 + 10s^3 + 52s^2 + 118s + 75 = 0$$

Choice (D)

35. If $K = 399.36$ then S^1 row becomes zero. The co-efficients of auxiliary equation are given by the s^2 row.

$$40.2s^2 + 75 + 399.36 = 0$$

$$s^2 = -11.8$$

$$\Rightarrow s = \pm j3.43$$

When $K = 399.36$, the system has roots on imaginary axis and so it oscillates. The frequency of oscillation is given by the value of root on imaginary axis.

Frequency of oscillation $\omega = 3.43 \text{ rad/sec}$ Choice (B)