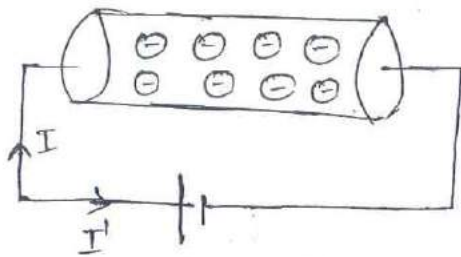


Fundamentals :-



where $I' = \text{Natural Current}$
 $I = \text{conventional Current}$

- * The basic quantity in electric circuit is "charge", charge of the electron is given by $-1.602 \times 10^{-19} \text{ C}$.
- * The flow of electrons is called as "current" (or) the time rate of charge is also called as "current".
- * By using conventional current only KVL & KCL eqns are developed. $I = (dQ/dt) \text{ C/s (or) Amps}$
- * To move the electron from one point to another point in particular direction external force is required, in electric circuits external force is provided by electromotive force (EMF). And it is given by

$$V = \frac{dw}{dQ} \quad \text{J/C (or) volts}$$

The time rate of energy is called as "Power".

$$P = \frac{dw}{dt}$$

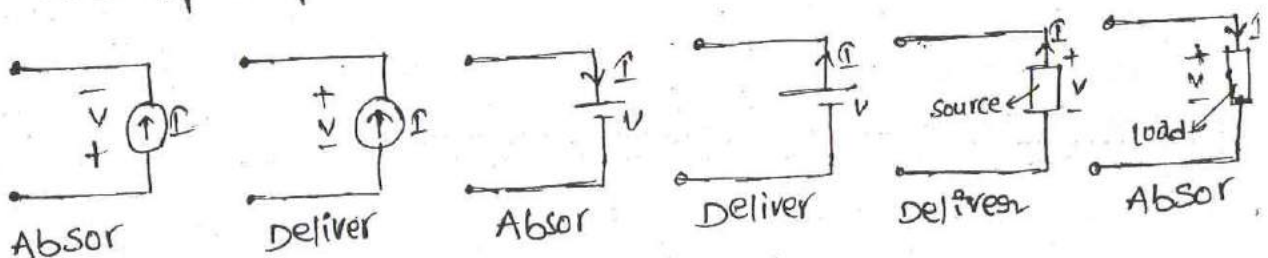
$$= \frac{dw}{dt} \times \frac{dQ}{dQ}$$

$$= \frac{dw}{dQ} \cdot \frac{dQ}{dt}$$

$$P = V \cdot I$$

Now we will discuss some more conclusions on power from the following diagrams.

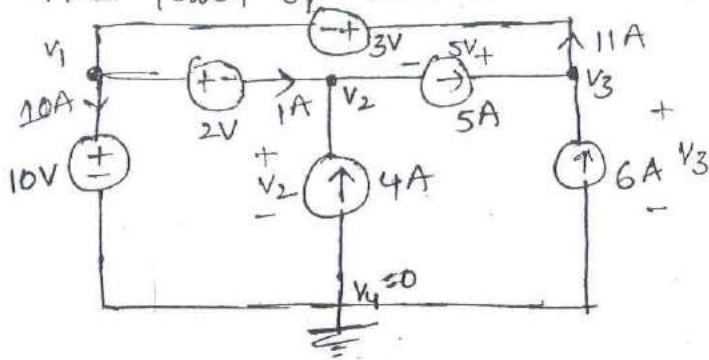
Ex:-



Note:- 1. Current is entering at +ve terminal element is absorbing power.

2. When current is leaving from +ve terminal, element is delivering power.

Prob find Power of each elements of the N/W shown.



$$\therefore V_1 = 10V$$

$$V_1 - V_2 = 2V$$

$$\Rightarrow V_2 = 8V$$

$$V_3 - V_1 = 3$$

$$V_3 = 13V$$

$$P_2 = V_2 I = 8 \times 4 = 32W \text{ (Deliver)}$$

$$P_3 = 13 \times 6 = 78W \text{ (Deliver)}$$

$$P_{5A \text{ branch}} = 5 \times 5 = 25W \text{ (Deliver)}$$

$$P_{3V} = 3 \times 11 = 33W \text{ (Absorb)}$$

$$P_{10V} = 10 \times 10 = 100W \text{ (Absorb)}$$

$$P_{2V} = 2 \times 1 = 2W \text{ (Absorb)}$$

Note:- In any N/W
delivering = absorbing
 $135W = 135W$
so our calculation is
exactly correct.

ENERGY:-

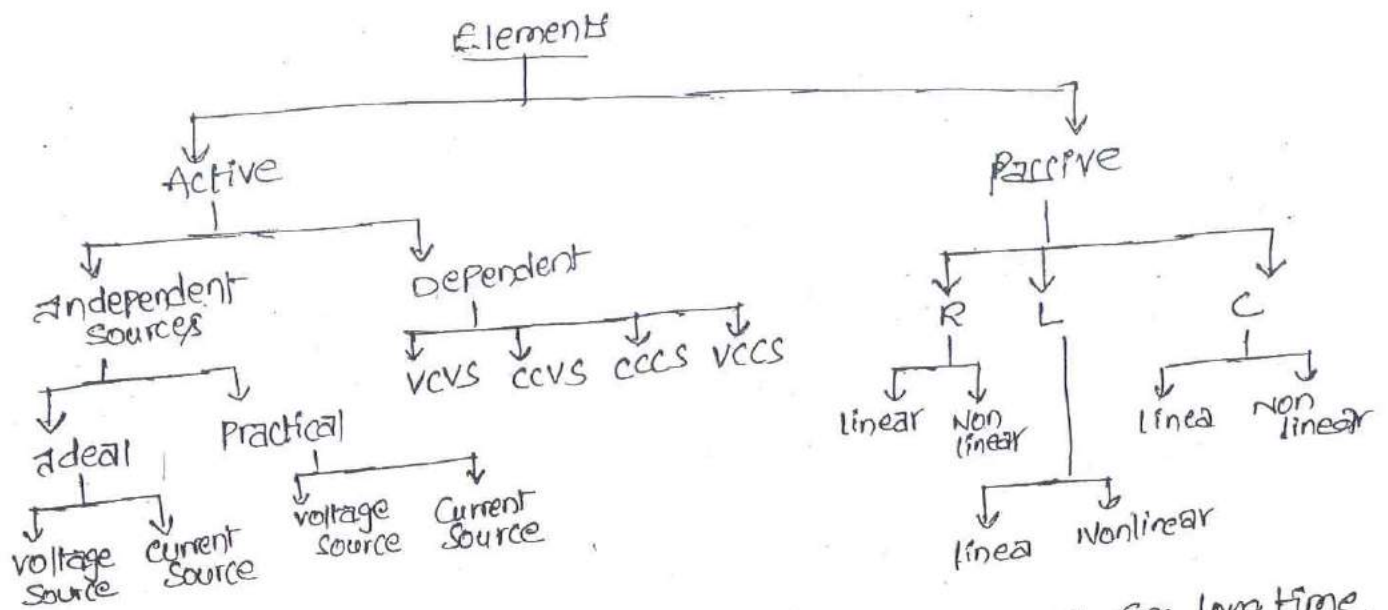
The capacity to do the work is called as "energy".

$$W = \int_0^t P dt$$

watt-sec
(or) joules

Classification of elements:-

- 1) Active & Passive elements
- 2) linear & nonlinear elements
- 3) unidirectional & bidirectional elements
- 4) time variant & time invariant elements
- 5) Lumped & distributed elements



Active Elements:-
 When the element is capable of delivering energy for long time (approximately ∞ time).

(OR)
 When the element is having property of internal amplification then the element is called as "active element".
 Ex:- voltage source, current source, transistor & OP-amp.

V, I sources $\rightarrow$ independent
 OP-amp, transistor $\rightarrow$ dependent

Note:-
 During discharging capacitor (or) inductor can deliver energy independently for short time and capacitor (or) inductor is not having property of internal amplification.

Passive elements:-

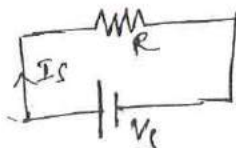
When the element is not capable of delivering energy independently then it is called as "passive element".

Ex:- (Resistor) Bulb

Transformer $\rightarrow$ It only stepup (or) stepdown the voltage. NOT " " the power. So there is no internal amplification.

Resistor:-

Resistance is a property of the resistor it opposes flow of current by doing so it converts electric energy to Heat energy.

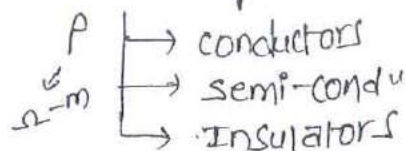


$$P = I^2 R$$

$$\therefore W = P \times t = \frac{I^2 R t}{\text{Heat energy}}$$

$$R = \frac{\rho l}{a}$$

Basically materials are classified into 3 types based on resistivity property.



Superconductor
 $\rho = 0$
Ex:- mercury at 4.15 K

$$R_t = R_0(1 + \alpha_0 t)$$

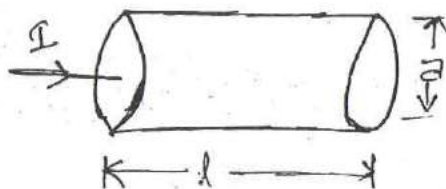
R_0 = Resistance at 0°C

α_0 = Tempⁿ Co-effⁿ

t = change in Tempⁿ

conductors have the +ve Tempⁿ Co-effⁿ
 Insulators " " -ve " " "

Ohm's law:-



Ohm's law states that at constant Tempⁿ current density is directly proportional electric field intensity.

$$J \propto E$$

$$J = \sigma E$$

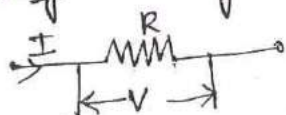
$$\frac{I}{a} = \frac{1}{\rho} \times \left(\frac{V}{l} \right)$$

$$\frac{V}{I} = \frac{\rho l}{a} = R$$

$$\therefore \frac{V}{I} = R$$

$$\left\{ \begin{array}{l} \because J = I/a \quad \text{A/m}^2 \\ E = \frac{V}{l} \quad \text{V/m} \\ \sigma = 1/\rho \quad \text{mho/m} \\ R = \frac{\rho l}{a} \end{array} \right.$$

Ohm's law states that at constant Tempⁿ potential difference across the elements is directly proportional to current flowing through element.



$$V \propto I$$

$$V = RI$$

$$R = \frac{V}{I} = \text{constant}$$

note:

$$\frac{1}{\sigma} = \frac{1}{\rho} \times \frac{V}{A}$$

$$\frac{1}{V} = \frac{A}{\rho l}$$

$$\frac{1}{V} = \frac{1}{R}$$

$$I = \frac{1}{R} V$$

$$I \propto V$$

** note:- ohm's law is valid when Tempⁿ & conductivity of the material are constant.

ohm's law
1st form *

$$J = \sigma E$$

→ Basic formula

$$V = RI$$

→ 2nd form

$$I = GV$$

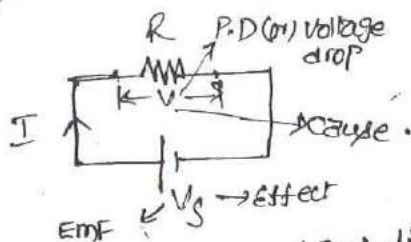
→ 3rd form

$$V = R \frac{dQ}{dt}$$

→ 4th Form

$$(\because G = \frac{1}{R}) \text{ mho or } S$$

Notes:-



which one is right?

$$I \propto V_s$$

EMF

$$V \propto I$$

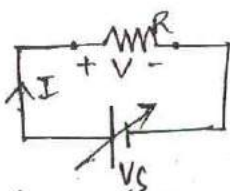
Potential diff. (or) voltage drop

both are right.

→ Diffⁿ b/w EMF & potential diffⁿ
↓
source voltage ↓
voltage drop.

→ out of these two effect is EMF & cause is P.D (or) voltage drop.
→ EMF is independent on current magnitude as well as resistance.
but potential diffⁿ depends " " " "

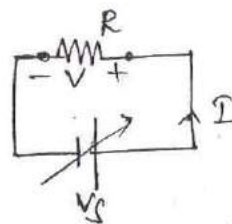
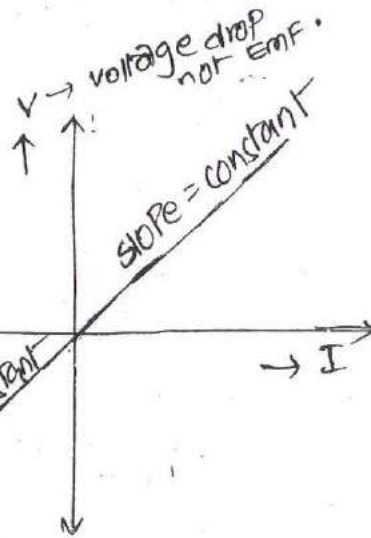
V-I Charⁿ :-



if $I \uparrow 10\% \Rightarrow V \uparrow 10\%$
 $I \uparrow 90\% \Rightarrow V \uparrow 90\%$

so

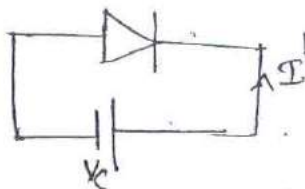
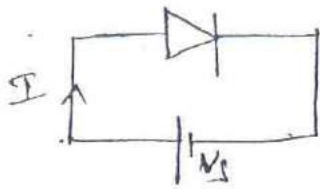
$$\frac{V}{I} = \text{constant} = R$$



Here just we are reversing the polarities. Analysis is same.

- * When element properties and charⁿ are independent on the direction of the current then the element is called as "Bidirectional element".
- * When element obeys the ohm's law then the element is called as "linear resistor".

- * Every linear element should obey the bidirectional property but not viceversa.



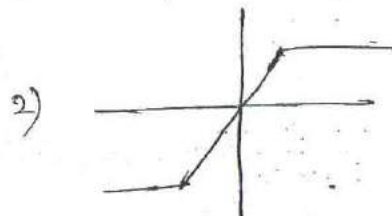
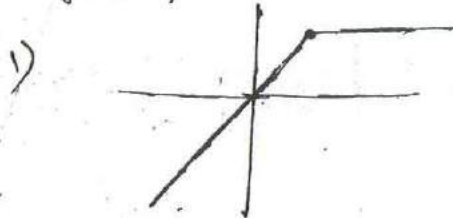
$$I \neq I'$$

- * When element properties and charⁿ depends on the direction of the current then the element is called as "unidirectional element".

Ex:- Diode

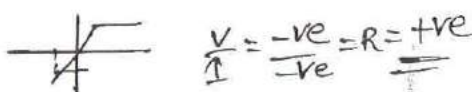
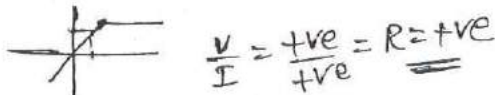
- * When element doesnot obeys the ohm's law then the element is called as Non linear Resistor.

Let us consider the following $V-I$ charⁿ & conclude which type of element it is?



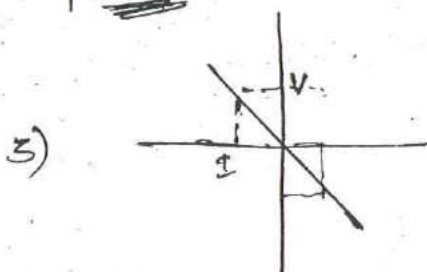
- * Non-linear
- * Bidirectional
- * Passive

- * Nonlinear
 - * unidirectional
- Active (or) passive = ?
- If charⁿ are identical then it is Bidirectional, otherwise unidirectional.



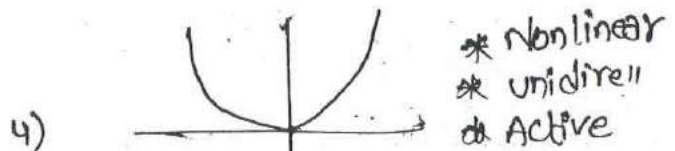
Whenever $\frac{V}{I}$ ratio is +ve, then it is passive. Always $R \geq 0$
 $L \geq 0$
 $C \geq 0$
 -ve values doesn't exist.

- so conclusion is
- * passive

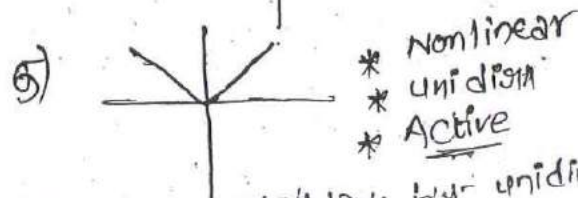


- * linear
- * Bi-directional
- * Active

When even $\frac{V}{I}$ ratio is -ve then it is a "Active element".



- * Nonlinear
- * unidireⁿ
- * Active



- * Nonlinear
- * unidireⁿ
- * Active

Here it obeys ohm's law, but unidireⁿ.
 Every linear element should be bidireⁿ.
 so non linear.

Notes:-

1. If $\frac{V}{I}$ is +ve in the both co-ordinates then the element is Passive.
2. When element obeys the bidirectional property char are identical in the opposite co-ordinates but not in the adjacent co-ordinates.
3. Every linear element should obey the bidirectional property but not viceversa.

Inductor:-

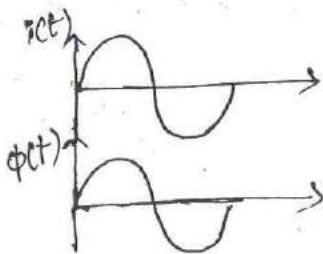
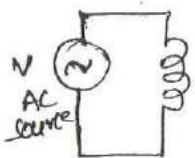
Diffⁿ b/w plain conductor & inductor.



Weak magⁿ field



due to twisted arrangement group of magnetic flux links are obtained. so strong magⁿ field is obtained.



Faraday's 1st law:-

When conductor cuts a magⁿ lines of the force an EMF induced in the conductor.

Faraday's 2nd law:-

EMF induced in the conductor is directly proportional to rate of change flux.

$$e \propto \frac{d\phi}{dt}$$

$$e = -N \frac{d\phi}{dt}$$

to satisfy lenz's law.

where e = statically induced EMF

practical ex:- Transformer

flux linkages,
 $\psi = N\phi$

$$v = \frac{d\psi}{dt} = e$$

$$\phi \propto i$$

$$\psi \propto \phi$$

$$\Rightarrow \psi \propto i$$

$$\psi = Li$$

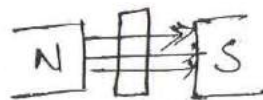
$$v = L \frac{di}{dt}$$

$$\Rightarrow L = \frac{v}{di/dt}$$

$$\psi = N\phi$$

$$\psi = Li$$

$$\Rightarrow L = \frac{N\phi}{i}$$



$$1) e \propto \frac{d\phi}{dt}$$

$$3) e = Blv \sin \theta$$

where e = dynamically induced EMF

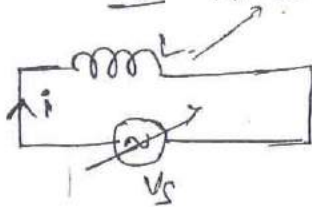
ex: Generator

where B = flux density
 l = active length of conductor
 v = linear velocity of conductor
 θ = phase angle between conductor & flux line

Networks...

1) When inductance of the inductor is independent on the current magnitude then the inductor is called as "linear inductor".

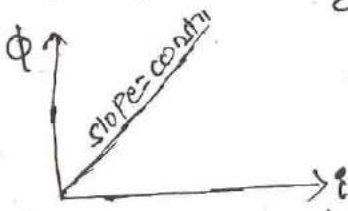
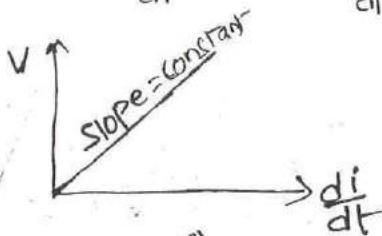
ex:- Aircore inductor



$$i \uparrow 10\% \quad \phi \uparrow 10\%$$

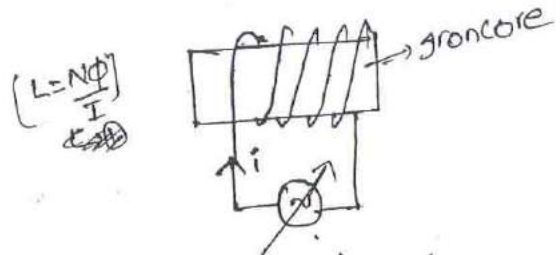
$$i \uparrow 90\% \quad \phi \uparrow 90\%$$

$$V = L \frac{di}{dt} \Rightarrow L = \frac{V}{\frac{di}{dt}}$$



2) When inductance of inductor depends on current magnitude then the inductor is called as "Non linear inductor".

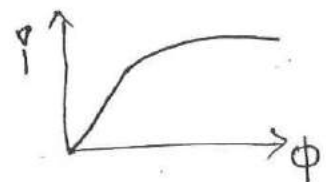
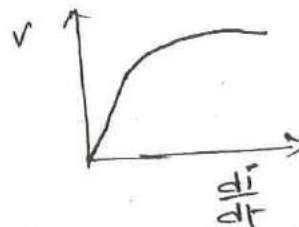
ex:- Iron core inductor



$$i \uparrow 10\% \quad \phi \uparrow 10\%$$

$$i \uparrow 60\% \quad \phi \uparrow 60\%$$

$$i \uparrow 90\% \quad \phi = \text{constant} \quad (\text{core is saturated})$$



Electric

Magnetic

$$1) i = \frac{\text{EMF}}{R}$$

$$1) \phi = \frac{\text{MMF}}{S}$$

$$2) i = \frac{\text{EMF}}{\left(\frac{\rho l}{a}\right)}$$

$$2) \phi = \frac{NI}{\frac{l}{\mu_0 \mu_r a}} \rightarrow 2$$

upto some position linearly then non-linear.

now substitute eq 2 in eq 1

$$L = \frac{N^2 \mu_0 \mu_r a}{l}$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ H/m}$$

μ_r = Relative permeability. ($\mu_r = 1$ for air)

permeability is the property of the medium in which magnetic field exist.

$$L = \frac{N^2 \mu_0 \mu_r a}{l} = \frac{N^2}{\left(\frac{l}{\mu_0 \mu_r a}\right)} = \frac{N^2}{S}$$

$$\therefore L = \frac{N^2}{S} \quad ***$$

By knowing the no. of turns and reluctance we can find out the reluctance.

Notes:-

$$V = L \frac{di}{dt}$$

→ This formula valid only for linear inductor.

$$i = \frac{1}{L} \int_{-\infty}^t V dt$$

Here voltage and current are related. So we can call this as "Ohm's law 5th form".

→ This is also valid only for linear inductor. Here Ohm's law is related to element like in resistor $i \propto V$. Similarly $i \propto \int_{-\infty}^t V dt$

Ohm's law 6th form

1. Power dissipation in ideal inductor is equal to zero since internal resistance = 0.
2. Inductor stores energy in the form of magnetic field (kinetic energy).

w.k.T $W = \int P dt$

$$P = V \cdot i = L \frac{di}{dt} \cdot i \rightarrow \text{Instantaneous Power}$$

$$W = \int P dt = \int L \cdot \frac{di}{dt} \cdot i dt = \frac{1}{2} Li^2 = \dots$$

$$\therefore W = \frac{1}{2} Li^2$$

3. Under steady state condition for DC source inductor acts as a short ckt.

$$V = L \frac{di}{dt}$$

$$\frac{di}{dt} = 0$$

$$\Rightarrow V = 0 \rightarrow \text{s.c}$$



So for Constant Current

$$\frac{di}{dt} = 0$$

Note:-

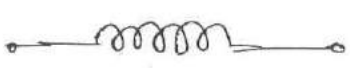
- 1) Inductor does not allow sudden change of currents since for sudden change of current infinite voltage is required.

$$V = L \frac{di}{dt}$$

$$\text{As } dt \rightarrow 0 \Rightarrow V = L \frac{di}{dt} = \infty$$

- 2) Inductor does not allow sudden change of currents since practical inductor ckt has finite value of time constant.

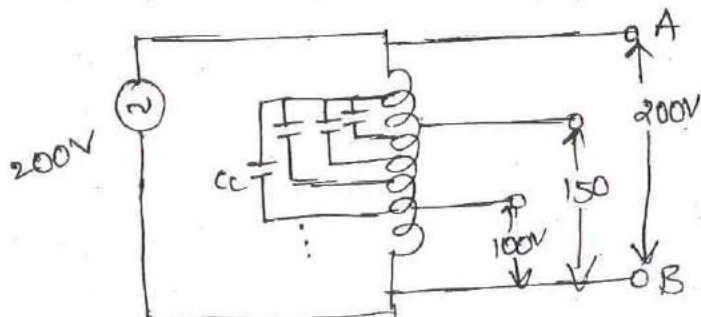
$$T = \frac{L}{R}$$

- 3)  ideal inductor $r=0 \rightarrow$ internal resistance

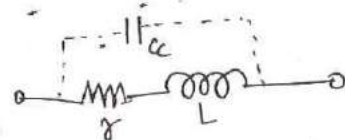


$$r = m\Omega$$

- 4) Interturn capacitance is present when inductor is operated either at high frequency (or) high voltage.



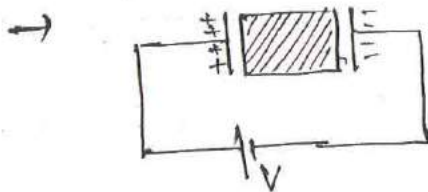
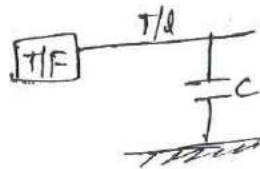
$C_c =$ Interturn capn
(or)
self capn



$$X_L = 2\pi fL; X_C = \frac{1}{2\pi fC}$$

so when f high $\Rightarrow X_C = \text{low}$ so entire current passes through self capn.

$\rightarrow$ self capn is also present in the T/F



$$Q \propto V$$

$$Q = CV$$

$$C = \frac{Q}{V}$$

coulombs/volt (or) farads

$$Q = CV$$

$$\frac{dQ}{dt} = C \frac{dV}{dt}$$

$$I = C \frac{dV}{dt} \rightarrow \text{ohm's law + thm form}$$

$$C = \frac{I}{\frac{dV}{dt}} \Rightarrow \text{cap limits sudden changes in current voltage.}$$

$$V = \frac{1}{C} \int_{-\infty}^t i dt \rightarrow \text{8th Form}$$

$$P = VI = V \cdot C \frac{dV}{dt} \rightarrow \text{instantaneous power}$$

$$W = \int P dt = \int V \cdot C \frac{dV}{dt} \cdot dt = \frac{1}{2} CV^2$$

$$W = \frac{1}{2} CV^2 \text{ Joules}$$

note:-

$$\frac{dV}{dt} = 0 \rightarrow \text{under steady state cond.}$$

$$\frac{dV}{dt} \rightarrow \text{not zero under transient.}$$

$$\frac{dQ}{dt} = C \frac{dV}{dt} = 0$$

$\rightarrow$ only for steady state cond. for generalize the expression we are taking $\frac{dV}{dt}$ as it is.

* power dissipation in ideal capacitor is equal to zero.

* capacitor stores energy in the form of electric field (potential energy)

$$C = \frac{\epsilon A}{d}$$

$$\epsilon = \epsilon_0 \epsilon_r$$

$$\epsilon_0 = 8.854 \times 10^{-12} \text{ Fm}$$

$\epsilon_r =$ Relative permittivity

(air $\epsilon_r = 1$)

* Permittivity is the property of the medium in which electric field exist.

A = Area of cross section of conduction plate
d = distance b/w two conducting plates.

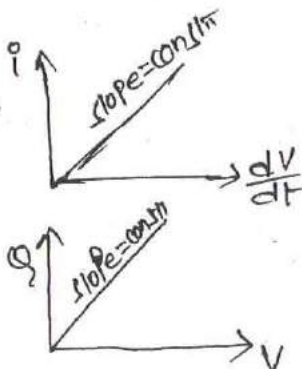
*

$$C = \frac{Q}{V}$$

$$V \uparrow 10\%, Q \uparrow 10\%$$

$$V \uparrow 90\%, Q \uparrow 90\%$$

$$i = C \frac{dV}{dt} \Rightarrow C = \frac{i}{\left(\frac{dV}{dt}\right)}$$

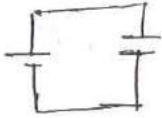


When capacitance of the capacitor is independent on the voltage magnitude then the capacitor is called as "linear capacitor"

* When capacitance of the capacitor depends on the voltage magnitude then the capacitor is called as "nonlinear capacitor"

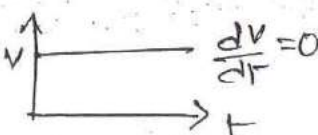
Ex:- varactor diode

$$C = \frac{Q}{V} = \text{variable} \rightarrow \text{for non linear capacitor.}$$

*  As the capacitor is continuously charging, at a particular point $i=0$.

In other words at steady state $\frac{dV}{dt} = 0 \Rightarrow i=0$

→ under steady state condⁿ for DC source capacitor acts as a "open circuit".

$$i = C \frac{dV}{dt}$$


$$\frac{dV}{dt} = 0$$

$$i = 0 \quad (\because \frac{dV}{dt} = 0)$$

↓
O.C

Note:-

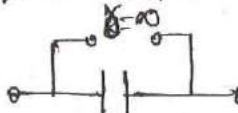
① *

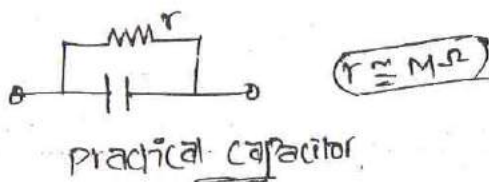
$$i = C \frac{dV}{dt}$$

$$\text{As } dt \rightarrow 0, i = C \frac{dV}{dt} = \infty$$

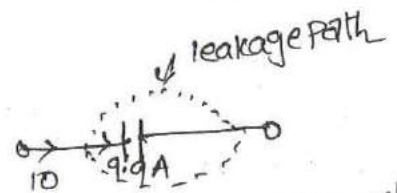
capacitor doesn't allow sudden changes in ~~err~~ currents, of voltage.
since for sudden change of voltages infinite current is required.

② capacitor does not allow sudden change of voltage since practical capacitor circuit has finite value of time constant.

Note:-  ideal capacitor



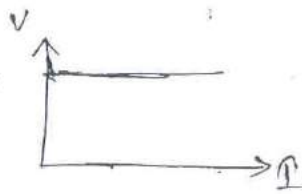
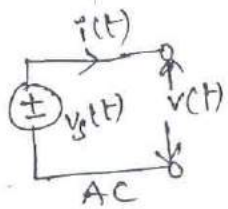
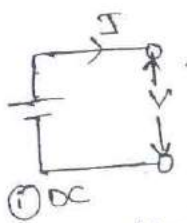
$$r \approx M\Omega$$



that's why we are connecting parallel.

$r = \text{leakage path res}^n$

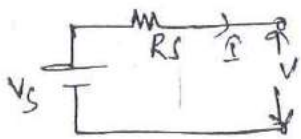
Air is the medium. Air offers high resⁿ. so it is order of Megaohms.



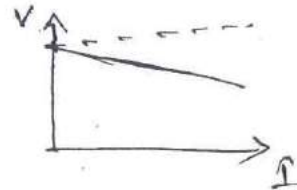
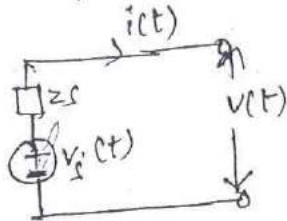
→ V-I charⁿ non linear.
Any charⁿ which starts from origin are linear.
→ so doesn't obey Ohm's law.

Ideal voltage source

→ Generally DC values represented by capital V, & I.



R_s = internal resistance



DC

AC

$$V_s = V + IR_s$$

$$\Rightarrow \underline{V = V_s - IR_s}$$

practical voltage sources

* Note:

* Ideal voltage source delivers energy at a specified voltage (V) which is independent on current delivered by the source.

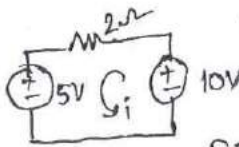
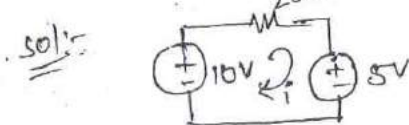
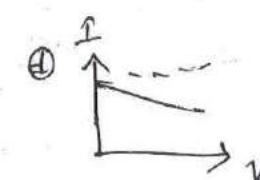
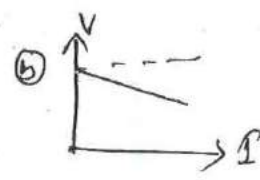
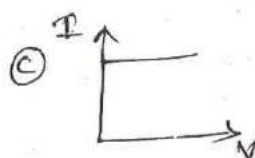
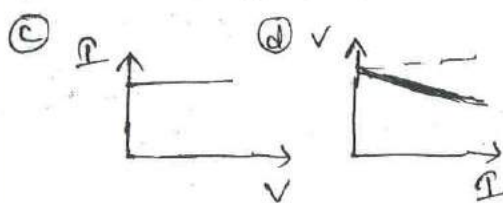
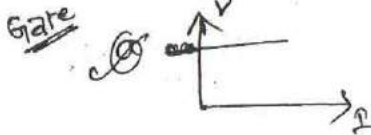
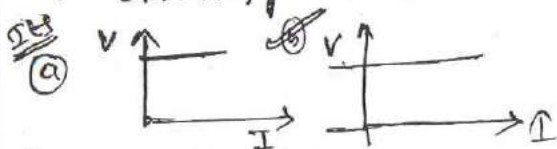
Internal resⁿ of ideal voltage source = 0

* practical voltage source delivers energy at specified voltage (V) which depends on current delivered by the source.

* independent voltage source does not obey's the Ohm's law since V-I charⁿ is Non linear.

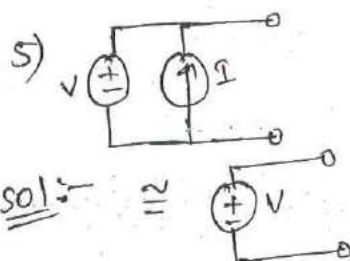
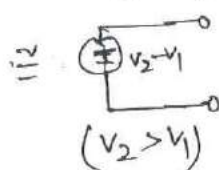
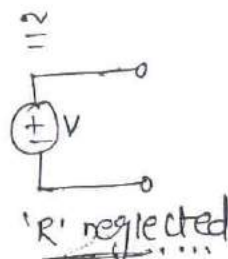
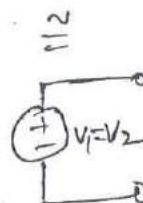
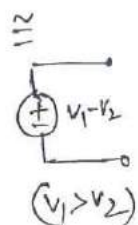
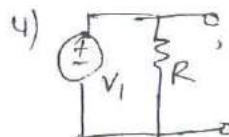
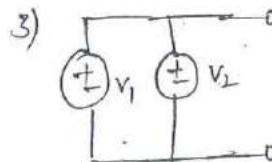
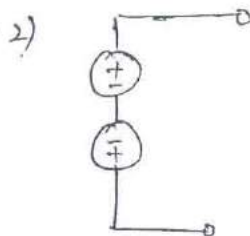
* Independent voltage source is unidirectional & Non linear element.

→ Identify V-I charⁿ ideal voltage source.



Based on options you have to select.

70

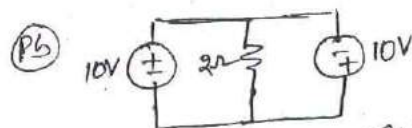


(A6)



Given Nlw is not satisfy the KVL. So we can't apply the Nlw Analysis.

Note:- w.r.to KVL voltage across all the parallel branches should be equal.



Ans:- NOT satisfy KVL.

by using
= above rules $\approx$

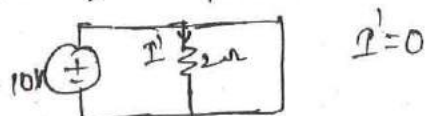


$\Rightarrow I = \frac{10}{2} = 5A$

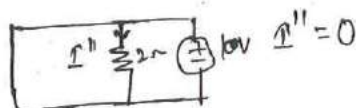
above rules =  $\therefore \quad \therefore \quad \therefore$

We have one doubt: when ever two or more sources are present,
we have to use super position theorem

case ①:-



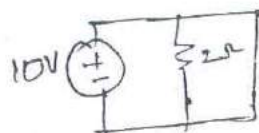
Case ii:-



w.r.to " Super position Theorem reduction Technique "

that means superposition theorem is wrong?

Let us consider case (i) or (ii)



this ckt will not satisfy the KVL. So we never apply superposition theorem to this ckt.

for the above circuit superposition theorem can not be applied. Since case (i) & case (ii) are not satisfy KVL.

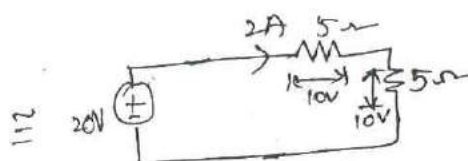
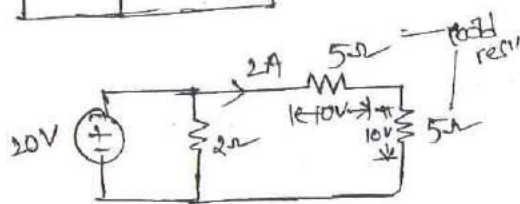
(P2)



$$I = \frac{20 \times 12}{20}$$

$$I_S = \frac{20 \times 2}{12}$$

Sol:-



With 2Ω res || & without 2Ω res || the load current is same. So while calculating the load current we can neglect the 2Ω res ||.

Now for ex || if he asking the source current / source power.

$$I_S = 10 + 2 = 12A ;$$

with 2Ω res ||

$$P_S = 12 \times 20 = 240W$$

without 2Ω res ||:-

$$I_S = 2A$$

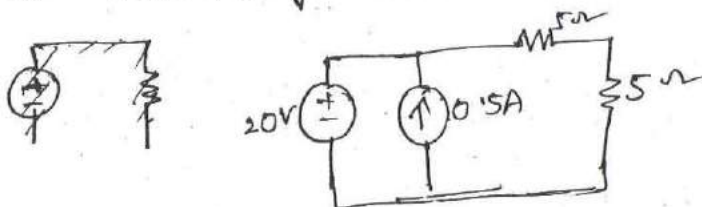
$$P_S = 20 \times 2 = 40W$$

So I_S & P_S are not same. Therefore 2Ω res || should not be neglected while calculating the source current & source power.

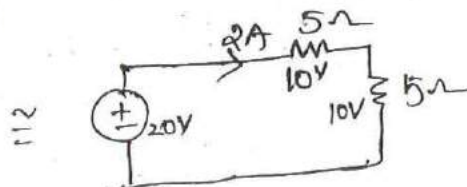
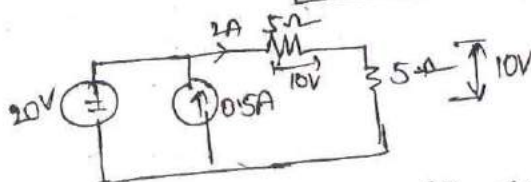
NOTE:- 1) In the above circuit 2Ω resistance can be neglected while calculating either load current (or) load voltage.

2) In the above circuit 2Ω resistance can not be neglected while calculating either source current (or) source power.

(P3)



Sol:-



So in both cases $I_{load} = 2A$.

Now $I_S = ?$

Without ~~res~~ current source

$$I_S = 2A$$

$$P_S = 20 \times 2 = 40W$$

with current source

$$I_S + 0.5 = 2$$

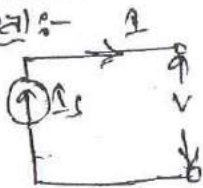
$$I_S = 1.5$$

$$P_S = 20 \times 1.5 = 30W$$

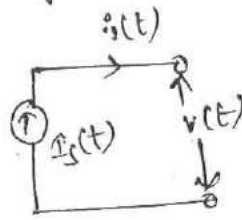
so while calculating P_S , I_S don't remove current source.

Note:- 1) In the above circuit current source can be neglected while calculating either load current or load voltage.
2) In the above circuit current source can not be neglected while calculating either voltage source current (or) voltage source Power.

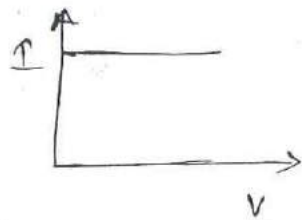
Ideal:-



D.C

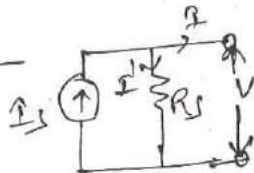


A.C



Since Time ~~var~~ not function of

Practical:-

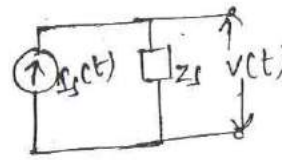


D.C

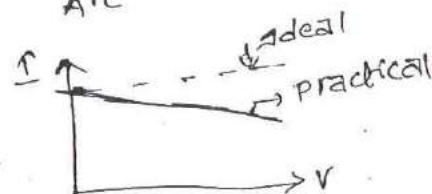
$$I_S = I + I'$$

$$I = I_S - I'$$

$$I = I_S - \frac{V}{R_S}$$

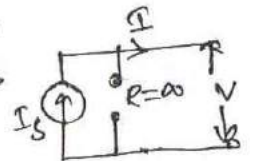


A.C

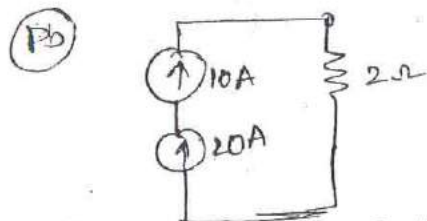
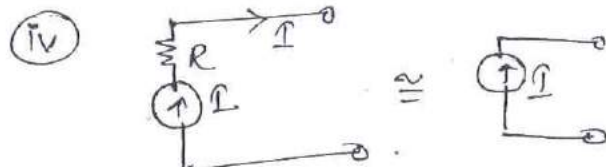
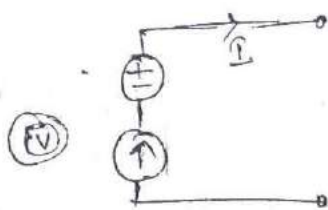
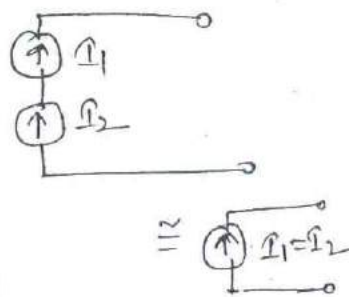
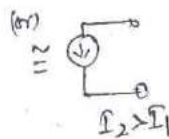
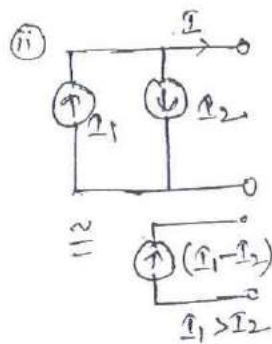
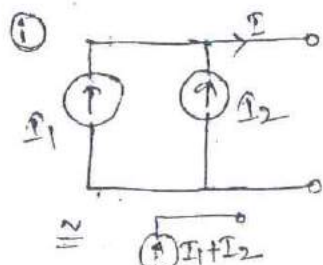


Note:-

1. Ideal Current Source delivers energy at specified current (I) which is independent on voltage across the source.
2. Internal resⁿ of Ideal Current Source $= \infty \rightarrow$
3. Practical Current Source delivers energy at specified current (i) which depends on voltage across the source.
4. Independent Current Source does not obey's the ohm's law since $V-I$ charⁿ is Nonlinear.

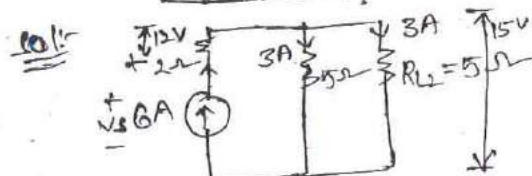
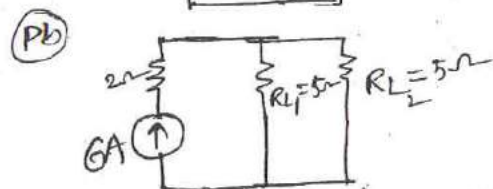
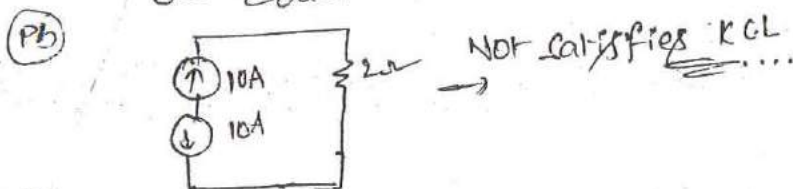


Note:- In Real Time applications No Independent Current Source is Exist. But dependent ^(on system) current source ~~are~~ exist.
(Just for Convience only we take taking on modifying the Voltage Source into Current source)



(a) 10A (b) 20A (c) 30A ~~(d) None~~
(Not satisfy KCL)

Sol:- W.r.to KCL Current flowing through all the series elements should be equal.

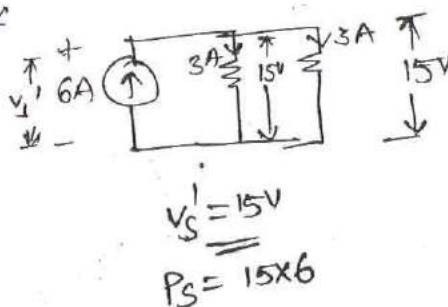


$$-V_s + 12 + 15 = 0$$

$$V_s = 27V$$

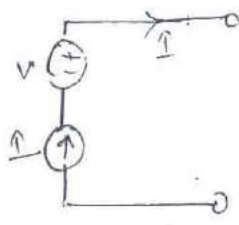
$$P_s = 27 \times 6$$

Based on Reduction technique we can eliminate the resistance 2Ω .



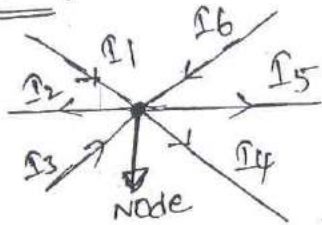
Note:-

- 1) In the above circuit 2Ω resistance can be neglected while calculating either load current (or) load voltage....
- 2) In the above circuit 2Ω resistance can not be neglected while calculating either voltage across current source (or) power of the current source.



Explanation:- 1. In the given circuit voltage source can be neglected while calculating either load current or load voltage.
 2. In the above circuit voltage source cannot be neglected while calculating either voltage across current source (or) power of the current source.

KCL:-

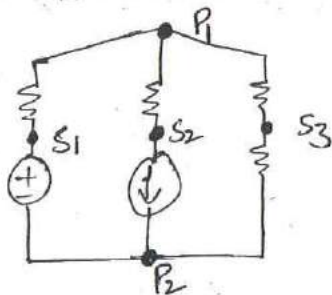


Mathematical Expression:-

$$I_1 - I_2 + I_3 - I_4 - I_5 + I_6 = 0$$

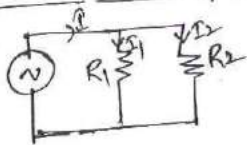
note:-
 (node) $\left\{ \begin{array}{l} \text{simple node} \\ \text{principle node} \end{array} \right.$

- * KCL works based on the principle of "law of Conservation of charge"
- * KCL states that algebraic sum of currents meeting at a point is equal to zero.
- * When the two elements are connected together then the common point is called as "Simple Node".
- * When more than two elements are connected together then the common pt is called as "principle Node".



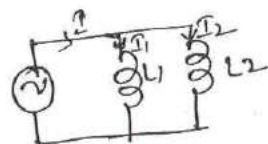
where
 S_1, S_2, S_3 are $\rightarrow$ Simple Nodes
 $P_1, P_2 \rightarrow$ Principle Nodes

Current division Rule:-



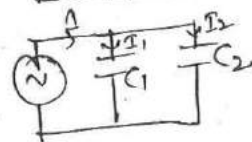
$$I_1 = I \cdot \frac{R_2}{R_1 + R_2} ; I_2 = I \cdot \frac{R_1}{R_1 + R_2}$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2}$$



$$I_1 = I \cdot \frac{L_2}{L_1 + L_2} ; I_2 = I \cdot \frac{L_1}{L_1 + L_2}$$

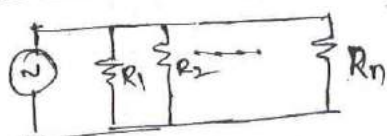
$$\frac{1}{L_{eq}} = \frac{1}{L_1} + \frac{1}{L_2}$$



$$I_1 = I \cdot \frac{C_2}{C_1 + C_2} ; I_2 = I \cdot \frac{C_1}{C_1 + C_2}$$

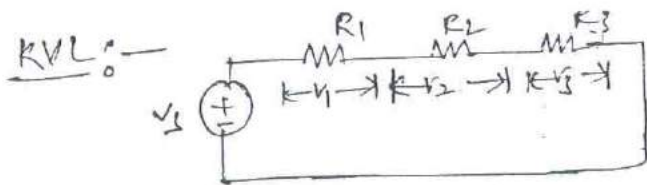
$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$$

With 'n' branches:-

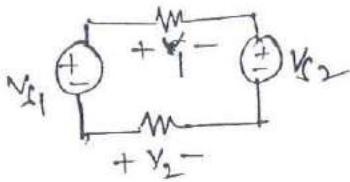


$$I_1 = I \cdot \frac{\frac{1}{R_1}}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}}$$

similarly for inductor & opposite to capacitor.



$$V_1 + V_2 + V_3 - V_s = 0$$



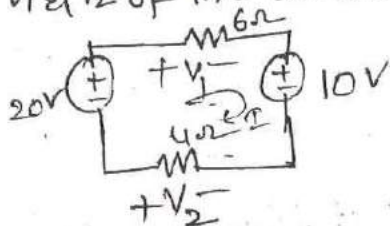
$$-V_{s1} + V_1 + V_{s2} - V_2 = 0$$

$$\Rightarrow V_2 + V_{s1} = V_1 + V_{s2}$$

* KVL works based on the principle of law of conservation of energy.

* KVL states that Algebraic sum of the voltages in a closed loop is equal to zero.

(pb) Find V_1 & V_2 of the ckt shown?



$$\text{Sol: } -20 + V_1 + 10 - V_2 = 0$$

$$V_1 - V_2 = 10$$

$$-20 + 6I_1 + 10 + 4I_1 = 0$$

$$2I_1 = 10$$

$$I_1 = 5A$$

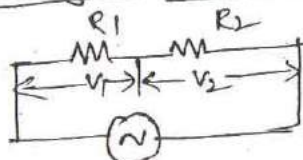
$$\therefore V_1 = 30V$$

$$V_2 = 20V$$

$$V_1 = 6V$$

$$V_2 = -10V$$

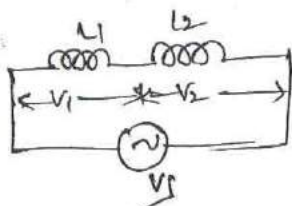
(pb) voltage division Rule:-



$$R_{eq} = R_1 + R_2$$

$$V_1 = V_s \cdot \frac{R_1}{R_1 + R_2}$$

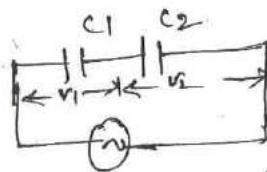
$$V_2 = V_s \cdot \frac{R_2}{R_1 + R_2}$$



$$L_{eq} = L_1 + L_2$$

$$V_1 = \frac{L_1}{L_1 + L_2} \cdot V_s$$

$$V_2 = V_s \cdot \frac{L_2}{L_1 + L_2}$$



$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$V_1 = \frac{C_2}{C_1 + C_2} \cdot V_s$$

$$V_2 = \frac{C_1}{C_1 + C_2} \cdot V_s$$

note:- for analysis of any N/w field theory

N/w Theory $\rightarrow$ low frequ

developing mathematical eqns are complex.

Dev " " simple.

Always we obtain approximate results. Accurate results in KVL, KCL.

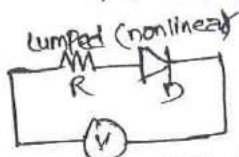
are possible in field theory, we use Gauss law, Ampere's law like that.

Ex: Wireless transmission can u write KVL, KCL?
we can't write.

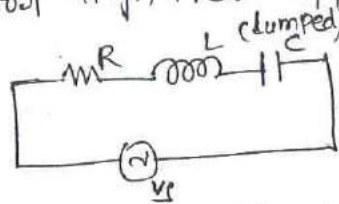
→ KVL & KCL fails for high freq.

Conclusions:-

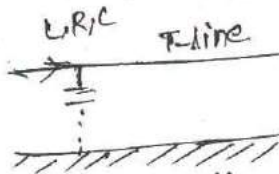
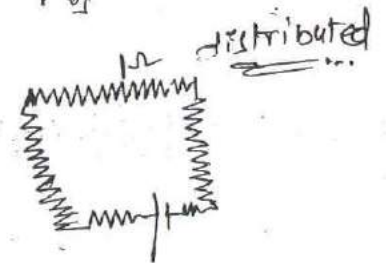
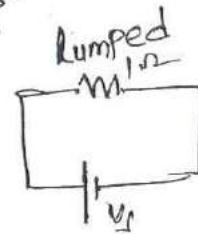
- * field theory can be obtained for low & high freq applications.
- * In the field theory accurate results are obtained, but developing mathematical eqns are more complex.
- * N/W theory is applied only for low freq applications.
- * In the N/W theory approximate results are obtained and developing mathematical eqns is simple.
- * KVL & KCL fails for high freq applications.



KVL applicable since law of conservation of energy, ohm's law not applicable since nonlinear.



$V_s = Ri(t) + L \frac{di(t)}{dt} + \frac{1}{C} \int i(t) dt$
ohm's law applicable since linear.



for the given T/L we can able to find

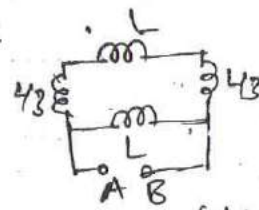
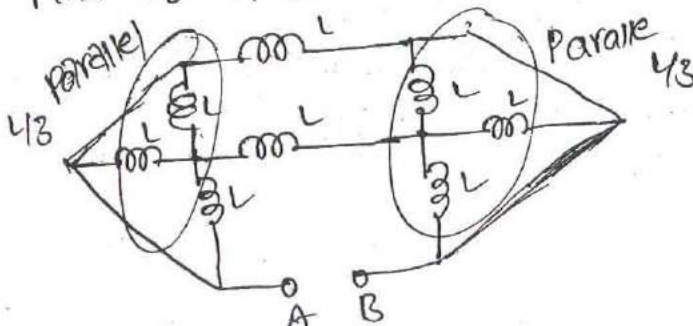
$$J = \sigma E$$

KVL, KCL not possible ohm's law is applicable since $J = \sigma E$.

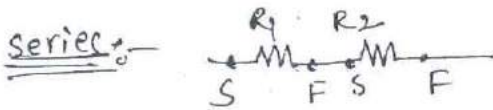
- * KVL & KCL "fail" for distributed parameters, since in the distributed parameters electrically it is not possible to isolate inductance and capacitance effects.
- * ohm's law can be applied for lumped (linear) & distributed parameters.

- * KVL & KCL are applied for lumped parameters. (linear, nonlinear, unidirectional, bidirectional, time variant & invariant elements).

find eqn inductance w.r.t to A & B.



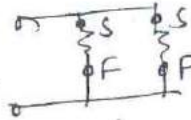
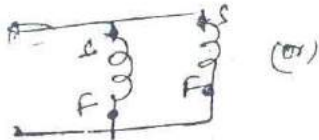
$$L_{AB} = \frac{(2L/3 + L) \parallel L}{1} = \frac{5L/3 \parallel L}{1} = \frac{5L}{8}$$



series

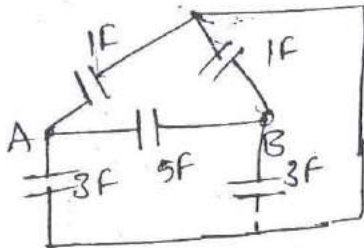
s → starting end
f → finishing end

parallel:-

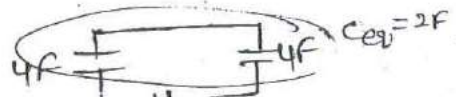
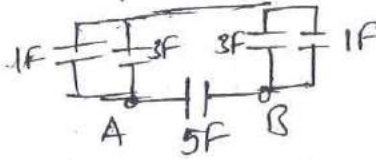


(pb)

find eqn capn w.r. to A & B.



Sol:-

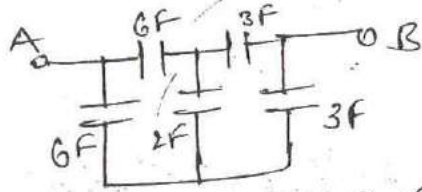


$C_{eq} = 2F$

$C_{ab} = 7F$

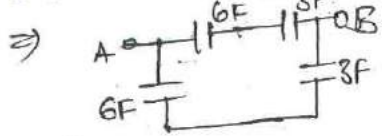
(pb)

find eqn cap w.r. to A & B?



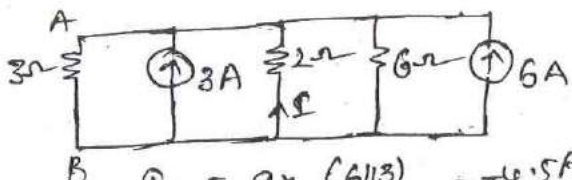
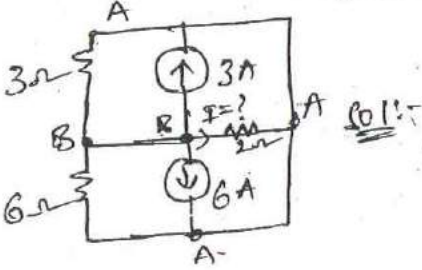
Sol:-

bridge balance. so $\frac{6F}{2F} = \frac{3F}{3F}$



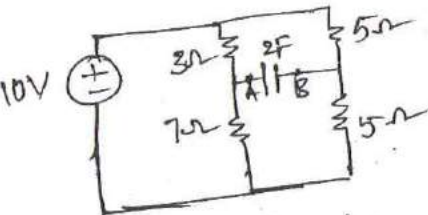
$\Rightarrow C_{AB} = 4F$

(pb)



$\frac{I_{2\Omega}}{2\Omega} = -9 \times \frac{(6/3)}{(6/3)+2} = -4.5A$

(pb)



find energy of the capacitor of the circuit shown?

for DC capacitor openckt.

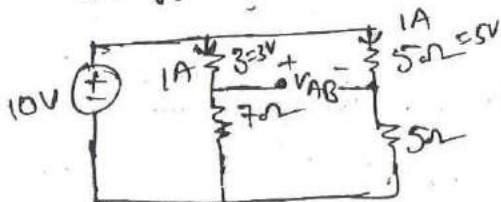
$V_{AB} = V_A - V_B = 3 - 5 = -2V$

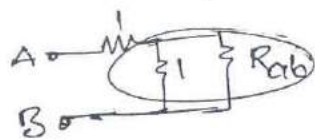
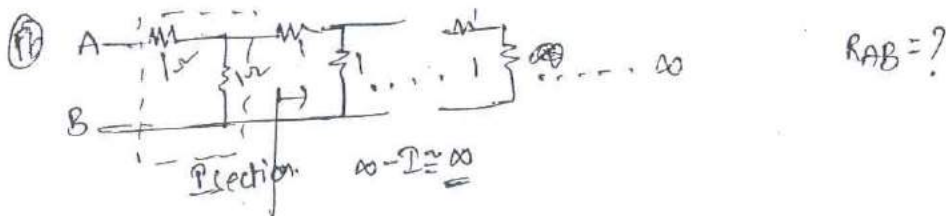
$V_{AB} = -2V$

$\therefore E = \frac{1}{2} (2)(4) = 4 \text{ Joules}$

Sol:-

Energy = $\frac{1}{2} CV^2$





$$R_{AB} = 1 + \frac{R_{AB}}{R_{AB} + 1}$$

$$R_{AB}^2 + R_{AB} = R_{AB} + 1 + R_{AB}$$

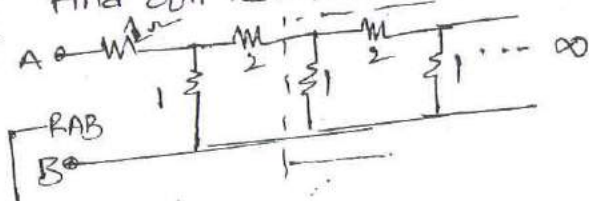
$$R_{AB}^2 - R_{AB} + 1 = 0$$

$$R_{AB} = \frac{1 \pm \sqrt{1 - 4(-1)}}{2}$$

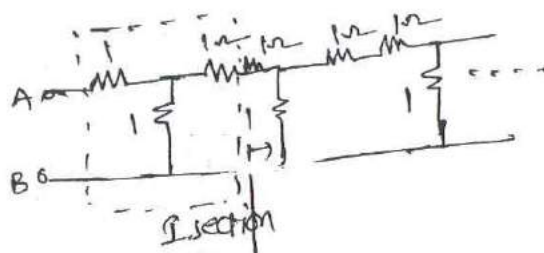
$$= \frac{1 \pm \sqrt{5}}{2}$$

$$\therefore R_{AB} = \frac{1 + \sqrt{5}}{2} \Omega$$

② Find eqll resw.r.to A & B.



Sol:-

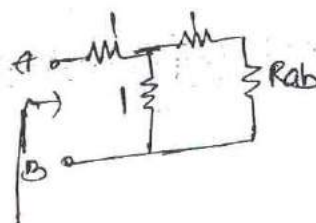


$$\therefore R_{AB} = 1 + \frac{(R_{AB} + 1)}{(R_{AB} + 2)}$$

$$R_{AB}^2 + 2R_{AB} = 2R_{AB} + 3$$

$$R_{AB} = \pm \sqrt{3}$$

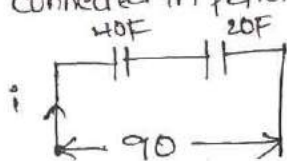
$$R_{AB} = \sqrt{3} \Omega$$



③ When two capacitors of 40F & 20F are connected in series to a source voltage of 90V. When two capacitors are charged fully they are connected in parallel. Find 'V' across capacitors in parallel connection.

(a) 45V (b) 30V (c) 40V (d) 60V

Sol:-

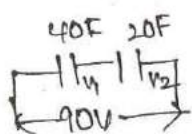


$$C_{eq} = \frac{40 \times 20}{40 + 20} = \frac{40}{3}$$

$$Q = C_{eq} \cdot V$$

$$Q = \frac{40}{3} \times 90 = 1200C$$

So charge on $C_1 = 1200C$
" $C_2 = 1200C$



(or)

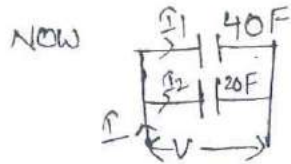
$$V_1 = 90 \times \frac{20}{60} = 30V$$

$$Q = CV = 30 \times 40 = 1200C$$

$$V_2 = 90 \times \frac{40}{60} = 60V$$

$$Q = CV = 60 \times 20 = 1200C$$

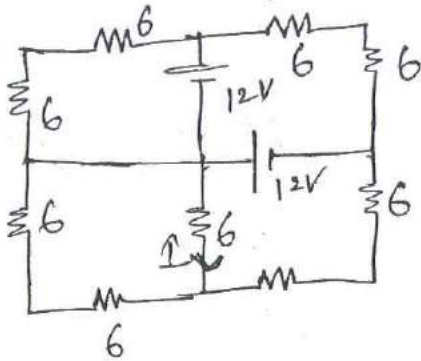
$$\therefore Q_T = 1200 + 1200 = \underline{\underline{2400}}$$



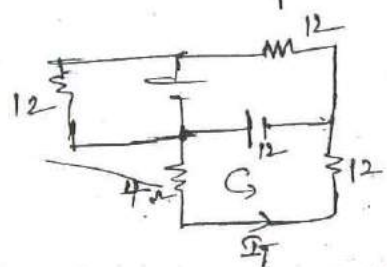
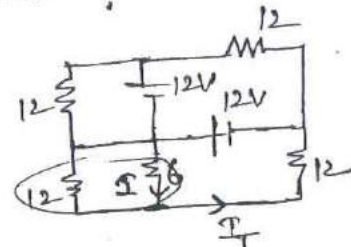
$$C_{eq} = 40 + 20 = 60$$

$$\therefore V = \frac{Q_T}{C_{eq}} = \frac{2400}{60} = \underline{\underline{40V}}$$

→ find the value of 'I' for the N/W shown?



sol:-



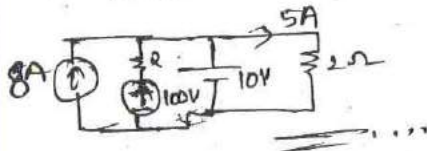
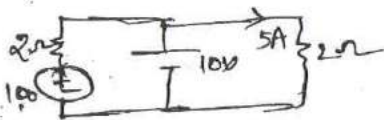
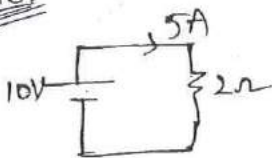
$$\therefore \text{therefore } I_T = \underline{\underline{\frac{12}{16} A}}$$

$$\frac{12}{16} = 0.75 \times \frac{12}{16}$$

$$= \frac{1}{3} = 0.33 \underline{\underline{A}}$$

$$I_{6\Omega} = I = \frac{12}{16} \times \frac{12}{(12+6)} = 0.5 \underline{\underline{A}}$$

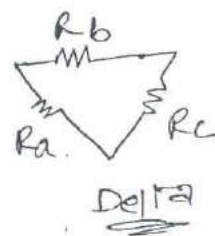
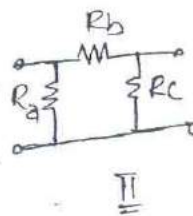
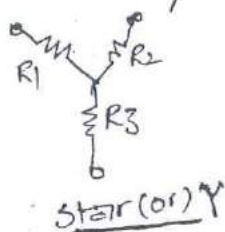
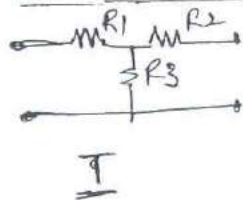
NOTE:-



(voltage source (or) current source)
As the ~~same~~ sources are connected in this manner there is no change in load current.

NOTE:- When elements are connected either in series nor in parallel to reduce the N/W star-delta transformation is used.

Star - Delta Transformations :-



Delta to star :-

$$R_1 = \frac{R_a R_b}{R_a + R_b + R_c}$$

$$R_2 = \frac{R_b R_c}{R_a + R_b + R_c}$$

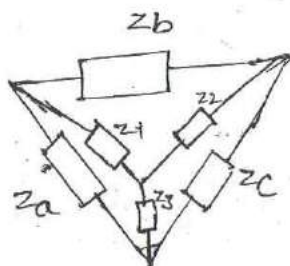
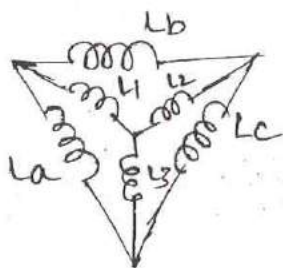
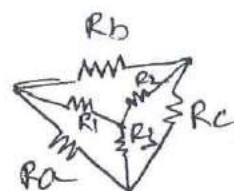
$$R_3 = \frac{R_a R_c}{R_a + R_b + R_c}$$

Star to Delta

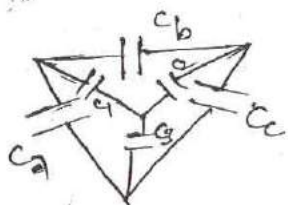
$$R_a = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2}$$

$$R_b = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3}$$

$$R_c = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1}$$



The procedure of doing transformation either from Δ to Y (or) Y to Δ for the resistors, inductors and impedances is same.



$$\frac{1}{C_1} = \frac{\frac{1}{C_a} \cdot \frac{1}{C_b}}{\frac{1}{C_a} + \frac{1}{C_b} + \frac{1}{C_c}} ; \frac{1}{C_a} = \frac{\frac{1}{C_1} \cdot \frac{1}{C_2} + \frac{1}{C_2} \cdot \frac{1}{C_3} + \frac{1}{C_3} \cdot \frac{1}{C_1}}{\frac{1}{C_2}}$$

$$\frac{1}{C_2} = \frac{\frac{1}{C_b} \cdot \frac{1}{C_c}}{\frac{1}{C_a} + \frac{1}{C_b} + \frac{1}{C_c}} ; \frac{1}{C_b} = \frac{\frac{1}{C_1} \cdot \frac{1}{C_2} + \frac{1}{C_2} \cdot \frac{1}{C_3} + \frac{1}{C_3} \cdot \frac{1}{C_1}}{\frac{1}{C_3}}$$

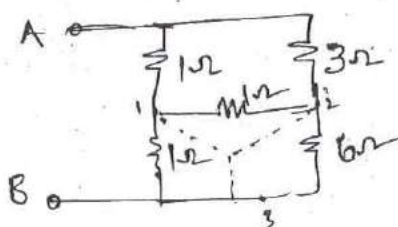
$$\frac{1}{C_3} = \frac{\frac{1}{C_a} \cdot \frac{1}{C_b}}{\frac{1}{C_a} + \frac{1}{C_b} + \frac{1}{C_c}} ; \frac{1}{C_c} = \frac{\frac{1}{C_1} \cdot \frac{1}{C_2} + \frac{1}{C_2} \cdot \frac{1}{C_3} + \frac{1}{C_3} \cdot \frac{1}{C_1}}{\frac{1}{C_1}}$$

Star to delta

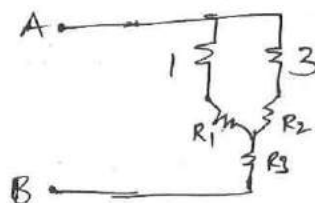
Delta to star

(Pb)

Find equiv resn w.r.to A & B?



Sol:-



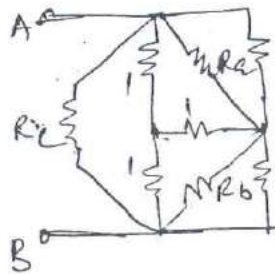
$$R_1 = \frac{1 \times 1}{1 + 1} = \frac{1}{2}$$

$$R_2 = \frac{6}{8}$$

$$R_3 = \frac{6}{8}$$

$$\therefore R_{ab} = \left(\left(1 + \frac{1}{2} \right) \parallel \left(3 + \frac{6}{8} \right) \right) + \left(\frac{6}{8} \right)$$

$$= (1.125 \parallel 3.75) + (0.75)$$



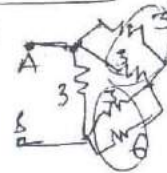
$$R_A = 1 \times 1 + 1 \times 1 + 1 \times 1$$

$$= 3 \Omega$$

$$R_B = 3 \Omega$$

$$R_C = 3 \Omega$$

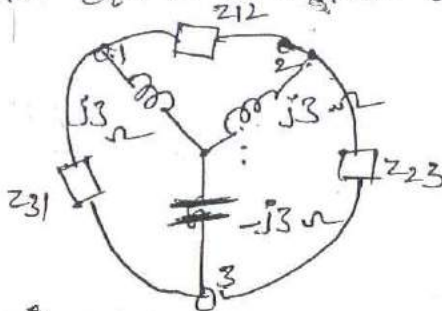
$$\therefore A \rightarrow B = \frac{3 \times 3}{3+3+3} = 1.5 \Omega$$



Note:—when resist of equal values are transformed from star to delta resist is increased by 3 times.

When capacitors of equal value transformed from star to delta capacitance decreased by 3 times.

(Pb) obtain Eqn Δ connection of the N/w shown.



$$\therefore Z_{12} = j3 \Omega$$

$$\rightarrow Z_{23} = j3 \Omega$$

$$\rightarrow Z_{31} = -j3 \Omega$$

$$\text{Sol:— } Z_{12} = \frac{Z_1 Z_2 + Z_2 Z_3 + Z_3 Z_1}{Z_3}$$

$$= Z_1 + Z_2 + \frac{Z_1 Z_2}{Z_3}$$

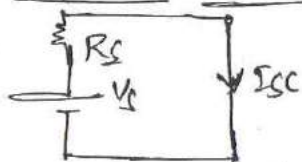
$$= j3 + j3 + \frac{(j3)(j3)}{(-j3)}$$

$$= j3 \dots \dots$$

$$Z_{23} = \frac{(Z_2) + Z_3 + \frac{Z_2 Z_3}{Z_1}}{Z_1} = j3 + \frac{(-j3) + \frac{(j3)(-j3)}{j3}}{j3}$$

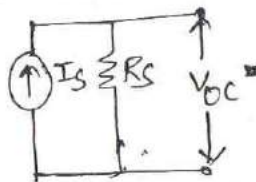
$$Z_{31} = \frac{(-j3) + j3 + \frac{(-j3)(j3)}{j3}}{j3} = -j3$$

Source Transformation Theorem:—



$$I_s = I_{sc} = \frac{V_s}{R_s}$$

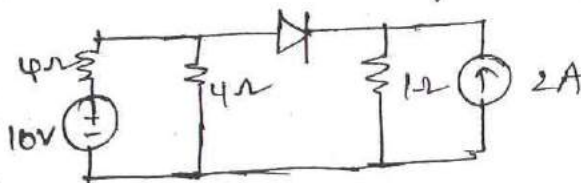
$$R_s = R_s$$



$$V_s = V_{oc} = I_s R_s$$

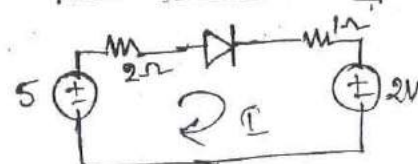
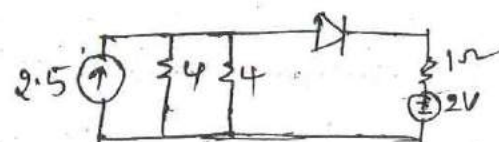
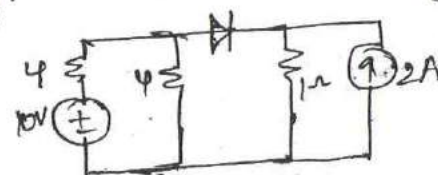
$$R_s = R_s$$

(Pb) Find current flowing through ideal diode of the ckt shown.



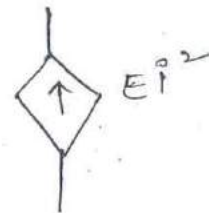
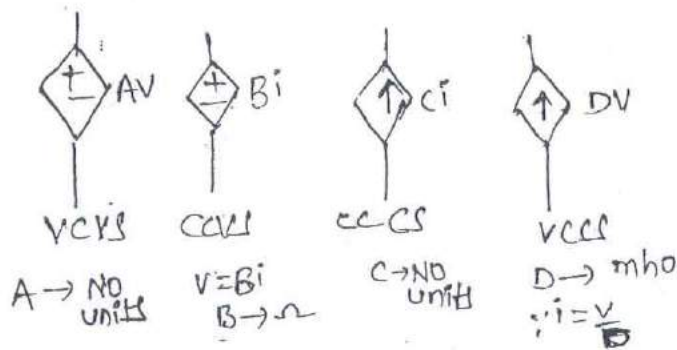
Sol:—

ideal diode $\rightarrow$ S.C in F.B, O.C in R.B.



$$\therefore I_D = \frac{3}{3} = 1A$$

so Diode in F.B $\Rightarrow$ S.C



All sources are linear dependent sources.

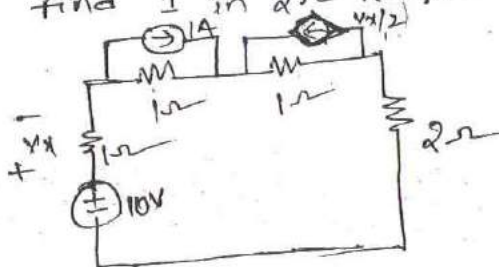
Nonlinear

As $i \uparrow 10\% \Rightarrow I \uparrow 100\%$

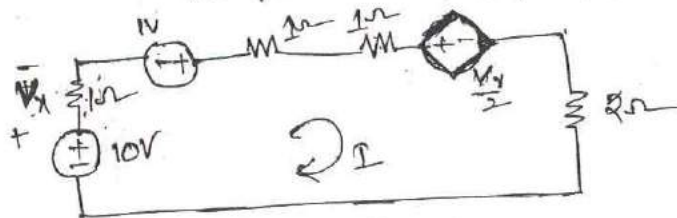
$V = Bi$
 As $10\% \uparrow$ in $i \Rightarrow 10\% \uparrow$ in V
 so linear...

(Pb)

find 'I' in a resistor?



Sol:- while applying source transformation for dependent source wherever dependent source magnitude depends without disturbing that element transformation can be applied.



$$\Rightarrow -10 + 5I - 1 + \frac{V_x}{2} = 0$$

$$\Rightarrow V_x = 5I$$

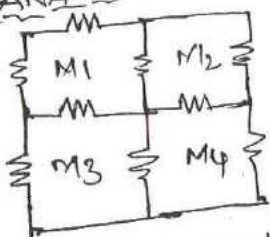
$$\frac{5V_x}{2} + 5I = 11 \quad \text{--- (1)}$$

from (1) & (2) $V_x = 2V$; $\therefore I = 2A$

$$V_x = I \times 1 \quad \text{--- (2)}$$

MECHANICAL ANALYSIS:-

(Pb)



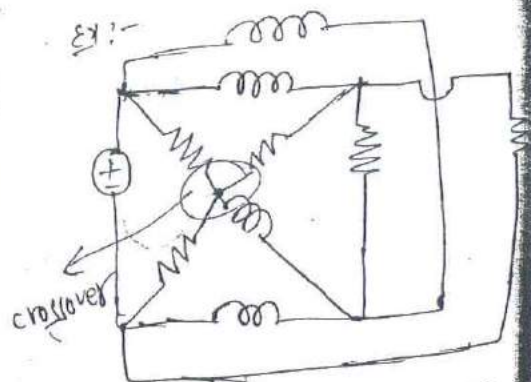
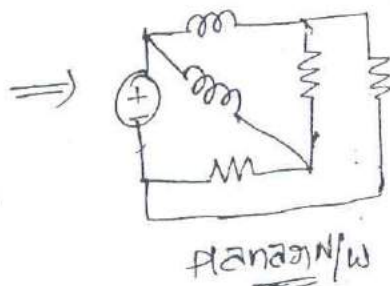
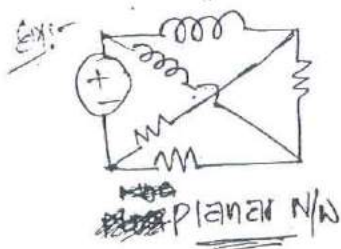
* Planar N/w:- when the N/w is drawn without crossover is called "planar N/w".

* Nonplanar N/w:- when the N/w is drawn with crossover is called "non planar N/w".

Mesh:- * Mesh is the loop it does not consists of any inner loop. Mesh analysis can be applied only for planar N/w's.

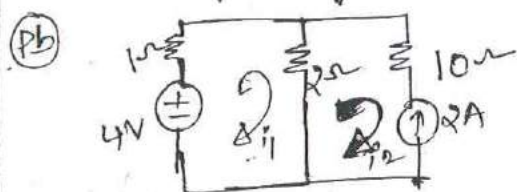
* When the N/w is drawn on plane without any cross over then the N/w is called as "planar N/w".

The above N/w is a planar N/w.



Procedure of Mesh Analysis:-

1. Identify total no. of meshes in the given N/W.
2. Assign the current direction for each mesh.
3. Develop KVL equation for each mesh.
4. By solving KVL eqns find loop currents.



Mesh (1):- $-4 + i_1 + 2(i_1 - i_2) = 0$
 $-4 + i_1 + 2i_1 - 2i_2 = 0$
 $3i_1 - 2i_2 = 4 \rightarrow (1)$

Sol:- No. of meshes = 2.

Mesh (2):- $i_2 = -2A$

(1) $\Rightarrow 3i_1 + 4 = 4$
 $\Rightarrow i_1 = 0$

Note:-

Total no. of eqns = Total no. of meshes

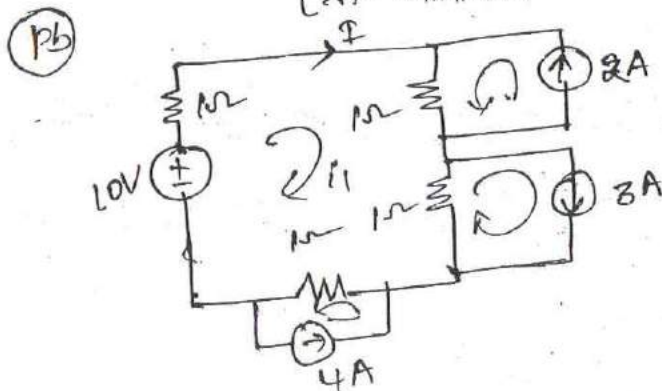
$e = M = 2$

$e = b - (N - 1)$
 $= 3 - (2 - 1)$
 $= 2$

Total no. of meshes possible = $b - (n) + 1$

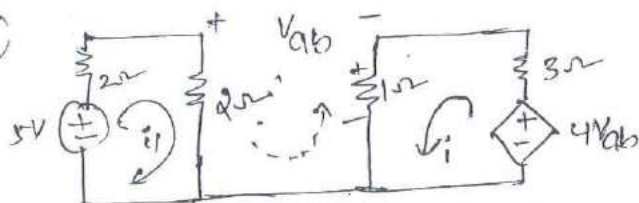
Note:- In the above N/W to find the loop currents minimum 1 eqn is required. (Since ^{due to} current source $i_2 = -2A$ can written directly).

[If minimum is not there $Ans = 2$]



Sol:- $-10V + (i_1) + (2 \times 1) - (i_2 \times 1) + (4 \times 1) = 0$
 $\Rightarrow i_1 = \frac{7}{4}$

(Pb)



find 'i' in the ckt shown?

Sol:-

$$-5 + 2.5i_1 = 0 \Rightarrow i_1 = \frac{5}{2.5} = 2 \text{ A}$$

$$-V_{ab} + 2.5 - (1)i = 0$$

$$-V_{ab} + 2.5 - V_{ab} = 0$$

$$\Rightarrow V_{ab} = 1.25$$

for mesh(2):-

$$-4V_{ab} + 3i + i = 0$$

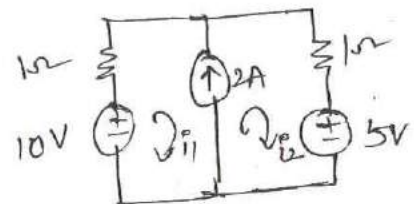
$$-V_{ab} + i = 0$$

$$i = V_{ab}$$

$$\therefore i = 1.25 \text{ A}$$

(Pb)

Find I_1 & I_2 of the circuit shown?



Note:- When Current source branch is common for two meshes it is possible to find solution by using Super Mesh technique.

Sol:-

$$-10 + i_1 + i_2 + 5 = 0 \rightarrow (1) \text{ (KVL)}$$

$$i_2 - i_1 = 2 \rightarrow (2) \text{ (KCL)}$$

$$\text{from (1) \& (2)} \quad i_1 = 1.5 \text{ A}$$

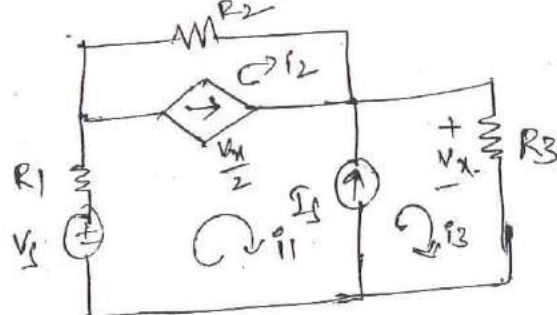
$$i_2 = 3.5 \text{ A}$$

Note:-

Mesh $\rightarrow$ KVL + Ohm's law
Supermesh $\rightarrow$ KVL + KCL + Ohm's law

(Pb)

Develop mathematical eqns of the N/w shown.



Sol:-

$$-V_1 + i_1 R_1 + i_2 R_2 + i_3 R_3 = 0 \rightarrow (1)$$

$$i_1 - i_3 = \frac{V_x}{2} \rightarrow (2)$$

$$i_3 - i_1 = I_s \rightarrow (3)$$

$$V_x = i_3 R_3 \rightarrow (4)$$

$$\text{from (2)} \Rightarrow i_1 - i_3 = \frac{i_3 R_3}{2}$$

$$\Rightarrow 2i_1 - 2i_3 = i_3 R_3$$

$$2i_1 - i_3(R_3 + 2) = 0 \rightarrow (5)$$

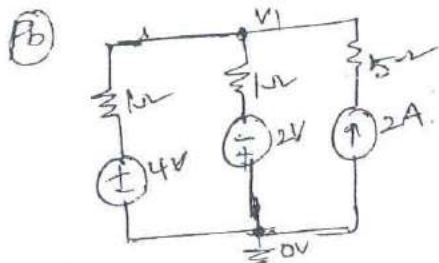
Nodal Analysis:-

* (for parallel ckt Nodal Analysis is better)

* Nodal Analysis can be applied for planar & non planar N/w.

Procedure of Nodal Analysis:-

- 1) Identify total No. of nodes in the given N/w.
- 2) Assign the voltage at each node, one of the nodes is taken as a reference node. And reference node potential should be equal to ground potential (0V).
- 3) Develop KCL eqn at each non reference node.
- 4) By solving KCL eqns find Node voltages.

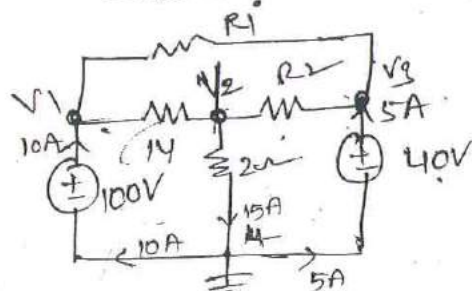


Sol:-

$$\frac{V_1 - 4}{1} + \frac{V_1 + 2}{1} = 2$$

$$\Rightarrow V_1 = 2V, \dots$$

Prob find R_1 & R_2 of the N/w shown?



Sol:-

$$V_1 = 100V$$

$$V_3 = 40V$$

$$\frac{V_2 - V_1}{14} + \frac{V_2}{2} + \frac{V_2 - V_3}{R_2} = 0 \rightarrow (1)$$

$$\frac{V_3 - V_1}{R_1} + \frac{V_3 - V_2}{R_2} = 5 \rightarrow (2)$$

$$\frac{V_1 - V_3}{R_1} + \frac{V_1 - V_2}{14} = 10 \rightarrow (3)$$

$$\therefore \Rightarrow \frac{40 - 100}{R_1} + \frac{40 - V_2}{R_2} = 10$$

$$\frac{15}{2\Omega} = 15A$$

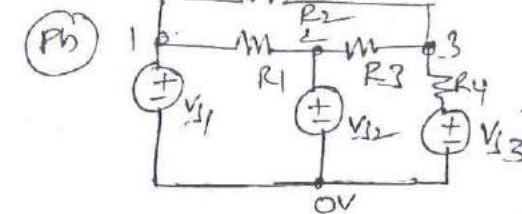
$$V_2 = 30V$$

$$(3) \Rightarrow \frac{60}{R_1} + \frac{70}{14} = 10$$

$$\Rightarrow R_1 = 12\Omega$$

$$(2) \Rightarrow R_2 = 1\Omega$$

Note:-
In nodal analysis total no. of eqns = $n-1$
where n = no. of nodes



Sol:- no. of eqns = $n-1$

$$= 4-1$$

$$= 3$$

$$= \dots$$

from the ckt

$$V_1 = V_{11}$$

$$V_2 = V_{12}$$

$$\dots$$

Now at node (3)

$$\frac{V_3 - V_1}{R_4} + \frac{V_3 - V_2}{R_3} + \frac{V_3 - V_1}{R_2} = 0$$

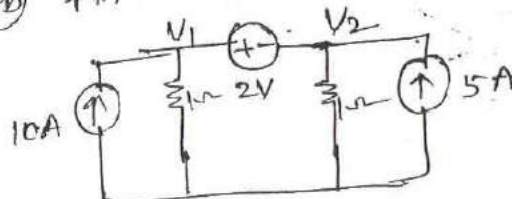
$$\Rightarrow V_3 = \dots$$

So we require only one equation

Note:-

To find the node voltages in the above n/w minimum one eqn is required.

Prob find V_1 & V_2 of the N/w shown?



Sol:-

$$\frac{V_1}{1} - 10 + \frac{V_2}{1} - 5 = 0$$

$$V_1 + V_2 = 15 \rightarrow (1)$$

$$V_1 - V_2 = 2 \rightarrow (2)$$

$$\Rightarrow V_1 = 8.5V$$

$$V_2 = 10.5V$$

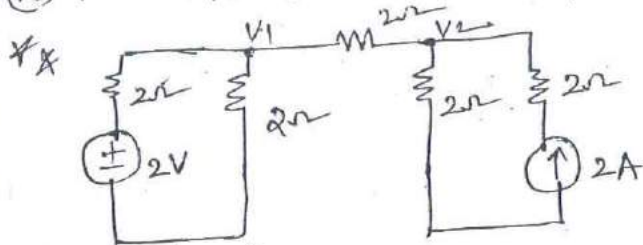
Note:- When ideal voltage source is connected b/w two non touching reference nodes, it is possible to find solution by using Super Node technique.

Note:-

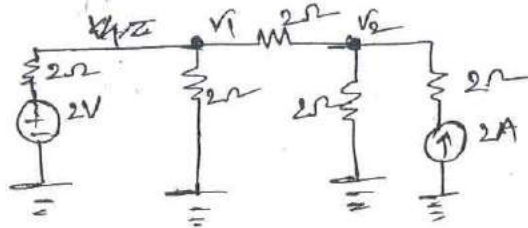
Nodal $\rightarrow$ KCL + Ohm's law

SuperNode $\rightarrow$ KCL + KVL + Ohm's law

(Pb) Find V_1 & V_2 of the circuit shown?



Sol:-

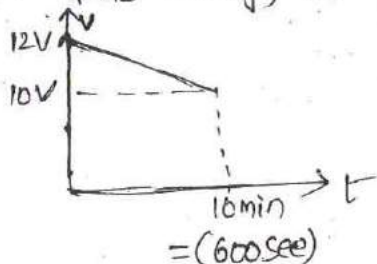


$$\frac{V_1}{2} + \frac{V_1 - 2}{2} + \frac{V_1 - V_2}{2} = 0 \quad \text{--- (1)}$$

$$\frac{V_2}{2} + \frac{V_2 - V_1}{2} = 2 \quad \text{--- (2)}$$

from (1) & (2) $V_1 = 1.6V$
 $V_2 = 2.8V$

(Pb) A Fully charged mobile phone is good for 10min talktime. During talktime Battery delivers a constant current of 2A. The voltage char. during talktime is as shown in the figure. Find energy of the Battery during talktime?



Sol:-

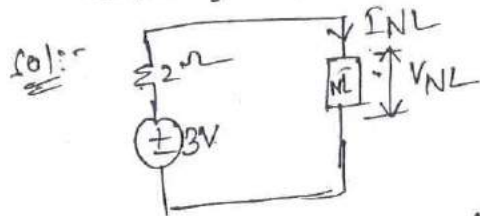
$$\text{Total Area} = \frac{1}{2} (600 \times 2) + (600 \times 10) = 6600 \Rightarrow V \times t$$

$$W = (V \times t) \times I \\ = 6600 \times 2 \\ = 13.2 \text{ kJ}$$

1200
6000
7200

(Pb) A practical DC source of 3V with internal res. of 2Ω is connected to non linear res. The char. of non linear res. is given by $V_{NL} = I_{NL}^2$. Find

Power dissipation in the non linear resistor?



Sol:-

$$-3 + 2I_{NL} + V_{NL} = 0$$

$$-3 + 2I_{NL} + I_{NL}^2 = 0$$

$$\Rightarrow I_{NL} = 1A$$

$$P_{NL} = 1A$$

$$V_{NL} = I_{NL}^2 = 1A$$

$$P_{NL} = V_{NL} \times I_{NL} = 1 \times 1 = 1W$$

Since linear power systems $P \propto t$
 $P \times t = \text{Energy}$
 $\Rightarrow$ Area under the curve