

CBSE Test Paper 01
Chapter 05 Arithmetic Progression

1. In an AP, if $a = 4$, $n = 7$ and $a_n = 4$, then the value of 'd' is **(1)**
 - a. 0
 - b. 1
 - c. 3
 - d. 2
2. The next two terms of the AP : $k, 2k + 1, 3k + 2, 4k + 3, \dots$ are **(1)**
 - a. $5k + 4$ and $6k + 5$
 - b. $4k + 4$ and $4k + 5$
 - c. $5k + 5$ and $6k + 6$
 - d. $5k$ and $6k$
3. The common difference of the A.P. can be **(1)**
 - a. only negative
 - b. only zero
 - c. positive, negative or zero
 - d. only positive
4. The 7th term from the end of the A.P. $-11, -8, -5, \dots, 49$ is **(1)**
 - a. 28
 - b. 31
 - c. -11
 - d. -8
5. The common difference of the A.P whose $a_n = -3n + 7$ is **(1)**
 - a. 3
 - b. 1
 - c. -3
 - d. 2
6. If 5 times the 5th term of an AP is equal to 10 times the 10th term, show that its 15th term is zero. **(1)**
7. Write the first term a and the common difference d of A.P. $-1.1, -3.1, -5.1, -7.1, \dots$ **(1)**

-
8. For what value of n are the n^{th} term of the following two AP's are same 13, 19, 25, and 69, 68, 67 **(1)**
9. Find k , if the given value of x is the k^{th} term of the given AP $5\frac{1}{2}$, 11, $16\frac{1}{2}$, 22, ..., $x = 550$. **(1)**
10. Find the 6th term from the end of the A.P. 17, 14, 11, ..., - 40 **(1)**
11. How many terms of the AP 17, 15, 13, 11, ... must be added to get the sum 72? **(2)**
12. Find n . Given a = first term = -18.9, d = common difference = 2.5, a_n = the n th term = 3.6, $n = ?$ **(2)**
13. Find the number of terms in each of the following APs. 18, $15\frac{1}{2}$, 13,, - 47. **(2)**
14. The first and the last terms of an AP are 5 and 45 respectively. If the sum of all its terms is 400, find the common difference and the number of terms. **(3)**
15. The 14th term of an A.P. is twice its 8th term. If the 6th term is -8, then find the sum of its first 20 terms. **(3)**
16. Find the 6th term from end of the AP 17, 14, 11, ..., -40. **(3)**
17. The houses of a row in a colony are numbered consecutively from 1 to 49. Show that there is a value of x such that the sum of the numbers of the houses preceding the house numbered x is equal to the sum of the numbers of the houses following it. Find the value of x . **(3)**
18. The sum of first n terms of an A.P. is $3n^2 + 4n$. Find the 25th term of this A.P. **(4)**
19. If sum of first 6 terms of an A.P. is 36 and that of the first 16 terms is 256, find the sum of the first 10 terms. **(4)**
20. The sum of the third and the seventh terms of an AP is 6 and their product is 8. Find the sum of the first sixteen terms of the AP. **(4)**

CBSE Test Paper 01
Chapter 05 Arithmetic Progression

Answers

1. a. 0

Explanation: Given: $a = 4$, $n = 7$ and $a_n = 4$, then

$$a_n = a + (n - 1) d$$

$$\Rightarrow 4 = 4 + (7 - 1) d$$

$$\Rightarrow 4 - 4 = 6d$$

$$\Rightarrow 6d = 0$$

$$\Rightarrow d = 0$$

2. a. $5k + 4$ and $6k + 5$

Explanation: Given: $k, 2k + 1, 3k + 2, 4k + 3, \dots$

$$\text{Here } d = 2k + 1 - k = k + 1$$

Therefore, the next two terms are

$$4k + 3 + k + 1 = 5k + 4 \text{ and } 5k + 4 + k + 1 = 6k + 5$$

3. c. positive, negative or zero

Explanation: The common difference of the A.P. can be positive, e.g. 1, 2, 3, 4 d is +ve and series is increasing negative e.g. 4, 3, 2, 1 d is -ve and series is decreasing

or zero also and the AP becomes constant e.g. 4, 4, 4, 4

4. b. 31

Explanation: Reversing the given A.P., we have

$$49, 46, 43, \dots, -11$$

$$\text{Here, } a = 49, d = 46 - 49 = -3 \text{ and } n = 7$$

$$\therefore a_n = a + (n - 1) d$$

$$\Rightarrow a_7 = 49 + (7 - 1) \times (-3)$$

$$= 49 + 6 \times (-3)$$

$$\Rightarrow a_7 = 49 - 18 = 31$$

5. c. -3

Explanation: Given: $a_n = -3n + 7$

Putting $n = 1, 2, 3$, we get

$$a = -3 \times 1 + 7 = -3 + 7 = 4$$

$$a_2 = -3 \times 2 + 7 = -6 + 7 = 1$$

$$a_3 = -3 \times 3 + 7 = -9 + 7 = -2$$

$$\therefore \text{Common difference } (d) = a_2 - a = 1 - 4 = -3$$

6. Let 1st term = a and common difference = d .

$$a_5 = a + 4d, a_{10} = a + 9d$$

$$\text{According to the question, } 5 \times a_5 = 10 \times a_{10} \Rightarrow 5(a + 4d) = 10(a + 9d) \Rightarrow 5a + 20d = 10a + 90d \Rightarrow a = -14d$$

$$\text{Now, } a_{15} = a + 14d \Rightarrow a_{15} = -14d + 14d = 0.$$

7. -1.1, -3.1, -5.1, -7.1, ...

$$\text{First term } (a) = -1.1$$

We know that common difference is difference between any two consecutive terms of an A.P.

$$\begin{aligned} \text{So, common difference } (d) &= (-3.1) - (-1.1) \\ &= -3.1 + 1.1 \\ &= -2 \end{aligned}$$

8. n^{th} term of 13, 19, 25, = n^{th} term of 69, 68, 67,

$$13 + (n - 1) 6 = 69 + (n - 1) (-1)$$

$$13 + 6n - 6 = 69 - n + 1$$

$$n + 6n = 70 - 7$$

$$7n = 63$$

$$n = 9$$

Therefore, $n = 9$

9. $a = 5\frac{1}{2} = \frac{11}{2}$, $d = a_2 - a_1 = 11 - \frac{11}{2} = \frac{11}{2}$ and $x = 550$

$$\text{A.T.Q., } a_k = x$$

$$\Rightarrow a + (k - 1)d = 550$$

$$\Rightarrow \frac{11}{2} + (k - 1)\frac{11}{2} = 550$$

$$\Rightarrow \frac{11}{2} + \frac{11}{2}k - \frac{11}{2} = 550$$

$$\Rightarrow \frac{11}{2}k = 550$$

$$\Rightarrow k = \frac{550 \times 2}{11} = 100$$

10. A.P. is 17, 14, 11, ..., -40

We have,

l = Last term = -40, a = 17 and, d = Common difference = $14 - 17 = -3$

\therefore 6th term from the end = $l - (n - 1)d$

$$= l - (6 - 1)d$$

$$= -40 - 5 \times (-3)$$

$$= -40 + 15$$

$$= -25$$

So, 6th term of given A.P. is -25.

11. Given A.P. is 17, 15, 13, 11,

Here, 1st term (a) = 17 and common difference (d) = $(15 - 17) = -2$

Let the sum of n terms be 72. Then,

$$S_n = 72$$

$$\Rightarrow \frac{n}{2} \cdot \{2a + (n - 1)d\} = 72$$

$$\Rightarrow n \cdot \{2 \times 17 + (n - 1)(-2)\} = 144$$

$$\Rightarrow n(36 - 2n) = 144$$

$$\Rightarrow 2n^2 - 36n + 144 = 0$$

$$\Rightarrow n^2 - 18n + 72 = 0$$

$$\Rightarrow n^2 - 12n - 6n + 72 = 0$$

$$\Rightarrow n(n - 12) - 6(n - 12) = 0$$

$$\Rightarrow (n - 12)(n - 6) = 0$$

$$\Rightarrow n = 6 \text{ or } n = 12.$$

\therefore sum of first 6 terms = sum of first 12 terms = 72.

This means that the sum of all terms from 7th to 12th is zero.

12. $a_n = a + (n - 1)d$

$$\Rightarrow 3.6 = -18.9 + (n - 1)(2.5)$$

$$\Rightarrow 3.6 + 18.9 = (n - 1)(2.5)$$

$$\Rightarrow 22.5 = (n - 1)(2.5)$$

$$\Rightarrow n - 1 = \frac{22.5}{2.5}$$

$$\Rightarrow n - 1 = 9$$

$$\Rightarrow n = 10$$

13. $18, 15\frac{1}{2}, 13, \dots, -47$

Here, $a = 18$

$$d = 15\frac{1}{2} - 18 = \frac{31}{2} - 18 = -\frac{5}{2}$$

$$a_n = -47$$

Let the number of terms be n .

Then,

$$a_n = -47$$

$$\Rightarrow a + (n - 1)d = -47$$

$$\Rightarrow 18 + (n - 1)\left(-\frac{5}{2}\right) = -47$$

$$\Rightarrow -\frac{5}{2}(n - 1) = -47 - 18$$

$$\Rightarrow -\frac{5}{2}(n - 1) = -65$$

$$\Rightarrow \frac{5}{2}(n - 1) = 65$$

$$\Rightarrow n - 1 = \frac{65 \times 2}{5}$$

$$\Rightarrow n - 1 = 26$$

$$\Rightarrow n = 26 + 1$$

$$\Rightarrow n = 27$$

Hence, the number of terms of the given AP is 27.

14. Let the given AP contains n terms.

First term, $a = 5$

Last term, $l = 45$

$$S_n = 400$$

$$\Rightarrow \frac{n}{2} [a + l] = 400$$

$$\Rightarrow \frac{n}{2} [5 + 45] = 400$$

$$\Rightarrow n \times 50 = 800$$

$$\Rightarrow n = 16$$

Thus, the given AP contains 16 terms.

Let d be the common difference of the given AP.

then,

$$T_{16} = 45$$

$$\Rightarrow a + 15d = 45$$

$$\Rightarrow 5 + 15d = 45$$

$$\Rightarrow 15d = 40$$

$$\Rightarrow d = \frac{40}{15} = \frac{8}{3}.$$

Therefore, common difference of the given AP is $\frac{8}{3}$.

15. Let first term be a and common difference be d .

$$\text{Here, } a_{14} = 2a_8$$

$$a + 13d = 2(a + 7d)$$

$$a + 13d = 2a + 14d$$

$$a = -d \dots (i)$$

$$a_6 = -8$$

$$a + 5d = -8 \dots (ii)$$

Putting the value of a from (i) in (ii), we get

$$-d + 5d = -8$$

$$4d = -8$$

$$d = -2$$

Put $d = -2$ in (i)

$$a = -(-2)$$

$$a = 2$$

So, $a = 2, d = -2$

$$S_{20} = \frac{20}{2} [2 \times 2 + (20 - 1)(-2)]$$

$$= 10 [4 + 19 \times (-2)]$$

$$= 10(4 - 38)$$

$$= 10 \times (-34)$$

$= -340$. Which is the required sum of first 20 terms.

16. The given AP is 17, 14, 11,, -40

$$\text{Here, } a = 17$$

$$d = 14 - 17 = -3$$

$$l = -40$$

Let there be n terms between in the given AP

Then, n th term $= -40$

$$\Rightarrow a + (n - 1)d = -40 \therefore a_n = a + (n - 1)d$$

$$\Rightarrow 17 + (n - 1)(-3) = -40$$

$$\Rightarrow (n - 1) (-3) = -40 - 17$$

$$\Rightarrow (n - 1) (-3) = -57$$

$$\Rightarrow n - 1 = \frac{-57}{-3}$$

$$\Rightarrow n - 1 = 19$$

$$\Rightarrow n = 19 + 1$$

$$\Rightarrow n = 20$$

Hence, there are 20 terms in the given AP.

Now, 6th term from the end

= (20 - 6 + 1)th term from the beginning

= 15th term from the beginning

$$= a + (15 - 1)d \because a_n = a + (n - 1)d$$

$$= 17 + 14 (-3)$$

$$= 17 - 42$$

$$= -25$$

Hence, the 6th term from the end of the given AP is -25.

17. According to the question, we have to find the value of x.

We are given an AP, namely 1, 2, 3, ..., (x - 1), x, (x + 1), ..., 49

such that $1 + 2 + 3 + \dots + (x - 1) = (x + 1) + (x + 2) + \dots + 49$.

Thus, we have $S_{x-1} = S_{49} - S_x \dots$ (i)

Using the formula, $S_n = \frac{n}{2} (a + l)$ in (i), we have,

$$\frac{(x-1)}{2} \cdot \{1 + (x - 1)\} = \frac{49}{2} \cdot (1 + 49) - \frac{x}{2} \cdot (1 + x)$$

$$\Rightarrow \frac{x(x-1)}{2} + \frac{x(x+1)}{2} = 1225$$

$$\Rightarrow 2x^2 = 2450 \Rightarrow x^2 = 1225 \Rightarrow x = \sqrt{1225} = 35$$

Hence, x = 35.

18. According to the question,

Sum of n terms of the A.P. $S_n = 3n^2 + 4n$

$$S_1 = 3 \times 1^2 + 4 \times 1 = 7 = t_1 \dots (i)$$

$$S_2 = 3 \times 2^2 + 4 \times 2 = 20 = t_1 + t_2 \dots (ii)$$

$$S_3 = 3 \times 3^2 + 4 \times 3 = 39 = t_1 + t_2 + t_3 \dots (iii)$$

From (i), (ii), (iii)

$$t_1 = 7, t_2 = 13, t_3 = 19$$

$$\text{Common difference, } d = 13 - 7 = 6$$

$$\begin{aligned} 25^{\text{th}} \text{ of the term of this A.P., } t_{25} &= 7 + (25 - 1)6 \\ &= 7 + 144 = 151 \end{aligned}$$

\therefore The 25th term of the A.P. is 151.

19. Consider the A.P. whose first term and common difference are 'a' and 'd' respectively.

If sum of first 6 terms of an A.P. is 36.

$$S_6 = 36$$

$$\therefore \frac{6}{2} [2a + (6 - 1)d] = 36 \left[\because S_n = \frac{n}{2} [2a + (n - 1)d] \right]$$

$$\Rightarrow 3[2a + 5d] = 36$$

$$\Rightarrow 2a + 5d = \frac{36}{3}$$

$$\Rightarrow 2a + 5d = 12 \dots(i)$$

If sum of first 16 terms is 256,

$$\text{So, } S_{16} = 256$$

$$\Rightarrow \frac{16}{2} [2a + (16 - 1)d] = 256$$

$$\Rightarrow 8[2a + 15d] = 256$$

$$\Rightarrow 2a + 15d = \frac{256}{8}$$

$$\Rightarrow 2a + 15d = 32 \dots(ii)$$

Subtracting (i) from (ii), we get

$$2a + 15d = 32 \dots(ii)$$

$$2a + 5d = 12 \text{ [From (i)]}$$

$$\begin{array}{r} - \quad - \quad - \\ \hline 10d = 20 \end{array}$$

$$2a + 15d = 32$$

$$2a + 5d = 12$$

$$\begin{array}{r} - \quad - \quad - \\ \hline 10d = 20 \end{array}$$

$$\Rightarrow d = 2$$

Now, $2a + 5d = 12$ [From (i)]

$$\Rightarrow 2a + 5(2) = 12$$

$$\Rightarrow 2a + 10 = 12$$

$$\Rightarrow 2a = 12 - 10$$

$$\Rightarrow a = \frac{2}{2}$$

$$\Rightarrow a = 1$$

Hence, $a = 1$ and $d = 2$

$$\text{So, } S_{10} = \frac{10}{2} [2a + (10 - 1)d]$$

$$= 5[2(1) + 9(2)]$$

$$= 5[2 + 18]$$

$$= 5[20]$$

$$= 100$$

$$\Rightarrow S_{10} = 100$$

Hence, the sum of first 10 terms is 100.

20. Let the first term and the common difference of the AP be a and d respectively.

According to the question,

Third term + seventh term = 6

$$\Rightarrow [a + (3 - 1)d] + [a + (7 - 1)d] = 6 = a + (n - 1)d$$

$$\Rightarrow (a + 2d) + (a + 6d) = 6 \Rightarrow 2a + 8d = 6$$

$$\Rightarrow a + 4d = 3 \dots (1)$$

Dividing throughout by 2 &

(third term) (seventh term) = 8

$$\Rightarrow (a + 2d)(a + 6d) = 8$$

$$\Rightarrow (a + 4d - 2d)(a + 4d + 2d) = 8$$

$$\Rightarrow (3 - 2d)(3 + 2d) = 8$$

$$\Rightarrow 9 - 4d^2 = 8$$

$$\Rightarrow 4d^2 = 1 \Rightarrow d^2 = \frac{1}{4} \Rightarrow d = \pm \frac{1}{2}$$

Case I, when $d = \frac{1}{2}$

$$\text{Then from (1), } a + 4\left(\frac{1}{2}\right) = 3$$

$$\Rightarrow a + 2 = 3 \Rightarrow a = 3 - 2 \Rightarrow a = 1$$

\therefore Sum of first sixteen terms of the AP = S_{16}

$$= \frac{16}{2} [2a + (16 - 1)d] \because S_n = \frac{n}{2} [2a + (n - 1)d]$$

$$= 8[2a + 15d]$$

$$= 8[2(1) + 15\left(\frac{1}{2}\right)]$$

$$= 8\left[12 + \frac{15}{2}\right]$$

$$= 8\left[\frac{19}{2}\right]$$

$$= 4 \times 19 = 76$$

Case II. When $d = -\frac{1}{2}$

Then from (1),

$$a + 4\left(-\frac{1}{2}\right) = 3$$

$$\Rightarrow a - 2 = 3 \Rightarrow a = 3 + 2 \Rightarrow a = 5$$

\therefore Sum of first sixteen terms of the AP = S_{16}

$$= \frac{16}{2}[2a + (16 - 1)d] \because S_n = \frac{n}{2}[2a + (n - 1)d]$$

$$= 8[2a + 15d] = 8\left[2(5) + 15\left(-\frac{1}{2}\right)\right] = 8\left[10 - \frac{15}{2}\right] = 8\left[\frac{5}{2}\right] = 20$$