

CBSE Test Paper 04
Chapter 7 Coordinate Geometry

1. The centroid of a triangle whose vertices are (3, -7), (-8, 6) and (5, 10) is **(1)**
 - a. (0, 3)
 - b. (1, 3)
 - c. (3, 3)
 - d. (0, 9)
2. If the point P(2, 1) lies on the line segment joining points A(4, 2) and B(8, 4), then AP is equal to **(1)**
 - a. $AP = \frac{1}{4}AB$
 - b. $AP = \frac{1}{2}AB$
 - c. $AP = \frac{1}{3}AB$
 - d. $AP = PB$
3. If the points (x, y), (1, 2) and (7, 0) are collinear, then the relation between 'x' and 'y' is given by **(1)**
 - a. $3x - y - 7 = 0$
 - b. $3x + y + 7 = 0$
 - c. $x + 3y - 7 = 0$
 - d. $x - 3y + 7 = 0$
4. The points A(1, 2), B(5, 4), C(3, 8) and D(-1, 6) are the vertices of a **(1)**
 - a. Rectangle
 - b. Rhombus
 - c. Square
 - d. Parallelogram
5. The triangle whose vertices are (-3, 0), (1, -3) and (4, 1) is _____ triangle. **(1)**
 - a. Obtuse triangle
 - b. equilateral
 - c. right angled isosceles
 - d. scalene
6. If 18, a, b, -3 are in A.P., then find a + b. **(1)**

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7. Find the radius of the circle whose end points of diameter are (24,1) and (2,23)] **(1)**
 8. Find the distance between the following pairs of points: (2, 3), (4,1) **(1)**
 9. Find the coordinates of the point on y-axis which is nearest to the point (- 2, 5). **(1)**
 10. What is the distance between the points A(c,0) and B(0, - c)? **(1)**
 11. Use distance formula to show that the points A (- 2,3), B (1, 2) and C (7,0) are collinear. **(2)**
 12. If the mid-point of the line joining (3,4) and (k, 7) is (x, y) and $2x + 2y + 1 = 0$ find the value of k. **(2)**
 13. Show that the mid-point of the line segment joining the points (5, 7) and (3, 9) is also the mid-point of the line segment joining the points (8, 6) and (0, 10). **(2)**
 14. If (5,2), (- 3,4) and (x, y) are collinear, show that $x + 4y - 13 = 0$. **(3)**
 15. If the point C(-1, 2) divides the line segment AB in the ratio 3 : 4, where the coordinates of A are (2, 5), find the coordinates of B. **(3)**
 16. The three vertices of a parallelogram ABCD taken in order are A (-1, 0), B(3, 1) and C(2, 2). Find the height of a parallelogram with AD as its base. **(3)**
 17. Find the ratio in which the line segment joining the points A(3, - 3) and B(- 2,7) is divided by the x-axis. Also, find the coordinates of the point of division. **(3)**
 18. Find the point on the x-axis which is equidistant from (2,-5) and (-2,9) **(4)**
 19. The points A (x_1, y_1), B (x_2, y_2) and C (x_3, y_3) are the vertices of $\triangle ABC$.
 - i. The median from A meets BC at D. Find the coordinates of the point D.
 - ii. Find the coordinates of the point P on AD such that $AP : PD = 2:1$.
 - iii. Find the points of coordinates Q and R on medians BE and CP respectively such that $BQ : QE = 2 : 1$ and $CR : RP = 2 : 1$.
 - iv. What are the coordinates of the centroid of the triangle ABC? **(4)**
 20. Find the coordinates of the points Q on the x-axis which lies on the perpendicular bisector of the line segment joining the points A(-5, -2) and B(4, -2). Name the type of triangle formed by the points Q, A and B. **(4)**

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Solution

1. a. (0, 3)

Explanation: Given: $(x_1, y_1) = (3, -7)$, $(x_2, y_2) = (-8, 6)$ and $(x_3, y_3) = (5, 10)$

Coordinates of Centroid of triangle = $x = \frac{x_1+x_2+x_3}{3}$ and $y = \frac{y_1+y_2+y_3}{3}$

$$\therefore x = \frac{3-8+5}{3} = \frac{0}{3} = 0$$

$$\text{and } y = \frac{-7+6+10}{3} = \frac{9}{3} = 3$$

Therefore, the coordinates of centroid of triangle are (0, 3).

2. b. $AP = \frac{1}{2}AB$

Explanation: $AP = \sqrt{(2-4)^2 + (1-2)^2}$

$$= \sqrt{4+1} = \sqrt{5} = \text{units}$$

$$AB = \sqrt{(8-4)^2 + (4-2)^2}$$

$$= \sqrt{16+4} = \sqrt{20} = 2\sqrt{5} \text{ units}$$

Here $AB = 2 \times AP$

$$\therefore AP = \frac{1}{2} AB$$

3. c. $x + 3y - 7 = 0$

Explanation: Given: $(x_1, y_1) = (x, y)$, $(x_2, y_2) = (1, 2)$ and $(x_3, y_3) = (7, 0)$ and these are collinear

$$\therefore \frac{1}{2} |x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)| = 0$$

$$\Rightarrow \frac{1}{2} |x(2 - 0) + 1(0 - y) + 7(y - 2)| = 0$$

$$\Rightarrow \frac{1}{2} |2x - y + 7y - 14| = 0$$

$$\Rightarrow 2x + 6y - 14 = 0 \Rightarrow x + 3y - 7 = 0$$

4. c. Square

Explanation: Given: The points A(1, 2), B(5, 4), C(3, 8) and D(-1, 6)

$$\therefore AB = \sqrt{(5-1)^2 + (4-2)^2} = \sqrt{16+4} = 2\sqrt{5} \text{ units}$$

$$BC = \sqrt{(3-5)^2 + (8-4)^2} = \sqrt{4+16} = 2\sqrt{5} \text{ units}$$

$$CD = \sqrt{(-1-3)^2 + (6-8)^2} = \sqrt{16+4} = 2\sqrt{5} \text{ units}$$

$$AD = \sqrt{(-1 - 1)^2 + (6 - 2)^2} = \sqrt{4 + 16} = 2\sqrt{5} \text{ units}$$

Therefore the 4 sides AB , BC, CD and DA are equal

$$\text{and the diagonal } AC = \sqrt{(3 - 1)^2 + (8 - 2)^2} = \sqrt{4 + 36} = 2\sqrt{10} \text{ units}$$

$$\text{and } BD = \sqrt{(-1 - 5)^2 + (6 - 4)^2} = \sqrt{36 + 4} = 2\sqrt{10} \text{ units}$$

Therefore diagonals AC and BD are equal

Since, all 4 sides are equal and both diagonals are also equal.

Therefore, the given quadrilateral is a square.

5. c. right angled isosceles

Explanation: Let A (-3, 0), B(1, -3) and C (4, 1) are the vertices of a triangle ABC.

$$\therefore AB = \sqrt{(1 + 3)^2 + (-3 - 0)^2} = \sqrt{16 + 9} = \sqrt{25} = 5 \text{ units}$$

$$BC = \sqrt{(4 - 1)^2 + (1 + 3)^2} = \sqrt{9 + 16} = \sqrt{25} = 5 \text{ units}$$

$$CA = \sqrt{(-3 - 4)^2 + (0 - 1)^2} = \sqrt{49 + 1} = \sqrt{50} = 5\sqrt{2} \text{ units}$$

Now, check if $AC^2 = AB^2 + BC^2$

$$\Rightarrow (5\sqrt{2})^2 = (5)^2 + (5)^2$$

$$\Rightarrow 50 = 50$$

Therefore, $\triangle ABC$ is a right-angled triangle. and also $AB = BC = 5$ units

Therefore triangle ABC is a right-angled isosceles triangle

6. Since 18, a, b, and - 3 are in A.P., Then

$$a - 18 = -3 - b$$

$$\text{or, } a + b = -3 + 18$$

$$\text{or, } a + b = 15$$

7. $(x_1, y_1) = (24, 1)$ and $(x_2, y_2) = (2, 23)$

$$\begin{aligned} \text{Diameter of Circle} = d &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \sqrt{(2 - 24)^2 + (23 - 1)^2} \\ &= \sqrt{(-22)^2 + (22)^2} = \sqrt{(22)^2(1 + 1)} \\ &= 22\sqrt{2} \text{ units} \end{aligned}$$

$$\text{Therefore, Radius of circle, } r = \frac{d}{2} = \frac{22\sqrt{2}}{2} = 11\sqrt{2} \text{ units}$$

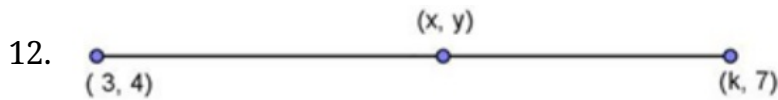
8. Applying Distance Formula to find distance between points (2, 3) and (4, 1), we get

$$d = \sqrt{(4 - 2)^2 + (1 - 3)^2} = \sqrt{(2)^2 + (-2)^2} = \sqrt{4 + 4} = \sqrt{8} = 2\sqrt{2} \text{ units}$$

9. The point on y-axis that is nearest to the point(-2,5) is (0,5).

$$\begin{aligned}
 10. \quad AB &= \sqrt{(0-c)^2 + (-c-0)^2} \\
 &= \sqrt{c^2 + c^2} \\
 &= \sqrt{2c^2} \\
 &= \sqrt{2}c
 \end{aligned}$$

$$\begin{aligned}
 11. \quad AB &= \sqrt{(1+2)^2 + (2-3)^2} = \sqrt{9+1} = \sqrt{10} \\
 BC &= \sqrt{(7-1)^2 + (0-2)^2} = \sqrt{36+4} = \sqrt{40} = 2\sqrt{10} \\
 AC &= \sqrt{(7+2)^2 + (0-3)^2} = \sqrt{81+9} = \sqrt{90} = 3\sqrt{10} \\
 \text{Since } AB + BC &= \sqrt{10} + 2\sqrt{10} = (1+2)\sqrt{10} = 3\sqrt{10} = AC \\
 \text{Hence, the points A, B and C are collinear.}
 \end{aligned}$$



Since, (x, y) is the mid-point

$$x = \frac{3+k}{2}, y = \frac{4+7}{2} = \frac{11}{2}$$

Again,

$$2x + 2y + 1 = 0$$

$$\Rightarrow 2 \times \frac{(3+k)}{2} + 2 \times \frac{11}{2} + 1 = 0$$

$$\Rightarrow 3 + k + 11 + 1 = 0$$

$$\Rightarrow 3 + k + 12 = 0$$

$$\Rightarrow k + 15 = 0$$

$$\Rightarrow k = -15$$

13. Let A(5, 7), B(3, 9), C(8, 6) and D(0, 10) be the given points. Therefore, by mid-point formula, we have,

$$\text{Coordinates of the mid-point of AB are } \left(\frac{5+3}{2}, \frac{7+9}{2} \right) = (4, 8)$$

$$\text{Coordinates of the mid-point of CD are } \left(\frac{8+0}{2}, \frac{6+10}{2} \right) = (4, 8)$$

Therefore, the mid-point of AB = mid point of CD.

14. Since the points are collinear

The area of triangle = 0

\therefore Area of triangle = 0

$$\frac{1}{2} [x_1 (y_2 - y_3) + x_2 (y_3 - y_1) + x_3 (y_1 - y_2)] = 0$$

$$\begin{aligned}
& \frac{1}{2}[5(4-y) + (-3)(y-2) + x(2-4)] = 0 \\
& = \frac{1}{2}[20 - 5y - 3y + 6 + (-2x)] = 0 \\
& \frac{1}{2}[-2x - 8y + 26] = 0 \\
& x + 4y - 13 = 0
\end{aligned}$$

Hence Proved.

15. Given: A (2,5) and C(-1,2)

Let the coordinate of the point B be (a,b).

it is given that AC : BC = 3:4

Then, by section formula , coordinates of C are given by

$$-1 = \frac{3 \times a + 4 \times 2}{3+4} \text{ and } 2 = \frac{3 \times b + 4 \times 5}{3+4}$$

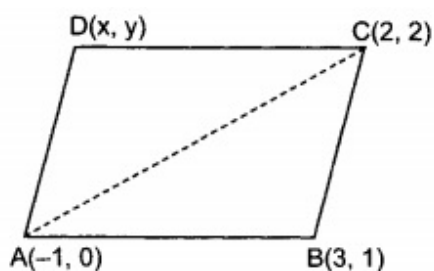
$$\therefore -7 = 3a+8 \text{ and } 14 = 3b+20$$

$$\therefore 3a = -15 \text{ and } 3b = -6$$

$$\therefore a = -5 \text{ and } b = -2$$

Hence, coordinates of B are (-5,-2).

16.



Area of $\triangle ABC$

$$= \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

$$= \frac{1}{2} [-1(1 - 2) + 3(2 - 0) + 2(0 - 1)]$$

$$= \frac{1}{2} [1 + 6 - 2] = \frac{5}{2} \text{ sq. units}$$

Area of $\parallel\text{gm} = 2 \times \text{area of } \triangle ABC$

$$\Rightarrow \text{Area of } \parallel\text{gm} = 2 \times \frac{5}{2} = 5 \text{ sq. units}$$

Let coordinates of D are (x, y)

$$\text{Mid point of AC} = \left(\frac{-1+2}{2}, \frac{0+2}{2} \right) = \left(\frac{1}{2}, 1 \right)$$

$$\text{Mid-point of BD} = \left(\frac{3+x}{2}, \frac{1+y}{2} \right)$$

\therefore Diagonals of a $\parallel\text{gm}$ bisect each other

\therefore Mid-point of BD = Mid-point of AC

$$\Rightarrow \left(\frac{3+x}{2}, \frac{1+y}{2} \right) = \left(\frac{1}{2}, 1 \right)$$

$$\Rightarrow \frac{3+x}{2} = \frac{1}{2} \text{ and } \frac{1+y}{2} = 1$$

$$\Rightarrow x = -2$$

$$\Rightarrow y = 1$$

$$\text{Now AD} = \sqrt{(-1+2)^2 + (0+1)^2} = \sqrt{2}$$

Also area of \triangle gm = base \times height

$$\Rightarrow \text{AD} \times \text{height} = 5$$

$$\Rightarrow \sqrt{2} \times \text{height} = 5$$

$$\Rightarrow \text{height} = \frac{5}{\sqrt{2}} = \frac{5}{2}\sqrt{2} \text{ units.}$$

17. According to the question,

A (3,-3) and B (-2, 7)

On the x-axis, the y-coordinate is zero

So, let the point be (x, 0)

Let the ratio be k : 1

$$(x, 0) = \left(\frac{-2k+3}{k+1}, \frac{7k-3}{k+1} \right)$$

$$\Rightarrow \frac{7k-3}{k+1} = 0$$

$$\Rightarrow 7k - 3 = 0$$

$$\Rightarrow k = \frac{3}{7}$$

\therefore The line is divided in the ratio of 3:7

$$\Rightarrow \frac{-2k+3}{k+1} = x$$

$$\Rightarrow \frac{-2 \times \frac{3}{7} + 3}{\frac{3}{7} + 1} = x$$

$$\Rightarrow \frac{-\frac{6}{7} + 3}{\frac{10}{7}} = x$$

$$\Rightarrow \frac{\frac{-6+21}{7}}{\frac{10}{7}} = x$$

$$\Rightarrow \frac{\frac{15}{7}}{\frac{10}{7}} = x$$

$$\Rightarrow x = \frac{3}{2}$$

Coordinate of y is 0 at x-axis,

\therefore The coordinates of the point at which x axis divides AB is $\left(\frac{3}{2}, 0 \right)$ in ratio of 3:7.

18. Let the point of x-axis be P(x, 0)

Given A(2, -5) and B(-2, 9) are equidistant from P

That is PA = PB

Hence $PA^2 = PB^2 \rightarrow (1)$

Distance between two points is $\sqrt{[(x_2 - x_1)^2 + (y_2 - y_1)^2]}$

$$PA = \sqrt{[(2 - x)^2 + (-5 - 0)^2]}$$

$$PA^2 = 4 - 4x + x^2 + 25$$

$$= x^2 - 4x + 29$$

$$\text{Similarly, } PB^2 = x^2 + 4x + 85$$

Equation (1) becomes

$$x^2 - 4x + 29 = x^2 + 4x + 85$$

$$- 8x = 56$$

$$x = -7$$

Hence the point on x-axis is (-7, 0)

19. A(x_1, y_1), B(x_2, y_2), C(x_3, y_3) are the three vertices of $\triangle ABC$.

i. Median from A meets BC at D.

\therefore D is the mid-point of BC.

$$\therefore \text{Coordinates of } D = \left(\frac{x_2 + x_3}{2}, \frac{y_2 + y_3}{2} \right)$$

ii. P divides AD in the ratio 2 : 1.

$$\begin{aligned} \therefore \text{Coordinates of P} &= \left(\frac{2 \times \frac{x_2 + x_3}{2} + 1 \times x_1}{2 + 1}, \frac{2 \times \frac{y_2 + y_3}{2} + 1 \times y_1}{2 + 1} \right) \\ &= \left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3} \right) \end{aligned}$$

iii. Median from B meet AC at E and median from C meets AB at F.

\therefore E is the mid-point of AC and F is the mid-point of AB.

$$\therefore \text{Coordinates of } E = \left(\frac{x_1 + x_3}{2}, \frac{y_1 + y_3}{2} \right) \text{ and}$$

$$\text{Coordinates of } F = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Q divides BE in the ratio 2 : 1.

$$\begin{aligned} \therefore \text{Coordinates of Q} &= \left(\frac{2 \times \frac{x_1 + x_3}{2} + 1 \times x_2}{2 + 1}, \frac{2 \times \frac{y_1 + y_3}{2} + 1 \times y_2}{2 + 1} \right) \\ &= \left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3} \right) \end{aligned}$$

R divides CF in the ratio 2 : 1.

$$\begin{aligned}\therefore \text{Coordinates of R} &= \left(\frac{2 \times \frac{x_1+x_2}{2} + 1 \times x_3}{2+1}, \frac{2 \times \frac{y_1+y_2}{2} + 1 \times y_3}{2+1} \right) \\ &= \left(\frac{x_1+x_2+x_3}{3}, \frac{y_1+y_2+y_3}{3} \right)\end{aligned}$$

iv. Coordinates of centroid of

$$\Delta ABC = \left(\frac{x_1+x_2+x_3}{3}, \frac{y_1+y_2+y_3}{3} \right)$$

20. Let Q(x, 0) be a point on x-axis which lies on the perpendicular bisector of AB.

Therefore, QA = QB

$$\Rightarrow QA^2 = QB^2$$

$$\Rightarrow (-5 - x)^2 + (-2 - 0)^2 = (4 - x)^2 + (-2 - 0)^2$$

$$\Rightarrow (x + 5)^2 + (-2)^2 = (4 - x)^2 + (-2)^2$$

$$\Rightarrow x^2 + 25 + 10x + 4 = 16 + x^2 - 8x + 4$$

$$\Rightarrow 10x + 8x = 16 - 25$$

$$\Rightarrow 18x = -9$$

$$\Rightarrow x = \frac{-9}{18} = \frac{-1}{2}$$

Hence, the point Q is $\left(\frac{-1}{2}, 0 \right)$.

$$\text{Now, } QA^2 = \left[-5 + \frac{1}{2} \right]^2 + [-2 - 0]^2$$

$$= \left(\frac{-9}{2} \right)^2 + \frac{4}{1}$$

$$\Rightarrow QA^2 = \frac{81}{4} + \frac{4}{1} = \frac{81+16}{4} = \frac{97}{4}$$

$$\Rightarrow QA = \sqrt{\frac{97}{4}} = \frac{\sqrt{97}}{2} \text{ units}$$

$$\text{Now, } QB^2 = \left(4 + \frac{1}{2} \right)^2 + (-2 - 0)^2 = \left(\frac{9}{2} \right)^2 + (-2)^2$$

$$\Rightarrow QB^2 = \frac{81}{4} + \frac{4}{1} = \frac{81+16}{4} = \frac{97}{4}$$

$$\Rightarrow QB = \sqrt{\frac{97}{4}} = \frac{\sqrt{97}}{2} \text{ units}$$

$$\text{and } AB = \sqrt{(4 + 5)^2 + [-2 - (-2)]^2} = \sqrt{(9)^2} = 9 \text{ units}$$

$$\Rightarrow AB = 9 \text{ units}$$

As QA = QB

So, ΔQAB is an isosceles Δ .