Construction of Quadrilaterals

- A unique quadrilateral can be constructed, if any five measurements of the quadrilateral are given.
- Construction of a quadrilateral when four sides and a diagonal are given:

Example:

Construct a quadrilateral WXYZ, where WX = 4.5 cm, XY = 5 cm, YZ = 5.5 cm, ZW = 3 cm, and WY = 6 cm.

Solution:

Step 1:

Draw a line WY of length 6 cm. Draw an arc of radius 4.5 cm with W as centre and another arc of length 5 cm with Y as centre. The intersection of the two arcs will be the point, X.

Join WX and XY.

Step 2:

The point, Z, will be on the opposite side of point X with respect to WY.

Draw an arc of length 3 cm taking W as centre and another arc of length 5.5 cm taking Y as centre. The intersection of these arcs will be the point, Z.

Join WZ and YZ.

WXYZ is the required quadrilateral.



• Construction of a quadrilateral when two diagonals and three sides are given

Example:

Construct a quadrilateral PQRS, where PR = 7 cm, QS = 8 cm, PQ = 5 cm, QR = 5 cm, and PS = 5.5 cm.

Solution:

The steps of constructing quadrilateral PQRS are as follows:

Step 1:

Draw a line PR of length 7 cm. Draw an arc of radius 5 cm taking P as centre and an arc of radius 5 cm taking R as centre. The point of intersection of these two arcs will be the point, Q.

Join PQ and RQ.



Step 2:

With Q as centre, draw an arc of radius 8 cm. The point, S, will lie on this arc.

Then, taking P as centre, draw an arc of radius 5.5 cm. The intersection point of the two arcs will be the point, S.

Join PS and RS.



PQRS is the required quadrilateral.

• Construction of a quadrilateral when three sides and two included angles are given

Example:

Construct a quadrilateral PQRS with SR = 6.5 cm, PS = 5 cm, QR = 3 cm, $\angle R$ = 120°, and $\angle S$ = 70°.

Solution:

The steps of construction are as follows:

Step 1:

Draw SR = 6.5 cm. Draw \angle SRX = 120° at R and \angle RSY = 70° at S.



Step 2:

With S as centre, draw an arc of radius 5 cm intersecting SY at P.

With R as centre, draw an arc of radius 3 cm intersecting RX at Q. Join PQ to obtain the required quadrilateral PQRS.



• Construction of a quadrilateral when two adjacent sides and three angles are given:

Example:

Construct a quadrilateral ABCD, where AB = 6 cm, AD = 4 cm, $\angle A = 90^\circ$, $\angle B = 105^\circ$, and $\angle D = 60^\circ$.

Solution:

Step 1:

Draw a line segment AB of length 6 cm. Make $\angle ABX = 105^{\circ}$ at B and $\angle BAY = 90^{\circ}$ at A.

Step 2:

With A as centre, draw an arc of radius 4 cm to cut the ray AY at point D. At D, $draw \angle ADZ = 60^{\circ}$.

The point of intersection of the rays, BX and DZ, will be the point, C.

ABCD is the required quadrilateral.

