

Total No. of Questions - 24

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No.

Total No. of Printed Pages - 4

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Part - III
MATHEMATICS, Paper - II (B)
(Coordinate Geometry and Calculus)
(English Version)

Time : 3 Hours**Max. Marks : 75**

Note : This question paper consists of three sections A, B and C.

SECTION A **$10 \times 2 = 20$** **I. Very Short Answer Type Questions.**

- i). Attempt all questions.
 - ii) Each question carries two marks.
1. Find the equation of a circle which is concentric with $x^2 + y^2 - 6x - 4y - 12 = 0$ and passing through (-2, 14).
 2. Find the value of 'k', if the points (1, 3) and (2, k) are conjugate with respect to the circle $x^2 + y^2 = 35$.
 3. Find the equation of the radical axis of the circles $x^2 + y^2 - 3x - 4y + 5 = 0$ and $3(x^2 + y^2) - 7x + 8y - 11 = 0$.
 4. Find the coordinates of the points on the parabola $y^2 = 8x$ whose focal distance is 10.
 5. If $3x - 4y + k = 0$ is a tangent to the hyperbola $x^2 - 4y^2 = 5$, then find the value of 'k'.

6. Evaluate $\int \sqrt{1 - \sin 2x} dx$ on $I \subset \left[2n\pi - \frac{3\pi}{4}, 2n\pi + \frac{\pi}{4}\right]$, $n \in \mathbb{Z}$.

7. Evaluate $\int \cos \sqrt{x} dx$ on IR .

8. Evaluate $\int_{-\pi/2}^{\pi/2} \frac{\cos x}{1+e^x} dx$.

9. Find the area of the region enclosed by $y = x^3 + 3$, $y = 0$,
 $x = -1$, $x = 2$. *Note*

10. Find the order and degree of the differential equation

$$\left[\frac{d^2y}{dx^2} + \left(\frac{dy}{dx} \right)^3 \right]^{6/5} = 6y.$$

SECTION B

5 × 4 = 20

II. Short Answer Type Questions.

- i) Attempt any five questions.
- ii) Each question carries four marks.

11. Find the equation of the tangent to $x^2 + y^2 - 2x + 4y = 0$ at $(3, -1)$. Also find the equation of tangent parallel to it.

12. Find the equation of the circle passing through the points of intersection of the circles $x^2 + y^2 - 8x - 6y + 21 = 0$,
 $x^2 + y^2 - 2x - 15 = 0$ and $(1, 2)$.

13. If the normal at one end of a latus rectum of the ellipse

$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ passes through one end of the minor axis, then show that $e^4 + e^2 = 1$ (e = eccentricity of the ellipse).

14. Find the eccentricity, length of latus rectum, foci and the equations of directrices of the ellipse $9x^2 + 16y^2 = 144$.

15. Prove that the point of intersection of two perpendicular tangents to the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ lies on the circle $x^2 + y^2 = a^2 - b^2$.

16. Evaluate $\int_{-a}^a x^2 (a^2 - x^2)^{3/2} dx$.

17. Solve the differential equation $\frac{dy}{dx} = e^{x-y} + x^2 e^{-y}$.

SECTION C

5 × 7 = 35

III. Long Answer Type Questions.

- i) Attempt any five questions.
- ii) Each question carries seven marks.

18. Find the equation of a circle passing through $(2, -3)$ and $(-4, 5)$ and having a centre on $4x + 3y + 1 = 0$.

19. Show that the circles $x^2 + y^2 - 4x - 6y - 12 = 0$ and $5(x^2 + y^2) - 8x - 14y - 32 = 0$ touch each other. Also find the point of contact and common tangent at this point of contact.

20. Find the equation of the parabola whose axis is parallel to X -axis and which passes through the points $(-2, 1)$, $(1, 2)$ and $(-1, 3)$.

21. Evaluate $\int \sqrt{\frac{5-x}{x-2}} dx$ on $(2, 5)$.

22. Obtain the reduction formula for $I_n = \int \tan^n x dx$, n being a positive integer $n \geq 2$ and deduce the value of $\int \tan^6 x dx$.

23. Evaluate $\int_0^1 \frac{\log(1+x)}{1+x^2} dx$.

24. Find the solution of the equation $x(x-2) \frac{dy}{dx} - 2(x-1)y = x^3(x-2)$, which satisfies the condition that $y=9$ when $x=3$.
