

(Given $H \Rightarrow$ very small)

① $F_{D1} = F_{D2}$
 $\tau_1 A_1 = \tau_2 A_2$ ($A_1 = A_2 = A$)

$\tau_1 = \tau_2$

$\mu_1 \cdot \frac{v}{y} = \mu_2 \cdot \frac{v}{(H-y)}$

$\mu_1 (H-y) = \mu_2 \cdot y$

$\frac{\mu_1 H}{(\mu_1 + \mu_2)} = y$

- a) the drag force is equal on both side of the plate
 b) the total drag force is mini.

IES
10 mark

② $F_{DT} = F_{D1} + F_{D2}$
 $= \tau_1 A + \tau_2 A$
 $= \mu_1 \frac{v}{y} A + \mu_2 \frac{v}{(H-y)} A$
 $= v \cdot A \left(\frac{\mu_1}{y} + \frac{\mu_2}{(H-y)} \right)$

for mini.

$\frac{dF_{DT}}{dy} = 0$

$\frac{\sqrt{\mu_2}}{H-y} = \frac{\sqrt{\mu_1}}{y}$

$-\frac{\mu_1}{y^2} + \frac{\mu_2}{(H-y)^2} = 0$

$y = \frac{H \cdot \sqrt{\mu_1}}{\sqrt{\mu_1} + \sqrt{\mu_2}}$

(Weight = Resistive force)

$Mg = \text{Resistive force}$

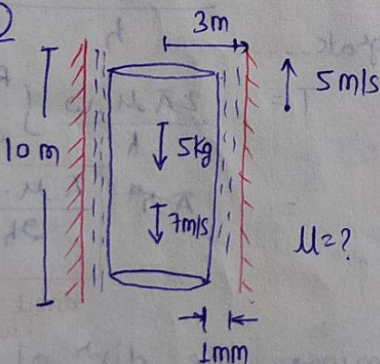
$5 \times 9.81 = \tau \cdot A$

$= \mu \cdot \frac{v}{h} \cdot A$

$= \frac{\mu \times (7 - (-5)) \cdot (2\pi \cdot (3) \times 10)}{1 \times 10^{-3}}$

$\mu = 2.16 \times 10^{-5} \frac{N \cdot s}{m^2}$

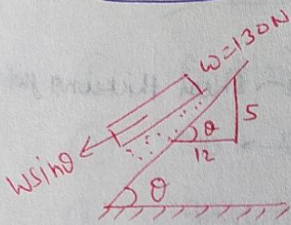
Pb - ④



$\tau = \mu \cdot \frac{v}{h}$ Relative velocity

exact surface area of cylinder $= 2\pi r h + 2\pi r^2$
 $= 2\pi r (r + h)$
 lateral surface area of cylinder $= (2\pi r h)$

Pb-17



$$W \sin \theta = \tau_0 \cdot A$$

$$130 \times \frac{5}{13} = \mu \cdot \frac{V}{L} A = \mu \times \frac{0.5}{0.5 \times 10^{-2}} \times 1 =$$

$$\mu = 0.5 \text{ NS/m}^2 \text{ Ans}$$

Rheology

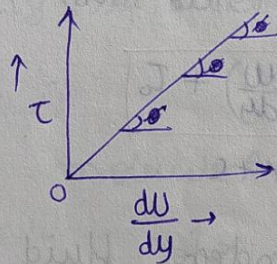
It is branch of science which deals with study of different type of fluid in flow

Newtonian fluid:-

Obeys newton law

$$\tau = \mu \frac{du}{dy}$$

$$y = m \cdot x$$



slope of curve = μ

example $\rightarrow$ oil, Kerosene, water, mercury, Air, petrol

Non-Newtonian fluid:-

Don't obey newtonian fluid

$$\tau = A \left(\frac{du}{dy} \right)^n$$

A = Consistency index

n = Flow behaviour index

Pseudo-plastic

(पतले fluid isme)
ayenge

$$n < 1$$

$$\tau = A \left(\frac{du}{dy} \right)^n$$

$$\tau = \underbrace{A \left(\frac{du}{dy} \right)^{n-1}}_{\mu_{\text{apparent}}} \cdot \frac{du}{dy}$$

$\mu_{\text{apparent}} \downarrow$

Ex. Blood
milk

Dilatant

(moti fluid isme ayenge)

$$n > 1$$

$$\tau = A \left(\frac{du}{dy} \right)^n$$

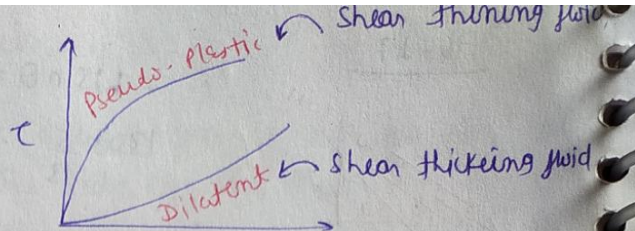
$$\tau = \underbrace{A \left(\frac{du}{dy} \right)^{n-1}}_{\mu_{\text{apparent}}} \cdot \frac{du}{dy}$$

$\mu_{\text{apparent}} \uparrow$

Ex. saturated solution of
sugar, Rice, Starch, solution
Honey.

Pseudo-plastic and Dilatant are

"time independent fluid"



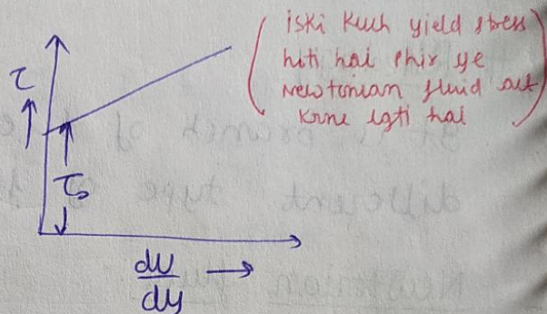
Bingham Plastic fluid :- / ideal Plastic $\frac{du}{dy}$

$$\tau = A \left(\frac{du}{dy} \right)^n + B$$

$$A = \mu$$

$$n = 1$$

$$B = \tau_0 \text{ (yield stress)}$$



$$\tau = \mu \left(\frac{du}{dy} \right) + \tau_0$$

$$y = mx + c$$

- Ex. - Toothpaste
- sewage sludge
- mud clay

time dependent fluid

$$\tau = A \left(\frac{du}{dy} \right)^n + B$$

$B > 0$

Thixotropic
($n < 1$)

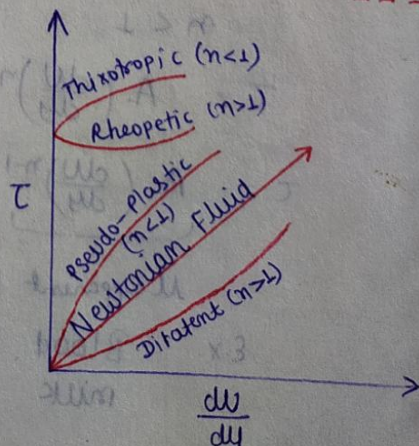
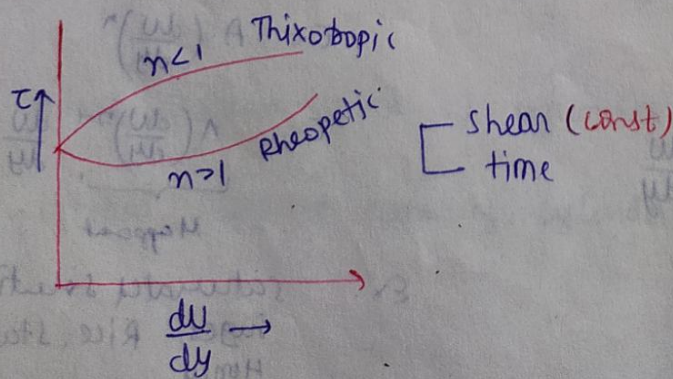
(μ apparent decreases
w.r.t time)

Ex: some paint
Painter ink

Rheopetic
($n > 1$)

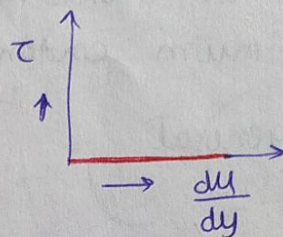
(μ apparent increases
w.r.t time)

Ex: gypsum paste in water.



Ideal fluid :-

- ① Frictionless and "Inviscid fluid" ($\mu=0$) ($\tau=0$)
- ② No - surface tension.
- ③ Incompressible ④ viscosity zero



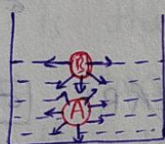
Visco-elastic fluid :-

these type of fluid having

a property of elasticity upto certain extent

Surface tension effect :-

Experimental view



$\sigma = 0.073 \text{ N/m}$
for air water
interface at
temp of 20°C

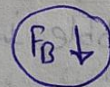
molecule A (inside of liquid)



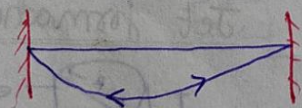
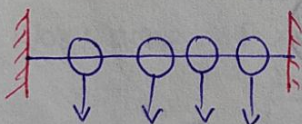
$F_A = 0$

$\sigma = 0.480 \text{ N/m}$
for air & mercury
interface at
temp. 20°C

molecule B (At the surface)

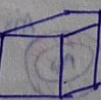


In general

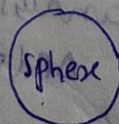
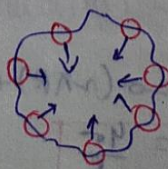


In general

Volume fix



(mini surface
Area)



Maths $\rightarrow$

$$\sigma = \frac{F}{L}$$

(F = tensile force)

(L = length)

i.e. = (the effect of cohesive force at the surface)

It is the property of liquid by virtue of which tries to minimise the surface area upto the maximum extent.

In general

Droplet formation

$$P_o / P_i$$

$$P_i = P_o$$

$$P_o$$

$$P_i > P_o$$

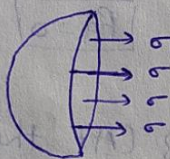
$$P_i$$

$$P_o$$

$$P_i > P_o$$

$$\Delta P = P_i - P_o$$

Water droplet →



Radius = R

Force analysis

$$\Delta P (\pi R^2) = \sigma (2\pi R)$$

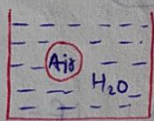
$$\Delta P = \frac{2\sigma}{R}$$

$$\text{Pressure} = \frac{\text{Force} \times \text{Area}}{\text{Area}} \quad \sigma = \frac{F}{l}$$

$$\sigma \cdot l = F$$

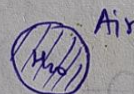
$$P = F \times A$$

Air bubble in H₂O

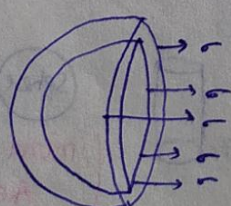


$$\Delta P = \frac{2\sigma}{R}$$

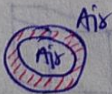
Create special group



② Soap bubble :-



Radius = R

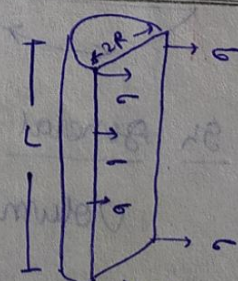


Force analysis

$$\Delta P (\pi R^2) = 2\sigma (2\pi R) + \sigma (2\pi R)$$

$$\Delta P = \frac{4\sigma}{R}$$

③ Jet formation



Force analysis

$$\Delta P (2RL) = \sigma L + \sigma L$$

$$\Delta P = \frac{\sigma}{R}$$