## mutual coherence function $\Gamma_{ii}$ Mutual temporal interval τ $\boldsymbol{\Gamma}_{12}(\tau) = \langle \boldsymbol{\psi}_1(t) \boldsymbol{\psi}_2^*(t+\tau) \rangle$ (8.97)coherence $\psi_i$ (complex) wave disturbance function at spatial point i $\gamma_{12}(\tau) = \frac{\langle \boldsymbol{\psi}_1(t) \boldsymbol{\psi}_2^*(t+\tau) \rangle}{[\langle |\boldsymbol{\psi}_1|^2 \rangle \langle |\boldsymbol{\psi}_2|^2 \rangle]^{1/2}}$ t time (8.98)Complex degree mean over time $\langle \cdot \rangle$ of coherence $=\frac{\Gamma_{12}(\tau)}{[\Gamma_{11}(0)\Gamma_{22}(0)]^{1/2}}$ complex degree of coherence Yij (8.99)complex conjugate combined intensity Itot Combined $I_{\text{tot}} = I_1 + I_2 + 2(I_1I_2)^{1/2} \Re[\gamma_{12}(\tau)]$ Ii intensity of disturbance at intensity<sup>a</sup> point i (8.100)R real part of $V(\tau) = \frac{2(I_1I_2)^{1/2}}{I_1 + I_2} |\gamma_{12}(\tau)|$ Fringe visibility (8.101)if $|\gamma_{12}(\tau)|$ is a constant: $V = \frac{I_{\rm max} - I_{\rm min}}{I_{\rm max} + I_{\rm min}}$ $I_{\text{max}}$ max. combined intensity (8.102) $I_{\min}$ min. combined intensity if $I_1 = I_2$ : $V(\tau) = |\gamma_{12}(\tau)|$ (8.103) $\gamma(\tau) = \frac{\langle \psi_1(t)\psi_1^*(t+\tau)\rangle}{\langle |\psi_1(t)^2|\rangle}$ $\gamma(\tau)$ degree of temporal coherence (8.104)Complex degree $I(\omega)$ specific intensity of temporal $=\frac{\int I(\omega)e^{-i\omega\tau}d\omega}{\int I(\omega)d\omega}$ radiation angular frequency ω coherence<sup>b</sup> (8.105)speed of light c $\Delta \tau_{\rm c}$ coherence time Coherence time $\Delta \tau_{\rm c} = \frac{\Delta l_{\rm c}}{c} \sim \frac{1}{\Delta v}$ (8.106) $\Delta l_{\rm c}$ coherence length and length $\Delta v$ spectral bandwidth $\gamma(\mathbf{D})$ degree of spatial coherence $\gamma(\boldsymbol{D}) = \frac{\langle \boldsymbol{\psi}_1 \boldsymbol{\psi}_2^* \rangle}{[\langle |\boldsymbol{\psi}_1|^2 \rangle \langle |\boldsymbol{\psi}_2|^2 \rangle]^{1/2}}$ spatial separation of points 1 (8.107)Complex degree and 2 of spatial $=\frac{\int I(\hat{s})e^{ikD\cdot\hat{s}}\,\mathrm{d}\Omega}{\int I(\hat{s})\,\mathrm{d}\Omega}$ $I(\hat{s})$ specific intensity of distant coherence<sup>c</sup> (8.108)extended source in direction $\hat{s}$ $d\Omega$ differential solid angle ŝ unit vector in the direction of $\frac{\langle I_1 I_2 \rangle}{\lceil \langle I_1 \rangle^2 \langle I_2 \rangle^2 \rceil^{1/2}} = 1 + \gamma^2(\boldsymbol{D})$ Intensity dΩ (8.109)correlation<sup>d</sup> k wavenumber Speckle $\operatorname{pr}(I) = \frac{1}{\langle I \rangle} e^{-I/\langle I \rangle}$ intensity (8.110)probability density pr distribution<sup>e</sup> $\Delta w_{\rm c}$ characteristic speckle size Speckle size $\Delta w_{\rm c} \simeq \frac{\lambda}{-}$ wavelength λ (coherence (8.111)source angular size as seen α width) from the screen

## 8.7 Coherence (scalar theory)

<sup>*a*</sup>From interfering the disturbances at points 1 and 2 with a relative delay  $\tau$ .

<sup>b</sup>Or "autocorrelation function."

<sup>c</sup>Between two points on a wavefront, separated by **D**. The integral is over the entire extended source.

 $^{d}$ For wave disturbances that have a Gaussian probability distribution in amplitude. This is "Gaussian light" such as from a thermal source.

<sup>e</sup>Also for Gaussian light.