## Long Answer Type Questions

# [4 Marks]

Que 1. Construct a triangle ABC in which BC = 7 cm,  $\angle B$  = 75° and AB + AC = 13 cm.

Sol. Steps of Construction



(i) Draw BC = 7 cm.

(ii) Construct  $\angle$ YBC = 75°.

(iii) From ray BY, cut-off line segment BD = AB + AC = 13 cm.

(iv) Join CD.

(v) Draw the perpendicular bisector of CD meeting BY at A.

(vi) Join AC to obtain the required triangle ABC.

### Justification

Since A lied on the perpendicular bisector of CD.

:. AC =AD Now BD = 13 cm  $\Rightarrow$  BA + AD = 13 cm  $\Rightarrow$  BA + AC = 13 cm Hence,  $\triangle$ ABC is the required triangle. Que 2. Construct a triangle PQR in which QR = 6 cm,  $\angle$ Q = 60° and PR – PQ = 2 cm.

Sol. Steps of Construction



(i) Draw QR = 6 cm.

(ii) Construct  $\angle$ YQR = 60°.

(iii) Produce YQ to Y' to form line YQY'.

(iv) From ray QY', cut-off line segment QS = 2 cm.

(v) Join SR.

(vi) Draw perpendicular bisector of RS which intersect QY at P.

(vii) Join PR to obtain required  $\Delta PQR$ .

#### Justification

As P lies on the perpendicular bisector of RS. Therefore, PR = PS = PQ + QS = PQ + 2 cm $\Rightarrow PR - PQ = 2 \text{ cm}$ Hence,  $\Delta PQR$  is the required triangle. Que 3. Construct a triangle ABC in which BC = 8 cm,  $\angle B$  = 45° and AB – AC = 3.5 cm.





(i) Draw BC = 8 cm.

(ii) Construct  $\angle$ YBC = 45°

(iii) From ray BY, cut-off line segment

BD = 3.5 cm.

(iv) Join CD.

(v) Draw perpendicular bisector of CD intersecting BY at A.

(vi) Join AC to obtain the required triangle ABC.

#### Justification

As A lies on the perpendicular bisector of CD. Therefore,

AD = AC Now, BD = 3.5 cm

 $\Rightarrow$  AB – AD = 3.5 cm

 $\Rightarrow$  AB – AC = 3.5 cm

Hence,  $\triangle ABC$  is the required triangle.

Que 4. Construct a triangle XYZ in which  $\angle Y = 30^{\circ}$ ,  $\angle Z = 90^{\circ}$  and XY + YZ + ZX = 11 cm.

#### Sol. Steps of Construction



(i) Draw a line segment AB = 11 cm.

(ii) At A, construct an angle of 30° and B construct an angle of 90°.

(iii) Bisect these angles. Let bisector of these angles intersect at point X.

(iv) Draw perpendicular bisector CD of XA to intersect AB at Y and EF of XB to intersect AB at Z.

(v) Join XY and XY to obtain requires  $\Delta$ XYZ.

#### Justification

Since Y lies on the perpendicular bisector of XB. Therefore,

 $\begin{array}{c} ZB = ZX\\ \Rightarrow \qquad \angle ZBX = \angle ZXB\\ \text{Now,} \qquad AB = AY + YZ + ZB \qquad \Rightarrow \qquad AB = XY + YZ + ZX\\ \text{In } \Delta XAY, \text{ we have}\\ \qquad \qquad \angle XYZ = \angle YXA + \angle YAX = 2 \angle YAX = \angle A\\ \text{In } XBZ, \text{ we have}\\ \qquad \qquad \qquad \angle XZY = \angle ZBX + \angle ZXB = 2 \angle ZBX = \angle B\end{array}$ 

Que 5. Construct a right triangle whose base is 12 cm and sum of its hypotenuse and other side is 18 cm.

Sol. Steps of Construction



(i) Draw BC = 12 cm.

(ii) Construct ∠CBY = 90°

(iii) From ray BY, cut-off line segment BD = 10 cm.

(iv) Join CD.

(v) Draw AC to obtain the required  $\triangle ABC$ .

#### Justification

Since A lies on the perpendicular bisector of CD. Therefore,

Now,

AD = AC BD = BA + AD

 $\Rightarrow$  BD = AB + AC

Hence,  $\triangle ABC$  is the required triangle.