

KINETIC THEORY OF GASES

"With thermodynamics one can calculate almost everything crudely; with kinetic theory, one can calculate fewer things, but more accurately." - Eugene Wigner



LEARNING OBJECTIVES

In this unit, the student is exposed to

- necessity of kinetic theory of gases
- the microscopic origin of pressure and temperature
- · correlate the internal energy of the gas and translational kinetic energy of gas molecules
- meaning of degrees of freedom
- calculate the total degrees of freedom for mono atomic, diatomic and triatomic molecules
- law of equipartition of energy
- calculation of the ratio of C_p and C_v
- mean free path and its dependence with pressure, temperature and number density
- Brownian motion and its microscopic origin



KINETIC THEORY

9.1.1 Introduction

Thermodynamics is basically a macroscopic We discussed macroscopic parameters like pressure, temperature and volume of thermodynamical systems in unit 8. In this unit we discuss the microscopic origin of pressure and temperature by considering a thermodynamic system as collection of particles or molecules. Kinetic theory relates pressure and temperature to molecular motion of sample of a gas and it is a bridge between Newtonian mechanics and thermodynamics. The present chapter introduces the kinetic nature of gas molecules.

9.1.2 Postulates of kinetic theory of gases

Kinetic theory is based on certain assumptions which makes the mathematical treatment simple. None of these assumptions are strictly true yet the model based on these assumptions can be applied to all gases.

- 1. All the molecules of a gas are identical, elastic spheres.
- 2. The molecules of different gases are different.
- 3. The number of molecules in a gas is very large and the average separation between them is larger than size of the gas molecules.
- 4. The molecules of a gas are in a state of continuous random motion.
- 5. The molecules collide with one another and also with the walls of the container.





- 6. These collisions are perfectly elastic so that there is no loss of kinetic energy during collisions.
- 7. Between two successive collisions, a molecule moves with uniform velocity.
- 8. The molecules do not exert any force of attraction or repulsion on each other except during collision. The molecules do not possess any potential energy and the energy is wholly kinetic.
- 9. The collisions are instantaneous. The time spent by a molecule in each collision is very small compared to the time elapsed between two consecutive collisions.
- 10. These molecules obey Newton's laws of motion even though they move randomly.

9.2

PRESSURE EXERTED BY A GAS

9.2.1 Expression for pressure exerted by a gas

Consider a monoatomic gas of N molecules each having a mass m inside a cubical container of side l as shown in the Figure 9.1 (a).

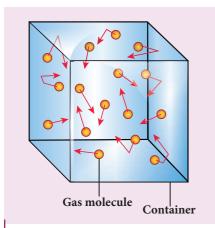




Figure 9.1 (a) Container of gas molecules

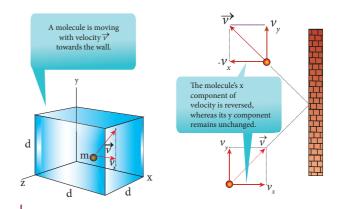


Figure 9.1 (b) Collision of a molecule with the wall

The molecules of the gas are in random motion. They collide with each other and also with the walls of the container. As the collisions are elastic in nature, there is no loss of kinetic energy, but a change in momentum occurs.

The molecules of the gas exert pressure on the walls of the container due to collision on it. During each collision, the molecules impart certain momentum to the wall. Due to transfer of momentum, the walls experience a continuous force. The force experienced per unit area of the walls of the container determines the pressure exerted by the gas. It is essential to determine the total momentum transferred by the molecules in a short interval of time.

A molecule of mass m moving with a velocity \vec{v} having components (v_x, v_y, v_z) hits the right side wall. Since we have assumed that the collision is elastic, the particle rebounds with same speed and its x-component is reversed. This is shown in the Figure 9.1 (b). The components of velocity of the molecule after collision are $(-v_x, v_y, v_z)$.

The x-component of momentum of the molecule before collision = mv_x



The change in momentum of the molecule in x direction

=Final momentum – initial momentum = $-mv_x - mv_x = -2mv_x$

According to law of conservation of linear momentum, the change in momentum of the wall = $2mv_x$

Note

In x direction, the total momentum of the system before collision is equal to momentum of the molecule

 (mv_x) since the momentum of the wall is zero. According to the law of conservation of momentum the total momentum of system after the collision must be equal to total momentum of system before collision. The momentum of the molecule (in x direction) after the collision is $-mv_x$ and the momentum of the wall after the collision is $2mv_x$. So total momentum of the system after the collision is $(2mv_x-mv_x)=mv_x$ which is same as the total momentum of the system before collision.

The number of molecules hitting the right side wall in a small interval of time Δt is calculated as follows.

The molecules within the distance of $v_x \Delta t$ from the right side wall and moving towards the right will hit the wall in the time interval Δt . This is shown in the Figure 9.2. The number of molecules that will hit the right side wall in a time interval Δt is equal to the product of volume $(Av_x \Delta t)$ and number density of the molecules (n). Here A is area of the wall and n is number of molecules per unit volume $\left(\frac{N}{V}\right)$. We have assumed that the number density is the same throughout the cube.



UNIT 9 KINETIC THEORY OF GASES

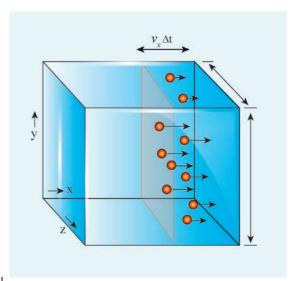


Figure 9.2 Number of molecules hitting the wall

Not all the n molecules will move to the right, therefore on an average only half of the n molecules move to the right and the other half moves towards left side.

The number of molecules that hit the right side wall in a time interval Δt

$$= \frac{n}{2} A v_{x} \Delta t \tag{9.1}$$

In the same interval of time Δt , the total momentum transferred by the molecules

$$\Delta p = \frac{n}{2} A v_x \, \Delta t \times 2 m v_x = A v_x^2 \, m n \Delta t \qquad (9.2)$$

From Newton's second law, the change in momentum in a small interval of time gives rise to force.

The force exerted by the molecules on the wall (in magnitude)

$$F = \frac{\Delta p}{\Delta t} = nmAv_x^2 \tag{9.3}$$

Pressure, P =force divided by the area of the wall

$$P = \frac{F}{A} = nmv_x^2 \tag{9.4}$$

Since all the molecules are moving completely in random manner, they do not have same speed. So we can replace the term v_x^2 by the average $\overline{v_x^2}$ in equation (9.4)

Since the gas is assumed to move in random direction, it has no preferred direction of motion (the effect of gravity on the molecules is neglected). It implies that the molecule has same average speed in all the three direction. So, $\overline{v_x^2} = \overline{v_y^2} = \overline{v_z^2}$. The mean

square speed is written as

$$\overline{v^{2}} = \overline{v_{x}^{2}} + \overline{v_{y}^{2}} + \overline{v_{z}^{2}} = 3v_{x}^{2}$$

$$\overline{v_{x}^{2}} = \frac{1}{2}\overline{v^{2}}$$

Using this in equation (9.5), we get

$$P = \frac{1}{3} n m \overline{v^2} \text{ or } P = \frac{1}{3} \frac{N}{V} m \overline{v^2}$$

$$as \left[n = \frac{N}{V} \right]$$
(9.6)

The following inference can be made from the above equation. The pressure exerted by the molecules depends on

- **Number density** $n = \frac{N}{V}$. It implies that if the number density increases then pressure will increase. For example when we pump air inside the cycle tyre or car tyre essentially the number density increases and as a result the pressure increases.
- (ii) Mass of the molecule Since the pressure arises due to momentum transfer to the wall, larger mass will have larger momentum for a fixed speed. As a result the pressure will increase.
- (iii) Mean square speed For a fixed mass if we increase the speed, the average speed will also increase. As a result the pressure will increase.

For simplicity the cubical container is taken into consideration. The above result is true for any shape of the container as the area A does not appear in the final expression (9.6). Hence the pressure exerted by gas molecules on the wall is independent of area of the wall (A).

Kinetic interpretation of temperature

To understand the microscopic origin of temperature in the same way,

Rewrite the equation (9.6)

$$P = \frac{1}{3} \frac{N}{V} m \overline{v^2}$$

$$PV = \frac{1}{3} N m \overline{v^2}$$
(9.7)

Comparing the equation (9.7) with ideal gas equation PV=NkT,

$$NkT = \frac{1}{3}Nmv^{2}$$

$$kT = \frac{1}{3}mv^{2}$$
(9.8)

Multiply the above equation by 3/2 on both sides,

$$\frac{3}{2}kT = \frac{1}{2}m\overline{v^2}$$
 (9.9)

R.H.S of the equation (9.9) is called average kinetic energy of a single molecule (\overline{KE}).

The average kinetic energy per molecule

$$\overline{KE} = \epsilon = \frac{3}{2} kT \tag{9.10}$$

Equation (9.9) implies that the temperature of a gas is a measure of the average translational kinetic energy per molecule of the gas.



definition of temperature studied in lower classes:

Temperature is the degree of hotness or coldness!

Equation 9.10 is a very important result from kinetic theory of gas. We can infer the following from this equation.

- •
- (i) The average kinetic energy of the molecule is directly proportional to absolute temperature of the gas. The equation (9.9) gives the connection between the macroscopic world (temperature) to microscopic world (motion of molecules).
- (ii) The average kinetic energy of each molecule depends only on temperature of the gas not on mass of the molecule. In other words, if the temperature of an ideal gas is measured using thermometer, the average kinetic energy of each molecule can be calculated without seeing the molecule through naked eye.

By multiplying the total number of gas molecules with average kinetic energy of each molecule, the internal energy of the gas is obtained.

Internal energy of ideal gas $U = N\left(\frac{1}{2}m\overline{v^2}\right)$ By using equation (9.9)

$$U = \frac{3}{2}NkT \tag{9.11}$$

From equation (9.11), we understand that the internal energy of an ideal gas depends only on absolute temperature and is independent of pressure and volume.

EXAMPLE 9.1

A football at 27°C has 0.5 mole of air molecules. Calculate the internal energy of air in the ball.

Solution

The internal energy of ideal gas = $\frac{3}{2} NkT$.

The number of air molecules is given in terms of number of moles so, rewrite the expression as follows



UNIT 9 KINETIC THEORY OF GASES

$$U = \frac{3}{2}\mu RT$$

Since $Nk = \mu R$. Here μ is number of moles.

Gas constant
$$R = 8.31 \frac{J}{molk}$$

Temperature T = 273+27=300K

$$U = \frac{3}{2} \times 0.5 \times 8.31 \times 300 = 1869.75J$$
This is approximately equivalent to the

This is approximately equivalent to the kinetic energy of a man of 57 kg running with a speed of 8 m s⁻¹.

9.2.3 Relation between pressure and mean kinetic energy

From earlier section, the internal energy of the gas is given by

$$U = \frac{3}{2}NkT$$

The above equation can also be written as

$$U = \frac{3}{2} PV$$

since PV = NkT

$$P = \frac{2}{3} \frac{U}{V} = \frac{2}{3} u \tag{9.12}$$

From the equation (9.12), we can state that the pressure of the gas is equal to two thirds of internal energy per unit volume or internal energy density $(u = \frac{U}{V})$.

Writing pressure in terms of mean kinetic energy density using equation (9.6)

$$P = \frac{1}{3}nm\overline{v^2} = \frac{1}{3}\rho\overline{v^2}$$
 (9.13)

where $\rho = nm = mass \ density$ (Note n is number density)

Multiply and divide R.H.S of equation (9.13) by 2, we get

$$P = \frac{2}{3} \left(\frac{\rho}{2} \overline{v^2} \right) \tag{9.14}$$

$$P = \frac{2}{3}\overline{KE}$$

9.2.4 Some elementary deductions from kinetic theory of gases

Boyle's law:

From equation (9.12), we know that $PV = \frac{2}{3}U$

But the internal energy of an ideal gas is equal to N times the average kinetic energy (\in) of each molecule.

$$U = N \in$$

For a fixed temperature, the average translational kinetic energy \in will remain constant. It implies that

$$PV = \frac{2}{3} N \in$$
 Thus $PV = constant$

Therefore, pressure of a given gas is inversely proportional to its volume provided the temperature remains constant. This is Boyle's law.

Charles' law:

From the equation (9.12), we get $PV = \frac{2}{3}U$

For a fixed pressure, the volume of the gas is proportional to internal energy of the gas or average kinetic energy of the gas and the average kinetic energy is directly proportional to absolute temperature. It implies that

$$V \propto T \text{ or } \frac{V}{T} = constant$$

This is Charles' law.

Avogadro's law:

This law states that at constant temperature and pressure, equal volumes of all gases contain the same number of molecules. For two different gases at the same temperature and pressure, according to kinetic theory of gases, From equation (9.6)

$$P = \frac{1}{3} \frac{N_1}{V} m_1 \overline{v_1^2} = \frac{1}{3} \frac{N_2}{V} m_2 \overline{v_2^2}$$
 (9.15)

where $\overline{v_1^2}$ and $\overline{v_2^2}$ are the mean square speed for two gases and N_1 and N_2 are the number of gas molecules in two different gases.

At the same temperature, average kinetic energy per molecule is the same for two gases.

$$\frac{1}{2}m_{1}\overline{v_{1}^{2}} = \frac{1}{2}m_{2}\overline{v_{2}^{2}} \tag{9.16}$$

Dividing the equation (9.15) by (9.16) we get $N_1 = N_2$

This is Avogadro's law. It is sometimes referred to as Avogadro's hypothesis or Avogadro's Principle.

9.2.5 Root mean square speed (v_{rms})

Root mean square speed (v_{rms}) is defined as the square root of the mean of the square of speeds of all molecules. It is denoted by $v_{rms} = \sqrt{\overline{v^2}}$

Equation (9.8) can be re-written as,

mean square speed
$$\overline{v^2} = \frac{3kT}{m}$$
 (9.17)

root mean square speed,

$$v_{\rm rms} = \sqrt{\frac{3kT}{m}} = 1.73\sqrt{\frac{kT}{m}}$$
 (9.18)

From the equation (9.18) we infer the following

(i) rms speed is directly proportional to square root of the temperature and inversely proportional to square root of mass of the molecule. At a given temperature the molecules of lighter mass move faster on an average than the molecules with heavier masses.

nitrogen at the same temperature.

(ii) Increasing the temperature will increase the r.m.s speed of molecules

We can also write the $v_{\rm rms}$ in terms of gas constant R. Equation (9.18) can be rewritten as follows

$$v_{\rm rms} = \sqrt{\frac{3N_A kT}{N_A m}}$$
 Where N_A is Avogadro number.

Since $N_A k = R$ and $N_A m = M$ (molar mass)

The root mean square speed or r.m.s speed

$$v_{\rm rms} = \sqrt{\frac{3RT}{M}} \tag{9.19}$$

The equation (9.6) can also be written in terms of rms speed $P = \frac{1}{3} nmv_{rms}^2$

since
$$v_{rms}^2 = \overline{v^2}$$



Root mean square speed is not the same as average speed. Average speed is 0.92 times of r.m.s speed.

Impact of v_{rms} in nature:

1. Moon has no atmosphere.

The escape speed of gases on the surface of Moon is much less than the root mean square speeds of gases due to low gravity. Due to this all the gases escape from the surface of the Moon.

2. No hydrogen in Earth's atmosphere.

As the root mean square speed of hydrogen is much greater than that of nitrogen, it easily escapes from the earth's atmosphere.

In fact, the presence of nonreactive nitrogen instead of highly combustible hydrogen deters many disastrous consequences.



Unit 9 Kinetic theory of gases

EXAMPLE 9.2

A room contains oxygen and hydrogen molecules in the ratio 3:1. The temperature of the room is 27°C. The molar mass of 0_2 is 32 g mol⁻¹ and of H_2 is 2 g mol⁻¹. The value of gas constant R is 8.32 J mol⁻¹ K⁻¹

Calculate

- (a) rms speed of oxygen and hydrogen molecule
- (b) Average kinetic energy per oxygen molecule and per hydrogen molecule
- (c) Ratio of average kinetic energy of oxygen molecules and hydrogen molecules

Solution

(a) Absolute Temperature $T=27^{\circ}C=27+273=300 \text{ K}.$

Gas constant R=8.32 J $mol^{-1} k^{-1}$

For Oxygen molecule: Molar mass $M=32 g=32 \times 10^{-3} \text{ kg mol}^{-1}$

rms speed
$$v_{rms} = \sqrt{\frac{3RT}{M}} = \sqrt{\frac{3 \times 8.32 \times 300}{32 \times 10^{-3}}}$$

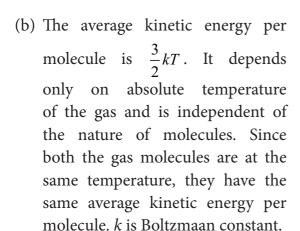
= 483.73 m s⁻¹ \approx 484 m s⁻¹

For Hydrogen molecule:

Molar mass M = 2 × 10⁻³ kg mol⁻¹
rms speed
$$v_{rms} = \sqrt{\frac{3RT}{M}} = \sqrt{\frac{3 \times 8.32 \times 300}{2 \times 10^{-3}}}$$

$$= 1934 \, m \, s^{-1} = 1.93 \, k \, m \, s^{-1}$$

Note that the rms speed is inversely proportional to \sqrt{M} and the molar mass of oxygen is 16 times higher than molar mass of hydrogen. It implies that the rms speed of hydrogen is 4 times greater than rms speed of oxygen at the same temperature. 1934



$$\frac{3}{2}kT = \frac{3}{2} \times 1.38 \times 10^{-23} \times 300 = 6.21 \times 10^{-21} J$$

(c) Average kinetic energy of total oxygen molecules = $\frac{3}{2}N_0kT$ where N_0 - number of oxygen molecules in the room

Average kinetic energy of total hydrogen molecules = $\frac{3}{2} N_H kT$ where N_H - number of hydrogen molecules in the room.

It is given that the number of oxygen molecules is 3 times more than number of hydrogen molecules in the room. So the ratio of average kinetic energy of oxygen molecules with average kinetic energy of hydrogen molecules is 3:1.

9.2.6 Mean (or) average speed (\overline{v})

It is defined as the mean (or) average of all the speeds of molecules

If $v_1, v_2, v_3, \dots, v_N$ are the individual speeds of molecules then

$$\overline{v} = \frac{v_1 + v_2 + v_3 \dots + v_n}{N} = \sqrt{\frac{8RT}{\pi M}} = \sqrt{\frac{8kT}{\pi m}}$$
 (9.20)

Here M- Molar Mass and m - mass of the molecule.

$$\overline{v} = 1.60\sqrt{\frac{kT}{m}} \tag{9.21}$$

9.2.7. Most probable speed

It is defined as the speed acquired by most of the molecules of the gas.

$$v_{mp} = \sqrt{\frac{2RT}{M}} = \sqrt{\frac{2kT}{m}} \tag{9.22}$$

$$v_{mp} = 1.41 \sqrt{\frac{kT}{m}} \tag{9.23}$$

The derivation of equations (9.20), (9.22) is beyond the scope of the book

Comparison of v_{rms} , \overline{v} and v_{mp}

Among the speeds $v_{\rm rms}$ is the largest and $v_{\rm mp}$ is the least

$$v_{\rm rms} > \overline{v} > v_{\rm mp}$$

Ratio-wise,

$$v_{\rm rms}$$
: \overline{v} : $v_{\rm mp} = \sqrt{3}$: $\sqrt{\frac{8}{\pi}}$: $\sqrt{2} = 1.732$: 1.6: 1.414

EXAMPLE 9.3

Ten particles are moving at the speed of 2, 3, 4, 5, 5, 5, 6, 6, 7 and 9 m s⁻¹. Calculate rms speed, average speed and most probable speed.

Solution

The average speed
$$\frac{1}{v} = \frac{2+3+4+5+5+5+6+6+7+9}{10} = 5.2 \, m \, s^{-1}$$

To find the rms speed, first calculate the mean square speed v^2

$$\frac{1}{v^2} = \frac{2^2 + 3^2 + 4^2 + 5^2 + 5^2 + 5^2 + 6^2 + 6^2 + 7^2 + 9^2}{10}$$

 $=30.6 \, m^2 \, s^{-2}$

The rms speed

$$v_{rms} = \sqrt{\overline{v^2}} = \sqrt{30.6} = 5.53 \, \text{m s}^{-1}$$

The most probable speed is 5 m s⁻¹ because three of the particles have that speed.



Calculate the rms speed, average speed and the most probable speed of 1 mole of hydrogen molecules at 300 K. Neglect the mass of electron.

Solution

The hydrogen atom has one proton and one electron. The mass of electron is negligible compared to the mass of proton.

Mass of one proton = $1.67 \times 10^{-27} kg$.

One hydrogen molecule = 2 hydrogen atoms = $2 \times 1.67 \times 10^{-27} kg$.

The average speed

$$\overline{v} = \sqrt{\frac{8kT}{\pi m}} = 1.60\sqrt{\frac{kT}{m}} =$$

$$= 1.60\sqrt{\frac{(1.38 \times 10^{-23}) \times (300)}{2(1.67 \times 10^{-27})}} = 1.78 \times 10^{3} \, ms^{-1}$$

(Boltzmann Constant k = $1.38 \times 10^{-23} J K^{-1}$)

The rms speed
$$v_{rms} = \sqrt{\frac{3kT}{m}} = 1.73\sqrt{\frac{kT}{m}}$$

= 1.73 $\sqrt{\frac{(1.38 \times 10^{-23}) \times (300)}{2(1.67 \times 10^{-27})}} = 1.93 \times 10^{3} \, m \, s^{-1}$
Most probable speed $v_{mp} = \sqrt{\frac{2kT}{m}} = 1.41\sqrt{\frac{kT}{m}}$
= 1.41 $\sqrt{\frac{(1.38 \times 10^{-23}) \times (300)}{2(1.67 \times 10^{-27})}} = 1.57 \times 10^{3} \, m \, s^{-1}$

Note that $v_{\rm rms} > \overline{v} > v_{\rm mp}$

9.2.8 **Maxwell-Boltzmann** speed distribution function

In a classroom, the air molecules are moving in random directions. The speed of each molecule is not the same even though macroscopic parameters like temperature and pressure are fixed. Each molecule collides with every other molecule and they exchange their speed. In the previous section

172

UNIT 9 KINETIC THEORY OF GASES

we calculated the rms speed of each molecule and not the speed of each molecule which is rather difficult. In this scenario we can find the number of gas molecules that move with the speed of 5 m s⁻¹ to 10 m s⁻¹ or 10 m s⁻¹ to 15 m s⁻¹ etc. In general our interest is to find how many gas molecules have the range of speed from v to v + dv. This is given by Maxwell's speed distribution function.

$$N_{v} = 4\pi N \left(\frac{m}{2\pi kT}\right)^{\frac{3}{2}} v^{2} e^{-\frac{mv^{2}}{2kT}}$$
 (9.24)

The above expression is graphically shown as follows

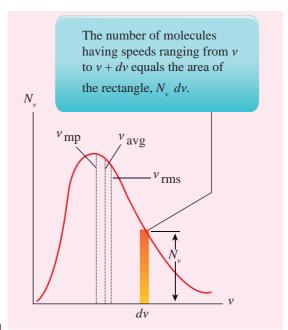


Figure 9.3 Maxwell's molecular speed distribution

From the Figure 9.3, it is clear that, for a given temperature the number of molecules having lower speed increases parabolically

 (v^2) but decreases exponentially $(e^{-\frac{1}{2kT}})$ after reaching most probable speed. The rms speed, average speed and most probable speed are indicated in the Figure 9.3. It can be seen that the rms speed is greatest among the three.

need to integrate
$$\int_{50}^{60} 4\pi N \left(\frac{m}{2\pi kT}\right)^{\frac{3}{2}} v^2 e^{-\frac{mv^2}{2kT}} dv =$$

= $N(50 to 60 ms^{-1})$. In general the number of molecules within the range of speed v and v+dv is given by

$$\int_{v}^{v+dv} 4\pi N \left(\frac{m}{2\pi kT}\right)^{\frac{3}{2}} v^{2} e^{-\frac{mv^{2}}{2kT}} dv = N(v \text{ to } v + dv).$$

The exact integration is beyond the scope of the book. But we can infer the behavior of gas molecules from the graph.

- (i) The area under the graph will give the total number of gas molecules in the system
- (ii) Figure 9.4 shows the speed distribution graph for two different temperatures. As temperature increases, the peak of the curve is shifted to the right. It implies that the average speed of each molecule will increase. But the area under each graph is same since it represents the total number of gas molecules.



Interestingly once the gas molecule attains equilibrium, the number of molecules in the given range

of speeds are fixed. For example if a molecule initially moving with speed 12 m s⁻¹, collides with some other molecule and changes its speed to 9 m s⁻¹, then the other molecule initially moving with different speed reaches the speed 12 m s⁻¹ due to another collision. So in general once the gas molecules attain equilibrium, the number of molecules that lie in the grange of v to v+dv is always fixed.

9.3

DEGREES OF FREEDOM

9.3.1 Definition

The minimum number of independent coordinates needed to specify the position and configuration of a thermo-dynamical system in space is called the degree of freedom of the system.



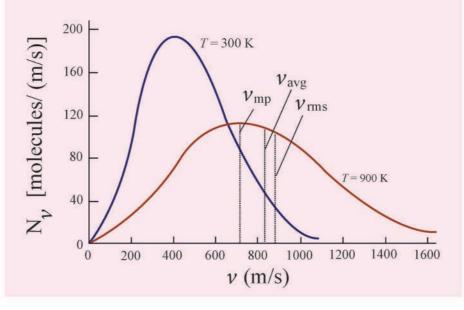


Figure 9.4 Maxwell distribution graph for two different temperatures



- 1. A free particle moving along x-axis needs only one coordinate to specify it completely. So its degree of freedom is one.
- 2. Similarly a particle moving over a plane has two degrees of freedom.
- 3. A particle moving in space has three degrees of freedom.

Suppose if we have N number of gas molecules in the container, then the total number of degrees of freedom is f = 3N.

But, if the system has q number of constraints (restrictions in motion) then the degrees of freedom decreases and it is equal to f = 3N-q where N is the number of particles.

9.3.2 Monoatomic molecule

A monoatomic molecule by virtue of its nature has only three translational degrees of freedom.

Therefore f = 3

Example: Helium, Neon, Argon

9.3.3 Diatomic molecule

There are two cases.

1. At Normal temperature

A molecule of a diatomic gas consists of two atoms bound to each other by a force of attraction. Physically the molecule can be regarded as a system of two point masses fixed at the ends of a massless elastic spring.

The center of mass lies in the center of the diatomic molecule. So, the motion of the center of mass requires three translational degrees of freedom (figure 9.5 a). In addition, the diatomic molecule can rotate

UNIT 9 KINETIC THEORY OF GASES

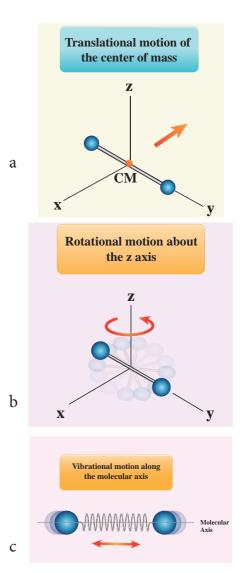


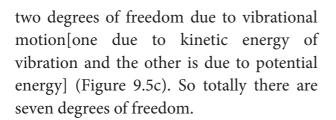
Figure 9.5 Degree of freedom of diatomic molecule

about three mutually perpendicular axes (figure 9.5 b). But the moment of inertia about its own axis of rotation is negligible (about y axis in the figure 9.5). Therefore, it has only two rotational degrees of freedom (one rotation is about Z axis and another rotation is about X axis). Therefore totally there are five degrees of freedom.

$$f = 5$$

2. At High Temperature

At a very high temperature such as 5000 K, the diatomic molecules possess additional



$$f = 7$$

Examples: Hydrogen, Nitrogen, Oxygen.

9.3.4 Triatomic molecules

There are two cases.

Linear triatomic molecule

In this type, two atoms lie on either side of the central atom as shown in the Figure 9.6

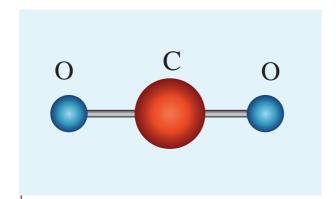


Figure 9.6 A linear triatomic molecule.

Linear triatomic molecule has three translational degrees of freedom. It has two rotational degrees of freedom because it is similar to diatomic molecule except there is an additional atom at the center. At normal temperature, linear triatomic molecule will have five degrees of freedom. At high temperature it has two additional vibrational degrees of freedom. So a linear triatomic molecule has seven degrees of freedom.

Example: Carbon dioxide.

Non-linear triatomic molecule

In this case, the three atoms lie at the vertices of a triangle as shown in the Figure 9.7

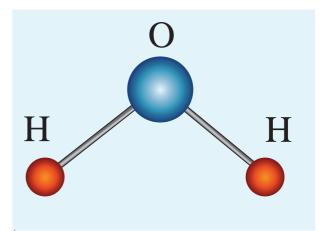


Figure 9.7 A non-linear triatomic molecule

It has three translational degrees of freedom and three rotational degrees of freedom about three mutually orthogonal axes. The total degrees of freedom, f = 6

Example: Water, Sulphurdioxide.

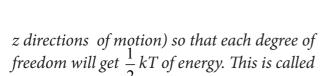
9.4

LAW OF EQUIPARTITION OF ENERGY

We have seen in Section 9.2.1 that the average kinetic energy of a molecule moving in x direction is $\frac{1}{2}m\overline{v_x^2} = \frac{1}{2}kT$.

Similarly, when the motion is in y direction, $\frac{1}{2}m\overline{v_y^2} = \frac{1}{2}kT$ and for the motion along z direction, $\frac{1}{2}m\overline{v_z^2} = \frac{1}{2}kT$.

According to kinetic theory, the average kinetic energy of system of molecules in thermal equilibrium at temperature T is uniformly distributed to all degrees of freedom (x or y or



law of equipartition of energy.

Average kinetic energy of a monatomic molecule (with f=3) = $3 \times \frac{1}{2}kT = \frac{3}{2}kT$

Average kinetic energy of diatomic molecule at low temperature (with f = 5)

$$= 5 \times \frac{1}{2}kT = \frac{5}{2}kT$$

Average kinetic energy of a diatomic molecule at high temperature (with f=7)

$$=7 \times \frac{1}{2}kT = \frac{7}{2}kT$$

Average kinetic energy of linear triatomic molecule (with f = 7) = $7 \times \frac{1}{2}kT = \frac{7}{2}kT$

Average kinetic energy of nonlinear triatomic molecule (with f = 6) = $6 \times \frac{1}{2}kT = 3kT$

9.4.1 Application of law of equipartition energy in specific heat of a gas

Meyer's relation $C_P - C_V = R$ connects the two specific heats for one mole of an ideal gas.

Equipartition law of energy is used to calculate the value of $C_P - C_V$ and the ratio between them $\gamma = \frac{C_P}{C_V}$. Here γ is called adiabatic exponent.

i) Monatomic molecule

Average kinetic energy of a molecule

$$=\left[\frac{3}{2}kT\right]$$

Total energy of a mole of gas

$$= \frac{3}{2}kT \times N_A = \frac{3}{2}RT$$

176

UNIT 9 KINETIC THEORY OF GASES

For one mole, the molar specific heat at constant volume $C_V = \frac{dU}{dT} = \frac{d}{dT} \left[\frac{3}{2} RT \right]$

$$C_{V} = \left[\frac{3}{2}R\right]$$

$$C_P = C_V + R = \frac{3}{2}R + R = \frac{5}{2}R$$

The ratio of specific heats,

$$\gamma = \frac{C_P}{C_V} = \frac{\frac{5}{2}R}{\frac{3}{2}R} = \frac{5}{3} = 1.67$$

ii) Diatomic molecule

Average kinetic energy of a diatomic molecule at low temperature = $\frac{5}{2}kT$

Total energy of one mole of gas

$$= \frac{5}{2}kT \times N_A = \frac{5}{2}RT$$

(Here, the total energy is purely kinetic)

For one mole Specific heat at constant volume

$$C_V = \frac{dU}{dT} = \left[\frac{5}{2}RT\right] = \frac{5}{2}R$$

But
$$C_P = C_V + R = \frac{5}{2}R + R = \frac{7}{2}R$$

$$\therefore \gamma = \frac{C_P}{C_V} = \frac{\frac{7}{2}R}{\frac{5}{2}R} = \frac{7}{5} = 1.40$$

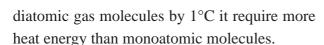
Energy of a diatomic molecule at high temperature is equal to $\frac{7}{2}RT$

$$C_{V} = \frac{dU}{dT} = \left[\frac{7}{2}RT\right] = \frac{7}{2}R$$

$$\therefore C_{P} = C_{V} + R = \frac{7}{2}R + R$$

$$C_{P} = \frac{9}{2}R$$

Note that the C_V and C_P are higher for diatomic molecules than the mono atomic molecules. It implies that to increase the temperature of



$$\therefore \gamma = \frac{C_p}{C_V} = \frac{\frac{9}{2}R}{\frac{7}{2}R} = \frac{9}{7} = 1.28$$

iii) Triatomic molecule

a) Linear molecule

Energy of one mole= $\frac{7}{2}kT \times N_A = \frac{7}{2}RT$

$$C_{V} = \frac{dU}{dT} = \frac{d}{dT} \left[\frac{7}{2}RT \right]$$

$$C_{V} = \frac{7}{2}R$$

$$C_{P} = C_{V} + R = \frac{7}{2}R + R = \frac{9R}{2}$$

$$\therefore \gamma = \frac{C_{P}}{C_{V}} = \frac{\frac{9}{2}R}{\frac{7}{2}R} = \frac{9}{7} = 1.28$$

b) Non-linear molecule

Energy of a mole = $\frac{6}{2}kT \times N_A = \frac{6}{2}RT = 3RT$

$$C_V = \frac{dU}{dT} = 3R$$

$$C_P = C_V + R = 3R + R = 4R$$

$$\therefore \gamma = \frac{C_P}{C_V} = \frac{4R}{3R} = \frac{4}{3} = 1.33$$

Note that according to kinetic theory model of gases the specific heat capacity at constant volume and constant pressure are independent of temperature. But in reality it is not sure. The specific heat capacity varies with the temperature.

EXAMPLE 9.5

Find the adiabatic exponent γ for mixture of μ_1 moles of monoatomic gas and μ_2 moles of a diatomic gas at normal temperature (27°C).

Solution

The specific heat of one mole of a monoatomic gas $C_V = \frac{3}{2} R$

For
$$\mu_1$$
 mole, $C_V = \frac{3}{2} \mu_1 R$ $C_P = \frac{5}{2} \mu_1 R$

The specific heat of one mole of a diatomic gas

$$C_V = \frac{5}{2} R$$

For μ_2 mole, $C_V = \frac{5}{2} \mu_2 R$ $C_P = \frac{7}{2} \mu_2 R$

The specific heat of the mixture at constant

volume
$$C_V = \frac{3}{2} \ \mu_1 R + \frac{5}{2} \ \mu_2 R$$

The specific heat of the mixture at constant

pressure
$$C_p = \frac{5}{2} \mu_1 R + \frac{7}{2} \mu_2 R$$

The adiabatic exponent $\gamma = \frac{C_p}{C_V} = \frac{5\mu_1 + 7\mu_2}{3\mu_1 + 5\mu_2}$

9.5

MEAN FREE PATH

Usually the average speed of gas molecules is several hundred meters per second even at room temperature (27°C). Odour from an open perfume bottle takes some time to reach us even if we are closer to the room. The time delay is because the odour of the molecules cannot travel straight to us as it undergoes a lot of collisions with the nearby air molecules and moves in a zigzag path. This average distance travelled by the molecule between two successive collisions is called mean free path (λ) . We can calculate the mean free path based on kinetic theory.

Expression for mean free path

We know from postulates of kinetic theory that the molecules of a gas are in random motion and they collide with each other. Between two successive collisions, a molecule

velocity. This path is called mean free path.

Consider a system of molecules each with diameter d. Let n be the number of molecules per unit volume.

Assume that only one molecule is in motion and all others are at rest as shown in the Figure 9.8

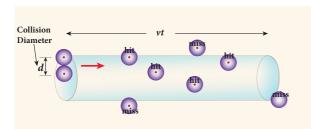


Figure 9.8 Mean free path

If a molecule moves with average speed v in a time t, the distance travelled is vt. In this time t, consider the molecule to move in an imaginary cylinder of volume πd^2vt . It collides with any molecule whose center is within this cylinder. Therefore, the number of collisions is equal to the number of molecules in the volume of the imaginary cylinder. It is equal to πd^2vtn . The total path length divided by the number of collisions in time t is the mean free path.

Mean free path, $\lambda = \frac{distance\ travelled}{Number\ of\ collisions}$

$$\lambda = \frac{vt}{n\pi d^2 vt} = \frac{1}{n\pi d^2} \tag{9.25}$$

Though we have assumed that only one molecule is moving at a time and other molecules are at rest, in actual practice all the molecules are in random motion. So the average relative speed of one molecule with respect to other molecules has to be taken into account. After some detailed calculations (you will learn in higher classes) the correct expression for mean free path



UNIT 9 KINETIC THEORY OF GASES

$$\lambda = \frac{1}{\sqrt{2}n\pi d^2} \tag{9.26}$$

The equation (9.26) implies that the mean free path is inversely proportional to number density. When the number density increases the molecular collisions increases so it decreases the distance travelled by the molecule before collisions.

Case1: Rearranging the equation (9.26) using 'm' (mass of the molecule)

$$\therefore \lambda = \frac{m}{\sqrt{2}\pi d^2 mn}$$

But mn=mass per unit volume = ρ (density of the gas)

$$\therefore \lambda = \frac{m}{\sqrt{2} \pi d^2 \rho} \tag{9.27}$$

Also we know that PV = NkT

$$P = \frac{N}{V}kT = nkT$$

$$\therefore n = \frac{P}{kT}$$

Substituting n= $\frac{P}{kT}$ in equation (9.26), we get

$$\lambda = \frac{kT}{\sqrt{2\pi}d^2P} \tag{9.28}$$

The equation (9.28) implies the following

- 1. Mean free path increases with increasing temperature. As the temperature increases, the average speed of each molecule will increase. It is the reason why the smell of hot sizzling food reaches several meter away than smell of cold food.
- 2. Mean free path increases with decreasing pressure of the gas and diameter of the gas molecules.



An oxygen molecule is travelling in air at 300 K and 1 atm, and the diameter of oxygen molecule is $1.2 \times 10^{-10} m$. Calculate the mean free path of oxygen molecule.

Solution

From (9.26)
$$\lambda = \frac{1}{\sqrt{2\pi nd^2}}$$

We have to find the number density *n* By using ideal gas law

$$n = \frac{N}{V} = \frac{P}{kT} = \frac{101.3 \times 10^3}{1.381 \times 10^{-23} \times 300}$$

 $=2.449\times10^{25}$ molecues/m³

$$\lambda = \frac{1}{\sqrt{2} \times \pi \times 2.449 \times 10^{25} \times (1.2 \times 10^{-10})^2}$$

$$=\frac{1}{15.65\times10^5}$$

$$\lambda = 0.63 \times 10^{-6} m$$



9.6

BROWNIAN MOTION

In 1827, Robert Brown, a botanist reported that grains of pollen suspended in a liquid moves randomly from one place to other. The random (Zig - Zag path) motion of pollen suspended in a liquid is called Brownian motion. In fact we can observe the dust particle in water moving in random directions. This discovery puzzled scientists for long time. There were a lot of explanations for pollen or dust to move in random directions but none of these explanations were found adequate. After a systematic study, Wiener and Gouy

proposed that Brownian motion is due to the bombardment of suspended particles by molecules of the surrounding fluid. But during 19th century people did not accept that every matter is made up of small atoms or molecules. In the year 1905, Einstein gave systematic theory of Brownian motion based on kinetic theory and he deduced the average size of molecules.

According to kinetic theory, any particle suspended in a liquid or gas is continuously bombarded from all the directions so that the mean free path is almost negligible. This leads to the motion of the particles in a random and zig-zag manner as shown in Figure 9.9. But when we put our hand in water it causes no random motion because the mass of our hand is so large that the momentum transferred by the molecular collision is not enough to move our hand.

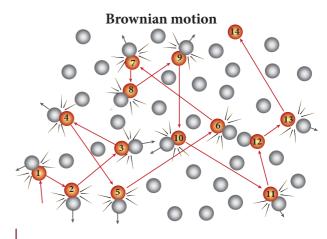


Figure 9.9 Particles in Brownian motion

Factors affecting Brownian Motion

- 1. Brownian motion increases with increasing temperature.
- 2. Brownian motion decreases with bigger particle size, high viscosity and density of the liquid (or) gas.



The experimental verification on Einstein's theoretical explanation of Brownian motion was done by Jean Perrin in the year 1908. The Einstein's explanation on Brownian motion and Perrin experiment was of great importance in physics because it provided direct evidence of reality of atoms and molecules.

SUMMARY

- Kinetic theory explains the microscopic origin of macroscopic parameters like temperature, pressure.
- The pressure exerted on the walls of gas container is due to the momentum imparted by the gas molecules on the walls.
- The pressure $P = \frac{1}{3}nm\overline{v^2}$. The pressure is directly proportional to the number density, mass of molecule and mean square speed.
- The temperature of a gas is a measure of the average translational kinetic energy per molecule of the gas. The average kinetic energy per molecule is directly proportional to absolute temperature of gas and independent of nature of molecules.
- The pressure is also equal to 2/3 of internal energy per unit volume.
- The rms speed of gas molecules = $v_{rms} = \sqrt{\frac{3kT}{m}} = 1.73 \sqrt{\frac{kT}{m}}$
- The average speed of gas molecules $\bar{v} = \sqrt{\frac{8kT}{\pi m}} = 1.60 \sqrt{\frac{kT}{m}}$
- The most probable speed of gas molecules $v_{mp} = \sqrt{\frac{2kT}{m}} = 1.41 \sqrt{\frac{kT}{m}}$
- Among the speeds v_{rms} is the largest and v_{mp} is the least

$$v_{rms} > \overline{v} > v_{mt}$$

 $v_{rms} > \overline{v} > v_{mp}$ The number of gas molecules in the range of speed v to v+dv is given by Maxwell-Boltzmann distribution

$$N_{\nu} d\nu = 4\pi N \left(\frac{m}{2\pi kT}\right)^{\frac{3}{2}} \nu^{2} e^{-\frac{m\nu^{2}}{2kT}} d\nu$$

- The minimum number of independent coordinates needed to specify the position and configuration of a thermodynamical system in space is called the degrees of freedom of the system. If a sample of gas has N molecules, then the total degrees of freedom f = 3N. If there are q number of constraints then total degrees of freedom f = 3N-q.
- For a monoatomic molecule, f = 3

For a diatomic molecule (at normal temperature), f = 5



For a diatomic molecule (at high temperature), f = 7

For a triatomic molecule (linear type), f = 7

For a triatomic molecule (non-linear type), f = 6

- The average kinetic energy of sample of gas is equally distributed to all the degrees of freedom. It is called law of equipartition of energy. Each degree of freedom will get $\frac{1}{2}kT$ energy.
- The ratio of molar specific heat at constant pressure and constant volume of a gas

$$\left[\gamma = \frac{C_p}{C_v}\right]$$

For

Monoatomic molecule: 1.67

Diatomic molecule (Normal temperature): 1.40

Diatomic molecule (High temperature): 1.28

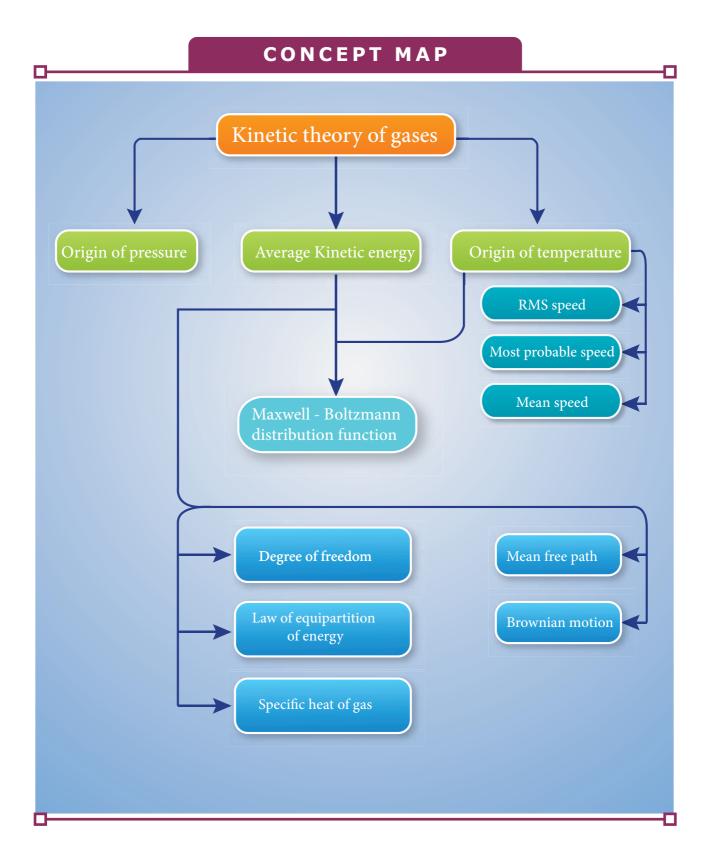
Triatomic molecule (Linear type): 1.28.

Triatomic molecule (Non-linear type): 1.33

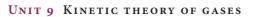
- The mean free path $\lambda = \frac{kT}{\sqrt{2\pi}d^2P}$. The mean free path is directly proportional to temperature and inversely proportional to size of the molecule and pressure of the molecule
- The Brownian motion explained by Albert Einstein is based on kinetic theory. It proves the reality of atoms and molecules.







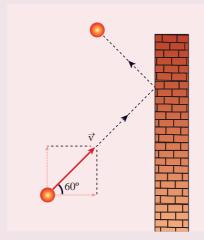






I. Multiple choice questions

1. A particle of mass m is moving with speed u in a direction which makes 60° with respect to x axis. It undergoes elastic collision with the wall. What is the change in momentum in x and y direction?



- (a) $\Delta p_x = -mu$, $\Delta p_y = 0$
- (b) $\Delta p_x = -2mu$, $\Delta p_y = 0$
- (c) $\Delta p_x = 0$, $\Delta p_y = mu$
- (d) $\Delta p_x = mu$, $\Delta p_y = 0$
- **2.** A sample of ideal gas is at equilibrium. Which of the following quantity is zero?
 - (a) rms speed
 - (b) average speed
 - (c) average velocity
 - (d) most probable speed
- 3. An ideal gas is maintained at constant pressure. If the temperature of an ideal gas increases from 100K to 10000K then the rms speed of the gas molecules
 - (a) increases by 5 times
 - (b) increases by 10 times
 - (c) remains same
 - (d) increases by 7 times

- **4.** Two identically sized rooms A and B are connected by an open door. If the room A is air conditioned such that its temperature is 4°C lesser than room B, which room has more air in it?
 - (a) Room A
 - (b) Room B
 - (c) Both room has same air
 - (d) Cannot be determined
- **5.** The average translational kinetic energy of gas molecules depends on
 - (a) number of moles and T
 - (b) only on T
 - (c) P and T
 - (d) P only
- **6.** If the internal energy of an ideal gas U and volume V are doubled then the pressure
 - (a) doubles
 - (b) remains same
 - (c) halves
 - (d) quadruples
- 7. The ratio $\gamma = \frac{C_p}{C_v}$ for a gas mixture consisting of 8 g of helium and 16 g of oxygen is (Physics Olympiad -2005)
 - (a) 23/15
 - (b) 15/23
 - (c) 27/17
 - (d) 17/27



8. A container has one mole of monoatomic ideal gas. Each molecule has f degrees of freedom. What is the ratio of $\gamma = \frac{C_p}{C_v}$

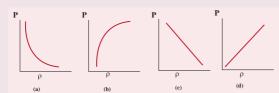


(b)
$$\frac{f}{2}$$

(c)
$$\frac{f}{f+2}$$

(b)
$$\frac{f}{2}$$
(d) $\frac{f+2}{f}$

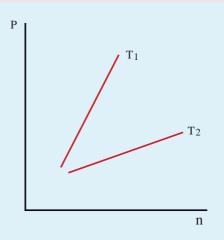
- 9. If the temperature and pressure of a gas is doubled the mean free path of the gas molecules
 - (a) remains same
 - (b) doubled
 - (c) tripled
 - (d) quadrapoled
- 10. Which of the following shows the correct relationship between pressure and density of an ideal gas at constant temperature?



- 11. A sample of gas consists of μ_1 moles of monoatomic molecules, μ_2 moles of diatomic molecules and μ_3 moles of linear triatomic molecules. The gas is kept at high temperature. What is the total number of degrees of freedom?
 - (a) $[3\mu_1 + 7(\mu_2 + \mu_3)] N_A$
 - (b) $[3\mu_1 + 7 \mu_2 + 6\mu_3] N_A$
 - (c) $[7\mu_1 + 3(\mu_2 + \mu_3)] N_A$
 - (d) $[3\mu_1 + 6(\mu_2 + \mu_3)] N_A$
- 12. If s_p and s_v denote the specific heats of nitrogen gas per unit mass at constant pressure and constant volume respectively, then (JEE 2007)
 - (a) $s_p s_v = 28R$
 - (b) $s_p s_v = R/28$
 - (c) $s_p s_v = R/14$
 - (d) $s_p s_v = R$

- 13. Which of the following gases will have least rms speed at a given temperature?
 - (a) Hydrogen
 - (b) Nitrogen
 - (c) Oxygen
 - (d) Carbon dioxide
- 14. For a given gas molecule at a fixed temperature, the area under Maxwell-Boltzmann distribution curve is equal to
 - (a) $\frac{PV}{kT}$

- (b) $\frac{kT}{PV}$
- (c) $\frac{P}{NkT}$
- (d) PV
- 15. The following graph represents the pressure versus number density for ideal gas at two different temperatures T_1 and T_2 . The graph implies



- (a) $T_1 = T_2$
- (b) $T_1 > T_2$
- (c) $T_1 < T_2$
- d) Cannot be determined

Answers:

- 1) a 2) c
- 3) b
- 4) a

- 5) a
- 6) b
- 7) c
- 8) d

17-08-2020 16:22:02

- 9) a
- 10) d
- 11) a
- 12) b

- 13) d
- 14) a
- 15) b



- **1.** What is the microscopic origin of pressure?
- **2.** What is the microscopic origin of temperature?
- 3. Why moon has no atmosphere?
- **4.** Write the expression for rms speed, average speed and most probable speed of a gas molecule.
- **5.** What is the relation between the average kinetic energy and pressure?
- **6.** Define the term degrees of freedom.
- 7. State the law of equipartition of energy.
- **8.** Define mean free path and write down its expression.
- **9.** Deduce Charles' law based on kinetic theory.
- **10.** Deduce Boyle's law based on kinetic theory.
- **11.** Deduce Avogadro's law based on kinetic theory.
- **12.** List the factors affecting the mean free path.
- **13.** What is the reason for Brownian motion?

III. Long answer questions

- **1.** Write down the postulates of kinetic theory of gases.
- **2.** Derive the expression of pressure exerted by the gas on the walls of the container.
- **3.** Explain in detail the kinetic interpretation of temperature.
- **4.** Describe the total degrees of freedom for monoatomic molecule, diatomic molecule and triatomic molecule.

- **5.** Derive the ratio of two specific heat capacities of monoatomic, diatomic and triatomic molecules
- **6.** Explain in detail the Maxwell Boltzmann distribution function.
- 7. Derive the expression for mean free path of the gas.
- **8.** Describe the Brownian motion.

IV Numerical Problems

1. A fresh air is composed of nitrogen $N_2(78\%)$ and oxygen $O_2(21\%)$. Find the rms speed of N_2 and O_2 at 20°C.

Ans: For
$$N_2$$
, $v_{\text{rms}} = 511 \text{ m s}^{-1}$
For O_2 , $v_{\text{rms}} = 478 \text{ m s}^{-1}$

2. If the rms speed of methane gas in the Jupiter's atmosphere is 471.8 m s⁻¹, show that the surface temperature of Jupiter is sub-zero.

3. Calculate the temperature at which the rms velocity of a gas triples its value at S.T.P. (standard temperature $T_1 = 273 \text{ K}$)

Ans:
$$T_2 = 2457 \text{ K}$$

4. A gas is at temperature 80°C and pressure $5 \times 10^{-10} N \, m^{-2}$. What is the number of molecules per m³ if Boltzmann's constant is $1.38 \times 10^{-23} \, J \, K^{-1}$

Ans:
$$1.02 \times 10^{11}$$

5. If 10^{20} oxygen molecules per second strike 4 cm² of wall at an angle of 30° with the normal when moving at a speed of 2×10^3 m s⁻¹, find the pressure exerted on the wall. (mass of one oxygen atom = 2.67×10^{-26} kg)

6. During an adiabatic process, the pressure of a mixture of monatomic and diatomic gases is found to be



proportional to the cube of the temperature. Find the value of $\gamma = (C_p/C_V)$

Ans: 3/2

7. Calculate the mean free path of air molecules at STP. The diameter of N_2 and O_2 is about $3 \times 10^{-10} \, m$

Ans: $\lambda \approx 9.3 \times 10^{-8} m$

8. A gas made of a mixture of 2 moles of oxygen and 4 moles of argon at temperature T. Calculate the energy of the gas in terms of RT. Neglect the vibrational modes.

Ans: 11RT

9. Estimate the total number of air molecules in a room of capacity 25 m³ at a temperature of 27°C.

Ans: 6.1×10^{26} molecules

BOOKS FOR REFERENCE

- 1. Serway and Jewett, Physics for scientist and Engineers with modern physics, Brook/Coole publishers, Eighth edition
- 2. Paul Tipler and Gene Mosca, Physics for scientist and engineers with modern physics, Sixth edition, W.H.Freeman and Company
- 3. H.C.Verma, Concepts of physics -Volume 2, Bharati Bhawan Publishers
- 4. Douglas C. Giancoli, Physics for scientist & Engineers, Pearson Publications, Fourth Edition
- 5. James Walker, Physics, Addison Wesley, Fourth Edition



UNIT-9(XI-Physics_Vol-2).indd 186 17-08-2020 16:22:02





ICT CORNER

Kinetic Theory of Gases

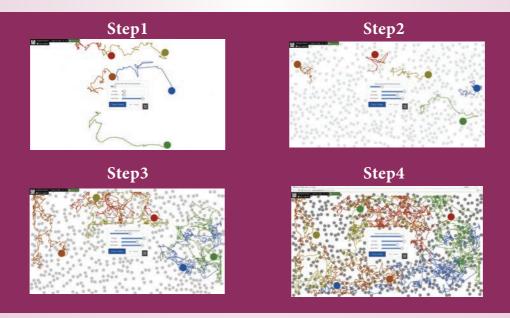


Through this activity you will be able to learn about the Brownian motion of the particles.



STEPS:

- Use the URL or scan the QR code to open 'interactive' simulation on "Brownian motion".
- Observe the movement of particles (Big balls) suspended in the gas at the initial stage. Observe the molecules in the gas by dragging the first slider. 'Drag to see what's actually going on'
- Find the variants such as "Energy", "Size Ratio" and "Mass Ratio" below the first slider. These variants can be lowered or increased.
- By dragging to the appropriate values of the variants, Brownian motion of the particles shall be observed.



URL:

http://labs.minutelabs.io/Brownian-Motion/

- * Pictures are indicative only.
- * If browser requires, allow **Flash Player** or **Java Script** to load the page.



Unit 9 Kinetic theory of gases



