

## Short Answer Type Questions – II

**Q.1. A cannot heat engine whose sink is at 200 K, has an efficiency 30%. By how much the temperature of the source be increased to have its efficiency equal to 50%. Keeping sink temperature constant.**

**Ans.** From the relation

$$\eta = 1 - \frac{T_2}{T_1}$$

or  $\frac{T_2}{T_1} = 1 - \frac{30}{100} = \frac{7}{10}$

or  $T_1 = \frac{10T_2}{7} = \frac{10 \times 200}{7} = 285.71 \text{ K}$

new efficiency is now 50%

$$\eta' = 1 - \frac{T_2}{T_1}$$

$$\frac{T_2}{T_1} = 1 - \eta'$$

$$\frac{T_2}{T_1} = 1 - \frac{50}{100} \text{ or } \frac{1}{2}$$

$$2T_2 = T_1$$

or  $T_1 = 2 \times 200 \text{ K}$

$$T_1 = 400 \text{ K}$$

Now increase in temperature of source

$$= 400 \text{ K} - 285.71 \text{ K}$$

$$= 114.3 \text{ K}$$

**Q.2. A refrigerator has to transfer an average of 263 J of heat per second from temperature  $-10^\circ\text{C}$  to  $25^\circ\text{C}$ . Calculate the average ideal reversible cycle and no other losses.**

**Ans.** Given:  $T_2 = 25 + 273 = 298 \text{ K}$

$$T_1 = -10 + 273 = 263 \text{ K}$$

From relation

$$\frac{Q_2}{Q_1} = \frac{T_2}{T_1}$$

Or  $Q_1 = \frac{T_2}{T_1} \times Q_2 = \frac{298}{263} \times 263$   
 $= 298 \text{ Js}^{-1}$

$$\begin{aligned}
 \therefore \text{Average power consumed} &= Q_1 - Q_2 \\
 &= (298 - 263) \text{ Js}^{-1} \\
 &= 35 \text{ W.}
 \end{aligned}$$

**Q.3. Assuming the domestic refrigerator as reversible engine working between melting point of ice and the room temperature of 27°C, calculate the energy in Joule that must be supplied to freeze one kg of water. (Given melting point of ice = 0°C L = 80 cal g<sup>-1</sup>)**

**Ans. Given:**  $T_1 = 27 + 273 = 300 \text{ K}$

$$T_2 = 0 + 273 = 273 \text{ K}$$

$$m = 1 \text{ kg} = 1000 \text{ g}; L = 80 \text{ cal g}^{-1}$$

Heat to be removed,

$$\begin{aligned}
 Q_2 &= mL \\
 &= 1000 \times 80 \text{ cal} \\
 &= 8 \times 10^4 \text{ cal}
 \end{aligned}$$

From the relation

$$\begin{aligned}
 \frac{Q_1}{Q_2} &= \frac{T_1}{T_2}, \\
 Q_1 &= \frac{T_1}{T_2} \times Q_2 = \frac{300}{273} \times 8 \times 10^4 \\
 &= 87912.1 \text{ cal}
 \end{aligned}$$

Energy required to be supplied,

$$\begin{aligned}
 W &= Q_1 - Q_2 \\
 &= (87912.1 - 80,000) \text{ cal} \\
 &= 7912.1 \text{ cal} = 7912.1 \times 4.2 \text{ J} \\
 &= 33230.8 \text{ J}
 \end{aligned}$$