V	ecto	ors	9
			_

			(c) 4	(d) 5
G Ordina	ary Thinking	10.	A hall has the dimensions corner ends up at a dian magnitude of its displaceme	$10 m \times 12 m \times 14 m$. A fly starting at metrically opposite corner. What is ent
	Objective Questions		(a) 17 <i>m</i>	(b) 26 <i>m</i>
Fundamental	s of Vectors		(c) 36 <i>m</i>	(d) 20 <i>m</i>
The vector projection of a vecto	or $3\hat{i} + 4\hat{k}$ on <i>y</i> -axis is [RPMT 2004]	11.	100 coplanar forces each α makes angle $\pi/50$ with the forces	equal to 10 N act on a body. Each t he preceding force. What is the resu
(a) 5	(b) 4		(a) 1000 N	(b) 500 <i>N</i>
(c) 3	(d) Zero		(c) 250 N	(d) Zero
Position of a particle in a recta Then its position vector will be	ngular-co-ordinate system is (3, 2, 5).	12.	The magnitude of a given (2, - 2, 0) must be	vector with end points $(4, -4, 0)$ and
(a) $3i + 5j + 2k$	(b) $3i + 2j + 5k$		(a) 6	(b) $5\sqrt{2}$
(c) $\hat{5i} + \hat{3j} + \hat{2k}$	(d) None of these		(c) 1	(d) $2\sqrt{10}$
If a particle moves from poin displacement vector be	nt P (2,3,5) to point Q (3,4,5). Its	13.	(c) 4 The expression $\left(\frac{1}{-1}\hat{i}+-\right)$	$\begin{pmatrix} \mathbf{u} \end{pmatrix} = 2\mathbf{v}\mathbf{r}\mathbf{u}$
(a) $\hat{i} + \hat{j} + 10\hat{k}$	(b) $\hat{i} + \hat{j} + 5\hat{k}$	-	$\sqrt{2}$	(2°)
(c) $\hat{i} + \hat{j}$	(d) $2\hat{i} + 4\hat{j} + 6\hat{k}$		(a) Unit vector	(b) Null vector
A force of 5 <i>N</i> acts on a particle 60° with vertical. Its vertical con	e along a direction making an angle of ponent be	14	(c) Vector of magnitude Given vector $\vec{A} = 2\hat{i} + 3\hat{i}$	$\sqrt{2}$ (d) Scalar the angle between $\overrightarrow{4}$ and wavis is
(a) 10 <i>N</i>	(b) 3 <i>N</i>	1-4-	Given vector $M = 2i + 5j$,	CPMT
(c) 4 <i>N</i>	(d) 2.5 N		(1) $\tan^{-1} 2/2$	(1) $\tan^{-1} 2/2$
If $A = 3\hat{i} + 4\hat{j}$ and $B = 7\hat{i}$ magnitude as <i>B</i> and parallel to	$i + 24\hat{j}$, the vector having the same A is		(a) $\tan \frac{3}{2}$ (c) $\sin^{-1} \frac{2}{3}$	(b) $\tan \frac{2}{3}$ (d) $\cos^{-1} \frac{2}{3}$
(a) $5\hat{i} + 20\hat{j}$	(b) $15\hat{i} + 10\hat{j}$	15.	The unit vector along $\hat{i} + \hat{j}$, is
(c) $20\hat{i} + 15\hat{j}$	(d) $15\hat{i} + 20\hat{j}$		(a) \hat{k}	(b) $\hat{i} + \hat{j}$
Vector \overrightarrow{A} makes equal angles components (in terms of magni	with x, y and z axis. Value of its tude of \overrightarrow{A}) will be		(c) $\hat{i} + \hat{j} = \frac{1}{\sqrt{2}}$	(d) $\frac{\hat{i}+\hat{j}}{2}$
(a) $\frac{A}{\sqrt{3}}$	(b) $\frac{A}{\sqrt{2}}$	16.	A vector is represented by	$3\hat{i} + \hat{j} + 2\hat{k}$. Its length in <i>XY</i> plane
_			(a) 2	(b) $\sqrt{14}$
(c) $\sqrt{3} A$	(d) $\frac{\sqrt{3}}{A}$		(c) $\sqrt{10}$	(d) $\sqrt{5}$
If $\vec{A} = 2\hat{i} + 4\hat{j} - 5\hat{k}$ the direc	tion of cosines of the vector \vec{A} are	17.	Five equal forces of 10 N e lying in one plane. If th	each are applied at one point and al a angles between them are equal,
(a) $\frac{2}{\sqrt{45}}, \frac{4}{\sqrt{45}} \text{ and } \frac{-5}{\sqrt{45}}$	(b) $\frac{1}{\sqrt{45}}, \frac{2}{\sqrt{45}} \text{ and } \frac{3}{\sqrt{45}}$		resultant force will be (a) Zero	[CBSE PMT 1995] (b) 10 N
(c) $\frac{4}{\sqrt{1-4}}$, 0 and $\frac{4}{\sqrt{1-4}}$	(d) $\frac{3}{\sqrt{2}}, \frac{2}{\sqrt{2}}$ and $\frac{5}{\sqrt{2}}$		(c) 20 <i>N</i>	(d) $10\sqrt{2}N$
V45 V45	V45 V45 V45	18.	The angle made by the vect	tor $A = \hat{i} + \hat{j}$ with <i>x</i> - axis is
The vector that must be add	ed to the vector $\hat{i} - 3\hat{j} + 2\hat{k}$ and			[EAMCET (Engg.) 1
$3\hat{i} + 6\hat{j} - 7\hat{k}$ so that the return the <i>y</i> -axis is	sultant vector is a unit vector along		(a) 90° (c) 22.5°	(b) 45° (d) 30°
(a) $4\hat{i} + 2\hat{j} + 5\hat{k}$	(b) $-4\hat{i}-2\hat{j}+5\hat{k}$	19.	Any vector in an arbitrary (or three)	direction can always be replaced by
(c) $3\hat{i}+4\hat{j}+5\hat{k}$	(d) Null vector		(a) Parallel vectors wh resultant	ich have the original vector as
How many minimum number magnitudes can be added to giv	of coplanar vectors having different e zero resultant		(b) Mutually perpendicul as their resultant	lar vectors which have the original ve
(a) 2	(b) 3			

.

	(c) Arbitrary vectors which resultant	Thave the original vector as then
	(d) It is not possible to resol	ve a vector
20.	Angular momentum is	[MNR 1986]
	(a) A scalar	(b) A polar vector
	(c) An axial vector	(d) None of these
21.	Which of the following is a vec	tor
	(a) Pressure	(b) Surface tension
	(c) Moment of inertia	(d) None of these
22.	If $\vec{P} = \vec{Q}$ then which of the fo	llowing is NOT correct
	(a) $\hat{P} = \hat{Q}$	(b) $ \vec{P} = \vec{Q} $
	(c) $\hat{PQ} = \hat{QP}$	(d) $\vec{P} + \vec{Q} = \hat{P} + \hat{Q}$
23.	The position vector of a par	rticle is $\vec{r} = (a\cos\omega t)\hat{i} + (a\sin\omega t)\hat{j}$.
	The velocity of the particle is	[CBSE PMT 1995]
	(a) Parallel to the position ve	ctor
	(b) Perpendicular to the posit	tion vector
	(c) Directed towards the orig	in
	(d) Directed away from the o	rigin
24.	Which of the following is a sca	lar quantity [AFMC 1998]
	(a) Displacement	(b) Electric field
	(c) Acceleration	(d) Work
		· · · ·
25.	If a unit vector is represented	by $0.\hat{5i} + 0.\hat{8j} + c\hat{k}$, then the value
25.	If a unit vector is represented of 'c' is	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994]
25.	If a unit vector is represented of 'c' is (a) 1	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$
25.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$
25.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$ A boy walks uniformally along	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$ the sides of a rectangular park of size
25. 26.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$ A boy walks uniformally along 400 m× 300 m, starting from	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$ the sides of a rectangular park of size om one corner to the other corner
25. 26.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$ A boy walks uniformally along 400 m× 300 m, starting fro diagonally opposite. Which of t [HP PMT 1999]	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$ the sides of a rectangular park of size om one corner to the other corner the following statement is incorrect
25. 26.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$ A boy walks uniformally along 400 m× 300 m, starting fro diagonally opposite. Which of t [HP PMT 1999] (a) He has travelled a distance	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$ the sides of a rectangular park of size om one corner to the other corner the following statement is incorrect e of 700 <i>m</i>
25. 26.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$ A boy walks uniformally along 400 m× 300 m, starting fro diagonally opposite. Which of t [HP PMT 1999] (a) He has travelled a distance (b) His displacement is 700 m	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$ the sides of a rectangular park of size om one corner to the other corner the following statement is incorrect e of 700 m m
25.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$ A boy walks uniformally along 400 m× 300 m, starting fro diagonally opposite. Which of t [HP PMT 1999] (a) He has travelled a distance (b) His displacement is 700 m (c) His displacement is 500 m	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$ the sides of a rectangular park of size om one corner to the other corner the following statement is incorrect e of 700 m m
25.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$ A boy walks uniformally along 400 m× 300 m, starting fro diagonally opposite. Which of t [HP PMT 1999] (a) He has travelled a distance (b) His displacement is 700 m (c) His displacement is 500 m (d) His velocity is not uniform	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$ the sides of a rectangular park of size om one corner to the other corner the following statement is incorrect e of 700 m m m
25. 26. 27.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$ A boy walks uniformally along 400 m× 300 m, starting fro diagonally opposite. Which of t [HP PMT 1999] (a) He has travelled a distance (b) His displacement is 700 r (c) His displacement is 500 r (d) His velocity is not uniform The unit vector parallel	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$ the sides of a rectangular park of size om one corner to the other corner the following statement is incorrect e of 700 m m n n throughout the walk to the resultant of the vectors
25. 26. 27.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$ A boy walks uniformally along 400 m× 300 m, starting fro diagonally opposite. Which of t [HP PMT 1999] (a) He has travelled a distance (b) His displacement is 700 m (c) His displacement is 500 m (d) His velocity is not uniform The unit vector parallel $\vec{A} = 4\hat{i} + 3\hat{j} + 6\hat{k}$ and $\vec{B} = -$	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$ the sides of a rectangular park of size om one corner to the other corner the following statement is incorrect are of 700 m m m n n throughout the walk to the resultant of the vectors $-\hat{i} + 3\hat{j} - 8\hat{k}$ is [EAMCET 2000]
25. 26. 27.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$ A boy walks uniformally along 400 m× 300 m, starting fro diagonally opposite. Which of t [HP PMT 1999] (a) He has travelled a distance (b) His displacement is 700 r (c) His displacement is 500 r (d) His velocity is not uniform The unit vector parallel $\vec{A} = 4\hat{i} + 3\hat{j} + 6\hat{k}$ and $\vec{B} = -$ (a) $\frac{1}{7}(3\hat{i} + 6\hat{j} - 2\hat{k})$	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$ the sides of a rectangular park of size om one corner to the other corner the following statement is incorrect e of 700 m m m n n throughout the walk to the resultant of the vectors $-\hat{i} + 3\hat{j} - 8\hat{k}$ is [EAMCET 2000] (b) $\frac{1}{7}(3\hat{i} + 6\hat{j} + 2\hat{k})$
25. 26. 27.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$ A boy walks uniformally along 400 m× 300 m, starting fro diagonally opposite. Which of the [HP PMT 1999] (a) He has travelled a distance (b) His displacement is 700 m (c) His displacement is 500 m (d) His velocity is not uniform The unit vector parallel $\vec{A} = 4\hat{i} + 3\hat{j} + 6\hat{k}$ and $\vec{B} = -$ (a) $\frac{1}{7}(3\hat{i} + 6\hat{j} - 2\hat{k})$ (c) $\frac{1}{49}(3\hat{i} + 6\hat{j} - 2\hat{k})$	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$ the sides of a rectangular park of size om one corner to the other corner the following statement is incorrect e of 700 m m m n throughout the walk to the resultant of the vectors $-\hat{i} + 3\hat{j} - 8\hat{k}$ is [EAMCET 2000] (b) $\frac{1}{7}(3\hat{i} + 6\hat{j} + 2\hat{k})$ (d) $\frac{1}{49}(3\hat{i} - 6\hat{j} + 2\hat{k})$
25. 26. 27.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$ A boy walks uniformally along 400 m× 300 m, starting fro diagonally opposite. Which of t [HP PMT 1999] (a) He has travelled a distance (b) His displacement is 700 r (c) His displacement is 500 r (d) His velocity is not uniforr The unit vector parallel $\vec{A} = 4\hat{i} + 3\hat{j} + 6\hat{k}$ and $\vec{B} = -$ (a) $\frac{1}{7}(3\hat{i} + 6\hat{j} - 2\hat{k})$ (c) $\frac{1}{49}(3\hat{i} + 6\hat{j} - 2\hat{k})$ Surface area is	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$ the sides of a rectangular park of size om one corner to the other corner the following statement is incorrect e of 700 m m n n n throughout the walk to the resultant of the vectors $-\hat{i} + 3\hat{j} - 8\hat{k}$ is [EAMCET 2000] (b) $\frac{1}{7}(3\hat{i} + 6\hat{j} + 2\hat{k})$ (d) $\frac{1}{49}(3\hat{i} - 6\hat{j} + 2\hat{k})$ [J&K CET 2002]
25. 26. 27.	If a unit vector is represented of 'c' is (a) 1 (c) $\sqrt{0.01}$ A boy walks uniformally along 400 m× 300 m, starting fro diagonally opposite. Which of t [HP PMT 1999] (a) He has travelled a distance (b) His displacement is 700 r (c) His displacement is 500 r (d) His velocity is not uniforr The unit vector parallel $\vec{A} = 4\hat{i} + 3\hat{j} + 6\hat{k}$ and $\vec{B} = -$ (a) $\frac{1}{7}(3\hat{i} + 6\hat{j} - 2\hat{k})$ (c) $\frac{1}{49}(3\hat{i} + 6\hat{j} - 2\hat{k})$ Surface area is (a) Scalar	by $0.5\hat{i} + 0.8\hat{j} + c\hat{k}$, then the value [CBSE PMT 1999; EAMCET 1994] (b) $\sqrt{0.11}$ (d) $\sqrt{0.39}$ the sides of a rectangular park of size om one corner to the other corner the following statement is incorrect e of 700 m m n n n n n throughout the walk to the resultant of the vectors $-\hat{i} + 3\hat{j} - 8\hat{k}$ is [EAMCET 2000] (b) $\frac{1}{7}(3\hat{i} + 6\hat{j} + 2\hat{k})$ (d) $\frac{1}{49}(3\hat{i} - 6\hat{j} + 2\hat{k})$ [J&K CET 2002] (b) Vector

29. With respect to a rectangular cartesian coordinate system, three vectors are expressed as

$$\vec{a} = 4\hat{i} - \hat{j}$$
, $\vec{b} = -3\hat{i} + 2\hat{j}$ and $\vec{c} = -k$

where $\hat{i}, \hat{j}, \hat{k}$ are unit vectors, along the *X*, *Y* and *Z*-axis respectively.

The unit vectors \hat{r} along the direction of sum of these vector is [Kerala CET (Engg.) 2003]

(a)
$$\hat{r} = \frac{1}{\sqrt{3}}(\hat{i} + \hat{j} - \hat{k})$$
 (b) $\hat{r} = \frac{1}{\sqrt{2}}(\hat{i} + \hat{j} - \hat{k})$
(c) $\hat{r} = \frac{1}{3}(\hat{i} - \hat{j} + \hat{k})$ (d) $\hat{r} = \frac{1}{\sqrt{2}}(\hat{i} + \hat{j} + \hat{k})$

- **30.** The angle between the two vectors $\vec{A} = 3\hat{i} + 4\hat{j} + 5\hat{k}$ and $\vec{B} = 3\hat{i} + 4\hat{j} + 5\hat{k}$ is [DPMT 2000]
 - (a) 60°

 $\vec{B} = 8\hat{i} + 8\hat{j}$ will be

32.

(c) 90° (d) None of these

31. The position vector of a particle is determined by the expression $\vec{r} = 3t^2\hat{i} + 4t^2\hat{j} + 7\hat{k}$

(b) Zero

[BHU 1995]

The distance traversed in first 10 sec is [DPMT 2002]

- (a) 500 m (b) 300 m
- (c) 150 *m* (d) 100 *m*

Unit vector parallel to the resultant of vectors $\vec{A} = 4\hat{i} - 3\hat{j}$ and

(a)
$$\frac{24\hat{i}+5\hat{j}}{13}$$
 (b) $\frac{12\hat{i}+5\hat{j}}{13}$
(c) $\frac{6\hat{i}+5\hat{j}}{13}$ (d) None of these

- **33.** The component of vector $A = 2\hat{i} + 3\hat{j}$ along the vector $\hat{i} + \hat{j}$ is [KCET 1997]
 - (a) $\frac{5}{\sqrt{2}}$ (b) $10\sqrt{2}$
 - (c) $5\sqrt{2}$ (d) 5

34. The angle between the two vectors $\vec{A} = 3\hat{i} + 4\hat{j} + 5\hat{k}$ and $\vec{B} = 3\hat{i} + 4\hat{j} - 5\hat{k}$ will be [Pb. CET 2001] (a) 90° (b) 0° (c) 60° (d) 45°

Addition and Subtraction of Vectors

- There are two force vectors, one of 5 N and other of 12 N at what angle the two vectors be added to get resultant vector of 17 N, 7 N and 13 N respectively
 (a) 0°, 180° and 90°
 (b) 0°, 90° and 180°
 (c) 0°, 90° and 90°
 (d) 180°, 0° and 90°
- 2. If $\vec{A} = 4\hat{i} 3\hat{j}$ and $\vec{B} = 6\hat{i} + 8\hat{j}$ then magnitude and direction of $\vec{A} + \vec{B}$ will be

Vectors II

(c)	$10, \tan^{-1}(5)$	(d)	$25, \tan^{-1}(3/4)$	
A tr	uck travelling due north at 20) <i>m/s</i>	turns west and travels at th	e
same	e speed. The change in its velo	ocity b	I IDEE AT 1000	
		(1)		.1
(a)	40 <i>m/s N</i> – <i>W</i>	(b)	$20\sqrt{2} m/s N - W$	13.
(c)	40 <i>m/s S</i> -W	(d)	$20\sqrt{2} m/s S - W$	c
lf th diffe	e sum of two unit vectors is rence is [CPMT 1995; CBSE P	a un MT 19	it vector, then magnitude o 89]	† 14.
(a)	$\sqrt{2}$	(b)	$\sqrt{3}$	
(c)	$1 / \sqrt{2}$	(d)	$\sqrt{5}$	
$\vec{A} =$	$\vec{i} = 2\hat{i} + \hat{j}, B = 3\hat{j} - \hat{k}$ and $\vec{C} = \hat{i}$	$= 6\hat{i}$	$-2\hat{k}$.	
Valı	ue of $\vec{A} - 2\vec{B} + 3\vec{C}$ would b	e		
(a)	$20\hat{i} + 5\hat{j} + 4\hat{k}$	(b)	$20\hat{i} - 5\hat{j} - 4\hat{k}$	
(c)	$4\hat{i}+5\hat{j}+20\hat{k}$	(d)	$\hat{5i} + \hat{4j} + 10\hat{k}$	15.
An c and the c	bject of <i>m kg</i> with speed of rebounds at the same speed change in momentum of the o	<i>v m/</i> : and s bject	s strikes a wall at an angle (ame angle. The magnitude o will be	θ f
(a)	$2mv\cos\theta$			16.
(1)	$2mv\sin\theta$	\backslash		
(b)				
(b) (c)	0		$\overrightarrow{v_1}$ θ θ $\overrightarrow{v_2}$	
(b) (c) (d)	0 2 <i>m v</i>		\vec{v}_1 θ θ \vec{v}_2	
(b) (c) (d) Two	0 $2mv$ forces, each of magnitude		\vec{v}_1 θ θ \vec{v}_2	e 17.
(b) (c) (d) Two mag	0 2 <i>mv</i> forces, each of magnitude nitude <i>F.</i> The angle between t	he tw	$\vec{v}_1 \qquad \theta \qquad \theta \qquad \vec{v}_2$ o forces is	e 17.
(b) (c) (d) Two mag ⁻ (a)	0 2 $m v$ forces, each of magnitude nitude F . The angle between t 45°	he tw (b)	\vec{v}_1 θ θ \vec{v}_2 no forces is [CBSE PMT 1990 120°	e 17.]
(b) (c) (d) Two mag ⁻ (a) (c)	0 2 <i>m v</i> forces, each of magnitude nitude <i>F.</i> The angle between t 45° 150°	he tw (b) (d)	\vec{v}_1 θ θ \vec{v}_2 o forces is [CBSE PMT 1990 120° 60°	e 17.]
(b) (c) (d) Two mag ⁻ (a) (c) For	0 2 <i>m v</i> forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector	he tw (b) (d) ors to	\vec{v}_1 $\vec{\theta}$ $\vec{\theta}$ \vec{v}_2 o forces is [CBSE PMT 1990 120° 60° be maximum, what must be	e 17.] e 18.
(b) (c) (d) Two mag ⁻ (a) (c) For the a (a)	0 2 m v forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector angle between them 0°	he tw (b) (d) prs to	\vec{v}_1 $\vec{\theta}$ $\vec{\theta}$ \vec{v}_2 o forces is [CBSE PMT 1990 120° 60° be maximum, what must be	e 17.] e 18.
 (b) (c) (d) Two mag (a) (c) For the a (a) (c) 	0 2 m v forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector angle between them 0° 90°	he tw (b) (d) ors to (b) (d)	\vec{v}_1 θ θ \vec{v}_2 o forces is [CBSE PMT 1990 120° 60° be maximum, what must be 60° 180°	e 17.] e 18.
 (b) (c) (d) Two mag (a) (c) For the a (a) (c) A pa N T 	0 2 m v forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector angle between them 0° 90° wrticle is simultaneously acted he net force on the particle is	he tw (b) (d) ors to (b) (d) by tv [CPA	\vec{v}_1 θ θ \vec{v}_2	e 17.] e 18. 3 19.
 (b) (c) (d) Two mag (a) (c) For the a (a) (c) A pa <i>N</i>. T (a) 	0 2 m v forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector angle between them 0° 90° wrticle is simultaneously acted he net force on the particle is 7 N	he tw (b) (d) ors to (b) (d) by tv [CPA (b)	\vec{v}_1 θ θ \vec{v}_2 o forces is [CBSE PMT 1990 120° 60° be maximum, what must be 60° 180° vo forces equal to 4 N and 2 TT 1979] 5 N	e 17.] e 18. 3 19.
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(b) (c) (d) Two mag (a) (c) For the a (a) (c) A pa <i>N</i> . T (a) (c) Two	0 2 m v forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector angle between them 0° 90° wrticle is simultaneously acted he net force on the particle is 7 N 1 N vectors \vec{A} and \vec{B} lie in a pl	he tw (b) (d) ors to (b) (d) by tv (CPA (b) (d) ane, a	\vec{v}_1 θ θ \vec{v}_2 [CBSE PMT 1990 120° 60° be maximum, what must be 60° 180° vo forces equal to 4 <i>N</i> and 2 N Between 1 <i>N</i> and 7 <i>N</i> another vector \vec{C} lies outsid	e 17.] a 18. 3 19.
 (b) (c) (d) Two mage (a) (c) For the a (a) (c) A paa N. T (a) (c) Two this 	0 2 m v forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector angle between them 0° 90° nuticle is simultaneously acted he net force on the particle is 7 N 1 N vectors \vec{A} and \vec{B} lie in a pliplane, then the resultant of the	he tw (b) (d) ors to (b) (d) (b) (d) (d) ane, a ese th	\vec{v}_1 θ θ \vec{v}_2	e 17.] 1 8. 3 19.
(b) (c) (d) Two mag (a) (c) For the a (a) (c) A pa (c) A pa (c) Two this (a) (b)	0 2 m v forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector angle between them 0° 90° nuticle is simultaneously acted he net force on the particle is 7 N 1 N vectors \vec{A} and \vec{B} lie in a pl plane, then the resultant of the Can be zero Cannot be zero	he tw (b) (d) ors to (b) (d) (b) (d) (d) ane, a ese th	$\vec{r}_{V_{1}} \qquad \vec{r}_{V_{2}} \qquad $	e 17. 17. 18. 18. 19.
(b) (c) (d) Two mag (a) (c) For the a (a) (c) A pa <i>N</i> . T (a) (c) Two this (a) (b) (c)	0 2 m v forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector angle between them 0° 90° writcle is simultaneously acted he net force on the particle is 7 N 1 N vectors \vec{A} and \vec{B} lie in a pl plane, then the resultant of the Can be zero Cannot be zero Lies in the plane containing	he tw (b) (d) ors to (b) (d) by tw [CPA (b) (d) (d) ane, a arease th $\vec{A} + \vec{A}$	\vec{r}_{1} \vec{r}_{2} $\vec{r}_{$	e 17. 18. 3 19. 20.
(b) (c) (d) Two mag (a) (c) For t the a (a) (c) A paa N. T (a) (c) Two this (a) (b) (c) (c) (c)	0 2 m v forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector angle between them 0° 90° nuticle is simultaneously acted he net force on the particle is 7 N 1 N vectors \vec{A} and \vec{B} lie in a pl plane, then the resultant of the Can be zero Cannot be zero Lies in the plane containing	he tw (b) (d) ors to (b) (d) by tw [CPA (b) (d) (d) ane, a $\vec{A} + \vec{C}$	$\vec{H} = \begin{pmatrix} \theta & \vec{V}_{2} \\ \vec{V}_{3} \\ \vec{V}_{4} \\ \vec{V}_{5} \\ \vec{V}_{5$	e 17. 18. 3 19. 20.
 (b) (c) (d) Two mag (a) (c) For the a (a) (c) A paa <i>N</i>. T (a) (c) Two this (a) (b) (c) (d) (c) (d) (c) (d) (c) (c) (c) (d) (c) (d) (c) (d) (c) (d) (c) (d) (a) (c) (c) (d) (c) (d) 	0 2 m v forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector angle between them 0° 90° multicle is simultaneously acted he net force on the particle is 7 N 1 N vectors \vec{A} and \vec{B} lie in a pluplane, then the resultant of the Can be zero Cannot be zero Lies in the plane containing Lies in the plane containing e resultant of the two forces nitude of larger force, the two	he tw (b) (d) prs to (b) (d) by tw [CPN (b) (d) ane, a ese th $\vec{A} + \vec{C}$ has a a force	\vec{r}_{V_1} $\vec{\theta}$ $\vec{\theta}$ \vec{v}_2 (CBSE PMT 1990) 120° 60° be maximum, what must be 60° 180° vo forces equal to 4 <i>N</i> and 2 XT 1979] 5 <i>N</i> Between 1 <i>N</i> and 7 <i>N</i> mother vector \vec{C} lies outsid three vectors <i>i.e.</i> , $\vec{A} + \vec{B} + \vec{C}$ \vec{B} a magnitude smaller than the s must be	e 17. 18. 3 19. e 20.
	0 2 m v forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector angle between them 0° 90° mitcle is simultaneously acted he net force on the particle is 7 N 1 N vectors \vec{A} and \vec{B} lie in a pl plane, then the resultant of the Cannot be zero Lies in the plane containing Lies in the plane containing e resultant of the two forces nitude of larger force, the two Different both in magnitude	he tw (b) (d) ors to (b) (d) (d) (d) (d) (d) (d) (ane, a $\vec{A} + \vec{C}$ has a force and of	\vec{r}_{V_1} $\vec{\theta}$ $\vec{\theta}$ \vec{v}_2 [CBSE PMT 1990 120° 60° be maximum, what must be 60° 180° vo forces equal to 4 <i>N</i> and 2 N Between 1 <i>N</i> and 7 <i>N</i> mother vector \vec{C} lies outsid aree vectors <i>i.e.</i> , $\vec{A} + \vec{B} + \vec{C}$ \vec{B} a magnitude smaller than the s must be direction	e 17. 18. 3 19. e 20.
(b) (c) (d) Two mag (a) (c) For f (a) (c) Two (c) Two this (a) (b) (c) (d) If th mag (a) (b)	0 2 m v forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector angle between them 0° 90° nucle is simultaneously acted he net force on the particle is 7 N 1 N vectors \vec{A} and \vec{B} lie in a pl plane, then the resultant of the Cannot be zero Lies in the plane containing Lies in the plane containing e resultant of the two forces nitude of larger force, the two Different both in magnitude Mutually perpendicular to o	he tw (b) (d) prs to (b) (d) by tw [CPA (b) (d) (d) ane, a ese th $\vec{A} + \vec{C}$ has a force and one ne and one	\vec{N} \vec{P} \vec{P} \vec{V}_2 \vec{V} \vec{V}_2 \vec{V} \vec{V}_2 \vec{V} \vec{V}_2 \vec{V} \vec{V}_2 \vec{V} \vec{V} \vec{V}_2 \vec{V} \vec{V} V	e 17. 18. 3 19. e 20. e 21.
(b) (c) (d) Two mag (a) (c) For f the a (a) (c) Two this (a) (b) (c) (d) If th mag (a) (c) (d)	0 2 m v forces, each of magnitude nitude <i>F</i> . The angle between t 45° 150° the resultant of the two vector angle between them 0° 90° multicle is simultaneously acted he net force on the particle is 7 N 1 N vectors \vec{A} and \vec{B} lie in a plup plane, then the resultant of the Can be zero Lies in the plane containing Lies in the plane containing e resultant of the two forces nitude of larger force, the two Different both in magnitude Mutually perpendicular to o Possess extremely small mag Point in opposite directions	he tw (b) (d) prs to (b) (d) by tw [CPN (b) (d) ane, a i \vec{A} + \vec{C} has a force and on ne and spintud	\vec{N} \vec{P} \vec{P} \vec{V}_2 V	e 17. a 18. 3 19. e 20. e 21.

(b) $5\sqrt{5}$, $\tan^{-1}(1/2)$

(a) 5, $\tan^{-1}(3/4)$

3.

4.

5.

6.

7.

8.

9.

10.

11.

	12.	Forces ${\cal F}_1$ and ${\cal F}_2$ act on a point mass in two mutually
		perpendicular directions. The resultant force on the point mass will be [CPMT 1991]
		(a) $F_1 + F_2$ (b) $F_1 - F_2$
		(c) $\sqrt{F_1^2 + F_2^2}$ (d) $F_1^2 + F_2^2$
	13.	If $ \vec{A} - \vec{B} = \vec{A} = \vec{B} $, the angle between \vec{A} and \vec{B} is
		(a) 60° (b) 0°
:		(c) 120° (d) 90° \rightarrow \rightarrow
	14.	Let the angle between two nonzero vectors A and B be 120° and \rightarrow
		resultant be $C \rightarrow $
		(a) C must be equal to $ A - B $
		(b) \vec{C} must be less than $ \vec{A} - \vec{B} $
		(c) \vec{C} must be greater than $ \vec{A} - \vec{B} $
		(d) \vec{C} may be equal to $ \vec{A} - \vec{B} $
	15.	The magnitude of vector \vec{A}, \vec{B} and \vec{C} are respectively 12, 5 and 13
) :		units and $\vec{A} + \vec{B} = \vec{C}$ then the angle between \vec{A} and \vec{B} is
		(a) 0 (b) π
	16	(c) $\pi/2$ (d) $\pi/4$
	10.	$\hat{6i} + \hat{7i}$ and $\hat{3i} + \hat{4i}$ is [BHII 2000]
		$(1) \frac{122}{122} \qquad (1) \frac{122}{122}$
		(a) $\sqrt{130}$ (b) $\sqrt{13.2}$
	17	(c) $\sqrt{202}$ (d) $\sqrt{160}$ A particle has displacement of 12 <i>m</i> towards east and 5 <i>m</i> towards
	17.	north then 6 m vertically upward. The sum of these displacements is
		(a) 12 (b) 10.04 m
	-0	(c) 14.31 m (d) None of these $\vec{1}$
	18.	The three vectors $A = 3i - 2j + k$, $B = i - 3j + 5k$ and
		C = 2i + j - 4k form
		(a) An equilateral triangle (b) Isosceles triangle (c) A right angled triangle (d) No triangle
;	19.	For the figure
		(a) $\vec{A} + \vec{B} = \vec{C}$
		(b) $\vec{B} + \vec{C} = \vec{A}$
		\overrightarrow{C} \overrightarrow{C} \overrightarrow{B}
		(c) $C + A = B$ ([CPM] 1983], $\vec{C} = 0$
	20.	(d) $\overrightarrow{A} + \overrightarrow{B} + \overrightarrow{C} = 0$ \overrightarrow{A} Let $\overrightarrow{C} = \overrightarrow{A} + \overrightarrow{B}$ then
		(a) $ \vec{C} $ is always greater then $ \vec{A} $
		(b) It is possible to have $ \vec{C} < \vec{A} $ and $ \vec{C} < \vec{B} $
		(c) C is always equal to $A + B$
		(d) C is never equal to $A + B$
	21.	The value of the sum of two vectors \vec{A} and \vec{B} with θ as the angle between them is [BHU 1996]
		(a) $\sqrt{A^2 + B^2 + 2AB\cos\theta}$ (b) $\sqrt{A^2 - B^2 + 2AB\cos\theta}$

(c)
$$\sqrt{A^2 + B^2 - 2AB\sin\theta}$$
 (d) $\sqrt{A^2 + B^2 + 2AB\sin\theta}$
22. Following sets of three forces act on a body. Whose resultant cannot be zero [CPMT 1985]
(a) 10, 10, 10 (b) 10, 10, 20
(c) 10, 20, 23 (d) 10, 20, 40
23. When three forces of 50 N, 30 N and 15 N act on a body, then the body is
(a) At rest
(b) Moving with a uniform velocity
(c) In equilibrium
(d) Moving with an acceleration
24. The sum of two forces acting at a point is 16 N. If the resultant force is 8 N and its direction is perpendicular to minimum force then the forces are [CPMT 1997]
(a) 6 N and 10 N (b) 8 N and 8 N
(c) 4 N and 12 N (d) 2 N and 14 N
25. If vectors P, Q and R have magnitude 5, 12 and 13 units and $\vec{P} + \vec{Q} = \vec{R}$, the angle between Q and R is [CEET 1998]

(a)
$$\cos^{-1}\frac{5}{12}$$
 (b) $\cos^{-1}\frac{5}{13}$
(c) $\cos^{-1}\frac{12}{13}$ (d) $\cos^{-1}\frac{7}{13}$

- **26.** The resultant of two vectors *A* and *B* is perpendicular to the vector *A* and its magnitude is equal to half the magnitude of vector *B*. The angle between *A* and *B* is
 - (a) 120° (b) 150°
 - (c) 135° (d) None of these
- **27.** What vector must be added to the two vectors $\hat{i} 2\hat{j} + 2\hat{k}$ and

 $2\hat{i} + \hat{j} - \hat{k}$, so that the resultant may be a unit vector along xaxis [BHU 1990]

- (a) $2\hat{i} + \hat{j} \hat{k}$ (b) $-2\hat{i} + \hat{j} - \hat{k}$ (c) $2\hat{i} - \hat{j} + \hat{k}$ (d) $-2\hat{i} - \hat{j} - \hat{k}$
- **28.** What is the angle between \vec{P} and the resultant of $(\vec{P} + \vec{Q})$ and

 $(\vec{P} - \vec{Q})$

(a) Zero (b) $\tan^{-1}(P/Q)$

(c)
$$\tan^{-1}(Q/P)$$
 (d) $\tan^{-1}(P-Q)/(P+Q)$

29. The resultant of \vec{P} and \vec{Q} is perpendicular to \vec{P} . What is the angle between \vec{P} and \vec{Q}

(a)
$$\cos^{-1}(P/Q)$$
 (b) $\cos^{-1}(-P/Q)$

- (c) $\sin^{-1}(P/Q)$ (d) $\sin^{-1}(-P/Q)$
- **30.** Maximum and minimum magnitudes of the resultant of two vectors of magnitudes P and Q are in the ratio 3:1. Which of the following relations is true

(a)
$$P = 2Q$$
 (b) $P = Q$
(c) $PQ = 1$ (d) None of these

31. The resultant of two vectors \vec{P} and \vec{Q} is \vec{R} . If Q is doubled, the new resultant is perpendicular to P. Then R equals (a) P (b) (P+Q) (c) Q

33.

(d)
$$(P-Q)$$

- **32.** Two forces, F_1 and F_2 are acting on a body. One force is double that of the other force and the resultant is equal to the greater force. Then the angle between the two forces is
 - (a) $\cos^{-1}(1/2)$ (b) $\cos^{-1}(-1/2)$ (c) $\cos^{-1}(-1/4)$ (d) $\cos^{-1}(1/4)$

(c)
$$\cos(-1/4)$$

Given that $\vec{A} + \vec{B} = \vec{C}$ and that \vec{C} is \perp to \vec{A} . Further if $|\vec{A}| = |\vec{C}|$, then what is the angle between \vec{A} and \vec{B}

(a)
$$\frac{\pi}{4}$$
 radian (b) $\frac{\pi}{2}$ radian (c) $\frac{3\pi}{4}$ radian (d) π radian

34. A body is at rest under the action of three forces, two of which are $\vec{F}_1 = 4\hat{i}, \vec{F}_2 = 6\hat{j}$, the third force is **[AMU 1996]**

(a)
$$4\hat{i} + 6\hat{j}$$
 (b) $4\hat{i} - 6\hat{j}$

(c)
$$-4\hat{i} + 6\hat{j}$$
 (d) $-4\hat{i} - 6\hat{j}$

35. A plane is revolving around the earth with a speed of 100 km/hr at a constant height from the surface of earth. The change in the velocity as it travels half circle is

(c)
$$100\sqrt{2} \, km \, / hr$$
 (d) 0

36. What displacement must be added to the displacement $2\hat{5i} - \hat{6j}m$ to give a displacement of 7.0 m pointing in the *x*-direction

(a)
$$18\hat{i} - 6\hat{j}$$
 (b) $32\hat{i} - 13\hat{j}$

(c)
$$-18\hat{i} + 6\hat{j}$$
 (d) $-25\hat{i} + 13\hat{j}$

37. A body moves due East with velocity 20 *km/hour* and then due North with velocity 15 *km/hour*. The resultant velocity

(h) 15 loss /h a

[AFMC 1995]

r I.....

38. The magnitudes of vectors \vec{A}, \vec{B} and \vec{C} are 3, 4 and 5 units respectively. If $\vec{A} + \vec{B} = \vec{C}$, the angle between \vec{A} and \vec{B} is

[CBSE PMT 1990]

(a)
$$\frac{\pi}{2}$$
 (b) $\cos^{-1}(0.6)$
(c) $\tan^{-1}\left(\frac{7}{5}\right)$ (d) $\frac{\pi}{4}$

- While travelling from one station to another, a car travels 75 km North, 60 km North-east and 20 km East. The minimum distance between the two stations is [AFMC 1993]
 - (a) 72 *km* (b) 112 *km*
 - (c) 132 *km* (d) 155 *km*
- **40.** A scooter going due east at 10 *ms* turns right through an angle of 90°. If the speed of the scooter remains unchanged in taking turn, the change is the velocity of the scooter is

[RPET 1998; KCET 2000]

					vectors 13
		[BHU 1994]		(a) $\tan^{-1}(2)$	(b) $\tan^{-1}(1/2)$
	(a) 20.0 <i>ms</i> south eastern	direction		(c) 45°	(d) o°
	(b) Zero		50.	Two forces of 12 N and 8	3 N act upon a body. The resultant force or
	(c) 10.0 <i>ms</i> in southern di	rection		the body has maximum v	value of [Manipal 2003]
	(d) 14.14 <i>ms</i> in south-west	direction		(a) 4 <i>N</i>	(b) 0 <i>N</i>
41.	A person goes 10 <i>km</i> n	orth and 20 <i>km</i> east. What will be		(c) 20 <i>N</i>	(d) 8 N
	displacement from initial po	int [AFMC 1994, 2003]	51.	Two equal forces (<i>P</i> each	 act at a point inclined to each other at an tude of their resultant is
	(a) 22.36 <i>km</i>	(b) 2 <i>km</i>		(a) $P/2$	(b) P/A
	(c) 5 <i>km</i>	(d) 20 <i>km</i>		(a) I / Z	
42.	Two forces $\vec{F}_1 = 5\hat{i} + 10\hat{i}$	$-20\hat{k}$ and $\vec{F}_{2} = 10\hat{i} - 5\hat{i} - 15\hat{k}$ act on	~~		(a) 2r
-	r single asign The same he	\vec{F} and \vec{F} is more by	52.	Sum of these vector is	$1 \ 2l + l \ j$ are added. The magnitude of th
	a single point. The angle be	tween r_1 and r_2 is nearly		$\sqrt{274}$	
		[AMU 1995]		(a) $\sqrt{274}$	(b) 38
	(a) 30°	(b) 45°		(c) 238	(d) 560
	(c) 60°	(d) 90°	53.	Two vectors \vec{A} and \vec{B}	are such that $\vec{A}+\vec{B}=\vec{A}-\vec{B}$. Then
43.	Which pair of the following	forces will never give resultant force of			[AMU (Med.) 2000
	() 2 M = 1 2 M			(a) $\vec{A} \cdot \vec{B} = 0$	(b) $\vec{A} \times \vec{B} = 0$
	(a) $2 / v$ and $2 / v$			→	→
	(c) 1 N and 3 N	(d) 1 N and 4 N		(c) $A = 0$	(d) $B = 0$
14.	Two forces $3N$ and $2N$ are	e at an angle θ such that the resultant is		Multiplic	ation of Vectors
	2 <i>R</i> . The value of θ is	[HP PMT 2000]			
	(a) 30°	(b) 60°	1.	If a vector $2i + 3j$	k + 8k is perpendicular to the vecto
	(c) 90°	(d) 120°		$4j-4i+\alpha k$. Then the	value of α is [CBSE PMT 2005]
45.	Three concurrent forces of	the same magnitude are in equilibrium.		(a) I	(b) 1
	What is the angle betwee	n the forces ? Also name the triangle		(a) —I	(b) $\frac{1}{2}$
	formed by the forces as side	25		. 1	
		[JIPMER 2000]		(c) $-\frac{1}{2}$	(d) 1
	(a) 60° equilateral triangle		_		
	(c) 120° 30° 30° an isosce	e les triangle	2.	If two vectors $2l + 3j$	$7 - k$ and $-4i - 6j - \lambda k$ are parallel to
	(d) 120° an obtuse angled	triangle		each other then value or	
				(a) 0	(b) 2
1 0.	If $ A+B = A + B $, the	n angle between A and B will be		(c) 3	(d) 4
		[CBSE PMT 2001]	3.	A body, acted upon by	y a force of 50 N is displaced through a direction making an angle of 60° with the
	$(a) 90^{\circ}$	(d) 60°		force. The work done by	the force be
47	The maximum and minim	um magnitude of the resultant of two		(a) 200 J	(b) 100 J
	given vectors are 17 units	and 7 <i>unit</i> respectively. If these two		(c) 300	(d) 250 /
	vectors are at right angles	to each other, the magnitude of their			
	resultant is	[Kerala CET (Engg.) 2000]	4.	A particle moves from p	position $3i + 2j - 6k$ to $14i + 13j + 9k$
	(a) 14	(d) 13		due to a uniform force	of $(4\hat{i}+\hat{j}+3\hat{k})N$. If the displacement in
48	The vector sum of two	forces is nernendicular to their vector		meters then work done v	vill be
, 0.	The vector sum of two	is the perpendicular to their vector			

- [CMEET 1995; Pb. PMT 2002, 03]
- (a) 100 J (b) 200 J
- (c) 300 J (d) 250 J

If for two vector \vec{A} and \vec{B} , sum $(\vec{A} + \vec{B})$ is perpendicular to the 5. difference $(\vec{A} - \vec{B})$. The ratio of their magnitude is

> (Manipal 2003] (b) 2

- [CBSE PMT 2003] differences. In that case, the forces
 - (a) Are equal to each other in magnitude
 - $(b) \quad \text{Are not equal to each other in magnitude} \\$
 - (c) Cannot be predicted
 - (d) Are equal to each other
- y component of velocity is 20 and x component of velocity is 10. The 49. direction of motion of the body with the horizontal at this instant is

	14 Vectors			
	(c) 3	(d) None of these	15.	If $ \vec{V}_1 + \vec{V}_2 = \vec{V}_1 - \vec{V}_2 $ and V_2 is finite, then [CPMT 1989]
6.	The angle between the vecto	rs \vec{A} and \vec{B} is θ . The value of the		(a) V_1 is parallel to V_2
	triple product $\vec{A}.(\vec{B}\times\vec{A})$ is	[CBSE PMT 1991, 2005]		$\vec{\mathbf{x}}_1 = \vec{\mathbf{x}}_2$
	(a) $A^2 B$	(b) Zero		(b) $V_1 - V_2$ (c) V_1 and V_2 are mutually perpendicular
	(a) $A^2 B \sin \theta$	(d) $A^2 R \cos \theta$		(b) \vec{v}_1 and \vec{v}_2 are indealing perpendicular
	(c) A D sino	(d) A D C030		$ (a) v_1 = v_2 $
7.	If $\vec{A} \times \vec{B} = \vec{B} \times \vec{A}$ then the an	gle between A and B is	16.	A force $F = (5i + 3j)$ Newton is applied over a particle which
		[AIEEE 2004]		displaces it from its origin to the point $r = (2i - 1j)$ metres. The work done on the particle is [MP PMT 1995]
	(a) π/2	(b) $\pi / 3$		(a) $-7 J$ (b) $+13 J$
	(c) <i>π</i>	(d) $\pi/4$		(c) +7 <i>J</i> (d) +11 <i>J</i>
8.	If $\vec{A} = 3\hat{i} + \hat{j} + 2\hat{k}$ and	$\vec{B} = 2\hat{i} - 2\hat{j} + 4\hat{k}$ then value of	17.	The angle between two vectors $-2\hat{i}+3\hat{j}+\hat{k}$ and $\hat{i}+2\hat{j}-4\hat{k}$ is
	$ \vec{A} \times \vec{B} $ will be	·		(a) 0° (b) 90° (c) 180° (d) None of the above
			18	The angle between the vectors $(\hat{i} + \hat{i})$ and $(\hat{i} + \hat{k})$ is
	(a) $8\sqrt{2}$	(b) $8\sqrt{3}$	101	[EAMCET 1995]
	(c) $8\sqrt{5}$	(d) $5\sqrt{8}$		(a) 30° (b) 45°
9.	The torque of the force $\vec{F} =$	$(2\hat{i} - 3\hat{j} + 4\hat{k})N$ acting at the point		(c) 60° (d) 90°
	$\vec{r} = (3\hat{i} + 2\hat{j} + 3\hat{k})m$ about t	he origin be	19.	A particle moves with a velocity $6\hat{i} - 4\hat{j} + 3\hat{k}m/s$ under the
		[CBSE PMT 1995]		influence of a constant force $\vec{F} = 20\hat{i} + 15\hat{j} - 5\hat{k}N$. The
	(a) $\hat{6i} - \hat{6j} + 12\hat{k}$	(b) $17\hat{i} - 6\hat{j} - 13\hat{k}$		instantaneous power applied to the particle is
	(c) $-\hat{6i}+\hat{6j}-12\hat{k}$	(d) $-17\hat{i}+6\hat{j}+13\hat{k}$		(a) 35 <i>J/s</i> (b) 45 <i>J/s</i>
10.	If $\vec{A} \times \vec{B} = \vec{C}$, then which of t	he following statements is wrong		(c) 25 <i>J/s</i> (d) 195 <i>J/s</i>
	(a) $\vec{C} \perp \vec{A}$	(b) $\vec{C} \perp \vec{B}$	20.	If $\vec{P}.\vec{Q} = PQ$, then angle between \vec{P} and \vec{Q} is [AIIMS 1999]
	(c) $\vec{C} \mid (\vec{A} + \vec{B})$	(d) $\vec{C} \mid (\vec{A} \times \vec{B})$		(a) 0° (b) 30°
11.	If a particle of mass m is mov	ing with constant velocity v parallel to		(c) 45° (d) 60°
	<i>x</i> -axis in <i>x-y</i> plane as shown	in fig. Its angular momentum with	21.	A force $\vec{F} = 5\hat{i} + 6\hat{j} + 4\hat{k}$ acting on a body, produces a
	respect to origin at any time t	(b) $muh \hat{k}$		displacement $S = 6i - 5k$. Work done by the force is
	(a) $mvo \kappa$	(b) $-mvo\kappa$		(a) 10 units (b) 18 units
	(c) <i>mvb i</i>	(d) <i>mv i</i>		(c) 11 units (d) 5 units
12.	Consider two vectors $\vec{F}_1 =$	$\hat{F}_2 = \hat{i} + \hat{k}$ and $\vec{F}_2 = \hat{j} + \hat{k}$. The	22.	The angle between the two vectors $\vec{A} = \hat{5i} + \hat{5j}$ and
	magnitude of the scalar produc	t of these vectors is [MP PMT 1987]		$\vec{B} = 5\hat{i} - 5\hat{j}$ will be [CPMT 2000]
	(a) 20	(b) 23		(a) Zero (b) 45°
	(c) $5\sqrt{33}$	(d) 26		(c) 90° (d) 180°
13.	Consider a vector $\vec{F}=$	$4\hat{i} - 3\hat{j}$. Another vector that is	23.	The vector $\vec{P} = a\hat{i} + a\hat{j} + 3\hat{k}$ and $\vec{Q} = a\hat{i} - 2\hat{j} - \hat{k}$ are
	perpendicular to \overrightarrow{F} is			perpendicular to each other. The positive value of <i>a</i> is [AFMC 2000: AIIMS 2002]
	(a) $\hat{4i} + \hat{3j}$	(b) $\hat{6i}$		(a) 3 (b) 4
	(c) $7\hat{k}$	(d) $3\hat{i} - 4\hat{j}$		(c) 9 (d) 13
14	Two vectors \vec{A} and \vec{B} are at	right angles to each other when	24.	A body, constrained to move in the Y -direction is subjected to a
· - •	(a) $\vec{A} + \vec{B} = 0$	(b) $\vec{A} - \vec{B} = 0$		torce given by $I' = (-2i + 15j + 6k)N$. What is the work done by this force in moving the body a distance 10 <i>m</i> along the <i>Y</i> -axis
	(c) $\vec{A} \times \vec{B} = 0$	$\vec{A} \cdot \vec{B} = 0$		(a) 20 <i>J</i> (b) 150 <i>J</i>
	(-)	(-)		

(c) 160 *J* (d) 190 *J*

25.	A particle moves in the <i>x-y</i> plane under the action of a force \vec{F} such	
	that the value of its linear momentum (\vec{P}) at anytime t is	
	$P_x = 2\cos t, p_y = 2\sin t$. The angle θ between \vec{F} and \vec{P} at a	24
	given time <i>t</i> . will be [MNR 1991; UPSEAT 2000]	34.
	(a) $\theta = 0^{\circ}$ (b) $\theta = 30^{\circ}$	
	(c) $\theta = 90^{\circ}$ (d) $\theta = 180^{\circ}$	
26.	The area of the parallelogram represented by the vectors $\vec{A} = 2\hat{i} + 3\hat{j}$ and $\vec{B} = \hat{i} + 4\hat{j}$ is	35.
	(a) 14 units (b) 7.5 units	
	(c) 10 units (d) 5 units	26
27.	A vector \vec{F}_1 is along the positive X-axis. If its vector product with	30.
	another vector \vec{F}_2 is zero then \vec{F}_2 could be	
	[MP PMT 1987]	
	(a) $4\hat{j}$ (b) $-(\hat{i}+\hat{j})$	
	(a) $(\hat{i} + \hat{k})$ (d) $(\hat{A}\hat{i})$	
	(c) $(j+k)$ (d) $(-4i)$	
28.	If for two vectors \vec{A} and $\vec{B}, \vec{A} \times \vec{B} = 0$, the vectors	37.
	(a) Are perpendicular to each other	
	(b) Are parallel to each other	
	(c) Act at an angle of 60°	
	(d) Act at an angle of 30°	38.
29.	The angle between vectors $(\vec{A} \times \vec{B})$ and $(\vec{B} \times \vec{A})$ is	
	(a) Zero (b) π	
	(c) $\pi/4$ (d) $\pi/2$	39.
30.	What is the angle between $(\vec{P} + \vec{Q})$ and $(\vec{P} \times \vec{Q})$	
	(c) ρ (b) π	
	(a) 0 (b) $\frac{1}{2}$	40.
	(c) $\frac{\pi}{4}$ (d) π	
31.	The resultant of the two vectors having magnitude 2 and 3 is 1. What is their cross product	
	(a) 6 (b) 3	
	(c) 1 (d) 0	
32.	Let $\vec{A} = \hat{i}A\cos\theta + \hat{j}A\sin\theta$ be any vector. Another vector \vec{B} which is normal to A is [BHU 1997]	41.
	(a) $\hat{i} B \cos \theta + j B \sin \theta$ (b) $\hat{i} B \sin \theta + j B \cos \theta$	
	(c) $\hat{i}B\sin\theta - jB\cos\theta$ (d) $\hat{i}B\cos\theta - jB\sin\theta$	
33.	The angle between two vectors given by $6\overline{i} + 6\overline{j} - 3\overline{k}$ and	42.
	$7\dot{i} + 4\ddot{j} + 4\ddot{k}$ is [EAMCET (Engg.) 1999]	
	(a) $\cos^{-1}\left(\frac{1}{\sqrt{3}}\right)$ (b) $\cos^{-1}\left(\frac{5}{\sqrt{3}}\right)$	43.

(c) $\sin^{-1}\left(\frac{2}{\sqrt{3}}\right)$	(d) $\sin^{-1}\left(\frac{\sqrt{5}}{3}\right)$
A vector \overrightarrow{A} points vertically up	ward and \vec{B} points towards north.
The vector product $\overrightarrow{A} \times \overrightarrow{B}$ is	[UPSEAT 2000]
(a) Zero	(b) Along west
(c) Along east	(d) Vertically downward
Angle between the vectors $(\hat{i} + \hat{j})$) and $(\hat{j}-\hat{k})$ is
(a) 90°	(b) 0°
(c) 180°	(d) 60°
The position vectors of p $A = 2\hat{i} + 4\hat{i} + 5\hat{i}$ p $A\hat{i} + 5\hat{j}$	oints A , B , C and D are
$A = 3i + 4j + 5\kappa, B = 4i + 5j$	j + 6K, C = /i + 9j + 3K and
D = 4i + 6j then the displacen (a) Perpendicular (b) Parallel	nent vectors <i>AB</i> and <i>CD</i> are
(c) Antiparallel	
(d) Inclined at an angle of 60°	
If force $(\vec{F}) = 4\hat{i} + 5\hat{j}$ and disp work done is	elacement $(\hat{s}) = 3\hat{i} + 6\hat{k}$ then the [Manipal 1995]
(a) 4×3	(b) 5×6
(c) 6×3	(d) 4×6
If $ \vec{A} \times \vec{B} = \vec{A} \cdot \vec{B} $, then angle	e between \overrightarrow{A} and \overrightarrow{B} will be
	[AIIMS 2000; Manipal 2000]
(a) 30°	(b) 45°
(c) 60° In an clockwise system	(a) 90° [CPMT 1990]
(a) $\hat{i} \times \hat{k} = \hat{i}$	(b) $\hat{i} \cdot \hat{i} = 0$
(c) $\hat{i} \times \hat{i} = 1$	(d) $\hat{k} \hat{i} = 1$
(c) $j \land j = 1$	$(\mathbf{u}) \mathbf{k} \cdot \mathbf{j} = 1$
The linear velocity of a rotating bo	bdy is given by $v = \omega \times r$, where ω
is the angular velocity and r is the	e radius vector. The angular velocity
of a body is $\omega = i - 2j + 2k$ a	nd the radius vector $r = 4j - 3k$,
then $ v $ is	
(a) $\sqrt{29}$ units	(b) $\sqrt{31}$ units
(c) $\sqrt{37}$ units	(d) $\sqrt{41}$ units
Three vectors \vec{a}, \vec{b} and \vec{c} sa	tisfy the relation $\vec{a}.\vec{b}=0$ and
a.c = 0. The vector a is paralled	el to [AllMS 1996]
(a) \dot{b}	(b) <i>c</i>
(c) $\vec{b}.\vec{c}$	(d) $\vec{b} \times \vec{c}$
The diagonals of a parallelogram	are $2\hat{i}$ and $2\hat{j}$. What is the area
(a) 0.5 units	(b) 1 unit
(c) 2 units	(d) 4 units
What is the unit vector perpe	ndicular to the following vectors
2i+2j-k and $6i-3j+2k$	

- $\frac{\hat{i}+10\hat{j}-18\hat{k}}{5\sqrt{17}}$ (b) $\frac{\hat{i} - 10\hat{j} + 18\hat{k}}{5\sqrt{17}}$ (a) (d) $\frac{\hat{i} + 10\hat{j} + 18\hat{k}}{5\sqrt{17}}$ (c) $\frac{\hat{i} - 10\hat{j} - 18\hat{k}}{5\sqrt{17}}$
- The area of the parallelogram whose sides are represented by the 44. vectors $\hat{i} + 3\hat{k}$ and $\hat{i} + 2\hat{j} - \hat{k}$ is
 - (a) $\sqrt{61}$ sq.unit (b) $\sqrt{59}$ sq.unit
 - (c) $\sqrt{49}$ sq.unit (d) $\sqrt{52}$ sq.unit
- The position of a particle is given by $\vec{r} = (\vec{i} + 2\vec{j} \vec{k})$ momentum 45. $\vec{P} = (\vec{3}\vec{i} + 4\vec{j} - 2\vec{k})$. The angular momentum is perpendicular to
 - (a) *x*-axis
 - (b) y-axis
 - (c) z-axis
 - (d) Line at equal angles to all the three axes
- Two vector A and B have equal magnitudes. Then the vector A + B46. is perpendicular to
 - (a) $A \times B$ (b) *A* – *B*
 - (c) 3A 3B(d) All of these
- Find the torque of a force $\vec{F} = -3\hat{i} + \hat{j} + 5\hat{k}$ acting at the point 47. $\vec{r} = 7\hat{i} + 3\hat{j} + \hat{k}$

[CPMT 1997; CBSE PMT 1997; CET 1998; DPMT 2004]

(a)
$$14\hat{i} - 38\hat{j} + 16\hat{k}$$
 (b) $4\hat{i} + 4\hat{j} + 6\hat{k}$
(c) $21\hat{i} + 4\hat{j} + 4\hat{k}$ (d) $-14\hat{i} + 34\hat{j} - 16\hat{k}$

The value of $(\vec{A} + \vec{B}) \times (\vec{A} - \vec{B})$ is 48.

[RPET 1991, 2002; BHU 2002]

- (b) $A^2 B^2$ (a) 0
- (c) $\vec{B} \times \vec{A}$ (d) $2(\vec{B} \times \vec{A})$
- If \vec{A} and \vec{B} are perpendicular vectors and vector 49. $\vec{A} = 5\hat{i} + 7\hat{j} - 3\hat{k}$ and $\vec{B} = 2\hat{i} + 2\hat{j} - a\hat{k}$. The value of *a* is

[EAMCET 1991]

(a)	- 2	(b)	8
(c)	- 7	(d)	- 8

A force vector applied on a mass is represented as 50. $\vec{F} = 6\hat{i} - 8\hat{j} + 10\hat{k}$ and accelerates with $1 m/s^2$. What will be the mass of the body in kg.

[CMEET 1995]

- (a) $10\sqrt{2}$ (b) 20
- (c) $2\sqrt{10}$ (d) 10

Two adjacent sides of a parallelogram are represented by the two 51. vectors $\hat{i} + 2\hat{j} + 3\hat{k}$ and $3\hat{i} - 2\hat{j} + \hat{k}$. What is the area of parallelogram

[AMU 1997]

- (a) 8 (b) $8\sqrt{3}$
- (c) $3\sqrt{8}$ (d) 192
- The position vectors of radius are $2\hat{i} + \hat{j} + \hat{k}$ and $2\hat{i} 3\hat{j} + \hat{k}$ 52. while those of linear momentum are $2\hat{i} + 3\hat{j} - \hat{k}$. Then the angular momentum is [BHU 1997]
 - [EAMICET 2Engel/1998] (b) $4\hat{i} - 8\hat{k}$ (d) $4\hat{i} - 8\hat{k}$ (c) $2\hat{i} - 4\hat{j} + 2\hat{k}$
- What is the value of linear velocity, if $\vec{\omega} = 3\hat{i} 4\hat{j} + \hat{k}$ and 53. $\vec{r} = 5\hat{i} - 6\hat{j} + 6\hat{k}$ [CBSE PMT 1999; CPMT 1999, 2001;

Pb. PMT 2000; Pb. CET 2000]

- (a) $\hat{6i} 2\hat{i} + 3\hat{k}$ (b) $\hat{6i} - 2\hat{i} + 8\hat{k}$ (c) $\hat{4i} - 1\hat{3i} + \hat{6k}$ (d) $-1\hat{8i} - 1\hat{3j} + 2\hat{k}$
- Dot product of two mutual perpendicular vector is 54.

[Haryana CEET 2002]

[Orissa JEE 2003]

(a) 0 (b) 1 (c) ∞ (d) None of these

When $\vec{A} \cdot \vec{B} = -|A||B|$, then 55.

- (a) \vec{A} and \vec{B} are perpendicular to each other
- (b) \vec{A} and \vec{B} act in the same direction
- (c) \vec{A} and \vec{B} act in the opposite direction
- (d) \vec{A} and \vec{B} can act in any direction
- If $|\vec{A} \times \vec{B}| = \sqrt{3}\vec{A}.\vec{B}$, then the value of $|\vec{A} + \vec{B}|$ is 56.

[CBSE PMT 2004]

(a)
$$\left(A^2 + B^2 + \frac{AB}{\sqrt{3}}\right)^{1/2}$$
 (b) $A + B$
(c) $(A^2 + B^2 + \sqrt{3}AB)^{1/2}$ (d) $(A^2 + B^2 + AB)^{1/2}$

- A force $\vec{F} = 3\hat{i} + c\hat{j} + 2\hat{k}$ acting on a particle causes a displacement $\vec{S} = -4\hat{i} + 2\hat{j} - 3\hat{k}$ in its own direction. If the work done is 6*J*, then the value of *c* will be [DPMT 1997]
 - (a) 12 (b) 6 (c) 1 (d) 0

A force $\vec{F} = (\hat{5i} + \hat{3j})N$ is applied over a particle which displaces it 58. from its original position to the point $\vec{s} = (2\hat{i} - 1\hat{j})m$. The work done on the particle is [BHU 2001]

(a) + 11 J (b) + 7 *J* (c) + 13 J(d) -7/

57.

59. If a vector \vec{A} is parallel to another vector \vec{B} then the resultant of the vector $\vec{A} \times \vec{B}$ will be equal to

				•	
(a)	A	(b)	\vec{A}		
(c)	Zero vector	(d)	Zero		

Lami's Theorem

- **1.** *P*, *Q* and *R* are three coplanar forces acting at a point and are in equilibrium. Given *P* = 1.9318 *kg wt*, $\sin\theta_1 = 0.9659$, the value of *R* is (in *kg wt*) [CET 1998]
 - (a) 0.9659 (b) 2 (c) 1
 - (d) $\frac{1}{2}$
 - 2

(a) Four

2. A body is in equilibrium under the action of three coplanar forces *P*, *Q* and *R* as shown in the figure. Select the correct statement

(a) $\frac{P}{\sin\alpha} = \frac{Q}{\sin\beta} = \frac{R}{\sin\gamma}$ (b) $\frac{P}{\cos\alpha} = \frac{Q}{\cos\beta} = \frac{R}{\cos\gamma}$ (c) $\frac{P}{\tan\alpha} = \frac{Q}{\tan\beta} = \frac{R}{\tan\gamma}$ (d) $\frac{P}{\sin\beta} = \frac{Q}{\sin\gamma} = \frac{R}{\sin\alpha}$

3. If a body is in equilibrium under a set of non-collinear forces, then the minimum number of forces has to be

(b) Three

- (c) Two (d) Five
- How many minimum number of non-zero vectors in different planes can be added to give zero resultant
 - (a) 2 (b) 3
 - (c) 4 (d) 5
- 5. As shown in figure the tension in the horizontal cord is 30 N. The weight W and tension in the string OA in Newton are [DPMT 1992]



Relative Velocity

1. Two cars are moving in the same direction with the same speed 30 *km/hr*. They are separated by a distance of 5 *km*, the speed of a car moving in the opposite direction if it meets these two cars at an interval of 4 minutes, will be

(a) 40 *km/hr* (b) 45 *km/hr*

[Pb. CET 1996]

3.

5.

6.

7.

8.

9.

[AIIMS 2000]

- (d) 15 *km/hr*
- **2.** A man standing on a road hold his umbrella at 30° with the vertical to keep the rain away. He throws the umbrella and starts running at 10 *km/hr*. He finds that raindrops are hitting his head vertically, the speed of raindrops with respect to the road will be
 - (a) 10 *km/hr* (b) 20 *km/hr*
 - (c) 30 *km/hr* (d) 40 *km/hr*
 - In the above problem, the speed of raindrops *w.r.t.* the moving man, will be

(a)
$$10 / \sqrt{2} \, km / h$$
 (b) $5 \, km/h$

(c)
$$10\sqrt{3} \, km \, / \, h$$
 (d) $5 \, / \, \sqrt{3} \, km \, / \, h$

4. A boat is moving with a velocity 3i + 4j with respect to ground. The water in the river is moving with a velocity -3i - 4j with respect to ground. The relative velocity of the boat with respect to water is

(a)
$$8j$$
 (b) $-6i-8j$

(c)
$$6i + 8j$$
 (d) $5\sqrt{2}$

A 150 m long train is moving to north at a speed of 10 m/s. A parrot flying towards south with a speed of 5 m/s crosses the train. The tin**[AFMAGagda**] the parrot the cross to train would be:

(a)	30 s	(b)	15 s
(c)	8 s	(d)	10 s

- A river is flowing from east to west at a speed of 5 m/min. A man on south bank of river, capable of swimming 10m/min in still water, wants to swim across the river in shortest time. He should swim
 - (a) Due north
 - (b) Due north-east
 - (c) Due north-east with double the speed of river
 - (d) None of these
- A person aiming to reach the exactly opposite point on the bank of a stream is swimming with a speed of 0.5 *m/s* at an angle of 120 with the direction of flow of water. The speed of water in the stream is [CBSE PMT 1999]
 - (a) 1 *m/s* (b) 0.5 *m/s*
 - (c) 0.25 m/s (d) 0.433 m/s
- A moves with 65 km/h while *B* is coming back of *A* with 80 km/h. The relative velocity of *B* with respect to *A* is

				[AFMC 2000]
(a)	80 <i>km/h</i>	(b)	60 <i>km/h</i>	
(c)	15 <i>km/h</i>	(d)	145 <i>km/h</i>	

- A thief is running away on a straight road on a jeep moving with a speed of 9 m/s. A police man chases him on a motor cycle moving at a speed of 10 m/s. If the instantaneous separation of jeep from the motor cycle is 100 m, how long will it take for the policemen to catch the thief
 - (a) 1 second (b) 19 second
 - (c) 90 second (d) 100 second
- **10.** A man can swim with velocity v relative to water. He has to cross a river of width d flowing with a velocity u (u > v). The distance through which he is carried down stream by the river is x. Which of the following statement is correct
 - (a) If he crosses the river in minimum time $x = \frac{du}{v}$

- (b) *x* can not be less than $\frac{du}{dt}$
- (c) For *x* to be minimum he has to swim in a direction making an angle of $\frac{\pi}{2} + \sin^{-1}\left(\frac{\nu}{u}\right)$ with the direction of the flow of

water

- (d) x will be max. if he swims in a direction making an angle of $\frac{\pi}{2} + \sin^{-1}\frac{\nu}{u}$ with direction of the flow of water
- A man sitting in a bus travelling in a direction from west to east with a speed of 40 *km/h* observes that the rain-drops are falling vertically down. To the another man standing on ground the rain will appear
 [HP PMT 1999]
 - (a) To fall vertically down
 - $(b) \quad \text{To fall at an angle going from west to east} \\$
 - (c) To fall at an angle going from east to west
 - (d) The information given is insufficient to decide the direction of rain.
- A boat takes two hours to travel 8 km and back in still water. If the velocity of water is 4 km/h, the time taken for going upstream 8 km and coming back is [EAMCET 1990]
 - (a) 2*h*
 - (b) 2h 40 min
 - (c) 1h 20 min
 - (d) Cannot be estimated with the information given
- 13. A 120 m long train is moving towards west with a speed of 10 m/s. A bird flying towards east with a speed of 5 m/s crosses the train. The time taken by the bird to cross the train will be

(a)	16 <i>sec</i>	(b)	12 <i>sec</i>
(c)	10 <i>sec</i>	(d)	8 sec

14. A boat crosses a river with a velocity of 8 km/h. If the resulting velocity of boat is 10 km/h then the velocity of river water is

(a)	4 <i>km/h</i>	((b)	6 <i>km/h</i>

(c) 8 *km/h* (d) 10 *km/h*

Critical Thinking

Objective Questions

1. If a vector \vec{P} making angles α , β , and γ respectively with the X, Y and Z axes respectively.

Then $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma =$ (a) 0 (b) 1 (c) 2 (d) 3

2. If the resultant of *n* forces of different magnitudes acting at a point is zero, then the minimum value of *n* is [SCRA 2000]

(a)	1	(b)	2
(c)	3	(d)	4

Can the resultant of 2 vectors be zero [111T 2000]

(a) Yes, when the 2 vectors are same in magnitude and direction

(b) No

- (c) Yes, when the 2 vectors are same in magnitude but opposite in sense
- (d) Yes, when the 2 vectors are same in magnitude making an angle of $\frac{2\pi}{2}$ with each other

5.

3.

- The sum of the magnitudes of two forces acting at point is 18 and the magnitude of their resultant is 12. If the resultant is at 90° with the force of smaller magnitude, what are the, magnitudes of forces [**Roorkee 199**]
- (a) 12, 5 (b) 14, 4
- (c) 5, 13 (d) 10, 8

A vector \vec{a} is turned without a change in its length through a small angle $d\theta$. The value of $|\vec{\Delta a}|$ and Δa are respectively

- (a) $0, a d\theta$ (b) $a d\theta, 0$
- (c) 0, 0 (d) None of these
- **6.** Find the resultant of three vectors $\overrightarrow{OA}, \overrightarrow{OB}$ and \overrightarrow{OC} shown in the following figure. Radius of the circle is *R*.



Figure shows *ABCDEF* as a regular hexagon. What is the value of $\overrightarrow{AB} + \overrightarrow{AC} + \overrightarrow{AD} + \overrightarrow{AE} + \overrightarrow{AF}$ *E D*



The length of second's hand in watch is 1 *cm.* The change in velocity of its tip in 15 seconds is [MP PMT 1987]

(a) Zero (b)
$$\frac{\pi}{30\sqrt{2}}$$
 cm/sec

(c)
$$\frac{\pi}{30} cm / \sec$$
 (d) $\frac{\pi\sqrt{2}}{30} cm / \sec$

A particle moves towards east with velocity 5 m/s. After 10 seconds its direction changes towards north with same velocity. The average acceleration of the particle is

[CPMT 1997; IIT-JEE 1982]

9.

8.

7.

(a) Zero

(b)
$$\frac{1}{\sqrt{2}}m/s^2 N-W$$

(c)
$$\frac{1}{\sqrt{2}}m/s^2 N - E$$
 (d) $\frac{1}{\sqrt{2}}m/s^2 S - W$

10. A force $\vec{F} = -K(\hat{y}\hat{i} + x\hat{j})$ (where *K* is a positive constant) acts on a particle moving in the *x-y* plane. Starting from the origin, the particle is taken along the positive *x-* axis to the point (*a*, 0) and then parallel to the *y*-axis to the point (*a*, *a*). The total work done by the forces \vec{F} on the particle is

[IIT-JEE 1998]

(a)
$$-2 Ka^2$$
 (b) $2 Ka^2$

(c)
$$-Ka^2$$
 (d) Ka^2

11. The vectors from origin to the points *A* and *B* are $\vec{A} = 3\hat{i} - 6\hat{j} + 2\hat{k}$ and $\vec{B} = 2\hat{i} + \hat{j} - 2\hat{k}$ respectively. The area of the triangle *OAB* be

(a)
$$\frac{5}{2}\sqrt{17}$$
 sq.unit
(b) $\frac{2}{5}\sqrt{17}$ sq.unit
(c) $\frac{3}{5}\sqrt{17}$ sq.unit
(d) $\frac{5}{3}\sqrt{17}$ sq.unit

12. A metal sphere is hung by a string fixed to a wall. The sphere is pushed away from the wall by a stick. The forces acting on the sphere are shown in the second diagram. Which of the following statements is wrong

(a)
$$P = W \tan \theta$$

(b) $\vec{T} + \vec{P} + \vec{W} = 0$
(c) $T^2 = P^2 + W^2$
(d) $T = P + W$

13. The speed of a boat is $5 \frac{km}{h}$ in still water. It crosses a river of width 1 km along the shortest possible path in 15 minutes. The velocity of the river water is

		[IIT 1988; CBSE PMT 1998, 2000]
(a)	1 <i>km/h</i>	(b) 3 <i>km/h</i>
(c)	4 km/h	(d) 5 <i>km/h</i>

- 14. A man crosses a 320 m wide river perpendicular to the current in 4 minutes. If in still water he can swim with a speed 5/3 times that of the current, then the speed of the current, in m/min is
 - (a) 30 (b) 40
 - (c) 50 (d) 60.

Assertion & Reason For AllMS Aspirants

Read the assertion and reason carefully to mark the correct option out of the options given below:

- (a) If both assertion and reason are true and the reason is the correct explanation of the assertion.
- (b) If both assertion and reason are true but reason is not the correct explanation of the assertion.
- (c) If assertion is true but reason is false.

- (d) If the assertion and reason both are false.
- (e) If assertion is false but reason is true.

1.	Assertion	:	$\vec{A} \times \vec{B}$ is perpendicular to both $\vec{A} + \vec{B}$ as well as $\vec{A} - \vec{B}$.
	Reason	:	$\vec{A} + \vec{B}$ as well as $\vec{A} - \vec{B}$ lie in the plane containing \vec{A} and \vec{B} , but $\vec{A} \times \vec{B}$ lies perpendicular to the plane containing \vec{A} and \vec{B} .
2.	Assertion	:	Angle between $\hat{i} + \hat{j}$ and \hat{i} is 45°
	Reason	:	$\hat{i} + \hat{j}$ is equally inclined to both \hat{i} and \hat{j} and the
			angle between \hat{i} and \hat{j} is 90°
3.	Assertion	:	If θ be the angle between \vec{A} and \vec{B} , then $\tan \theta = \frac{\vec{A} \times \vec{B}}{\vec{A} \cdot \vec{P}}$
	Reason	:	$A \times B$ is perpendicular to $A.B$
4.	Assertion	:	If $ A + B = A - B $, then angle between A
			and B is 90°
	Reason	:	$\vec{A} + \vec{B} = \vec{B} + \vec{A}$
5.	Assertion	:	Vector product of two vectors is an axial vector
	Reason	:	If \vec{v} = instantaneous velocity, \vec{r} = radius vector and
~			$\vec{\omega}$ = angular velocity, then $\vec{\omega} = v \times r$.
0.	Assertion	:	Minimum number of non-equal vectors in a plane required to give zero resultant is three.
	Reason	:	If $\vec{A} + \vec{B} + \vec{C} = \vec{0}$, then they must lie in one plane
7.	Assertion	:	Relative velocity of <i>A w.r.t. B</i> is greater than the velocity of either, when they are moving in opposite directions.
	Reason	:	Relative velocity of A w.r.t. $B = \vec{v}_A - \vec{v}_B$
8.	Assertion	:	Vector addition of two vectors \vec{A} and \vec{B} is commutative.
	Reason	:	$\vec{A} + \vec{B} = \vec{B} + \vec{A}$
9.	Assertion	:	$\vec{A}.\vec{B} = \vec{B}.\vec{A}$
	Reason	:	Dot product of two vectors is commutative.
10.	Assertion	:	$\vec{\tau} = \vec{r} \times F$ and $\vec{\tau} \neq F \times \vec{r}$
n.	Reason Assertion [1	: Roorl	A negative acceleration of a body is associated with a slowing down of a body.
	Reason	:	Acceleration is vector quantity.
12.	Assertion	:	A physical quantity cannot be called as a vector if its magnitude is zero.
	Reason	:	A vector has both, magnitude and direction.
13.	Assertion Reason	:	The sum of two vectors can be zero. The vector cancel each other, when they are equal and opposite
14.	Assertion	:	Two vectors are said to be like vectors if they have same direction but different magnitude.
	Reason	:	Vector quantities do not have specific direction.
15.	Assertion Reason	:	I he scalar product of two vectors can be zero. If two vectors are perpendicular to each other. their
16.	Assertion	:	scalar product will be zero. Multiplying any vector by an scalar is a meaningful
	Reason	:	operations. In uniform motion speed remains constant.

Vectors 19

	20 V	ectors
17.	Assertion	: A null vector is a vector whose magnitude is zero and direction is arbitrary.
	Reason	: A null vector does not exist.
18.	Assertion	: If dot product and cross product of $ec{A}$ and $ec{B}$ are
		zero, it implies that one of the vector \overrightarrow{A} and \overrightarrow{B} must be a null vector.
	Reason	: Null vector is a vector with zero magnitude.
19.	Assertion	: The cross product of a vector with itself is a null vector.
	Reason	: The cross-product of two vectors results in a vector quantity.
20.	Assertion	: The minimum number of non coplanar vectors whose sum can be zero, is four.
	Reason	: The resultant of two vectors of unequal magnitude can be zero.
21.	Assertion	: If $\vec{A}.\vec{B} = \vec{B}.\vec{C}$, then \vec{A} may not always be equal to \vec{C}
	Reason	: The dot product of two vectors involves cosine of the angle between the two vectors.
22.	Assertion	: Vector addition is commutative.
	Reason	: $(\vec{A} + \vec{B}) \neq (\vec{B} + \vec{A}).$

Г



Fundamentals of Vectors

1	d	2	b	3	C	4	d	5	d
6	а	7	а	8	b	9	b	10	d
11	d	12	d	13	а	14	b	15	С
16	С	17	а	18	b	19	С	20	С
21	d	22	d	23	b	24	d	25	b
26	b	27	а	28	а	29	а	30	d
31	а	32	b	33	а	34	а		

Addition and Subtraction of Vectors

1	а	2	b	3	d	4	b	5	b
6	a	7	b	8	а	9	d	10	b
11	d	12	C	13	a	14	C	15	C
16	С	17	C	18	C	19	C	20	b
21	а	22	d	23	d	24	а	25	C
26	b	27	b	28	а	29	b	30	а
31	C	32	C	33	C	34	d	35	a
36	С	37	d	38	а	39	C	40	d
41	а	42	b	43	d	44	d	45	a
46	C	47	d	48	a	49	а	50	C
51	C	52	a	53	d				

Multiplication of Vectors

1	с	2	b	3	d	4	a	5	а
6	b	7	c	8	b	9	b	10	d
11	b	12	d	13	C	14	d	15	с
16	С	17	b	18	C	19	b	20	a
21	а	22	c	23	a	24	b	25	c
26	d	27	d	28	b	29	b	30	b
31	d	32	c	33	d	34	b	35	d
36	b	37	a	38	b	39	а	40	a
41	d	42	d	43	C	44	b	45	a
46	а	47	a	48	d	49	d	50	а
51	b	52	b	53	d	54	а	55	c
56	d	57	a	58	b	59	C		

Lami's Theorem									
1	C	2	а	3	b	4	C	5	b

Relative Velocity

1	b	2	b	3	C	4	c	5	d
6	а	7	C	8	C	9	d	10	ac
11	b	12	b	13	d	14	b		

Critical Thinking Questions

1	с	2	с	3	с	4	с	5	b
6	b	7	d	8	d	9	b	10	C
11	а	12	d	13	b	14	d		

Assertion and Reason

1	а	2	а	3	d	4	b	5	c
6	b	7	а	8	b	9	а	10	С
11	b	12	е	13	а	14	C	15	а
16	b	17	С	18	b	19	b	20	C
21	а	22	C						

Fundamentals of Vectors

C Answers and Solutions

- (d) As the multiple of \hat{j} in the given vector is zero therefore this vector lies in XZ plane and projection of this vector on *y*-axis is zero.
- (b) If a point have coordinate (x, y, z) then its position vector = $x\hat{i} + y\hat{j} + z\hat{k}$.

 \hat{j}

(c) Displacement vector
$$\vec{r} = \Delta x \hat{i} + \Delta y \hat{j} + \Delta z \hat{k}$$

$$= (3-2)\hat{i} + (4-3)\hat{j} + (5-5)\hat{k} = \hat{i} + \hat{i} + (5-5)\hat{k} = \hat{i} + \hat$$

Y †

1.

2.

3.

5.

6.

 $F \sin 60^{\circ}$ The component of force in vertical direction

$$=F\cos\theta = F\cos 60^\circ = 5 \times \frac{1}{2} = 2.5 N$$

(d)
$$|B| = \sqrt{7^2 + (24)^2} = \sqrt{625} = 25$$

Unit vector in the direction of *A* will be $\hat{A} = \frac{3\hat{i} + 4\hat{j}}{5}$

So required vector =
$$25\left(\frac{3\hat{i}+4\hat{j}}{5}\right) = 15\hat{i}+20\hat{j}$$

(a) Let the components of \vec{A} makes angles α , β and γ with x, yand z axis respectively then $\alpha = \beta = \gamma$

$$\cos^{2} \alpha + \cos^{2} \beta + \cos^{2} \gamma = 1$$

$$\Rightarrow 3 \cos^{2} \alpha = 1 \Rightarrow \cos \alpha = \frac{1}{\sqrt{3}}$$

$$\therefore A_{x} = A_{y} = A_{z} = A \cos \alpha = \frac{A}{\sqrt{3}}$$
7. (a) $\vec{A} = 2\hat{i} + 4\hat{j} - 5\hat{k} \therefore | \vec{A}| = \sqrt{(2)^{2} + (4)^{2} + (-5)^{2}} = \sqrt{45}$

$$\therefore \cos \alpha = \frac{2}{\sqrt{45}}, \quad \cos \beta = \frac{4}{\sqrt{45}}, \quad \cos \gamma = \frac{-5}{\sqrt{45}}$$
8. (b) Unit vector along y axis $= \hat{j}$ so the required vector
$$= \hat{j} - [(\hat{i} - 3\hat{j} + 2\hat{k}) + (3\hat{i} + 6\hat{j} - 7\hat{k})] = -4\hat{i} - 2\hat{j} + 5\hat{k}$$
9. (b) $\vec{F}_{3} = \vec{F}_{1} + \vec{F}_{2}$
There should be minimum three coplaner
vectors having different magnitude which
should be added to give zero resultant
10. (d) Diagonal of the hall = $\sqrt{l^{2} + b^{2} + h^{2}}$

$$= \sqrt{10^{2} + 12^{2} + 14^{2}}$$

$$= \sqrt{100 + 144 + 196}$$

$$= \sqrt{400} = 20m$$

(d) Total angle = $100 \times \frac{\pi}{50} = 2\pi$ 11.

> So all the force will pass through one point and all forces will be balanced. *i.e.* their resultant will be zero.

12. (d)
$$\vec{r} = \vec{r_2} - \vec{r_1} = (-2\hat{i} - 2\hat{j} + 0\hat{k}) - (4\hat{i} - 4\hat{j} + 0\hat{k})$$

 $\Rightarrow \vec{r} = -6\hat{i} + 2\hat{j} + 0\hat{k}$
 $\therefore |\vec{r}| = \sqrt{(-6)^2 + (2)^2 + 0^2} = \sqrt{36 + 4} = \sqrt{40} = 2\sqrt{10}$
13. (a) $\vec{P} = \frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{j} \therefore |\vec{P}| = \sqrt{\left(\frac{1}{\sqrt{2}}\right)^2 + \left(\frac{1}{\sqrt{2}}\right)^2} = 1$
 \therefore It is a unit vector.

(b)

15. (c)
$$\hat{R} = \frac{\vec{R}}{|R|} = \frac{\hat{i} + \hat{j}}{\sqrt{1^2 + 1^2}} = \frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{j}$$

16. (c)
$$\vec{R} = 3\hat{i} + \hat{j} + 2\hat{k}$$

$$\therefore$$
 Length in XY plane = $\sqrt{R_x^2 + R_y^2} = \sqrt{3^2 + 1^2} = \sqrt{10}$

 $(a) \quad \mbox{If the angle between all forces which are equal and lying in one }$ 17. plane are equal then resultant force will be zero.

18. (b)
$$\vec{A} = \hat{i} + \hat{j} \Rightarrow |A| = \sqrt{1^2 + 1^2} = \sqrt{2}$$

 $\cos \alpha = \frac{A_x}{|A|} = \frac{1}{\sqrt{2}} = \cos 45^\circ \therefore \alpha = 45^\circ$

19. (c)

14.

20. (c) (d) All quantities are tensors. 21.

(d) $\vec{P} + \vec{Q} = P\hat{P} + Q\hat{Q}$ 22.

(b) $\vec{r} = (a\cos\omega t)\hat{i} + (a\sin\omega t)\hat{j}$ 23.

 \vec{v}

$$=\frac{d\vec{r}}{dt}=-a\omega\sin\omega\,t\,\hat{i}+a\omega\cos\omega\,t\,\hat{j}$$

As $\vec{r}.\vec{v} = 0$ therefore velocity of the particle is perpendicular to the position vector.

$$\Rightarrow \sqrt{(0.5)^2 + (0.8)^2 + c^2} = 1$$

By solving we get
$$c = \sqrt{0.11}$$

25.

Displacement
$$\overrightarrow{AC} = \overrightarrow{AB} + \overrightarrow{BC}$$

$$AC = \sqrt{(AB)^2 + (BC)^2} = \sqrt{(400)^2 + (300)^2} = 500m$$

Distance $= AB + BC = 400 + 300 = 700m$

(a) Resultant of vectors \vec{A} and \vec{B} 27.

$$\vec{R} = \vec{A} + \vec{B} = 4\hat{i} + 3\hat{j} + 6\hat{k} - \hat{i} + 3\hat{j} - 8\hat{k}$$
$$\vec{R} = 3\hat{i} + 6\hat{j} - 2\hat{k}$$
$$\hat{R} = \frac{\vec{R}}{|\vec{R}|} = \frac{3\hat{i} + 6\hat{j} - 2\hat{k}}{\sqrt{3^2 + 6^2 + (-2)^2}} = \frac{3\hat{i} + 6\hat{j} - 2\hat{k}}{7}$$

28. (a)
$$\phi = \vec{B}.\vec{A}$$
. In this formula \vec{A} is a area vector.

29. (a)
$$\vec{r} = \vec{a} + \vec{b} + \vec{c} = 4\hat{i} - \hat{j} - 3\hat{i} + 2\hat{j} - \hat{k} = \hat{i} + \hat{j} - \hat{k}$$

$$\hat{r} = \frac{\vec{r}}{|r|} = \frac{\hat{i} + \hat{j} - \hat{k}}{\sqrt{1^2 + 1^2 + (-1)^2}} = \frac{\hat{i} + \hat{j} - \hat{k}}{\sqrt{3}}$$

30. (d)
$$\cos \theta = \frac{\vec{A} \cdot \vec{B}}{|A|||B|} = \frac{9 + 16 + 25}{\sqrt{9 + 16 + 25}\sqrt{9 + 16 + 25}} = \frac{50}{50} = 1$$

 $\Rightarrow \cos \theta = 1 \therefore \theta = \cos^{-1}(1)$

31. (a)
$$\vec{r} = 3t^2\hat{i} + 4t^2\hat{j} + 7\hat{k}$$

at $t = 0$, $\vec{r_1} = 7\hat{k}$
at $t = 10 \sec$, $\vec{r_2} = 300\hat{i} + 400\hat{j} + 7\hat{k}$,
 $\vec{\Delta r} = \vec{r_2} - \vec{r_1} = 300\hat{i} + 400\hat{j}$
 $|\vec{\Delta r}| = |\vec{r_2} - \vec{r_1}| = \sqrt{(300)^2 + (400)^2} = 500m$

32. (b) Resultant of vectors
$$\vec{A}$$
 and \vec{B}
 $\vec{R} = \vec{A} + \vec{B} = 4\hat{i} - 3\hat{j} + 8\hat{i} + 8\hat{j} = 12\hat{i} + 5\hat{j}$
 $\hat{R} = \frac{\vec{R}}{|R|} = \frac{12\hat{i} + 5\hat{j}}{\sqrt{(12)^2 + (5)^2}} = \frac{12\hat{i} + 5\hat{j}}{13}$

Á

33. (a)
$$\frac{\vec{A}.\vec{B}}{|\vec{i}+\vec{j}|} = \frac{(2\hat{i}+3\hat{j})(\hat{i}+\hat{j})}{\sqrt{2}} = \frac{2+3}{\sqrt{2}} = \frac{5}{\sqrt{2}}$$

34. (a) $\cos\theta = \frac{\vec{A}.\vec{B}}{|A|||B|} = \frac{(3\hat{i}+4\hat{j}+5\hat{k})(3\hat{i}+4\hat{j}-5\hat{k})}{\sqrt{9+16+25}\sqrt{9+16+25}}$
 $= \frac{9+16-25}{50} = 0$
 $\Rightarrow \cos\theta = 0, \therefore \theta = 90^{\circ}$

Addition and Subtraction of Vectors

1. (a) For 17 *N* both the vector should be parallel *i.e.* angle between them should be zero.

For 7 $\,N$ both the vectors should be antiparallel $\it i.e.$ angle between them should be 180°

For 13 $\,N$ both the vectors should be perpendicular to each other i.e. angle between them should be 90°

2. (b) $\vec{A} + \vec{B} = 4\hat{i} - 3\hat{j} + 6\hat{i} + 8\hat{j} = 10\hat{i} + 5\hat{j}$ $|\vec{A} + \vec{B}| = \sqrt{(10)^2 + (5)^2} = 5\sqrt{5}$

$$\tan \theta = \frac{5}{10} = \frac{1}{2} \implies \theta = \tan^{-1} \left(\frac{1}{2}\right)$$

3. (d) From figure

4. (b) Let \hat{n}_1 and \hat{n}_2 are the two unit vectors, then the sum is

$$\vec{n}_s = \hat{n}_1 + \hat{n}_2$$
 or $n_s^2 = n_1^2 + n_2^2 + 2n_1n_2\cos\theta$
= 1 + 1 + 2 cos θ

Since it is given that n_s is also a unit vector, therefore

$$1 = 1 + 1 + 2\cos\theta \Rightarrow \cos\theta = -\frac{1}{2} \therefore \theta = 120^{\circ}$$

Now the difference vector is $\hat{n}_d = \hat{n}_1 - \hat{n}_2$ or $n_d^2 = n_1^2 + n_2^2 - 2n_1n_2\cos\theta = 1 + 1 - 2\cos(120^\circ)$

:.
$$n_d^2 = 2 - 2(-1/2) = 2 + 1 = 3 \implies n_d = \sqrt{3}$$

5. (b) $\vec{A} - 2\vec{B} + 3\vec{C} = (2\hat{i} + \hat{j}) - 2(3\hat{j} - \hat{k}) + 3(6\hat{i} - 2\hat{k})$ = $2\hat{i} + \hat{j} - 6\hat{j} + 2\hat{k} + 18\hat{i} - 6\hat{k} = 20\hat{i} - 5\hat{j} - 4\hat{k}$

6. (a)
$$\vec{P}_1 = mv\sin\theta \hat{i} - mv\cos\theta \hat{j}$$

and $\vec{P}_2 = mv\sin\theta \hat{i} + mv\cos\theta \hat{j}$

So change in momentum

$$\overrightarrow{\Delta P} = \overrightarrow{P}_2 - \overrightarrow{P}_1 = 2mv\cos\theta \hat{i}, |\Delta \overrightarrow{P}| = 2mv\cos\theta$$

7. (b)
$$R = \sqrt{A^2 + B^2 + 2AB\cos\theta}$$

By substituting, $A = F$, $B = F$ and $R = F$ we get
 $\cos\theta = \frac{1}{2}$: $\theta = 120^{\circ}$

8.

9.

(a)

(d) If two vectors \vec{A} and \vec{B} are given then the resultant $R_{\text{max}} = A + B = 7N$ and $R_{\text{min}} = 4 - 3 = 1N$ *i.e.* net force on the particle is between 1 N and 7 N.

10. (b) If \vec{C} lies outside the plane then resultant force can not be zero.

12.

13.

(c)
$$F = \sqrt{F_1^2 + F_2^2 + 2F_1F_2\cos 90^\circ} = \sqrt{F_1^2 + F_2^2}$$

(a)

14. (c)

15. (c)
$$C = \sqrt{A^2 + B^2}$$

The angle between *A* and *B* is $\frac{\pi}{2}$

16. (c)
$$\vec{R} = \vec{A} + \vec{B} = 6\hat{i} + 7\hat{j} + 3\hat{i} + 4\hat{j} = 9\hat{i} + 11\hat{j}$$

 $\therefore |\vec{R}| = \sqrt{9^2 + 11^2} = \sqrt{81 + 121} = \sqrt{202}$
17. (c) $R = \sqrt{12^2 + 5^2 + 6^2} = \sqrt{144 + 25 + 36} = \sqrt{205} = 14.31 \text{ m}$

18. (c)
$$\vec{A} = 3\hat{i} - 2\hat{j} + \hat{k}$$
, $\vec{B} = \hat{i} - 3\hat{j} + 5\hat{k}$, $\vec{C} = 2\hat{i} - \hat{j} + 4\hat{k}$
 $|\vec{A}| = \sqrt{3^2 + (-2)^2 + 1^2} = \sqrt{9 + 4 + 1} = \sqrt{14}$
 $|\vec{B}| = \sqrt{1^2 + (-3)^2 + 5^2} = \sqrt{1 + 9 + 25} = \sqrt{35}$
 $|\vec{A}| = \sqrt{2^2 + 1^2 + (-4)^2} = \sqrt{4 + 1 + 16} = \sqrt{21}$
 $\Delta a = R = \sqrt{A^2 + C^2}$ therefore ARC will be right of

As $B = \sqrt{A^2 + C^2}$ therefore *ABC* will be right angled triangle.

20. (b)
$$\vec{C} + \vec{A} = \vec{B}$$
.

The value of C lies between A - B and A + B

$$\therefore |\vec{C}| < |\vec{A}|$$
 or $|\vec{C}| < |\vec{B}|$

21. (a) **22.** (d)

23.

24.

(d) Here all the three force will not keep the particle in equilibrium so the net force will not be zero and the particle will move with an acceleration.

(a)
$$A + B = 16$$
 (given) ...(i)
 $\tan \alpha = \frac{B \sin \theta}{A + B \cos \theta} = \tan 90^{\circ}$
 $\therefore A + B \cos \theta = 0 \Rightarrow \cos \theta = \frac{-A}{B}$...(ii)

 $8 = \sqrt{A^2 + B^2 + 2AB\cos\theta}$...(iii) By solving eq. (i), (ii) and (iii) we get A = 6N, B = 10N(c) $|\vec{P}| = 5$, $|\vec{Q}| = 12$ and $|\vec{R}| = 13$ 25. $\cos\theta = \frac{Q}{R} = \frac{12}{13}$ \vec{Q} $\therefore \ \theta = \cos^{-1}\left(\frac{12}{13}\right)$ $\rightarrow P$ (b) $\frac{B}{2} = \sqrt{A^2 + B^2 + 2AB\cos\theta}$ 26. ...(i) $\therefore \tan 90^\circ = \frac{B\sin\theta}{A+B\cos\theta} \Rightarrow A+B\cos\theta = 0$ $\therefore \cos \theta = -\frac{A}{B}$ Hence, from (i) $\frac{B^2}{4} = A^2 + B^2 - 2A^2 \implies A = \sqrt{3} \frac{B}{2}$ $\Rightarrow \cos\theta = -\frac{A}{B} = -\frac{\sqrt{3}}{2}$: $\theta = 150^{\circ}$ (b) $(\hat{i} - 2\hat{j} + 2\hat{k}) + (2\hat{i} + \hat{j} - \hat{k}) + \vec{R} = i$ 27. \therefore Required vector $\vec{R} = -2\hat{i} + \hat{j} - \hat{k}$ (a) Resultant $\vec{R} = \vec{P} + \vec{Q} + \vec{P} - \vec{Q} = 2\vec{P}$ 28. The angle between \vec{P} and $2\vec{P}$ is zero. 29. (b) $\uparrow R$ λ

$$\Rightarrow \tan 90^\circ = \frac{Q \sin \theta}{P + Q \cos \theta} \Rightarrow P + Q \cos \theta = 0$$
$$\cos \theta = \frac{-P}{Q} \therefore \theta = \cos^{-1} \left(\frac{-P}{Q}\right)$$

30. (a) According to problem P + Q = 3 and P - Q = 1

By solving we get
$$P = 2$$
 and $Q = 1$ \therefore $\frac{P}{Q} = 2 \Rightarrow P = 2Q$

31. (c)

- **32.** (c)
- **33.** (c)

34. (d)
$$F_1 + F_2 + F_3 = 0 \Rightarrow 4\hat{i} + 6\hat{j} + F_3 = 0$$

 $\therefore \vec{F}_3 = -4\hat{i} - 6\hat{j}$
35. (a) $\Delta v = 2v \sin\left(\frac{\theta}{2}\right) = 2 \times v \times \sin 90^\circ$
 $= 2 \times 100 = 200 \ km/hr$

36. (c)

37. (d) Resultant velocity
$$= \sqrt{20^2 + 15^2}$$

 $= \sqrt{400 + 225} = \sqrt{625} = 25 \ km/hr$

38. (a)
$$C = \sqrt{A^2 + B^2}$$

 $= \sqrt{3^2 + 4^2} = 5$
 \therefore Angle between \vec{A} and \vec{B} is $\frac{\pi}{2}$
39. (c)
40. (d) $\vec{-v_1} \leftarrow \vec{-v_1} \leftarrow \vec{v_1} \leftarrow \vec{v_1} \leftarrow \vec{v_1} \leftarrow \vec{v_1} \leftarrow \vec{v_2} \leftarrow \vec{v_1} \leftarrow \vec{v_1} \leftarrow \vec{v_1} \leftarrow \vec{v_2} \leftarrow \vec{v_1} \leftarrow \vec{v_2} \leftarrow \vec{v_1} \leftarrow \vec{$

If the magnitude of vector remains same, only direction change by $\boldsymbol{\theta}$ then

$$\overrightarrow{\Delta v} = \overrightarrow{v_2} - \overrightarrow{v_1}$$
, $\overrightarrow{\Delta v} = \overrightarrow{v_2} + (-\overrightarrow{v_1})$

Magnitude of change in vector $|\overrightarrow{\Delta v}| = 2v \sin\left(\frac{\theta}{2}\right)$

$$|\overrightarrow{\Delta v}| = 2 \times 10 \times \sin\left(\frac{90^\circ}{2}\right) = 10\sqrt{2} = 14.14 \, m \, / \, s$$

Direction is south-west as shown in figure.

a. (a)
$$\overrightarrow{AC} = \overrightarrow{AB} + \overrightarrow{BC}$$

 $AC = \sqrt{(AB)^2 + (BC)^2}$
 $= \sqrt{(10)^2 + (20)^2}$
 $= \sqrt{100 + 400} = \sqrt{500} = 22.36 \, km$
42. (b) $\cos \theta = \frac{\overrightarrow{F_1} \cdot \overrightarrow{F_2}}{||F_1||||F_2||}$
 $= \frac{(5\hat{i} + 10\hat{j} - 20\hat{k}) \cdot (10\hat{i} - 5\hat{j} - 15\hat{k})}{\sqrt{25 + 100 + 400}\sqrt{100 + 25 + 225}} = \frac{50 - 50 + 300}{\sqrt{525}\sqrt{350}}$

$$\Rightarrow \cos\theta = \frac{1}{\sqrt{2}}$$
 $\therefore \ \theta = 45^{\circ}$

43. (d) If two vectors A and B are given then Range of their resultant can be written as $(A - B) \le R \le (A + B)$.

i.e.
$$R_{\max} = A + B$$
 and $R_{\min} = A - B$

If B = 1 and A = 4 then their resultant will lies in between 3N and 5N. It can never be 2N.

44. (d)
$$A = 3N$$
, $B = 2N$ then $R = \sqrt{A^2 + B^2} + 2AB\cos\theta$

$$R = \sqrt{9 + 4 + 12\cos\theta} \qquad \dots (i)$$

Now A = 6N, B = 2N then

$$2R = \sqrt{36 + 4} + 24\cos\theta \qquad \dots (ii)$$

from (i) and (ii) we get $\cos\theta = -\frac{1}{2}$: $\theta = 120^{\circ}$

45. (a) In *N* forces of equal magnitude works on a single point and their resultant is



zero then angle between any two forces is given

$$\theta = \frac{360}{N} = \frac{360}{3} = 120^{\circ}$$

If these three vectors are represented by three sides of triangle then they form equilateral triangle

- (c) Resultant of two vectors \vec{A} and \vec{B} can be given by 46. $\vec{R} = \vec{A} + \vec{B}$ $|\vec{R}| = |\vec{A} + \vec{B}| = \sqrt{A^2 + B^2 + 2AB\cos\theta}$ If $\theta = 0^{\circ}$ then $|\vec{R}| = A + B = |\vec{A}| + |\vec{B}|$ (d) $R_{\text{max}} = A + B = 17$ when $\theta = 0^{\circ}$ 47. $R_{\min} = A - B = 7$ when $\theta = 180^{\circ}$ by solving we get A = 12 and B = 5Now when $\theta = 90^{\circ}$ then $R = \sqrt{A^2 + B^2}$ $\Rightarrow R = \sqrt{(12)^2 + (5)^2} = \sqrt{169} = 13$ (a) If two vectors are perpendicular then their dot product must 48. be equal to zero. According to problem $\overrightarrow{}$ $\overrightarrow{}$ $\overrightarrow{}$ $\overrightarrow{}$ $\overrightarrow{}$ $\overrightarrow{A} \overrightarrow{A} \overrightarrow{A} \overrightarrow{A} \overrightarrow{D} \overrightarrow{D} \overrightarrow{D} \overrightarrow{A}$ $\vec{R}\vec{R} = 0$

$$(A+B).(A-B) = 0 \Longrightarrow A.A - A.B + B.A - B.E$$
$$\Rightarrow A^2 - B^2 = 0 \Longrightarrow A^2 = B^2$$

 \therefore A = B *i.e.* two vectors are equal to each other in magnitude.

(a) $v_y = 20$ and $v_x = 10$ 49.

> \therefore velocity $\vec{v} = 10\hat{i} + 20\hat{j}$ direction of velocity with x axis

$$\tan \theta = \frac{v_y}{v_x} = \frac{20}{10} = 2$$

$$\therefore \theta = \tan(2)$$

50. (c)
$$R_{\text{max}} = A + B$$
 when $\theta = 0^\circ$: $R_{\text{max}} = 12 + 8 = 20N$

51. (c)
$$R = \sqrt{A^2 + B^2} + 2AB\cos\theta$$

If $A = B = P$ and $\theta = 120^\circ$ then $R = P$

52. (a) Sum of the vectors
$$\vec{R} = 5\hat{i} + 8\hat{j} + 2\hat{i} + 7\hat{j} = 7\hat{i} + 15\hat{j}$$

magnitude of $\vec{R} = |\vec{R}| = \sqrt{49 + 225} = \sqrt{274}$

53. (d)

Multiplication of Vectors

(c) Given vectors can be rewritten as $\vec{A} = 2\hat{i} + 3\hat{j} + 8\hat{k}$ and 1. $\vec{B} = -4\hat{i} + 4\hat{j} + \alpha\hat{k}$

Dot product of these vectors should be equal to zero because they are perpendicular.

 $\therefore \vec{A} \cdot \vec{B} = -8 + 12 + 8\alpha = 0 \implies 8\alpha = -4 \implies \alpha = -1/2$

2. (b) Let
$$A = 2i + 3j - k$$
 and $B = -4i - 6j + \lambda k$

 \vec{A} and \vec{B} are parallel to each other

$$\frac{a_1}{b_1} = \frac{a_2}{b_2} = \frac{a_3}{b_3} \text{ i.e. } \frac{2}{-4} = \frac{3}{-6} = \frac{-1}{\lambda} \Longrightarrow \lambda = 2.$$

(d)
$$W = \vec{F} \cdot \vec{S} = FS \cos \theta$$

3.

4.

5.

6.

7.

8.

$$= 50 \times 10 \times \cos 60^\circ = 50 \times 10 \times \frac{1}{2} = 250 J$$

(a)
$$S = r_2 - r_1$$

 $W = \vec{F} \cdot \vec{S} = (4\hat{i} + \hat{j} + 3\hat{k}) \cdot (11\hat{i} + 11\hat{j} + 15\hat{k})$
 $= (4 \times 11 + 1 \times 11 + 3 \times 15) = 100 J.$

(a)
$$(A + B)$$
 is perpendicular to $(A - B)$. Thus
 $(\vec{A} + \vec{B}) \cdot (\vec{A} - \vec{B}) = 0$
or $A^2 + \vec{B} \cdot \vec{A} - \vec{A} \cdot \vec{B} - B^2 = 0$

Because of commutative property of dot product $\vec{A}.\vec{B} = \vec{B}.\vec{A}$ $A^{2} - B^{2} = 0$ or A = B

$$A - B = 0$$
 or $A =$

Thus the ratio of magnitudes A/B = 1

(b) Let $\vec{A} \cdot (\vec{B} \times \vec{A}) = \vec{A} \cdot \vec{C}$

Here
$$\vec{C} = \vec{B} \times \vec{A}$$
 Which is perpendicular to both vector
 \vec{A} and \vec{B} \therefore $\vec{A} \cdot \vec{C} = 0$

(c) We know that $\vec{A} \times \vec{B} = -(\vec{B} \times \vec{A})$ because the angle between these two is always 90°.

> But if the angle between \overrightarrow{A} and \overrightarrow{B} is 0 or π . Then $\vec{A} \times \vec{B} = \vec{B} \times \vec{A} = 0$.

(b)
$$\vec{A} \times \vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & 1 & 2 \\ 2 & -2 & 4 \end{vmatrix}$$

= $(1 \times 4 - 2 \times -2)\hat{i} + (2 \times 2 - 4 \times 3)\hat{j} + (3 \times -2 - 1 \times 2)\hat{k}$
= $8\hat{i} - 8\hat{j} - 8\hat{k}$
 \therefore Magnitude of $\vec{A} \times \vec{B} = |\vec{A} \times \vec{B}| = \sqrt{(8)^2 + (-8)^2 + (-8)^2}$

$$=8\sqrt{3}$$

(b)
$$\vec{\tau} = \vec{r} \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & 2 & 3 \\ 2 & -3 & 4 \end{vmatrix}$$

= $[(2 \times 4) - (3 \times -3)]\hat{i} + [(2 \times 3) - (3 \times 4)]\hat{j}$

+
$$[(3 \times -3) - (2 \times 2)]\hat{k} = 17\hat{i} - 6\hat{j} - 13\hat{k}$$

(d) From the property of vector product, we notice that \vec{C} must 10. be perpendicular to the plane formed by vector \vec{A} and \vec{B} . Thus \vec{C} is perpendicular to both \vec{A} and \vec{B} and $(\vec{A} + \vec{B})$ vector also, must lie in the plane formed by vector \vec{A} and \vec{B} . Thus \vec{C} must be perpendicular to $(\vec{A} + \vec{B})$ also but

the cross product $(\vec{A} \times \vec{B})$ gives a vector \vec{C} which can not be perpendicular to itself. Thus the last statement is wrong.

II. (b) We know that, Angular momentum

$$\vec{L} = \vec{r} \times \vec{p}$$
 in terms of component becomes

As motion is in *x-y* plane $(z = 0 \text{ and } P_z = 0)$, so \overrightarrow{P}

$$L = k \left(x p_y - y p_x \right)$$

Here x = vt, y = b, $p_x = mv$ and $p_y = 0$

$$\therefore \vec{L} = \vec{k} \left[vt \times 0 - b \, mv \right] = -mvb \, \hat{k}$$

12. (d)
$$\vec{F}_1 \cdot \vec{F}_2 = (2\hat{j} + 5\hat{k})(3\hat{j} + 4\hat{k})$$

- = 6 + 20 = 20 + 6 = 26
- (c) Force F lie in the x-y plane so a vector along z-axis will be perpendicular to F.
- 14. (d) $\vec{A}.\vec{B} = |\vec{A}| . |\vec{B}| . \cos \theta = \vec{A}.\vec{B}.\cos 90^\circ = 0$
- 15. (c)



$$\Rightarrow | \vec{V}_{\rm net} | = | \vec{V}_{\rm net}' |$$

So V_1 and V_2 will be mutually perpendicular.

16. (c)
$$W = \vec{F} \cdot \vec{r} = (5\hat{i} + 3\hat{j})(2\hat{i} - \hat{j}) = 10 - 3 = 7 J.$$

17. (b) $\cos \theta = \frac{\vec{A} \cdot \vec{B}}{|\vec{A}||\vec{B}|} = \frac{-2 + 6 - 4}{\sqrt{14}\sqrt{21}} = 0 \therefore \theta = 90^{\circ}$

18. (c)
$$(\hat{i} + \hat{j}).(\hat{j} + \hat{k}) = 0 + 0 + 1 + 0 = 1$$

 $\cos \theta = \frac{\vec{A}.\vec{B}}{|\vec{A}||\vec{B}|} = \frac{1}{\sqrt{2} \times \sqrt{2}} = \frac{1}{2} \therefore \theta = 60^{\circ}$
19. (b) $P = \vec{F}.\vec{v} = 20 \times 6 + 15 \times (-4) + (-5) \times 3$

9. (b)
$$P = F.v = 20 \times 6 + 15 \times (-4) + (-5) \times 3$$

= 120 - 60 - 15 = 120 - 75 = 45 J/s

20. (a)
$$\cos\theta = \frac{\vec{P}.\vec{Q}}{PQ} = 1 \therefore \theta = 0^{\circ}$$

21. (a) $W = \vec{F}.\vec{s} = (5\hat{i} + 6\hat{j} + 4\hat{k})(6\hat{i} - 5\hat{k}) = 30 - 20 = 10 J$
22. (c) $\vec{A}.\vec{B} = 0 \therefore \theta = 90^{\circ}$
23. (a) $\vec{P}.\vec{Q} = 0 \therefore a^2 - 2a - 3 = 0 \Rightarrow a = 3$
24. (b) $W = \vec{F}.\vec{r} = (-2\hat{i} + 15\hat{j} + 6\hat{k})(10\hat{j}) = 150$

25. (c)
$$P_x = 2\cos t$$
, $P_y = 2\sin t$ $\therefore \vec{P} = 2\cos t \hat{i} + 2\sin t \hat{j}$

$$\vec{F} = \frac{d\vec{P}}{dt} = -2\sin t \,\hat{i} + 2\cos t \,\hat{j}$$

$$\vec{F}.\vec{P}=0$$
 : $\theta=90^{\circ}$

26. (d)
$$|\vec{A} \times \vec{B}| = |(2\hat{i} + 3\hat{j}) \times (\hat{i} + 4\hat{j})| = |5\hat{k}| = 5 \text{ units}$$

- **27.** (d)
- **28.** (b) $\vec{A} \times \vec{B} = 0$ \therefore $\sin \theta = 0$ \therefore $\theta = 0^{\circ}$ Two vectors will be parallel to each other.
- **29.** (b) $\vec{A} \times \vec{B}$ and $\vec{B} \times \vec{A}$ are parallel and opposite to each other. So the angle will be π .
- **30.** (b) Vector $(\vec{P} + \vec{Q})$ lies in a plane and vector $(\vec{P} \times \vec{Q})$ is perpendicular to this plane *i.e.* the angle between given vectors is $\frac{\pi}{2}$.

31. (d)
$$\sqrt{2^2 + 3^2 + 2 \times 2 \times 3 \times \cos \theta} = 1$$

By solving we get $\theta = 180^\circ$ \therefore $\vec{A} \times \vec{B} = 0$

 $\label{eq:constraint} \textbf{32.} \qquad (c) \quad \text{Dot product of two perpendicular vector will be zero.}$

33. (d)
$$\cos\theta = \frac{\vec{AB}}{AB} = \frac{42 + 24 - 12}{\sqrt{36 + 36 + 9}\sqrt{49 + 16 + 16}} = \frac{56}{9\sqrt{71}}$$

 $\cos\theta = \frac{56}{9\sqrt{71}} \therefore \sin\theta = \frac{\sqrt{5}}{3} \text{ or } \theta = \sin^{-1}\left(\frac{\sqrt{5}}{3}\right)$

34. (b) Direction of vector
$$A$$
 is along z -axis $\therefore A = ak$
Direction of vector B is towards north $\therefore \vec{B} = b\hat{j}$
Now $\vec{A} \times \vec{B} = a\hat{k} \times b\hat{j} = ab(-\hat{j})$
 \therefore The direction is $\vec{A} \times \vec{B}$ is along west.

35. (d)
$$\cos \theta = \frac{A \cdot B}{|\vec{A}|| |\vec{B}|} = \frac{1}{\sqrt{2}\sqrt{2}} = \frac{1}{2} \therefore \theta = 60^{\circ}$$

36. (d)
$$\overrightarrow{AB} = (4\hat{i} + 5\hat{j} + 6\hat{k}) - (3\hat{i} + 4\hat{j} + 5\hat{k}) = \hat{i} + \hat{j} + \hat{k}$$

 $\overrightarrow{CD} = (4\hat{i} + 6\hat{j}) - (7\hat{i} + 9\hat{j} + 3\hat{k}) = -3\hat{i} - 3\hat{j} - 3\hat{k}$
 \overrightarrow{AB} and \overrightarrow{CD} are parallel, because its cross-products is 0.

37. (a)
$$W = \vec{F} \cdot \vec{S} = (4\hat{i} + 5\hat{j})(3\hat{i} + 6\hat{j}) = 12$$

38. (b)
$$|\vec{A} \times \vec{B}| = \vec{A} \cdot \vec{B} \Rightarrow AB \sin \theta = AB \cos \theta \Rightarrow \tan \theta = 1$$

 $\therefore \theta = 45^{\circ}$

40. (a)
$$\vec{v} = \vec{\omega} \times \vec{r} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -2 & 2 \\ 0 & 4 & -3 \end{vmatrix} = \hat{i}(6-8) - \hat{j}(-3) + 4\hat{k}$$
$$-2\vec{i} + 3\vec{j} + 4\vec{k}$$
$$|\vec{v}| = \sqrt{(-2)^2 + (3)^2 + 4^2} = \sqrt{29} \text{ unit}$$

41. (d) $\vec{a} \cdot \vec{b} = 0$ *i.e.* \vec{a} and \vec{b} will be perpendicular to each other $\vec{a} \cdot \vec{c} = 0$ *i.e.* \vec{a} and \vec{c} will be perpendicular to each other

 $ec{b} imes ec{c}$ will be a vector perpendicular to both $ec{b}$ and $ec{c}$

So \vec{a} is parallel to $\vec{b} \times \vec{c}$

42. (d) Area =
$$|\hat{2i} \times \hat{2j}| = |4\hat{k}| = 4$$
 unit

43. (c)
$$\vec{A} = 2\hat{i} + 2\hat{j} - \hat{k} \text{ and } \vec{B} = 6\hat{i} - 3\hat{j} + 2\hat{k}$$

 $\vec{C} = \vec{A} \times \vec{B} = (2\hat{i} + 2\hat{j} - \hat{k}) \times (6\hat{i} - 3\hat{j} + 2\hat{k})$
 $= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 2 & -1 \\ 6 & -3 & 2 \end{vmatrix} = \hat{i} - 10\hat{j} - 18\hat{k}$

Unit vector perpendicular to both \vec{A} and \vec{B}

$$=\frac{\hat{i}-10\hat{j}-18\hat{k}}{\sqrt{1^2+10^2+18^2}}=\frac{\hat{i}-10\hat{j}-18\hat{k}}{5\sqrt{17}}$$

44. (b)
$$\vec{A} = \hat{j} + 3\hat{k}$$
, $\vec{B} = \hat{i} + 2\hat{j} - \hat{k}$

$$\vec{C} = \vec{A} \times \vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & 1 & 3 \\ 1 & 2 & -1 \end{vmatrix} = -7\hat{i} + 3\hat{j} - \hat{k}$$

Hence area = $|\vec{C}| = \sqrt{49 + 9 + 1} = \sqrt{59} \ squart$

45. (a)
$$\vec{L} = \vec{r} \times \vec{p} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & -1 \\ 3 & 4 & -2 \end{vmatrix} = -\hat{j} - 2\hat{k}$$

i.e. the angular momentum is perpendicular to *x*-axis.

46. (a) $\vec{A} \times \vec{B}$ is a vector perpendicular to plane $\vec{A} + \vec{B}$ and hence perpendicular to $\vec{A} + \vec{B}$.

47. (a)
$$\vec{\tau} = \vec{r} \times \vec{F} = (7\hat{i} + 3\hat{j} + \hat{k})(-3\hat{i} + \hat{j} + 5\hat{k})$$

 $\vec{\tau} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 7 & 3 & 1 \\ -3 & 1 & 5 \end{vmatrix} = 14\hat{i} - 38\hat{j} + 16\hat{k}$

48. (d)
$$(\vec{A} + \vec{B}) \times (\vec{A} - \vec{B}) = \vec{A} \times \vec{A} - \vec{A} \times \vec{B} + \vec{B} \times \vec{A} - \vec{B} \times \vec{B}$$

$$= 0 - \vec{A} \times \vec{B} + \vec{B} \times \vec{A} - 0 = \vec{B} \times \vec{A} + \vec{B} \times \vec{A} = 2(\vec{B} \times \vec{A})$$

49. (d) For perpendicular vector $\vec{A} \cdot \vec{B} = 0$

$$\Rightarrow (5\hat{i} + 7\hat{j} - 3\hat{k}).(2\hat{i} + 2\hat{j} - a\hat{k}) = 0$$
$$\Rightarrow 10 + 14 + 3a = 0 \Rightarrow a = -8$$

50. (a) Mass =
$$\frac{\text{Force}}{\text{Acceleration}} = \frac{|F|}{a}$$

$$= \frac{\sqrt{36+64+100}}{1} = 10\sqrt{2} \ kg$$

(a) Area of parallelogram
$$= \vec{A} \times \vec{B}$$

 $= (\hat{i} + 2\hat{j} + 3\hat{k}) \times (3\hat{i} - 2\hat{j} + \hat{k})$
 $= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & 3 \\ 3 & -2 & 1 \end{vmatrix} = (8)\hat{i} + (8)\hat{j} - (8)\hat{k}$

Magnitude =
$$\sqrt{64 + 64 + 64} = 8\sqrt{3}$$

52. (b) Radius vector
$$\vec{r} = \vec{r_2} - \vec{r_1} = (2\hat{i} - 3\hat{j} + \hat{k}) - (2\hat{i} + \hat{j} + \hat{k})$$

$$\therefore \vec{r} = -4\hat{j}$$

Linear momentum $\vec{p} = 2\hat{i} + 3\hat{j} - \hat{k}$
 $\vec{L} = \vec{r} \times \vec{p} = (-4\hat{j}) \times (2\hat{i} + 3\hat{j} - \hat{k})$
 $= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & -4 & 0 \\ 2 & 3 & -1 \end{vmatrix} = 4\hat{i} - 8\hat{k}$
53. (d) $\vec{v} = \vec{\omega} \times \vec{r} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & -4 & 1 \\ 5 & -6 & 6 \end{vmatrix} = -18\hat{i} - 13\hat{j} + 2\hat{k}$

54. (a)

51.

55. (c)
$$\vec{A}.\vec{B} = AB\cos\theta$$

In the problem $\vec{A}.\vec{B} = -AB$ i.e. $\cos \theta = -1$ $\therefore \theta = 180^{\circ}$ *i.e.* \vec{A} and \vec{B} acts in the opposite direction.

56. (d)
$$|A \times B| = \sqrt{3}(A.B)$$

 $AB \sin\theta = \sqrt{3}AB \cos\theta \Rightarrow \tan\theta = \sqrt{3} \therefore \theta = 60^{\circ}$
Now $|\vec{R}| = |\vec{A} + \vec{B}| = \sqrt{A^2 + B^2 + 2AB \cos\theta}$
 $= \sqrt{A^2 + B^2 + 2AB\left(\frac{1}{2}\right)} = (A^2 + B^2 + AB)^{1/2}$
57. (a) $W = \vec{F}.\vec{s} = (3\hat{i} + c\hat{j} + 2\hat{k}).(-4\hat{i} + 2\hat{j} - 3\hat{k}) = -12 + 2c - 6$
Work done $= 6J$ (given)
 $\therefore -12 + 2c - 6 = 6 \Rightarrow c = 12$

58. (b)
$$W = \vec{F} \cdot \vec{s} = (5\hat{i} + 3\hat{j}) \cdot (2\hat{i} - \hat{j}) = 10 - 3 = 7 J$$

59. (c)
$$\vec{A} \times \vec{B} = AB\sin\theta \hat{n}$$

for parallel vectors $\,\theta=0^\circ\,$ or $\,180^\circ$, $\,\sin\theta=0$

$\therefore \vec{A} \times \vec{B} = \hat{0}$

Lami's Theorem



5

1.

(b)

Tcos 30° 30*N*

From the figure
$$T \sin 30^\circ = 30$$
 ...(i)

 $T\cos 30^{\circ} = W$...(ii)

By solving equation (i) and (ii) we get

 $W = 30\sqrt{3}N$ and T = 60N

Relative Velocity

The two car (say A and B) are moving with same velocity, the (b) relative velocity of one (say B) with respect to the other $A, v_{BA} = v_B - v_A = v - v = 0$

So the relative separation between them (= 5 km) always remains the same

Now if the velocity of car (say C) moving in opposite direction

to A and B, is V_C relative to ground then the velocity of car C

relative to A and B will be $v_{rel.} = v_C - v_C$

But as V is opposite to v

So $v_{rel} = v_c - (-30) = (v_c + 30) km/hr$.

So, the time taken by it to cross the cars A and B

$$t = \frac{u}{v_{rel}} \implies \frac{4}{60} = \frac{5}{v_C + 30}$$

- $\Rightarrow v_C = 45 \, km \, / hr.$
- (b) When the man is at rest w.r.t. the ground, the rain comes to 2. him at an angle 30° with the vertical. This is the direction of the velocity of raindrops with respect to the ground.

Here \vec{v}_{rg} = velocity of rain with respect to the ground

 v_{mg} = velocity of the man with respect to the ground.

and
$$v_m$$
 = velocity of the rain with respect to the man,

We have
$$\vec{v}_{rg} = \vec{v}_{rm} + \vec{v}_{mg}$$
(i)

Taking horizontal components equation (i) gives

$$v_{rg} \sin 30^\circ = v_{mg} = 10 \, km \, / \, hr$$

$$v_{rg} = \frac{10}{\sin 30^\circ} = 20 \, km \, / \, hr$$

(c) Taking vertical components equation (i) gives $v_{rg}\cos 30^\circ = v_{rm} = 20\frac{\sqrt{3}}{2} = 10\sqrt{3} \, km \, / \, hr$

(c) Relative velocity =
$$(3i + 4j) - (-3i - 4j) = 6i + 8j$$

= 5 - (-10) = 5 + 10 = 15 m / sec

Time taken by the parrot = $\frac{d}{v_{+}} = \frac{150}{15} = 10 \text{ sec}.$

(c)

01

3.

4.

5.

6.

7.

8.

9.

For shortest time, swimmer should swim along AB, so he will reach at point *C* due to the velocity of river. i.e. he should swim due north.

$$\sin 30^{\circ} = \frac{v_r}{v_m} = \frac{1}{2} \Rightarrow v_r = \frac{v_m}{2} = \frac{0.5}{2} = 0.25 \, m/s$$

(c) $\vec{v}_B + \vec{v}_A = \vec{v}_B + \vec{v}_A = 80 + 65 = 145 \, km/hr$

Instantaneous separation = 100 m

=10-9=1m/s

$$\text{ime} = \frac{\text{distance}}{\text{veclotiy}} = \frac{100}{1} = 100 \, \text{sec}.$$

10. (a,c)

11.

(b) A man is sitting in a bus and travelling from west to east, and the rain drops are appears falling vertically down.



 v_r = Actual velocity of rain^m which is falling at an angle θ with vertical

 v_{m} = velocity of rain *w.r.t.* to moving man

If the another man observe the rain then he will find that actually rain falling with velocity v_r at an angle going from west to east.

12. Boat covers distance of 16km in a still water in 2 hours. (b)

i.e.
$$v_B = \frac{16}{2} = 8 \text{ km} / hr$$

Now velocity of water $\Rightarrow v_w = 4 \text{ km} / hr$

Time taken for going upstream

$$t_1 = \frac{8}{v_B - v_w} = \frac{8}{8 - 4} = 2hr$$

(As water current oppose the motion of boat) Time taken for going down stream

$$t_2 = \frac{8}{v_B + v_w} = \frac{8}{8 + 4} = \frac{8}{12}hr$$

(As water current helps the motion of boat)

$$\therefore \text{ Total time } = t_1 + t_2 = \left(2 + \frac{8}{12}\right)hr \text{ or } 2hr 40 \text{ min}$$

13. (d) Relative velocity = 10 + 5 = 15 m / s.

Time taken by the bird to cross the train = $\frac{120}{15} = 8 \sec \theta$

14. (b)
$$\overrightarrow{v_{br}} = \overrightarrow{v_b} + \overrightarrow{v_r}$$

 $\Rightarrow v_{br} = \sqrt{v_b^2 + v_r^2}$
 $\Rightarrow 10 = \sqrt{8^2 + v_r^2}$
 $\Rightarrow v_r = 6km/hr.$

Critical Thinking Questions

- 1. (c) $\sin^2 \alpha + \sin^2 \beta + \sin \gamma$ = $1 - \cos^2 \alpha + 1 - \cos^2 \beta + 1 - \cos^2 \gamma$ = $3 - (\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma) = 3 - 1 = 2$
- 2. (c) If vectors are of equal magnitude then two vectors can give zero resultant, if they works in opposite direction. But if the vectors are of different magnitudes then minimum three vectors are required to give zero resultant.
- **3.** (c)
- **4.** (c) Let P be the smaller force and Q be the greater force then according to problem –

$$P + Q = 18 \qquad \dots \dots (i)$$

$$R = \sqrt{P^2 + Q^2 + 2PQ\cos\theta} = 12 \qquad \dots \dots (ii)$$

$$\tan \phi = \frac{Q\sin\theta}{P + Q\cos\theta} = \tan 90 = \infty$$

$$\therefore P + Q\cos\theta = 0 \qquad \dots \dots \dots (iii)$$

$$\operatorname{Term} him = 0 \quad (ii) \quad \dots \quad (iii)$$

By solving (i), (ii) and (iii) we will get P = 5, and Q = 13

5. (b) From the figure $|\overrightarrow{OA}| = a$ and $|\overrightarrow{OB}| = a$

Also from triangle rule
$$\overrightarrow{OB} - \overrightarrow{OA} = \overrightarrow{AB} = \Delta \overrightarrow{a}$$

 $\Rightarrow | \Delta \overrightarrow{a} | = AB$
Using angle $= \frac{\operatorname{arc}}{\operatorname{radius}}$
 $\Rightarrow AB = a \cdot d\theta$
So $| \Delta \overrightarrow{a} | = ad\theta$

 Δa means change in magnitude of vector *i.e.* $|\overrightarrow{OB}| - |\overrightarrow{OA}|$ $\Rightarrow a - a = 0$

So
$$\Delta a = 0$$

6. 7.

8.

10.

11.

(b)
$$R_{\text{net}} = R + \sqrt{R^2 + R^2} = R + \sqrt{2}R = R(\sqrt{2} + 1)$$

(d)

(d)
$$\Delta v = 2v \sin\left(\frac{90^\circ}{2}\right) = 2v \sin 45^\circ = 2v \times \frac{1}{\sqrt{2}} = \sqrt{2}v$$

$$= \sqrt{2} \times r\omega = \sqrt{2} \times 1 \times \frac{2\pi}{60} = \frac{\sqrt{2}\pi}{30} \ cm/s$$

9. (b)
$$\Delta v = 2v \sin\left(\frac{\theta}{2}\right) = 2 \times 5 \times \sin 45^\circ = \frac{10}{\sqrt{2}}$$

 $\therefore a = \frac{\Delta v}{\Delta t} = \frac{10/\sqrt{2}}{10} = \frac{1}{\sqrt{2}} m/s^2$

(c) For motion of the particle from
$$(0, 0)$$
 to $(a, 0)$
 $\vec{F} = -K(0\hat{i} + a\hat{j}) \Rightarrow \vec{F} = -Ka\hat{j}$
Displacement $\vec{r} = (a\hat{i} + 0\hat{j}) - (0\hat{i} + 0\hat{j}) = a\hat{i}$
So work done from $(0, 0)$ to $(a, 0)$ is given by
 $W = \vec{F} \cdot \vec{r} = -Ka\hat{j} \cdot a\hat{i} = 0$
For motion $(a, 0)$ to (a, a)
 $\vec{F} = -K(a\hat{i} + a\hat{j})$ and displacement
 $\vec{r} = (a\hat{i} + a\hat{j}) - (a\hat{i} + 0\hat{j}) = a\hat{j}$
So work done from $(a, 0)$ to (a, a) $W = \vec{F} \cdot \vec{r}$
 $= -K(a\hat{i} + a\hat{j}) \cdot a\hat{j} = -Ka^2$
So total work done $= -Ka^2$
(a) Given $\overrightarrow{OA} = \vec{a} = 3\hat{i} - 6\hat{j} + 2\hat{k}$ and $\overrightarrow{OB} = \vec{b} = 2\hat{i} + \hat{j} - 2\hat{k}$
 $\therefore (\vec{a} \times \vec{b}) = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & -6 & 2 \\ 2 & 1 & -2 \end{vmatrix}$
 $= (12 - 2)\hat{i} + (4 + 6)\hat{j} + (3 + 12)\hat{k}$
 $= 10\hat{i} + 10\hat{j} + 15\hat{k} \Rightarrow |\vec{a} \times \vec{b}| = \sqrt{10^2 + 10^2 + 15^2}$

Area of
$$\triangle OAB = \frac{1}{2} |\vec{a} \times \vec{b}| = \frac{5\sqrt{17}}{2}$$
 sq.unit.

 $=\sqrt{425} = 5\sqrt{17}$

$$T\sin\theta \longleftrightarrow \stackrel{T\cos\theta}{\longrightarrow} p$$

As the metal sphere is in equilibrium under the effect of three forces therefore $\vec{T} + \vec{P} + \vec{W} = 0$ From the figure $T \cos \theta = W$...(i) $T \sin \theta = P$...(ii)

From equation (i) and (ii) we get $P = W \tan \theta$

and
$$T^2 = P^2 + W^2$$
 (b)

Assertion and Reason

 (a) Cross product of two vectors is perpendicular to the plane containing both the vectors.

2 (a)
$$\cos \theta = \frac{(\hat{i} + \hat{j}).(\hat{i})}{|\hat{i} + \hat{j}||\hat{i}|} = \frac{1}{\sqrt{2}}$$
. Hence $\theta = 45^{\circ}$.

3 (d)
$$\frac{\vec{A} \times \vec{B}}{\vec{A}.\vec{B}} = \frac{AB\sin\theta \,\hat{n}}{AB\cos\theta} = \tan\theta \,\hat{n}$$

where \hat{n} is unit vector perpendicular to both \vec{A} and \vec{B} .

However
$$\frac{|\vec{A} \times \vec{B}|}{\vec{A}.\vec{B}} = \tan \theta$$

4 (b) $|\vec{A} + \vec{B}| = |\vec{A} - \vec{B}|$

$$\Rightarrow A^2 + B^2 + 2AB\cos\theta = A^2 + B^2 + 2AB\cos\theta$$

Hence $\cos \theta = 0$ which gives $\theta = 90^{\circ}$

Also vector addition is commutative.

Hence
$$\vec{A} + \vec{B} = \vec{B} + \vec{A}$$

5 (c) $\vec{v} = \vec{\omega} \times \vec{r}$

The expression $\vec{\omega} = \vec{v} \times \vec{r}$ is wrong.

- 6 (b) For giving a zero resultant, it should be possible to represent the given vectors along the sides of a closed polygon and minimum number of sides of a polygon is three.
- 7 (a) Since velocities are in opposite direction, therefore $v_{AB} \neq \vec{v}_A \vec{v}_B | = v_A + v_B$.

Which is greater than v_A or v_B

8 (b) Vector addition of two vectors is commutative *i.e.* $\vec{A} + \vec{B} = \vec{B} + \vec{A}$.

9 (a)

- 10 (c) Cross-product of two vectors is anticommutative. *i.e.* $\vec{A} \times \vec{B} = -\vec{B} \times \vec{A}$
- 11 (b)

16

- 12 (e) If a vector quantity has zero magnitude then it is called a null vector. That quantity may have some direction even if its magnitude is zero.
- 13 (a) Let \vec{P} and \vec{Q} are two vectors in opposite direction, then their sum $\vec{P} + (-\vec{Q}) = \vec{P} - \vec{Q}$

If $\vec{P} = \vec{Q}$ then sum equal to zero.

- 14 (c) If two vectors are in opposite direction, then they cannot be like vectors.
- **15** (a) If θ be the angle between two vectors \vec{A} and \vec{B} , then their scalar product, $\vec{A}.\vec{B} = AB\cos\theta$

If $\theta = 90^{\circ}$ then $\vec{A} \cdot \vec{B} = 0$

i.e. if \vec{A} and \vec{B} are perpendicular to each other then their scalar product will be zero.

(b) We can multiply any vector by any scalar.

For example, in equation $\vec{F} = m\vec{a}$ mass is a scalar quantity, but acceleration is a vector quantity.

17 (c) If two vectors equal in magnitude are in opposite direction, then their sum will be a null vector. A null vector has direction which is intermediate (or depends on direction of initial vectors) even its magnitude is zero.

18 (b)
$$A.B = |A|| |B| \cos \theta = 0$$

 $\vec{A} \times \vec{B} = \vec{A} \parallel \vec{B} \parallel \sin \theta = 0$

If \vec{A} and \vec{B} are not null vectors then it follows that $\sin\theta$ and $\cos\theta$ both should be zero simultaneously. But it cannot be possible so it is essential that one of the vector must be null vector.

20

(c) The resultant of two vectors of unequal magnitude given by $R = \sqrt{A^2 + B^2 + 2AB\cos\theta} \quad \text{cannot be zero for any value of}$ θ .

21 (a)
$$\overrightarrow{A.B} = \overrightarrow{B.C} \implies AB \cos \theta_1 = BC \cos \theta_2$$

 $\therefore A = C$, only when $\theta_1 = \theta_2$

So when angle between \vec{A} and \vec{B} is equal to angle between \vec{B} and \vec{C} only then \vec{A} equal to \vec{C}

22 (c) Since vector addition is commutative, therefore $\vec{A} + \vec{B} = \vec{B} + \vec{A}$.

lectors

0.4i + 0.8j + ck represents a unit vector when c is 1.

> (b) $\sqrt{0.2}$ (a) - 0.2

- (c) $\sqrt{0.8}$ (d) 0
- The angles which a vector $\hat{i} + \hat{j} + \sqrt{2} \hat{k}$ makes with X, Y and Z axes 2. respectively are

(a)	60°, 60°, 60°	(b)	45°, 45°, 45°
(c)	60°, 60°, 45°	(d)	45°, 45°, 60°

- The value of a unit vector in the direction of vector $A = \hat{5i} 1\hat{2j}$, з. is
 - (a) \hat{i} (b) \hat{i} (c) $(\hat{i} + \hat{j})/13$ (d) $(\hat{5i} - 12\hat{j})/13$
- Which of the following is independent of the choice of co-ordinate 4 svstem
 - (a) $\vec{P} + \vec{Q} + \vec{R}$ (b) $(P_{r} + Q_{r} + R_{r})\hat{i}$ (c) $P_{x}\hat{i} + Q_{y}\hat{j} + R_{z}\hat{k}$ (d) None of these
- A car travels 6 km towards north at an angle of 45° to the east and 5. then travels distance of 4 km towards north at an angle of 135° to the east. How far is the point from the starting point. What angle does the straight line joining its initial and final position makes with the east
 - $\sqrt{50}$ km and tan⁻¹(5) (a)
 - (b) 10 km and $\tan^{-1}(\sqrt{5})$
 - (c) $\sqrt{52} \ km$ and $\tan^{-1}(5)$
 - $\sqrt{52}$ km and $\tan^{-1}(\sqrt{5})$ (d)
- Given that $\vec{A} + \vec{B} + \vec{C} = 0$ out of three vectors two are equal in 6. magnitude and the magnitude of third vector is $\sqrt{2}$ times that of either of the two having equal magnitude. Then the angles between vectors are given by
 - (a) 30°, 60°, 90° (b) 45°, 45°, 90°
 - (c) 45°, 60°, 90° (d) 90°, 135°, 135°
- Two forces $F_1 = 1 N$ and $F_2 = 2 N$ act along the lines x = 0 and y7. = 0 respectively. Then the resultant of forces would be
 - (a) $\hat{i} + 2\hat{j}$ (b) $\hat{i} + \hat{j}$
 - (d) $2\hat{i} + \hat{i}$ (c) $3\hat{i} + 2\hat{j}$
- At what angle must the two forces (x + y) and (x y) act so that 8. the resultant may be $\sqrt{(x^2 + y^2)}$

(a)
$$\cos^{-1}\left(-\frac{x^2+y^2}{2(x^2-y^2)}\right)$$
 (b) $\cos^{-1}\left(-\frac{2(x^2-y^2)}{x^2+y^2}\right)$
(c) $\cos^{-1}\left(-\frac{x^2+y^2}{x^2-y^2}\right)$ (d) $\cos^{-1}\left(-\frac{x^2-y^2}{x^2+y^2}\right)$

- Self Evaluation Test -f 0

Following forces start acting on a particle at rest at the origin of the co-ordinate system simultaneously

 $\vec{F}_1 = -4\hat{i} - 5\hat{j} + 5\hat{k}$, $\vec{F}_2 = 5\hat{i} + 8\hat{j} + 6\hat{k}$, $\vec{F}_3 = -3\hat{i} + 4\hat{j} - 7\hat{k}$ and $\vec{F}_4 = 2\hat{i} - 3\hat{j} - 2\hat{k}$ then the particle will move

(b) $\ln y - z$ plane (a) $\ln x - y$ plane

9.

11.

- (c) $\ln x z$ plane (d) Along x -axis
- The resultant of $\vec{A} + \vec{B}$ is \vec{R}_1 . On reversing the vector \vec{B} , the 10. resultant becomes \vec{R}_2 . What is the value of $R_1^2 + R_2^2$
 - (a) $A^2 + B^2$ (b) $A^2 - B^2$ (c) $2(A^2 + B^2)$ (d) $2(A^2 - B^2)$
 - Figure below shows a body of mass M moving with the uniform speed on a circular path of radius, R. What is the change in acceleration in going from P_1 to P_2
 - P_2 (a) Zero (b) $v^2/2R$ (c) $2v^2 / R$ **-** R (d) $\frac{v^2}{P} \times \sqrt{2}$
- 12. A particle is moving on a circular path of radius r with uniform velocity v. The change in velocity when the particle moves from P to Q is $(\angle POQ = 40^\circ)$
 - (a) $2v\cos 40^{\circ}$ $2v \sin 40^{\circ}$ (b) $2v \sin 20^{\circ}$ (c)
 - $2v\cos 20^{\circ}$ (d)
- $\vec{A} = 2\hat{i} + 4\hat{j} + 4\hat{k}$ and $\vec{B} = 4\hat{i} + 2\hat{j} 4\hat{k}$ are two vectors. 13. The angle between them will be
 - (a) 0° (b) 45° (c) 60° (d) 90°
- If $\vec{A} = 2\hat{i} + 3\hat{j} \hat{k}$ and $\vec{B} = -\hat{i} + 3\hat{j} + 4\hat{k}$ then projection of \vec{A} 14. on \vec{B} will be

(a)
$$\frac{3}{\sqrt{13}}$$
 (b) $\frac{3}{\sqrt{26}}$



P

(c)
$$\sqrt{\frac{3}{26}}$$
 (d) $\sqrt{\frac{3}{13}}$

15. In above example a unit vector perpendicular to both \vec{A} and \vec{B} will be

(a)
$$+\frac{1}{\sqrt{3}}(\hat{i}-\hat{j}-\hat{k})$$
 (b) $-\frac{1}{\sqrt{3}}(\hat{i}-\hat{j}-\hat{k})$
(c) Both (a) and (b) (d) None of these

16. Two constant forces $F_1 = 2\hat{i} - 3\hat{j} + 3\hat{k}$ (N) and $F_2 = \hat{i} + \hat{j} - 2\hat{k}$ (N) act on a body and displace it from the position $r_1 = \hat{i} + 2\hat{j} - 2\hat{k}$ (m) to the position $r_2 = 7\hat{i} + 10\hat{j} + 5\hat{k}$ (m). What is the work done

- (a) 9 *J* (b) 41 *J*
- (c) 3 *J* (d) None of these
- 17. For any two vectors \vec{A} and \vec{B} , if $\vec{A} \cdot \vec{B} = |\vec{A} \times \vec{B}|$, the magnitude of $\vec{C} = \vec{A} + \vec{B}$ is equal to

(a)
$$\sqrt{A^2 + B^2}$$
 (b) $A + B$
(c) $\sqrt{A^2 + B^2 + \frac{AB}{\sqrt{2}}}$ (d) $\sqrt{A^2 + B^2 + \sqrt{2} \times AB}$

18. Which of the following is the unit vector perpendicular to \vec{A} and \vec{B}

(a)
$$\frac{\hat{A} \times \hat{B}}{AB \sin \theta}$$
 (b) $\frac{\hat{A} \times \hat{B}}{AB \cos \theta}$
(c) $\frac{\vec{A} \times \vec{B}}{AB \sin \theta}$ (d) $\frac{\vec{A} \times \vec{B}}{AB \cos \theta}$

- 19. Two vectors $P = 2\hat{i} + \hat{bj} + 2\hat{k}$ and $Q = \hat{i} + \hat{j} + \hat{k}$ will be parallel if
 - (a) b = 0 (b) b = 1(c) b = 2 (d) b = -4

20. Which of the following is not true ? If $\vec{A} = 3\hat{i} + 4\hat{j}$ and $\vec{B} = 6\hat{i} + 8\hat{j}$ where *A* and *B* are the magnitudes of \vec{A} and \vec{B}

(a) $\vec{A} \times \vec{B} = 0$ (b) $\frac{A}{B} = \frac{1}{2}$

(c)
$$A \cdot B = 48$$
 (d) $A = 5$

21. The area of the triangle formed by $2\hat{i} + \hat{j} - \hat{k}$ and $\hat{i} + \hat{j} + \hat{k}$ is

(a) 3 sq.unit

- (b) $2\sqrt{3}$ sq. unit
- (c) $2\sqrt{14}$ sq. unit

(d)
$$\frac{\sqrt{14}}{2}$$
 sq. unit

22. T

23.

24.

25.

Two trains along the same straight rails moving with constant speed 60 *km/hr* and 30 *km/hr* respectively towards each other. If at time t = 0, the distance between them is 90 *km*, the time when they collide is

- (a) 1 *hr* (b) 2 *hr*
- (c) 3 *hr* (d) 4 *hr*
- A steam boat goes across a lake and comes back (a) On a quite day when the water is still and (b) On a rough day when there is uniform air current so as to help the journey onward and to impede the journey back. If the speed of the launch on both days was same, in which case it will complete the journey in lesser time
 - (a) Case (a)
 - (b) Case (b)
 - (c) Same in both
 - (d) Nothing can be predicted
- To a person, going eastward in a car with a velocity of 25 km/hr, a train appears to move towards north with a velocity of $25\sqrt{3}$ km/hr. The actual velocity of the train will be
 - (a) 25 *km/hr* (b) 50 *km/hr*
 - (c) $5 \ km/hr$ (d) $5\sqrt{3} \ km/hr$
- A swimmer can swim in still water with speed υ and the river is flowing with velocity $\nu/2$. To cross the river in shortest distance, he should swim making angle θ with the upstream. What is the ratio of the time taken to swim across the shortest time to that is swimming across over shortest distance
 - (a) $\cos \theta$ (b) $\sin \theta$ (c) $\tan \theta$ (d) $\cot \theta$
- **26.** A bus is moving with a velocity 10 m/s on a straight road. A scooterist wishes to overtake the bus in 100 *s*. If the bus is at a distance of 1 km from the scooterist, with what velocity should the scooterist chase the bus

(SET -0)

- (a) 50 *m/s* (b) 40 *m/s*
- (c) 30 *m/s* (d) 20 *m/s*



1. (b)
$$\sqrt{(0.4)^2 + (0.8)^2 + c^2} = 1$$

 $\Rightarrow 0.16 + 0.64 + c^2 = 1 \Rightarrow c = \sqrt{0.2}$
2. (c) $\vec{R} = \hat{i} + \hat{j} + \sqrt{2}\hat{k}$
Comparing the given vector with $R = R_x\hat{i} + R_y\hat{j} + R_z\hat{k}$
 $R_x = 1, R_y = 1, R_z = \sqrt{2} \text{ and } |\vec{R}| = \sqrt{R_x^2 + R_y^2 + R_z^2} = 2$
 $\cos \alpha = \frac{R_x}{R} = \frac{1}{2} \Rightarrow \alpha = 60^\circ$
 $\cos \beta = \frac{R_y}{R} = \frac{1}{2} \Rightarrow \beta = 60^\circ$
 $\cos \gamma = \frac{R_z}{R} = \frac{1}{\sqrt{2}} \Rightarrow \gamma = 45^\circ$
3. (d) $\vec{A} = 5\hat{i} + 12\hat{j}, |\vec{A}| = \sqrt{5^2 + (-12)^2} = \sqrt{25 + 144} = 13$
Unit vector $\hat{A} = \frac{\vec{A}}{|\vec{A}|} = \frac{5\hat{i} - 12\hat{j}}{13}$
4. (a)
5. (c)



Net movement along x-direction $S = (6 - 4) \cos 45^\circ \hat{i}$

$$=2\times\frac{1}{\sqrt{2}}=\sqrt{2}$$
 km

7.

8.

9.

10.

Net movement along y-direction $S = (6 + 4) \sin 45^{\circ} \hat{j}$

$$=10\times\frac{1}{\sqrt{2}}=5\sqrt{2}\,km$$

Net movement from starting point

6.

$$|\vec{s}| = \sqrt{S_x^2 + S_y^2} = \sqrt{(\sqrt{2})^2 + (5\sqrt{2})^2} = \sqrt{52} \ km$$

Angle which makes with the east direction



From polygon law, three vectors having summation zero should form a closed polygon. (Triangle) since the two vectors are having same magnitude and the third vector is $\sqrt{2}$ times that of either of two having equal magnitude. *i.e.* the triangle should be right angled triangle Angle between A and B, $\alpha = 90^{\circ}$ Angle between *B* and *C*, $\beta = 135^{\circ}$ Angle between A and C, $\gamma = 135^{\circ}$ (d) x = 0 means y-axis $\Rightarrow \vec{F}_1 = \hat{j}$ y = 0 means x-axis $\Rightarrow \vec{F}_2 = 2\hat{i}$ so resultant $\vec{F} = \vec{F}_1 + \vec{F}_2 = 2\hat{i} + \hat{j}$ (a) $R^2 = A^2 + B^2 + 2AB\cos\theta$ Substituting, A = (x + y), B = (x - y) and $R = \sqrt{(x^2 + y^2)}$ we get $\theta = \cos^{-1} \left(-\frac{(x^2 + y^2)}{2(x^2 - y^2)} \right)$ (b) $F_1 + \vec{F}_2 + \vec{F}_3 + \vec{F}_4$

$$= (-4\hat{i} + 5\hat{i} - 3\hat{i} + 2\hat{i}) + (-5\hat{j} + 8\hat{j} + 4\hat{j} - 3\hat{j}) + (5\hat{k} + 6\hat{k} - 7\hat{k} - 2\hat{k}) = 4\hat{j} + 2\hat{k}$$

∴ the particle will move in *y* - *z* plane.
(c) $\vec{R}_1 = \vec{A} + \vec{B}$, $\vec{R}_2 = \vec{A} - \vec{B}$

$$R_{1}^{2} + R_{2}^{2} = \left(\sqrt{A^{2} + B^{2}}\right)^{2} + \left(\sqrt{A^{2} + B^{2}}\right)^{2} = 2\left(A^{2} + B^{2}\right)$$

11. (d) $\Delta a = 2a \sin\left(\frac{\theta}{a}\right) = 2a \times \sin 45^{\circ} = \sqrt{2}a = \sqrt{2}\frac{v^{2}}{a}$

(d)
$$\Delta a = 2a \sin\left(\frac{\theta}{2}\right) = 2a \times \sin 45^\circ = \sqrt{2}a = \sqrt{2}\frac{v}{R}$$

12. (b)
$$\Delta v = 2v \sin\left(\frac{\theta}{2}\right) = 2v \sin 20^\circ$$

13. (c)
$$\cos\theta = \frac{\overrightarrow{A} \cdot \overrightarrow{B}}{|\overrightarrow{A}| \cdot |\overrightarrow{B}|} = \frac{a_1b_1 + a_2b_2 + a_3b_3}{|\overrightarrow{A}| \cdot |\overrightarrow{B}|}$$
$$= \frac{2 \times 4 + 4 \times 2 - 4 \times 4}{|\overrightarrow{A}| \cdot |\overrightarrow{B}|} = 0$$
$$\therefore \theta = \cos^{-1}(0^\circ) \implies \theta = 90^\circ$$

14. (b)
$$|\vec{A}| = \sqrt{2^2 + 3^2 + (-1)^2} = \sqrt{4 + 9 + 1} = \sqrt{14}$$

 $|\vec{B}| = \sqrt{(-1)^2 + 3^2 + 4^2} = \sqrt{1 + 9 + 16} = \sqrt{26}$
 $\vec{A} \cdot \vec{B} = 2(-1) + 3 \times 3 + (-1)(4) = 3$
The projection of \vec{A} on $\vec{B} = \frac{\vec{A} \cdot \vec{B}}{|\vec{B}|} = \frac{3}{\sqrt{26}}$

15. (c)
$$\hat{n} = \frac{\vec{A} \times \vec{B}}{|\vec{A} \times \vec{B}|} = \frac{8\hat{i} - 8\hat{j} - 8\hat{k}}{8\sqrt{3}} = \frac{1}{\sqrt{3}}(\hat{i} - \hat{j} - \hat{k})$$

There are two unit vectors perpendicular to both \vec{A} and \vec{B} they are $\hat{n} = \pm \frac{1}{\sqrt{3}} (\hat{i} - \hat{j} - \hat{k})$

$$\begin{aligned} \mathbf{16.} \quad (a) \quad W &= \overline{F}(\overline{r_2} - \overline{r_1}) \\ &= (3\hat{i} - 2\hat{j} + \hat{k})(6\hat{i} + 8\hat{j} + 7\hat{k}) = 18 - 16 + 7 = 9 J \\ \mathbf{17.} \quad (d) \quad AB\cos\theta = AB\sin\theta \Rightarrow \tan\theta = 1 \therefore \theta = 45^{\circ} \\ &\therefore |\overline{C}| = \sqrt{A^2 + B^2 + 2AB\cos45^{\circ}} = \sqrt{A^2 + B^2 + \sqrt{2}AB} \\ \mathbf{18.} \quad (c) \quad \text{Vector perpendicular to } A \text{ and } B, \ \overline{A} \times \overline{B} = AB\sin\theta \hat{n} \\ &\therefore \text{ Unit vector perpendicular to } A \text{ and } B, \ \overline{A} \times \overline{B} = AB\sin\theta \hat{n} \\ &\therefore \text{ Unit vector perpendicular to } A \text{ and } B \\ &\hat{n} = \frac{\overline{A} \times \overline{B}}{|\ \overline{A}| \times |\ \overline{B}|| \sin\theta} \\ \\ \mathbf{19.} \quad (c) \quad P \text{ and } Q \text{ will be parallel if } \frac{2}{1} = \frac{b}{1} = \frac{2}{1} \quad \therefore b = 2 \\ \\ \mathbf{20.} \quad (b) \quad |\ \overline{A}| = 5 \ , |\ \overline{B}| = 10 \Rightarrow \frac{A}{B} = \frac{1}{2} \\ \\ \mathbf{21.} \quad (d) \quad \overline{A} = 2\hat{i} + \hat{j} - \hat{k}, \ \ \overline{B} = \hat{i} + \hat{j} + \hat{k} \\ \text{ Area of the triangle } = \frac{1}{2} (\overline{A} \times \overline{B}) \\ &= \frac{1}{2} \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 1 & -1 \\ 1 & 1 & 1 \end{vmatrix} = \frac{1}{2} |2\hat{i} - 3\hat{j} + \hat{k}| = \frac{1}{2} \sqrt{4 + 9 + 1} \\ &= \frac{\sqrt{14}}{2} sq.unit \end{aligned}$$

and time taken in coming back $t_2 = \frac{l}{v_b - v_a}$

[As current opposes the motion]

So
$$t_R = t_1 + t_2 = \frac{2l}{v_b [1 - (v_a / v_b)^2]}$$
(ii)

From equation (i) and (ii)

$$\frac{t_R}{t_Q} = \frac{1}{\left[1 - \left(v_a / v_b\right)^2\right]} > 1 \quad [\text{as } 1 - \frac{v_a^2}{v_b^2} < 1] \quad i.e. \ t_R > t_Q$$

i.e. time taken to complete the journey on quite day is lesser than that on rough day.

24. (a)
$$v_T = \sqrt{v_{TC}^2 + v_C^2} = \sqrt{(25\sqrt{3})^2 + (25)^2}$$

= $\sqrt{1875 + 625} = \sqrt{2500} = 25 \ km/hr$

25. (b)

26. (d) Let the velocity of the scooterist = v

Relative velocity of scooterist with respect to bus = (v - 10)

$$\Rightarrow S = (v - 10) \times 100 \Rightarrow 1000 = (v - 10) \times 100$$

$$\therefore v = 10 + 10 = 20 m/s$$

22. (a) The relative velocity $v_{rel.} = 60 - (-30) = 90 \text{ km} / hr.$

Distance between the train $s_{rel.} = 90 \ km$,

$$\therefore$$
 Time when they collide $=\frac{s_{rel.}}{v_{rel.}}=\frac{90}{90}=1\,hr.$

23. (b) If the breadth of the lake is *I* and velocity of boat is *v*. Time in going and coming back on a quite day

$$t_Q = \frac{l}{v_h} + \frac{l}{v_h} = \frac{2l}{v_h}$$
(i)

Now if $\boldsymbol{\nu}$ is the velocity of air- current then time taken in going across the lake,

$$t_1 = \frac{l}{v_b + v_a}$$
 [As current helps the motion]