

Class - 7th
Exercise - 4.1

Q) which of the following numbers are not perfect cube

(i) $216 = \underline{2 \times 2 \times 2} \times \underline{3 \times 3 \times 3}$

216 is perfect cube

$$\begin{array}{r|l} 2 & 216 \\ \hline 2 & 108 \\ \hline 2 & 54 \\ \hline 3 & 27 \\ \hline 3 & 9 \\ \hline 3 & 3 \\ \hline & 1 \end{array}$$

(ii) $128 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times (2)$

2 is left

$\therefore$ 128 is not a perfect cube

$$\begin{array}{r|l} 2 & 128 \\ \hline 2 & 64 \\ \hline 2 & 32 \\ \hline 2 & 16 \\ \hline 2 & 8 \\ \hline 2 & 4 \\ \hline 2 & 2 \\ \hline & 1 \end{array}$$

(iii) $1000 = \underline{2 \times 2 \times 2} \times \underline{5 \times 5 \times 5}$

1000 is a perfect cube

$$\begin{array}{r|l} 2 & 1000 \\ \hline 2 & 500 \\ \hline 2 & 250 \\ \hline 5 & 125 \\ \hline 5 & 25 \\ \hline 5 & 5 \\ \hline & 1 \end{array}$$

iv) $100 = 2 \times 2 \times 5 \times 5$

To make pair of 3 we need
one 2 and one 5
So 100 is not perfect cube

$$\begin{array}{r|l} 2 & 100 \\ \hline & 50 \\ 2 & \hline & 25 \\ 5 & \hline & 5 \\ 5 & \hline & 1 \end{array}$$

i) $46656 = \underbrace{2 \times 2 \times 2 \times 2 \times 2 \times 2}_{2^6} \times \underbrace{3 \times 3 \times 3 \times 3 \times 3 \times 3}_{3^6}$

∴ 46656 is a perfect cube

$$\begin{array}{r|l} 2 & 46656 \\ \hline & 23328 \\ 2 & \hline & 11664 \\ 2 & \hline & 5832 \\ 2 & \hline & 2916 \\ 2 & \hline & 1458 \\ 3 & \hline & 729 \\ 3 & \hline & 243 \\ 3 & \hline & 81 \\ 3 & \hline & 27 \\ 3 & \hline & 9 \\ 3 & \hline & 3 \\ 3 & \hline & 1 \end{array}$$

Q2 Find the smallest number by which each of the follow numbers must be multiplied to obtain a perfect cube.

(1) $243 = \underbrace{3 \times 3 \times 3 \times 3 \times 3}_{3^5}$

To make it perfect cube
we need one more 3
So we multiply by 3

$243 \times 3 = \underbrace{3 \times 3 \times 3 \times 3 \times 3}_{3^5} \times \underbrace{3 \times 3 \times 3}_{3^3}$

$\sqrt[3]{729} = \underbrace{3 \times 3 \times 3}_{3^3} \times \underbrace{3 \times 3 \times 3}_{3^3}$
 $= 3 \times 3$
 $= 9$

$$\begin{array}{r|l} 3 & 243 \\ \hline & 81 \\ 3 & \hline & 27 \\ 3 & \hline & 9 \\ 3 & \hline & 3 \\ 3 & \hline & 1 \end{array}$$

(i) $256 = \underline{2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2}$

To make it perfect cube
we need one more 2
 $\therefore$ we multiply by 2

$256 \times 2 = \underline{2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2}$

$\sqrt[3]{512} = 2 \times 2 \times 2$
 $= 8$

2	256
2	128
2	64
2	32
2	16
2	8
2	4
2	2
	1

(ii) $72 = \underline{2 \times 2 \times 2 \times 3 \times 3}$

To make it perfect cube
we need one more 3
 $\therefore$ we multiply by 3

$72 \times 3 = \underline{2 \times 2 \times 2 \times 3 \times 3 \times 3}$

$\sqrt[3]{216} = 2 \times 3 = 6$

2	72
2	36
2	18
3	9
3	3
	1

(iv) $675 = \underline{3 \times 3 \times 3 \times 5 \times 5}$

To make it perfect cube
we need one more 5
 $\therefore$ we multiply by 5

$675 \times 5 = \underline{3 \times 3 \times 3 \times 5 \times 5 \times 5}$

$\sqrt[3]{3375} = 3 \times 5 = 15$

3	675
3	225
3	75
5	25
5	5
	1

$$(V) 100 = 2 \times 2 \times 5 \times 5$$

To make it perfect cube

we need one 2 and one 5

∴ we multiply by 2×5

$$\begin{array}{r|l} 2 & 100 \\ \hline 2 & 50 \\ 5 & 25 \\ 5 & 5 \\ & 1 \end{array}$$

$$100 \times 2 \times 5 = \underline{2 \times 2 \times 2} \times \underline{5 \times 5 \times 5}$$

$$\sqrt[3]{1000} = 2 \times 5 = 10$$

Q3- Find the smallest number by which each of the following numbers must be divided to obtain a perfect cube.

$$(i) 81 = \underline{3 \times 3 \times 3} \times \textcircled{3}$$

3 left alone

∴ we divide with 3

$$81 \div 3 = \underline{3 \times 3 \times 3} \times \cancel{3}$$

$$\sqrt[3]{27} = \underline{3 \times 3 \times 3} = 3$$

$$\begin{array}{r|l} 3 & 81 \\ \hline 3 & 27 \\ 3 & 9 \\ 3 & 3 \\ & 1 \end{array}$$

$$(ii) 128 = \underline{2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2} \times \textcircled{2}$$

2 left alone

∴ we divide with 2

$$128 \div 2 = \underline{2 \times 2 \times 2 \times 2 \times 2 \times 2} \times \cancel{2}$$

$$64 = \underline{2 \times 2 \times 2 \times 2 \times 2 \times 2}$$

$$\sqrt[3]{64} = 2 \times 2 = 4$$

$$\begin{array}{r|l} 2 & 128 \\ \hline 2 & 64 \\ 2 & 32 \\ 2 & 16 \\ 2 & 8 \\ 2 & 4 \\ 2 & 2 \\ & 1 \end{array}$$

$$(III) 135 = \underline{3 \times 3 \times 3 \times 5}$$

5 left alone

∴ we divide with 5

$$135 \div 5 = \underline{3 \times 3 \times 3 \times 5}$$

$$27 = \underline{3 \times 3 \times 3}$$

$$\sqrt[3]{27} = 3$$

$$\begin{array}{r|l} 3 & 135 \\ \hline & 45 \\ 3 & 15 \\ \hline & 5 \\ 5 & 1 \\ \hline \end{array}$$

$$(IV) 192 = \underline{2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3}$$

3 left alone

∴ we divide with 3

$$192 \div 3 = \underline{2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3}$$

$$64 = \underline{2 \times 2 \times 2 \times 2 \times 2 \times 2}$$

$$\sqrt[3]{64} = 2 \times 2 = 4$$

$$\begin{array}{r|l} 2 & 192 \\ \hline & 96 \\ 2 & 48 \\ \hline & 24 \\ 2 & 12 \\ \hline & 6 \\ 2 & 3 \\ \hline & 1 \\ 3 & \\ \hline \end{array}$$

$$(V) 704 = \underline{2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 11}$$

11 left alone

∴ we divide by 11

$$704 \div 11 = \underline{2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 11}$$

$$64 = \underline{2 \times 2 \times 2 \times 2 \times 2 \times 2}$$

$$\sqrt[3]{64} = 2 \times 2 = 4$$

$$\begin{array}{r|l} 2 & 704 \\ \hline & 352 \\ 2 & 176 \\ \hline & 88 \\ 2 & 44 \\ \hline & 22 \\ 2 & 11 \\ \hline & 1 \\ 11 & \\ \hline \end{array}$$

Q4

Sides of cuboid = 5cm, 2cm and 5cm

$$\text{volume of cuboid} = 5 \times 2 \times 5 \\ \text{or } 5 \times 5 \times 2$$

to make cube we need one 5 and two 2

$$\therefore 5 \times 2 \times 2 = 20 \text{ is required number}$$