

# 4

## Root Locus Technique



### Multiple Choice Questions

- Q.1** Consider the points  $s_1 = -3 + j4$  and  $s_2 = -3 - j2$  in the s-plane. Then, for a system with the open-loop transfer function

$$G(s)H(s) = \frac{K}{(s+1)^4}$$

- (a)  $s_1$  is on the root locus, but not  $s_2$
- (b)  $s_2$  is on the root locus, but not  $s_1$
- (c) both  $s_1$  and  $s_2$  are on the root locus
- (d) neither  $s_1$  nor  $s_2$  is on the root locus

[GATE-1999]

- Q.2** The characteristic equation of a control system is given by

$$s(s+4)(s^2+2s+5) + k(s+1) = 0$$

What are the angles of the asymptotes for the root loci for  $k \geq 0$ ?

- (a)  $60^\circ, 180^\circ, 300^\circ$
- (b)  $0^\circ, 180^\circ, 300^\circ$
- (c)  $120^\circ, 180^\circ, 240^\circ$
- (d)  $0^\circ, 120^\circ, 240^\circ$

[ESE-2005]

- Q.3** The characteristic equation of a feedback control system is given by  $s^3 + 5s^2 + (K+6)s + K = 0$ . In the root loci diagram, the asymptotes of the root loci for large 'K' meet at a point in the s-plane whose coordinates are

- (a) (2, 0)
- (b) (-1, 0)
- (c) (-2, 0)
- (d) (-3, 0)

[ESE-1999]

- Q.4** The root locus plot of the system having the loop transfer function

$$G(s)H(s) = \frac{K}{s(s+4)(s^2+4s+5)}$$

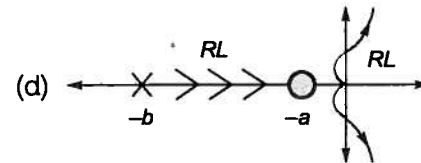
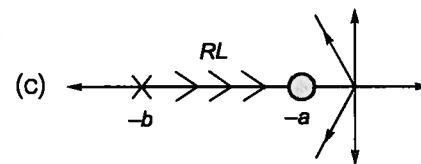
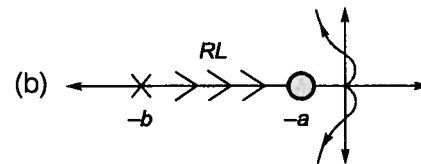
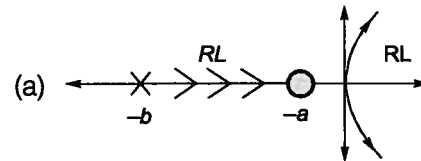
has

- (a) no breakaway point
- (b) three real breakaway points
- (c) only one breakaway point
- (d) one real and two complex breakaway points

[ESE-2001]

- Q.5** Which of the following is the following is the valid root loci

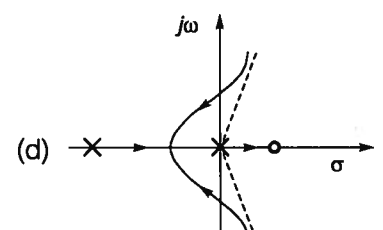
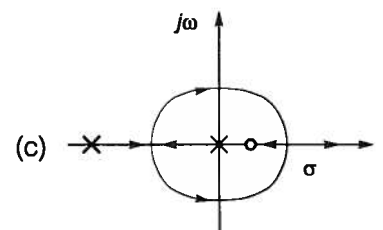
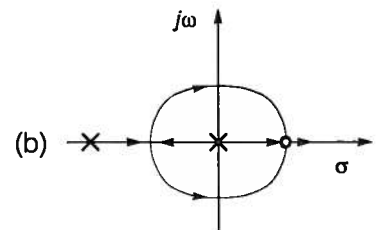
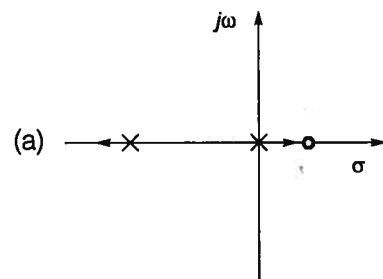
$$G(s) = \frac{K(s+a)}{s^2(s+b)} \quad |b| > |a|$$



- Q.6** An unity feedback system is given as,

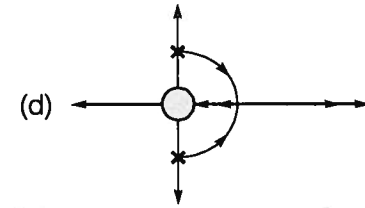
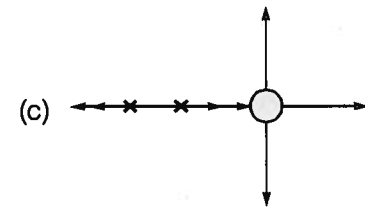
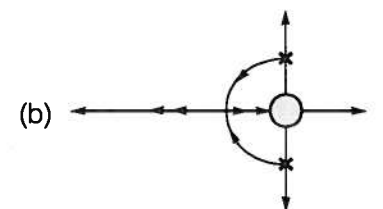
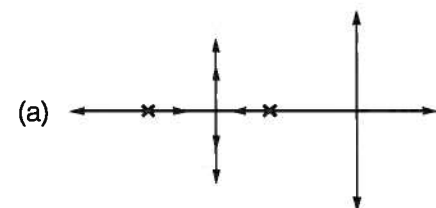
$$G(s) = \frac{K(1-s)}{s(s+3)}$$

Indicate the correct root locus diagram

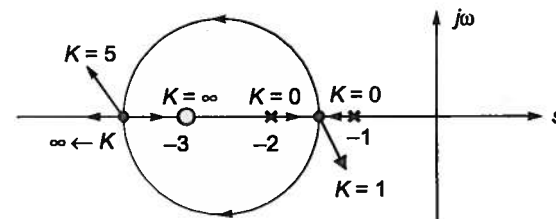


[GATE-2005, IES-2001]

**Q.7** The O.L.T.F of a system is  $G(s) = \frac{K}{s(s+\alpha)}$ . The valid root locus for  $0 < \alpha < \infty$  when  $K = 10$  is



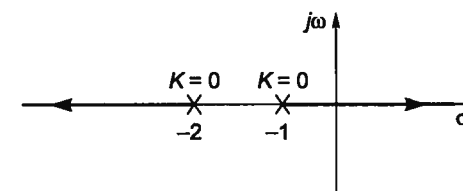
**Q.8** The root-locus diagram for a closed-loop feedback system is shown in the figure. The system is overdamped.



- (a) only if  $0 \leq K \leq 1$
- (b) only if  $1 < K < 5$
- (c) only if  $K > 5$
- (d) if  $0 < K < 1$  or  $K > 5$

[GATE-2001]

**Q.9** The root locus of a unity feedback system is shown in the figure.



The closed-loop transfer function of the system is

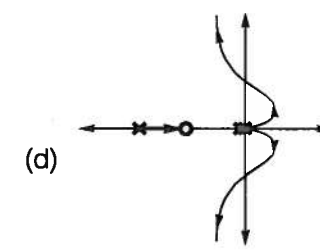
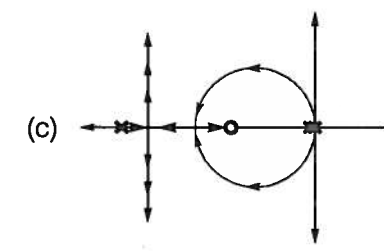
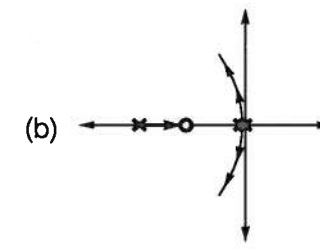
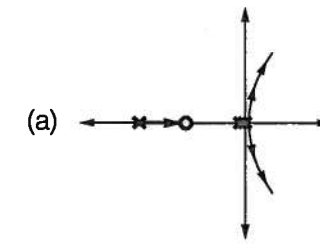
- (a)  $\frac{C(s)}{R(s)} = \frac{K}{(s+1)(s+2)}$
- (b)  $\frac{C(s)}{R(s)} = \frac{-K}{(s+1)(s+2)+K}$
- (c)  $\frac{C(s)}{R(s)} = \frac{K}{(s+1)(s+2)-K}$
- (d)  $\frac{C(s)}{R(s)} = \frac{K}{(s+1)(s+2)+K}$

[GATE-2014]

**Q.10** The OLTF of a control system is

$$G(s) = \frac{K(s+4/3)}{s^2(s+12)}$$

The valid RL will be



### Numerical Data Type Questions

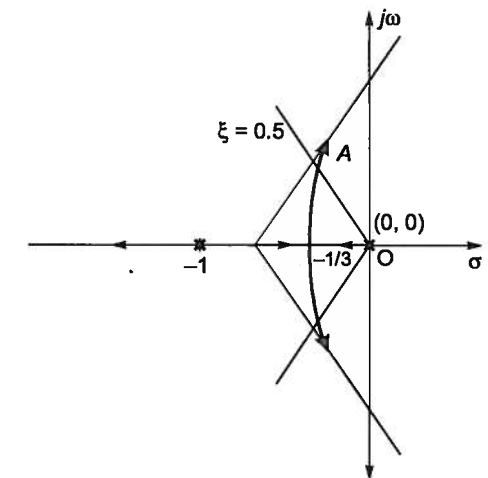
**Q.11** A unity feedback control system has an open-loop transfer function

$$G(s) = \frac{K}{s(s^2+7s+12)}$$

\_\_\_\_\_ is gain  $K$  for which  $s = -1 + j1$  will lie on the root locus of this system.

[GATE-2007]

**Q.12** The characteristic equation of a unity negative feedback system is  $1 + KG(s) = 0$ . The open loop transfer function  $G(s)$  has one pole at 0 and two poles at -1. The root locus of the system for varying  $K$  is shown in the figure.



The constant damping ratio line, for  $\xi = 0.5$ , intersects the root locus at point A. The distance from the origin to point A is given as 0.5. The value of  $K$  at point A is \_\_\_\_\_.

[GATE-2014]

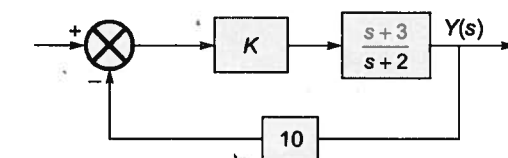
**Q.13** The open-loop transfer function of a unity feedback configuration is given as

$$G(s) = \frac{K(s+4)}{(s+8)(s^2-9)}$$

The value of a gain  $K(>0)$  for which  $-1 + j2$  lies on the root locus is \_\_\_\_\_.

[GATE-2015]

**Q.14** For the system shown in figure,  $s = -2.75$  lies on the root locus if  $K$  is \_\_\_\_\_.



[GATE-2015]



## Try Yourself

- T1. Consider a feedback system with characteristic equation

$$1 + \frac{K}{s(s+1)(s+2)} = 0$$

Compute the angles of the asymptotes of the root-locus branches with the real axis of the s-plane. Also find the centroid and the breakaway points of the root-locus of the system. Assume that  $K$  varies from 0 to  $\infty$ .

[Ans. Centroid  $\rightarrow (-1, 0)$

Breakaway point  $s = -0.422$ ]

- T2. Draw the root loci of the system showing all the relevant point for open-loop transfer function of the system given by

$$G(s) = \frac{K}{s(s^2 + 4s + 8)}$$

- T3. Given  $G(s)H(s) = \frac{K}{s(s+1)(s+4)}$  sketch the root locus of the system

(i) Determine the value of  $K$  for which the system is at the verge of instability.

[Ans:  $K = 20$ ]

(ii) For the damping ratio ( $\delta$ ) 0.34, determine the value of  $K$  and the gain margin (GM).

- T4. The forward-path transfer function of a *ufb* system is

$$G(s) = \frac{K(s+2)}{(s+3)(s^2 + 2s + 2)}$$

The angle of departure from the complex poles is  $\pm\phi_D$ ; where  $\phi_D =$  \_\_\_\_\_ degree.

[Ans: 108.4]

- T5. The forward path transfer function of a unity negative feedback system is given by

$$G(s) = \frac{K}{(s+2)(s-1)}$$

The value of  $K$  which will place both the poles of the closed-loop system at the same location, is \_\_\_\_\_.

[Ans:  $K = 2.25$ ]

