293



Total No. of Questions: 24 Total No. of Printed Pages: 4

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Regd.						
No.						

Part-III

MATHEMATICS, Paper - II (B)

(English version)

Time: 3 Hours]

[Max. Marks: 75

Note: This question paper consists of three sections A, B and C.

SECTION - A

 $10 \times 2 = 20$

- I. Very short answer type questions.
 - (i) Answer all questions.
 - (ii) Each question carries TWO marks.
 - 1. Find the equation of the Circle, whose extremities of a diameter are (-4, 3) and (3, -4).
 - 2. Find the centre and radius of the Sphere

$$x^2 + y^2 + z^2 - 2x + 4y - 6z - 2 = 0.$$

- 3. Find the value of K, if the lines 2x + 3y + 4 = 0 and x + y + k = 0 are conjugate with respect to $y^2 = 8x$.
- 4. If the eccentricity of a hyperbola is $\frac{5}{4}$, then find the eccentricity of its conjugate hyperbola.

- 5. Find the n^{th} derivative of $f(x) = \log (4x^2 9)$.
- 6. Evaluate:

$$\int \frac{\sin(\tan^{-1} x)}{1+x^2} dx , \quad \text{for } x \in \mathbb{R} .$$

7. Evaluate:

$$\int e^x \left(\sec x + \sec x \, \tan x \right) dx$$

on
$$I \subset \mathbb{R} \setminus \{(2n+1) \frac{\pi}{2} : n \in \mathbb{Z}\}$$

8. Evaluate:

$$\int_{0}^{4} |2-x| dx$$

- 9. Find the area bounded between the curves $y = x^2$, y = 2x.
- 10. Find the order and degree of the differential equation

$$\frac{d^2y}{dx^2} = \left[1 + \left(\frac{dy}{dx}\right)^2\right]^{\frac{5}{3}}.$$

SECTION-B

 $5 \times 4 = 20$

- II. Short answer type questions.
 - Attempt ANY FIVE questions.
 - (ii) Each question carries FOUR marks.
 - 11. If a point P is moving such that lengths of tangents drawn from P to the circles $x^2 + y^2 4x 6y 12 = 0$ and $x^2 + y^2 + 6x + 18y + 26 = 0$ are in the ratio 2:3; then find the equation of the locus of P.

- 12. The normal at a point t_1 on $y^2 = 4ax$ meets the parabola again at the point t_2 , then prove that $t_1t_2 + t_1^2 + 2 = 0$.
- **13.** Find the equations of the tangents to the hyperbola $x^2 4y^2 = 4$, which are *(i)* parallel, *(ii)* perpendicular to the line x + 2y = 0.
- 14. If PSQ is a chord passing through the focus S of a conic and 'l' is semilatus rectum, show that $\frac{1}{SP} + \frac{1}{SQ} = \frac{2}{l}$.
- 15. Evaluate:

$$\int \frac{1}{5 + 4\cos 2x} \ dx \ .$$

- **16.** Solve: $(xy^2 + x)dx + (yx^2 + y)dy = 0$.
- 17. Solve: $(1+x^2) \frac{dy}{dx} + y = e^{\tan^{-1}x}$.

SECTION-C

 $5 \times 7 = 35$

- III. Long answer type questions.
 - (i) Attempt ANY FIVE questions.
 - (ii) Each question carries SEVEN marks.
 - 18. Find the equation of Circle passing through the points (3, 4), (3, 2), (1, 4).
 - 19. Find the equation of the Circle which passes through the point (0, -3) and intersects the circles given by the equations $x^2 + y^2 6x + 3y + 5 = 0$ and $x^2 + y^2 x 7y = 0$ orthogonally.

- 20. A chord PQ of an ellipse S = 0 subtends a right angle at the centre of the ellipse. Show that the point of intersection of tangents at P and Q lies on another ellipse $\frac{x^2}{a^4} + \frac{y^2}{b^4} = \frac{1}{a^2} + \frac{1}{b^2}$.
- 21. If $y = e^{m \sin^{-1} x}$, then prove that $(1 - x^2)y_{n+2} - (2n+1)xy_{n+1} - (n^2 + m^2)y_n = 0$.
- 22. Obtain reduction formula for $I_n = \int \tan^n x \ dx$ for an integer $n \ge 2$, and deduce the value of $\int \tan^6 x \ dx$.
- 23. Evaluate:

$$\int_0^1 \sqrt{\frac{1-x}{1+x}} \ dx.$$

24. Find the approximate value of π from $\int_0^1 \frac{1}{1+x^2} dx$ using Simpson's rule by dividing [0,1] into 4 equal parts.