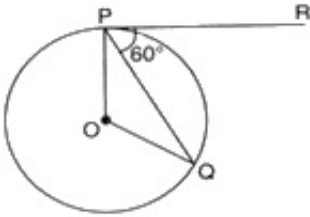


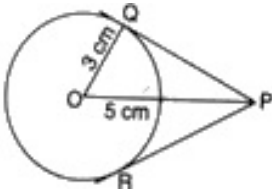
CBSE Test Paper 02

Chapter 10 Circles

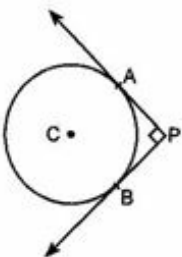
1. If O is the centre of a circle, PQ is a chord and tangent PR at P makes an angle of 60° with PQ, then $\angle POQ$ is equal to **(1)**



- a. 110°
b. 120°
c. 100°
d. 90°
2. In the given figure, if $OQ = 3$ cm, $OP = 5$ m, then the length of PR is **(1)**

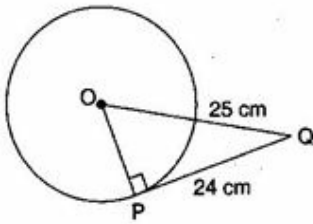


- a. 4 cm
b. 3 cm
c. 5 cm
d. 6 cm
3. In figure, PA and PB are two tangents drawn from an external point P to a circle with centre C and radius 4 cm. If $PA \perp PB$, then the length of each tangent is: **(1)**

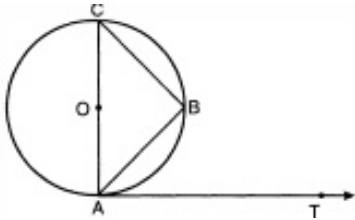


- a. 5 cm
b. 3 cm
c. 4 cm
d. 8 cm

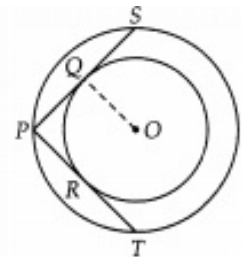
4. In the given figure, O is the centre of the circle with radius 10 cm. If $AB \parallel CD$, $AB = 16$ cm and $CD = 12$ cm, the distance between the two chords AB and CD is : **(1)**
- 12 cm
 - 20 cm
 - 16 cm
 - 14 cm
5. The length of tangent PQ, from an external point Q is 24 cm. If the distance of the point Q from the centre is 25 cm, then the diameter of the circle is **(1)**



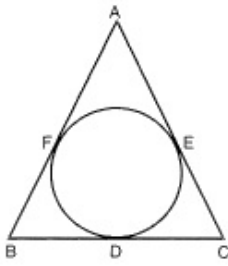
- 15 cm
 - 14 cm
 - 12 cm
 - 7 cm
6. In the given figure, AB is a chord of the circle and AOC is its diameter such that $\angle ACB = 50^\circ$. If AT is the tangent to the circle at the point A, find $\angle BAT$ **(1)**



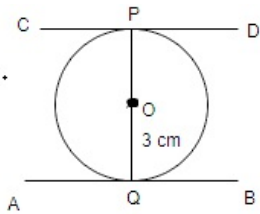
7. What term will you use for a line which intersect a circle at two distinct points? **(1)**
8. In the fig. there are two concentric circles with centre O. PRT and PQS are tangents to the inner circle from a point P lying on the outer circle. If $PR = 5$ cm find the length of PS. **(1)**



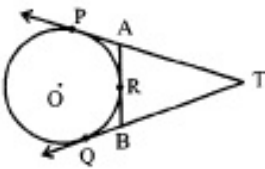
9. A triangle ABC is drawn to circumscribe a circle. If $AB = 13$ cm, $BC = 14$ cm and $AE = 7$ cm, then find AC. **(1)**



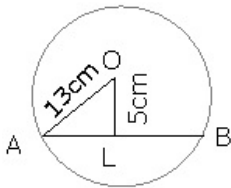
10. Find the distance between two parallel tangents of a circle of radius 3 cm. **(1)**



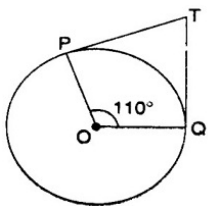
11. In the given figure, TP and TQ are tangents from T to the circle with centre O and R is any point on the circle. If AB is a tangent to the circle at R, prove that $TA + AR = TB + BR$. **(2)**



12. In figure, if $OL = 5$ cm, $OA = 13$ cm, then length of AB is **(2)**

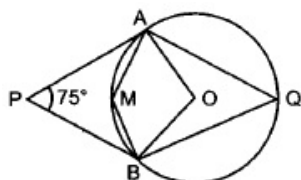


13. In figure, if TP and TQ are the two tangents to a circle with centre O so that $\angle POQ = 110^\circ$, then find $\angle PTQ$. **(2)**

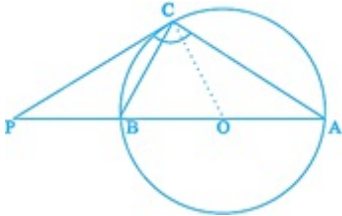


14. From an external point P, tangents PA and PB are drawn to a circle with centre O. At one point E on the circle tangent is drawn which intersects PA and PB at C and D respectively. If $PA = 14$ cm, find the perimeter of $\triangle PCD$. **(3)**

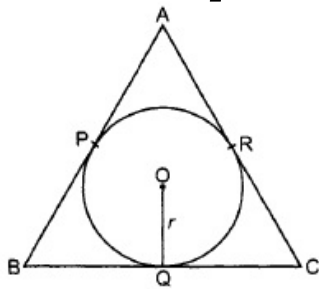
15. In the given figure, O is the centre of the circle. Determine $\angle AQB$ and $\angle AMB$, if PA and PB are tangents **(3)**



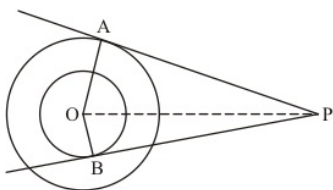
16. Prove that the line segment joining the points of contact of two parallel tangents of a circle, passes through its centre. **(3)**
17. The tangent at a point C of a circle and a diameter AB when extended intersect at P. If $\angle PCA = 110^\circ$, find $\angle CBA$.
[Hint: Join C with centre O]. **(3)**



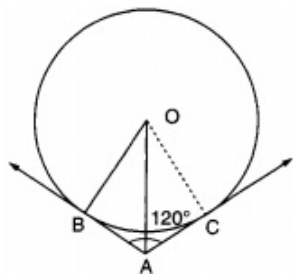
18. In figure, the sides AB, BC and CA of triangle ABC touch a circle with centre O and radius r at P, Q and R respectively. Prove that
- $AB + CQ = AC + BQ$
 - $\text{Area (ABC)} = \frac{1}{2} (\text{perimeter of } \triangle ABC) \times r$ **(4)**



19. In Fig. there are two concentric circles with centre O of radii 5 cm and 3 cm. From an external point P, tangents PA and PB are drawn to these circles. If AP = 12 cm, find the length of BP. **(4)**



20. In fig. two tangents AB and AC are drawn to a circle with centre O such that $\angle BAC = 120^\circ$. Prove that $OA = 2AB$. **(4)**



CBSE Test Paper 02
Chapter 10 Circles

Solution

1. b. 120°

Explanation: Here $\angle RPO = 90^\circ$

$$\angle RPQ = 60^\circ \text{ (given)}$$

$\therefore \angle OPQ = 90^\circ - 60^\circ = 30^\circ$ $\angle PQO = 30^\circ$ Also [Opposite angles of equal radii] Now,
In triangle OPQ,

$$\angle OPQ + \angle PQO + \angle QOP = 180^\circ$$

$$\Rightarrow 30^\circ + 30^\circ + \angle QOP = 180^\circ$$

$$\Rightarrow \angle QOP = 120^\circ$$

2. a. 4 cm

Explanation: Here $\angle Q = 90^\circ$ [Angle between tangent and radius through the point of contact]

Now, in right angled triangle OPQ,

$$OP^2 = OQ^2 + PQ^2$$

$$\Rightarrow (5)^2 = (3)^2 + PQ^2$$

$$\Rightarrow PQ^2 = 25 - 9 = 16$$

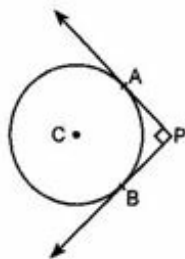
$$\Rightarrow PQ = 4 \text{ cm}$$

But $PQ = PR$ [Tangents from one point to a circle are equal]

Therefore, $PR = 4 \text{ cm}$

3. c. 4 cm

Explanation:

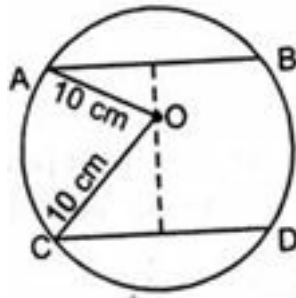


Construction: Joined AC and BC. Here $CA \perp AP$ and $CB \perp BP$ and $PA \perp PB$ Also
 $AP = PB$

Therefore, BPAC is a square. $\Rightarrow AP = PB = BC = 4 \text{ cm}$

4. d. 14 cm

Explanation:



Let OP be the perpendicular to chord AB and P bisects the chord AB and OQ be the perpendicular to chord CD and Q bisects the chord CD.

$\therefore AP = BP = 8 \text{ cm}$ and $CQ = DQ = 6 \text{ cm}$

In triangle AOP, $OA^2 = OP^2 + AP^2$

$$\Rightarrow (10)^2 = OP^2 + (8)^2$$

$$\Rightarrow OP^2 = 100 - 64 = 36$$

$$\Rightarrow OP = 6 \text{ cm}$$

And in right angled triangle COQ,

$$OC^2 = OQ^2 + CQ^2$$

$$\Rightarrow (10)^2 = OQ^2 + (6)^2$$

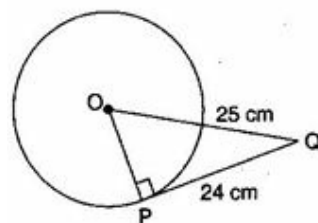
$$\Rightarrow OQ^2 = 100 - 36 = 64$$

$$\Rightarrow OQ = 8 \text{ cm}$$

Therefore, distance between two chord AB and CD = $OP + OQ = 6 + 8 = 14 \text{ cm}$

5. b. 14 cm

Explanation:



Here $\angle OPQ = 90^\circ$ [Angle between tangent and radius through the point of contact]

$$\therefore OQ^2 = OP^2 + PQ^2 \Rightarrow (25)^2 = OP^2 + (24)^2$$

$$\Rightarrow OP^2 = 625 - 576 \Rightarrow OP^2 = 49$$

$$\Rightarrow OP^2 = 49 \Rightarrow OP = 7 \text{ cm}$$

Therefore, the diameter = $2 \times OP = 2 \times 7 = 14 \text{ cm}$

$$\begin{aligned}
6. \quad & \therefore \angle ACB = 50^\circ \\
& \angle CBA = 90^\circ \text{ (Angle in semi-circle)} \\
& \therefore \angle OAB = 90^\circ - 50^\circ \\
& = 40^\circ \\
& \angle BAT = 90^\circ - \angle OAB \\
& = 90^\circ - 40^\circ \\
& = 50^\circ
\end{aligned}$$

7. A line that intersects a circle at two points in a circle is called a Secant.

$$\begin{aligned}
8. \quad & PQ = PR = 5 \text{ cm (Length of Tangents from same external point are always equal)} \\
& \text{and } PQ = QS \text{ (perpendicular from center of the circle to the chord bisects the chord)} \\
& \therefore PS = 2PQ \\
& = 2 \times 5 = 10 \text{ cm}
\end{aligned}$$

$$\begin{aligned}
9. \quad & AF = AE = 7 \text{ cm (tangents from same external point are equal)} \\
& \therefore BF = AB - AF = 13 - 7 = 6 \text{ cm} \\
& BD = BF = 6 \text{ cm (tangents from same external point)} \\
& \therefore CD = BC - BD = 14 - 6 = 8 \text{ cm} \\
& CE = CD = 8 \text{ cm} \\
& \therefore AC = AE + EC \\
& = 7 + 8 = 15 \text{ cm.}
\end{aligned}$$

$$\begin{aligned}
10. \quad & \text{Distance between two parallel tangents} = \text{diameter} = PQ \\
& PQ = OP + OQ = 3 + 3 = 6 \text{ cm} \\
& \text{The total distance between two parallel tangents lines is 6 cm.}
\end{aligned}$$

$$\begin{aligned}
11. \quad & \text{Length of tangents from same external point are equal.} \\
& \therefore TP = TQ \\
& AP = AR \\
& \text{and } BR = BQ \\
& \text{We have, } TP = TQ \\
& \Rightarrow TA + AP = TB + BQ \\
& \Rightarrow TA + AR = TB + BR \\
& \text{Hence proved.}
\end{aligned}$$

$$\begin{aligned}
 12. \quad AB &= 2 AL = 2 \sqrt{OA^2 - OL^2} \\
 &= 2 \sqrt{13^2 - 5^2} \\
 &= 2 \sqrt{169 - 25} = 2 \sqrt{144} \\
 &= 2 \times 12 = 24 \text{ cm}
 \end{aligned}$$

$$13. \quad \angle POQ = 110^\circ$$

$\angle OPT = 90^\circ$ [Angle between tangent and radius through the point of contact]

$\angle OQT = 90^\circ$ [Angle between tangent and radius through the point of contact]

In quadrilateral OPTQ,

$$\angle POQ + \angle OQT + \angle PTQ = 360^\circ$$

\therefore The sum of all the angles of a quadrilateral is 360° .

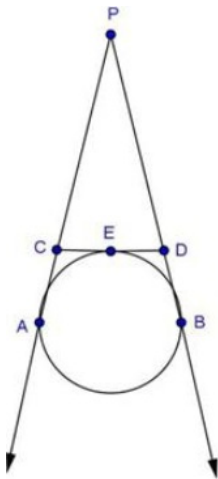
$$\Rightarrow 110^\circ + 90^\circ + 90^\circ + \angle PTQ = 360^\circ$$

$$\Rightarrow 290^\circ + \angle PTQ = 360^\circ$$

$$\Rightarrow \angle PTQ = 360^\circ - 290^\circ = 70^\circ$$

\Rightarrow Hence, the $\angle PTQ$ is 70° .

14. We have,



$$AC = CE, BD = DE$$

$$\text{And, } AP = BP = 14 \text{ cm}$$

$$\therefore \text{ Perimeter of } \triangle PCD = PC + CD + PD$$

$$\Rightarrow \text{ Perimeter of } \triangle PCD = PC + (CE + ED) + PD$$

$$= (PC + CE) + (ED + PD)$$

$$= (PC + AC) + (BD + PD)$$

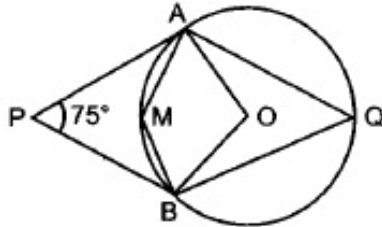
$$= PA + PB$$

$$= 14 + 14$$

$$= 28$$

\therefore Perimeter of $\triangle PCD = 28$ cm.

15. Given,



$OA \perp PA$ and

$OB \perp PB$

$$\therefore \angle OAP = 90^\circ \text{ and } \angle OBP = 90^\circ$$

$$\Rightarrow \angle OAP + \angle OBP = 180^\circ$$

PBOA is cyclic quadrilateral

$$\therefore \angle APB + \angle AOB = 180^\circ$$

$$\Rightarrow \angle AOB = 180^\circ - 75^\circ = 105^\circ$$

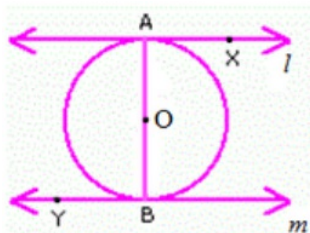
Now $\angle AOB = 2\angle AQB$

$$\therefore \angle AQB = \frac{1}{2}(105^\circ) = 52.5^\circ$$

Now $\angle AMB + \angle AQB = 180^\circ$

$$\Rightarrow \angle AMB = 180^\circ - 52.5^\circ = 127.5^\circ$$

16.



Given: l and m are the tangent to a circle such that $l \parallel m$, intersecting at A and B respectively.

To prove: AB is a diameter of the circle.

Proof:

A tangent at any point of a circle is perpendicular to the radius through the point of contact.

$$\therefore \angle XAO = 90^\circ$$

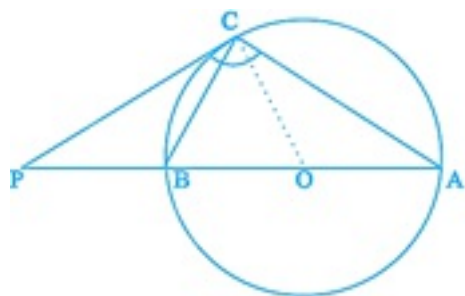
$$\text{and } \angle YBO = 90^\circ$$

Since $\angle XAO + \angle YBO = 180^\circ$

An angle on the same side of the transversal is 180° .

Hence the line AB passes through the centre and is the diameter of the circle.

17. According to the question, we are given that tangent at a point C of a circle and a diameter AB when extended intersect at P. If $\angle PCA = 110^\circ$, find $\angle CBA$.



OC and CP are radius and tangent respectively at contact point C.

So, $\angle OCP = 90^\circ$

$\angle OCA = \angle ACP - \angle OCP$

$\Rightarrow \angle OCA = 110^\circ - 90^\circ$

$\Rightarrow \angle OCA = 20^\circ$

In $\triangle OAC$,

$OA = OC$ [Radii of same circle]

Therefore, $\angle OCA = \angle A = 20^\circ$ [Since, Angles opposite to equal sides are equal]

CP and CB are tangent and chord of a circle.

Therefore, $\angle CBP = \angle A$ [Angles in alternate segments are equal]

In $\triangle CAP$,

$\angle P + \angle A + \angle ACP = 180^\circ$ [Angled sum property of a triangle]

$\Rightarrow \angle P + 20^\circ + 110^\circ = 180^\circ$

$\Rightarrow \angle P = 180^\circ - 130^\circ$

$\Rightarrow \angle P = 50^\circ$

In $\triangle BPC$,

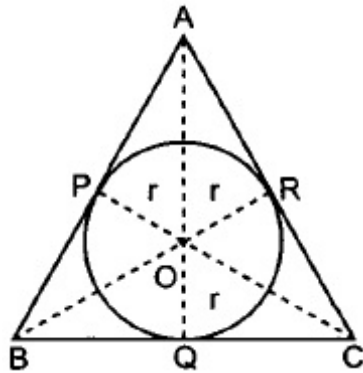
Exterior angle $\angle CBA = \angle P + \angle BCP$

$\Rightarrow \angle CBP = 50^\circ + 20^\circ$

$\Rightarrow \angle CBP = 70^\circ$

18. Given, the sides AB, BC and CA of triangle ABC touch a circle with centre O and radius

r at P, Q and R respectively.



(i) $AP = AR$ [Tangents from A] ...(i)

Similarly, $BP = BQ$...(ii)

$CR = CQ$...(iii)

Now,

$\therefore AP = AR$

$\Rightarrow (AB - BP) = (AC - CR)$

$\Rightarrow AB + CR = AC + BP$

$\Rightarrow AB + CQ = AC + BQ$ [Using eq. (ii) and (iii)]

(ii) Let $AB = x$, $BC = y$, $AC = z$

\therefore Perimeter of $\triangle ABC = x + y + z$...(iv)

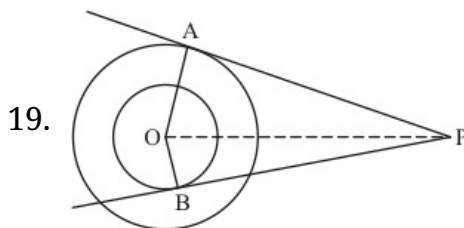
Area of $\triangle ABC = \frac{1}{2}$ [area of $\triangle AOB$ + area of $\triangle BOC$ + area of $\triangle AOC$]

\Rightarrow Area of $\triangle ABC = \frac{1}{2} \times AB \times OP + \frac{1}{2} \times BC \times OQ + \frac{1}{2} \times AC \times OR$

\Rightarrow Area of $\triangle ABC = \frac{1}{2} \times x \times r + \frac{1}{2} \times y \times r + \frac{1}{2} \times z \times r$

\Rightarrow Area of $\triangle ABC = \frac{1}{2} (x + y + z) \times r$

\Rightarrow Area of $\triangle ABC = \frac{1}{2} (\text{Perimeter of } \triangle ABC) \times r$



Join OA, OB and OP.

$\angle OAP = 90^\circ$ as the tangent makes a right angle with the radius of the circle at the point of contact.

In $\triangle OAP$, we have,

$$OP^2 = OA^2 + AP^2$$

$$\Rightarrow OP^2 = 5^2 + 12^2$$

$$\Rightarrow OP = 13 \text{ cm}$$

$\angle OBP = 90^\circ$ as the tangent makes a right angle with the radius of the circle at the point of contact.

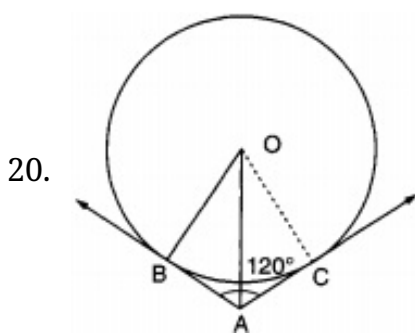
In $\triangle OBP$, we have,

$$OP^2 = OB^2 + BP^2$$

$$\Rightarrow 13^2 = 3^2 + BP^2$$

$$\Rightarrow BP^2 = 169 - 9 = 160$$

$$\Rightarrow BP = \sqrt{160} \text{ cm} = 4\sqrt{10} \text{ cm}$$



In \triangle 's OAB and OAC, we have,

$$\angle OBA = \angle OCA = 90^\circ$$

$$OA = OA \text{ [Common]}$$

$$AB = AC \text{ [}\because \text{ Tangents from an external point are equal in length]}$$

Therefore, by RHS congruence criterion, we have,

$$\triangle OBA \cong \triangle OCA$$

$$\Rightarrow \angle OAB = \angle OAC \text{ [By c.p.c.t.]}$$

$$\therefore \angle OAB = \angle OAC = \frac{1}{2} \angle BAC$$

$$= \frac{1}{2} \times 120^\circ = 60^\circ$$

$$\Rightarrow \angle OAB = \angle OAC = 60^\circ$$

In $\triangle OBA$, we have,

$$\cos B = \frac{AB}{OA}$$

$$\Rightarrow \cos 60^\circ = \frac{AB}{OA}$$

$$\Rightarrow \frac{1}{2} = \frac{AB}{OA}$$

$$\Rightarrow OA = 2AB$$

Hence proved.