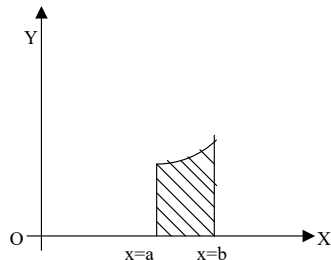


NUMERICAL INTEGRATION & AREAS

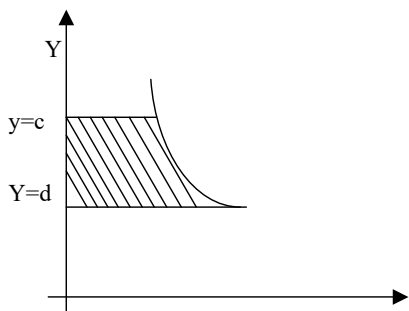
AREA OF PLANE CURVES

- If $y = f(x)$ is continuous in $[a, b]$ then the area bounded by the curve $y = f(x)$, the x-axis and $x = a, x = b (a < b)$ is given by

$$\int_a^b |f(x)| dx$$

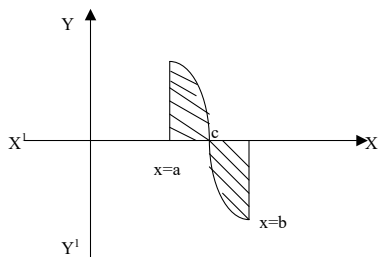


- The area bounded by the curve $x = f(y)$, the axis of y and two abscissae $y = c$ and $y = d$ is given by $\int_c^d |f(y)| dy$

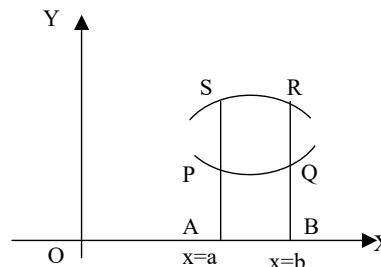


- Let $f(x) \geq 0$ in $[a, c]$ and $f(x) \leq 0$ in $[c, b]$, so that the curve crosses the x-axis at c . Then the curve lies partly above the x-axis and partly below the x-axis. Hence required area is

$$\int_a^b |f(x)| dx = \int_a^c f(x) dx + \int_c^b -f(x) dx$$



- Let the area enclosed between the two curves $y = f_1(x)$ and $y = f_2(x)$ and ordinates $x = a, x = b (b > a)$ is denoted by R. Then the area of the region $R = \text{Area of the region ASRB} - \text{Area of the region APQB} = \int_a^b f_2(x) dx - \int_a^b f_1(x) dx$.



- The area of one arc of the curve $y = \sin ax$ and x-axis is $2/a$ square units.
- The area of one arc of the curve $y = \cos ax$ and x-axis is $2/a$ square units.
- The area of the triangle formed by the lines $y = m_1x + c_1, y = m_2x + c_2, y = m_3x + c_3$ is $\frac{1}{2} \left| \sum \frac{(c_1 - c_2)^2}{m_1 - m_2} \right|$ sq. units.
- The area of the parallelogram formed by $a_1x + b_1y + c_1 = 0, a_1x + b_1y + d_1 = 0, a_2x + b_2y + c_2 = 0, a_2x + b_2y + d_2 = 0$ is $\left| \frac{(c_1 - d_1)(c_2 - d_2)}{a_1b_2 - a_2b_1} \right|$ sq. units.
- The area of rhombus formed by $ax \pm by \pm c = 0$ is $\frac{2c^2}{|ab|}$ sq. units
- The area of the triangle formed by the tangent and normal at $P(x_1, y_1)$ and x-axis (m is the slope of tangent) is $\frac{1}{2} y_1^2 \left| m + \frac{1}{m} \right|$ sq. units.
- The area of the triangle formed by the tangent and normal at $P(x_1, y_1)$ and y-axis (m is the

slope of tangent) is $\frac{1}{2}x_1^2 \left| m + \frac{1}{m} \right|$ sq. units.

- The area of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ is πab sq. units.
- The area between the parabolas $y^2 = 4ax$ and $x^2 = 4by$ is $\frac{16ab}{3}$ sq. units.
- The area between the parabola $y^2 = 4ax$ and the line $y = mx$ is $\frac{8a^2}{3m^3}$ sq. units.
- The area between the parabola $y^2 = 4ax$ and its latusrectum is $\frac{8a^2}{3}$ sq. units.
- The area enclosed by the curve $\left(\frac{x}{a}\right)^{\frac{2}{3}} + \left(\frac{y}{b}\right)^{\frac{2}{3}} = 1$ is $\frac{3\pi ab}{8}$ sq. units.
- The area of the asteroid $x^{\frac{2}{3}} + y^{\frac{2}{3}} = a^{\frac{2}{3}}$ is $\frac{3\pi a^2}{8}$ sq. units.
- The area bounded by $\sqrt{x} + \sqrt{y} = \sqrt{a}$ and the co-ordinate axes is $\frac{a^2}{6}$ sq. units.
- The area enclosed between one arc of the cycloid $x = a(\theta + \sin \theta)$, $y = a(1 - \cos \theta)$ and its base is $3\pi a^2$ sq. units.
- **Trapezoidal Rule:** Let $y = f(x)$ be given function and for equally spaced $(n+1)$ arguments $x = a, a+h, a+2h, \dots, a+(n-1)h, a+nh = b$ and $y_0 = f(x_0)$, $y_1 = f(x_1)$, $\dots, y_{n-1} = f(x_{n-1})$, $y_n = f(x_n)$ in $[a, b]$ then $\int_a^b y dx = \frac{h}{2} [(y_0 + y_n) + 2(y_1 + y_2 + \dots + y_{n-1})]$.
- **Simpson's Rule:** Let $y = f(x)$ be given func-

tion and for equally spaced $(n+1)$ arguments $x = a, a+h, a+2h, \dots, a$

$+ (n-1)h, a+nh = b$ and $y_0 = f(x_0)$, $y_1 = f(x_1)$, $\dots, y_{n-1} = f(x_{n-1})$, $y_n = f(x_n)$ here $[a, b]$ is divided into n subintervals where n is even then $\int_a^b y dx =$

$$\frac{h}{3} [(y_0 + y_n) + 4(y_1 + y_3 + \dots + y_{n-1}) + 2(y_2 + y_4 + \dots + y_{n-2})]$$

PROBLEMS:

1. A curve is passing through the points (1,2), (1.5,2.4), (2,2.7), (2.5,2.8), (3,3) then the area bounded by the curve, X-axis and $x=1$, $x=3$ using Simpson's rule is
1. 5 2. 5.1 3. 5.2 4. 5.4
2. If the graph of $y = f(x)$ passes through (0,0), (0.5,0.19), (1,0.34), (1.5,0.43), (2,0.47) then $\int_0^2 f(x) dx$ by Simpson's rule is
1. 0.605 2. 0.61 3. 0.601 4. 0.615
3. The interval $[1,7]$ is divided into 6 equal intervals and the value of $\int_1^7 (x^2 + x + 1) dx$ using Trapezoidal and Simpson's rules are respectively Δ_1 and Δ_2 then
1. $\Delta_1 = \Delta_2$ 2. $\Delta_1 > \Delta_2$
3. $\Delta_1 < \Delta_2$ 4. $\Delta_1 - \Delta_2 = 2$
4. Using Simpson's rule, by taking 4 equal parts, the value of $\int_1^5 \frac{1}{x} dx =$
1. 1.58 2. 1.62 3. 1.75 4. 2.3
5. Using Simpson's rule, by taking 4 equal parts, the value of $\int_1^5 (2x-1) dx =$
1. 22 2. 20.7 3. 20 4. 19.7
6. Using Trapezoidal rule, by taking 4 equal intervals, the value of $\int_1^5 (2x+1) dx =$
1. 5 2. 8 3. 28 4. 28.2
7. Using Trapezoidal rule, by taking 3 equal intervals, the value of $\int_1^4 3x^2 dx =$
1. 24.5 2. 34.5 3. 64.5 4. 74.5

8. If $\log_{10} 100 = 2, \log_{10} 101 = 2.004,$
 $\log_{10} 102 = 2.0086, \log_{10} 103 = 2.0128$ then
 $\int_{100}^{103} \log_{10} x dx$ by Trapezoidal rule is
 1. 6.0193 2. 6.0019
 3. 6.1093 4. 6.11993
9. A river is 80 meters wide. The depth “d” in meters at a distance x meters from one bank to other bank is given by the following table.
- | | | | | |
|-----------|----|----|----|----|
| x meters: | 0 | 10 | 20 | 30 |
| d meters: | 0 | 4 | 7 | 9 |
| | 40 | 50 | 60 | 70 |
| | 12 | 15 | 14 | 8 |
| | | | | 0 |
- The approximate area of cross section using Simpson’s rule is
 1. 700 sq. mts. 2. 800 sq. mts
 3. 720 sq. mts 4. 740 sq. mts.
10. A curve is drawn to pass through the following points.
- | | | | | | | |
|-------|-----|-----|-----|---|-----|-----|
| x : 1 | 1.5 | 2 | 2.5 | 3 | 3.5 | 4 |
| y : 2 | 2.4 | 2.7 | 2.8 | 3 | 2.6 | 2.1 |
- Using Simpson’s rule the approximate area bounded by the curve, the X-axis and the lines $x=1$ and $x=4$ is
 1. 6.78 sq. units 2. 7.78 sq. units
 3. 7.73 sq. units 4. 7.68 sq. units
11. The values of $f(x)$ at the nodal points are
- | | | | | |
|-------|---|------|------|------|
| x: | 0 | 0.25 | 0.5 | 0.75 |
| f(x): | 1 | 0.8 | 0.67 | 0.57 |
- 0.5
 The approximate area bounded by the curve, the X-axis and the lines $x=0, x=1$ using Simpson’s rule is
 1. 0.693 sq. units 2. 0.793 sq. units
 3. 0.0693 sq. units 4. 0.593 sq. units
12. The velocity of a train which starts from rest is given by the following table, the time being recorded in minutes from start and speed in KMPH
- | | | | | |
|----------|----|----|----|----|
| Minute:2 | 4 | 6 | 8 | 10 |
| KMPH: 10 | 18 | 25 | 29 | 32 |
| | 12 | 14 | 16 | 18 |
| | 20 | 11 | 5 | 2 |
| | | | | 0 |
- The approximate total distance in 20 minutes run by the train by Simpson’s rule
 1. 5.155 2. 5.05 3. 5 4. 4.99

13. Given that $e^0 = 1, e = 2.72, e^2 = 7.39,$
 $e^3 = 20.09, e^4 = 54.6$. The approximate area bounded by the curve $y = e^x$ between lines $x=0$ to $x=4$ using Simpson’s rule is
 1. 53.873 2. 55 3. 54.5 4. 54
14. If $f(22) = 0.39, f(23) = 0.41,$
 $f(24) = 0.43, f(25) = 0.44$ and
 $f(26) = 0.46$ then $\int_{22}^{26} f(x) dx$ Using Simpson’s rule is
 1. 1.6 2. 1.7 3. 1.8 4. 1.9
15. The values of $f(x)$ for $x=0,1,2,3,4,5,6$ are given by 2,4,10,16,20,24,38 respectively then
 $\int_0^6 f(x) dx$ by Using Simpson’s rule is
 1. 90 2. 91 3. 92 4. 93
16. In Trapezoidal rule, the curve $y = f(x)$ between two successive ordinates is approximated as
 1. straight line 2. parabola
 3. cubic parabola 4. arc of a circle
17. Using simpson’s rule the part of the curve $y = f(x)$ between 3 successive ordinates is assumed as
 1. straight line 2. parabola
 3. cubic parabola 4. arc of a circle

KEY

1-10	3	1	2	2	3
	3	3	1	1	2
11-17	1	1	1	2	3
	1	2			

LEVEL - I

1. The area enclosed by the curve $|x| + |y| = 1$ in sq. units is
 1. 2 2. 4 3. 1 4. 1/2
2. The area of the region bounded by the curve $y = x^3$, x-axis and the ordinates $x=1, x=4$ is
 1. $\frac{255}{4}$ sq. units 2. $\frac{225}{2}$ sq. units
 3. $\frac{125}{3}$ sq. units 4. $\frac{124}{3}$ sq. units

3. the area of the region bounded by the curve $y = x^2$, x-axis and the ordinates $x=0$, $x=2$ is
1. $\frac{8}{3}$ sq. units
 2. $\frac{3}{8}$ sq. units
 3. 24 sq. units
 4. 25 sq. units
4. The area bounded by the parabola $y = 4x^2$, X-axis between the ordinates $x=2$, $x=4$ is
1. $\frac{224}{3}$ sq. units
 2. $\frac{125}{3}$ sq. units
 3. $\frac{122}{3}$ sq. units
 4. $\frac{121}{3}$ sq. units
5. The area of the region bounded by $y = [x]$ and the ordinates $x=1$, $x=2$ in sq. units is
1. 2
 2. 1
 3. 4
 4. $\frac{1}{2}$
6. The area bounded by the curve $x^2 = 4y$ and the line $x=2$ in sq. units is
1. 1
 2. $\frac{2}{3}$
 3. $\frac{3}{2}$
 4. 2
7. The area bounded by the curve $y = 1 + \frac{8}{x^2}$ with X-axis and ordinates at $x=2$ and $x=4$ in sq. units is
1. 4
 2. 2
 3. $\frac{1}{2}$
 4. 5
8. The area bounded by the parabola $y = 4 - x^2$ and X-axis in sq. units is
1. $\frac{32}{3}$
 2. $\frac{16}{3}$
 3. $\frac{8}{3}$
 4. $\frac{1}{3}$
9. The area bounded by the X-axis and the curve $y = 4x - x^2 - 3$ in sq. units is
1. $\frac{1}{3}$
 2. $\frac{2}{3}$
 3. $\frac{4}{3}$
 4. $\frac{7}{3}$
10. The area of the region bounded by the curve $y^2 = 4ax$ and the line $x=a$ is
1. $\frac{8a^2}{3}$ sq. units
 2. $\frac{4a^2}{3}$ sq. units
 3. $\frac{a^2}{3}$ sq. units
 4. $\frac{16a^2}{3}$ sq. units
11. The area bounded by the curve $y = 7x - 10 - x^2$ with X-axis is
1. 9 sq. units
 2. 3 sq. units
 3. $\frac{9}{2}$ sq. units
 4. 4 sq. units
12. The area bounded by any one of the arc of the curve $y = \sin x$ in sq. units with X axis
1. 2 sq. units
 2. 1 sq. unit
 3. $\frac{2}{3}$ sq. unit
 4. $\frac{1}{2}$ sq. units
13. The area bounded by the curve $y = \cos x$ in $[0, \pi]$ is
1. 1 sq. unit
 2. 2 sq. unit
 3. $\frac{3}{2}$ sq. units
 4. 5 sq. units
14. The area bounded by the ellipse $3x^2 + 2y^2 = 6$ with the co-ordinate axes in sq. units is
1. $\sqrt{6}\pi$
 2. $\sqrt{8}\pi$
 3. $\sqrt{12}\pi$
 4. $\sqrt{3}\pi$
15. The area bounded by the ellipse $b^2x^2 + a^2y^2 = a^2b^2$ in the first quadrant in sq. units is
1. πab
 2. $\frac{\pi ab}{2}$
 3. $\frac{\pi ab}{4}$
 4. $\frac{\pi ab}{3}$
16. The area bounded by the parabola $y = x^2$ and the straight line $y=2x$ is
1. $\frac{4}{3}$ sq. units
 2. $\frac{3}{4}$ sq. units
 3. $\frac{2}{3}$ sq. units
 4. $\frac{1}{3}$ sq. units
17. The area bounded by the curve $y = \sin 2x + \cos 2x$ and the x-axis between the ordinates $x=0$, $x = \frac{\pi}{4}$ is
1. 1 sq. unit
 2. $\frac{1}{2}$ sq. unit
 3. $\frac{2}{3}$ sq. units
 4. 0 sq. units
18. The area bounded by the curve $y = \cos x$, x-axis between the ordinates $x = 0$, $x = 2\pi$ is
1. 1 sq. unit
 2. 4 sq. units
 3. $\frac{2}{3}$ sq. units
 4. 2 sq. units
19. The area bounded by the curve $y = \sin x$, x-axis between the ordinates $x = -\pi$, $x = \pi$ is
1. 2 sq. units
 2. 3 sq. units
 3. 4 sq. units
 4. $\frac{1}{2}$ sq. units
20. The area of the curve $x = a \cos^3 t$, $y = b \sin^3 t$ in sq. units is
1. $\frac{3\pi ab}{4}$
 2. $\frac{3\pi ab}{8}$
 3. $\frac{\pi ab}{4}$
 4. $\frac{\pi ab}{8}$

21. The area bounded by the parabola $y^2 = 4x$ and its latusrectum is
1. $\frac{8}{3}$ sq. units
 2. $\frac{3}{8}$ sq. units
 3. 12 sq. units
 4. $\frac{1}{3}$ sq. units
22. The area bounded by the curve $x = 4 - y^2$ and the Y-axis is
1. $32/3$ sq. units
 2. $22/5$ sq. units
 3. $1/3$ sq. units
 4. $64/3$ sq. units
23. The area bounded by the curve $x = a \left(\frac{1-t^2}{1+t^2} \right)$, $y = \frac{2at}{1+t^2}$ in sq. units is
1. $\frac{\pi a^2}{2}$
 2. πa^2
 3. $\frac{\pi a^2}{4}$
 4. $\frac{3\pi a^2}{2}$
24. The area bounded by the curve $y = \frac{x^2}{2}$ bounded by $x = 0, x = 2$ and $y = 0$ is
1. $\frac{4}{5}$ sq. units
 2. $\frac{3}{2}$ sq. units
 3. $\frac{3}{4}$ sq. units
 4. $\frac{4}{3}$ sq. units
25. The area bounded by the curve $y = (x-4)(x-1)$ and the X-axis is
1. $\frac{6}{5}$ sq. units
 2. $\frac{9}{4}$ sq. units
 3. $\frac{9}{2}$ sq. units
 4. $\frac{5}{6}$ sq. units
26. The area between the curve $y^2 = 9x$ and the line $y = 3x$ is
1. $\frac{1}{3}$ sq. units
 2. $\frac{8}{3}$ sq. units
 3. $\frac{1}{2}$ sq. units
 4. $\frac{1}{5}$ sq. units
27. The area bounded by the curve $xy = 4$, x-axis between the ordinates $x=2, x=4$ is
1. $\log 2$ sq. units
 2. $2 \log 2$ sq. units
 3. $3 \log 2$ sq. units
 4. $4 \log 2$ sq. units
28. The area bounded by the circle $x^2 + y^2 = a^2$ with the co-ordinate axes is
1. πa^2 sq. units
 2. $\frac{\pi a^2}{4}$ sq. units
 3. $4\pi a^2$ sq. units
 4. $\frac{\pi}{6}$ sq. units
29. The area of the region bounded by $\sqrt{x} + \sqrt{y} = 1$ in the first quadrant is
1. 1 sq. unit
 2. $\frac{1}{2}$ sq. units
 3. $\frac{1}{6}$ sq. units
 4. $\frac{1}{5}$ units
30. Area bounded by the curve $x = a \cos \theta, y = b \sin \theta$ is
1. πab sq. units
 2. $\frac{\pi ab}{4}$ sq. units
 3. $2\pi ab$ sq. units
 4. $\frac{\pi ab}{2}$ sq. units
31. The area between the curve $y = (x-1)^2 - 25$ and X-axis in sq. units is
1. $\frac{250}{3}$
 2. $\frac{500}{3}$
 3. $\frac{750}{3}$
 4. $\frac{1000}{3}$
32. The area of the region $y = ax - bx^2$ bounded by X-axis in sq. units is
1. $\frac{a^3}{6b^2}$
 2. $\frac{a^3}{6}$
 3. a
 4. b
33. The area of the region bounded by $y = \sin^4 x$, X-axis and ordinates $x = 0, x = 2\pi$ (in sq. units)
1. $\frac{3\pi}{4}$
 2. $\frac{\pi}{4}$
 3. $\frac{3\pi}{2}$
 4. 3π

KEY

1-10	1	1	1	1	2
	2	1	1	3	1
11-20	3	1	2	1	3
	1	1	2	3	2
21-30	1	1	2	4	3
	3	4	1	3	1
31-33	2	1	1		

LEVEL - II

1. The area of the region bounded by the curve $y = x^2 + 1$ and $y = 2x - 2$ between $x = -1$ and $x = 2$ is
 1. 9 sq. units 2. 12 sq. units
 3. 15 sq. units 4. 14 sq. units
2. The area bounded by the two parabolas $y^2 = 4ax$ and $x^2 = 4ay$ is
 1. $16a^2$ units 2. $\frac{16a^2}{3}$ sq. units
 3. $\frac{32a^2}{3}$ sq. units 4. $\frac{64a^2}{3}$ sq. units
3. The area bounded by the two parabolas $y^2 = 8x$ and $x^2 = 8y$ is
 1. 64 sq. units 2. $\frac{64}{3}$ sq. units
 3. $\frac{32}{3}$ sq. units 4. $\frac{1}{3}$ sq. units
4. The area bounded by the two curves $y = \sqrt{x}$ and $x = \sqrt{y}$ is
 1. $\frac{1}{3}$ sq. units 2. $\frac{2}{3}$ sq. units
 3. $\frac{1}{5}$ sq. units 4. $\frac{1}{7}$ sq. units
5. The area bounded by the two parabolas $y^2 = 4ax$ and $x^2 = 4by$ is
 1. $16ab$ sq. units 2. $4ab$ sq. units
 3. $8ab$ sq. units 4. $\frac{16ab}{3}$ sq. units
6. The area bounded by the parabola $y^2 = 4ax$ and the line $y = mx$ is
 1. $\frac{8a^2}{m^3}$ sq. units 2. $\frac{8a}{m^3}$ sq. units
 3. $\frac{8a}{m}$ sq. units 4. $\frac{8a^2}{3m^3}$ sq. units
7. The area bounded by $y^2 = 4ax$ and $y = mx$ is $\frac{a^2}{3}$ sq. units then $m =$
 1. 1 2. 2 3. 3 4. 4
8. The area of the elliptic quadrant with the semi major axis and semi minor axis as 6 and 4 respectively
 1. 6π sq. units 2. 4π sq. units
 3. 24π sq. units 4. 12π sq. units
9. The area enclosed between $y = \sin 2x$, $y = \sqrt{3} \sin x$ between $x = 0$ and $x = \frac{\pi}{6}$ is
 1. $\frac{7}{4} - \sqrt{3}$ sq. units 2. $\frac{7}{4} + \sqrt{3}$ sq. units
 3. $\frac{7\sqrt{3}}{4}$ sq. units 4. $7 - \frac{\sqrt{3}}{4}$ sq. units
10. The area of the region bounded by the curve $y = \sin x$, x-axis between the ordinates $x = 0, x = 2\pi$ is
 1. 1 sq. units 2. 2 sq. units
 3. 3 sq. units 4. 4 sq. units
11. The area bounded by the two curves $y = \sin x$, $y = \cos x$ and the X-axis in the first quadrant is
 1. $2 - \sqrt{2}$ sq. units 2. $2 + \sqrt{2}$ sq. units
 3. $2(\sqrt{2} - 1)$ sq. units 4. 4 sq. units
12. The area bounded by the curves $y = \sin x$, $y = \cos x$ and the y-axis and the first point of intersection is
 1. $\sqrt{2}$ sq. units 2. $\sqrt{2} - 1$ sq. units
 3. $2 + \sqrt{2}$ sq. units 4. 0 sq. units
13. The area of the region bounded by the curve $y = x \sin x$ and X-axis between $x = 0, x = 2\pi$ is
 1. 4π sq. units 2. 2π sq. units
 3. $\frac{\pi}{3}$ sq. units 4. $\frac{\pi}{4}$ sq. units
14. The area bounded by the curves $y = \cos x$, $y = \cos 2x$ between the ordinates $x = 0, x = \frac{\pi}{3}$ are in the ratio
 1. $2\sqrt{3} : 4 - \sqrt{3}$ 2. 2 : 1
 3. $2\sqrt{3} : 4 + \sqrt{3}$ 4. 1 : 3

15. The area bounded by $y=\sin x$, $y=\cos x$ between any two successive intersections is
 1. 2 2. $\sqrt{2}$ 3. $2\sqrt{2}$ 4. 4
16. The area bounded by $y = \cos x$, $y = x+1$ and $y = 0$ in the second quadrant is
 1. $\frac{3}{2}$ sq. units 2. 2 sq. units
 3. 1 sq. unit 4. $\frac{1}{2}$ sq. units
17. The area bounded by the curve $y = \sin x$, $y = \cos x$, $x = 0$ and $x = \frac{\pi}{4}$ is
 1. $\sqrt{2} - 1$ sq. units 2. $\sqrt{2} + 1$ sq. units
 3. $2\sqrt{2}$ sq. units 4. $2\sqrt{2} - 1$ sq. units
18. The area of a region bounded by X-axis and the curves defined by $y = \tan x$, $-\frac{\pi}{3} \leq x \leq \frac{\pi}{3}$ and $y = \cot x$, $\frac{\pi}{6} \leq x \leq \frac{3\pi}{2}$ is
 1. $\log 3$ sq. units 2. $\log 5$ sq. units
 3. $\log 1$ sq. unit 4. $\log 2$ sq. units
19. Area bounded by the curve $y = \sin x - \cos x$ in $\left[0, \frac{\pi}{2}\right]$ in sq. units is
 1. 2 2. $2\sqrt{2}$
 3. $2(\sqrt{2} - 1)$ 4. $(\sqrt{2} - 1)$
20. The area bounded by the curve $y^2 = x$ and the line $x=4$ is
 1. $\frac{32}{3}$ sq. units 2. $\frac{16}{3}$ sq. units
 3. $\frac{8}{3}$ sq. units 4. $\frac{4}{3}$ sq. units
21. The area bounded by the parabola $y^2 = 4x$ and the line $y = 2x - 4$ on the Y-axis.
 1. 9 sq. units 2. 5 sq. units
 3. 4 sq. units 4. 2 sq. units
22. The area enclosed between the parabola $y^2 = 4ax$ and the lines $x=a$, $x=9a$ in sq. units is
 1. $8a^2$ 2. $\frac{8a^2}{3}$ 3. $\frac{208a^2}{3}$ 4. a^2
23. the area bounded by the parabola $x^2 = 4ay$, x-axis and the straight line $y=2a$ is
 1. $16\sqrt{2}a^2$ sq. units 2. $\frac{16\sqrt{2}}{3}a^2$ sq. units
 3. $\frac{32\sqrt{2}}{3}a^2$ sq. units 4. $\frac{32\sqrt{2}}{5}a^2$ sq. units
24. The area between the curve $y = x^2$ and $y = x + 2$ is
 1. $\frac{9}{2}$ sq. units 2. $\frac{3}{2}$ sq. units
 3. 9 sq. units 4. 6 sq. units
25. The area of the region to the left of the parabola $x = 2y^2$ to the right of the Y-axis and between $y=1$ and $y=3$ is
 1. $\frac{52}{3}$ sq. units 2. $\frac{9}{2}$ sq. units
 3. $\frac{13}{3}$ sq. units 4. $\frac{11}{2}$ sq. units
26. The area of the region between the curves $y = x^2$ and $y = x^3$ is
 1. $\frac{1}{12}$ sq. units 2. $\frac{1}{3}$ sq. units
 3. $\frac{1}{4}$ sq. units 4. $\frac{1}{2}$ sq. units
27. The area of the region bounded by $y = x$, $y = x^3$ is
 1. $\frac{1}{4}$ sq. units 2. $\frac{1}{12}$ sq. units
 3. $\frac{1}{3}$ sq. units 4. $\frac{1}{2}$ sq. units
28. The area of the region between the curve $y = 4x^2$ and the line $y = 6x - 2$ is
 1. $\frac{1}{9}$ sq. units 2. $\frac{1}{12}$ sq. units
 3. $\frac{3}{2}$ sq. units 4. $\frac{1}{5}$ sq. units
29. The part of the area bounded by the curve $x^2(y-1)=6$ between the ordinates $x=2$ and $x=3$ is 2 sq. units, if the ordinate $x=a$ divides the area into equal parts then $a=$
 1. $\sqrt{6}$ 2. $\sqrt{8}$ 3. $\frac{1}{\sqrt{2}}$ 4. $\frac{1}{\sqrt{3}}$

30. The area of the quadrilateral formed by the lines $y = 2x + 3$, $y = 0$, $x = 4$ and $x = 6$ is
 1. 26 sq. units 2. 24 sq. units
 3. 25 sq. units 4. 29 sq. units
31. The area in the first quadrant enclosed by the X-axis under the curve $x^2 + y^2 = 4$ and the line $x = \frac{y}{\sqrt{3}}$ is
 1. $\frac{\pi}{3}$ sq. units 2. $\frac{2\pi}{3}$ sq. units
 3. π sq. units 4. $\frac{\pi}{2}$ sq. units
32. Area of the region bounded by $y = |x|$ and $y = 2$ is
 1. 4 sq. units 2. 2 sq. units
 3. 1 sq. units 4. $\frac{1}{2}$ sq. units
33. Area of the region bounded by $y = |x|$ and $y = 1 - |x|$ is
 1. $\frac{1}{3}$ sq. units 2. 1 sq. units
 3. $\frac{1}{2}$ sq. unit 4. 2 sq. units
34. The area bounded by the parabola $x = y^2$ and the line $y = x - 6$ is
 1. $\frac{125}{3}$ sq. units 2. $\frac{125}{6}$ sq. units
 3. $\frac{125}{4}$ sq. units 4. $\frac{115}{3}$ sq. units
35. The area between the curves $y = \sqrt{x}$ and $y = x^3$ is
 1. $\frac{1}{12}$ sq. units 2. $\frac{5}{12}$ sq. units
 3. $\frac{3}{5}$ sq. units 4. $\frac{4}{5}$ sq. units
36. Area bounded by $y = \sqrt{a^2 - x^2}$, $x + y = 0$ and y-axis in sq. units is
 1. $a^2 \left(\frac{\pi}{2} \right)$ 2. $a^2 \left(\frac{\pi}{4} \right)$
 3. $a^2 \left(\frac{\pi}{8} \right)$ 4. $a^2 \pi$
37. The area of the triangle formed by the positive X-axis and the normal and tangent to the circle $x^2 + y^2 = 4$ at $(1, \sqrt{3})$ in sq. units is
 1. $\sqrt{3}$ 2. $\frac{1}{\sqrt{3}}$ 3. $2\sqrt{3}$ 4. $3\sqrt{3}$
38. The area bounded by $x^{2/3} + y^{2/3} = a^{2/3}$ in sq. units is
 1. $\frac{3\pi a^2}{8}$ 2. $\frac{3\pi a^2}{4}$ 3. $\frac{3\pi a^2}{16}$ 4. $\frac{3\pi a^2}{32}$
39. The area between the curves $y = \tan x$, $y = \cot x$ and x-axis $\left(0 \leq x \leq \frac{\pi}{2} \right)$ is
 1. $\log 2$ 2. $2 \log 2$ 3. $\frac{1}{2} \log 2$ 4. 1
40. Let A_n be the area bounded by the curve $y = (\tan x)^n$ and the lines $x = 0$, $y = 0$ and $x = \frac{\pi}{4}$ for $n \geq 2$, then $A_n + A_{n-2} =$
 1. $\frac{1}{n+1}$ 2. $\frac{1}{n-1}$ 3. $\frac{2}{n+1}$ 4. $\frac{2}{n-1}$
41. Area of the figure bounded by X-axis, $y = \sin^{-1} x$, $y = \cos^{-1} x$ and the first point of intersection from the origin is
 1. $2\sqrt{2}$ 2. $2\sqrt{2} + 1$ 3. $\sqrt{2} - 1$ 4. $\sqrt{2} + 1$
42. Area of the region $\{(x, y) / x^2 + y^2 \leq 1 \leq x + y\}$ is
 1. $\frac{\pi}{4} + \frac{1}{2}$ 2. $\frac{\pi}{4} - \frac{1}{2}$
 3. $\frac{\pi}{4} + \frac{3}{4}$ 4. $\pi + 1$
43. The area under the curve $y = x^2 - 3x + 2$ with boundaries as X-axis and the ordinates $x = 0$, $x = 3$ is
 1. $\frac{3}{5}$ sq. units 2. $\frac{11}{6}$ sq. units
 3. $\frac{7}{6}$ sq. units 4. $\frac{4}{5}$ sq. units
44. The area bounded by the curve $y = x^3 - 6x^2 + 8x$ and the x-axis is
 1. 8 sq. units 2. $\frac{8}{3}$ sq. units
 3. $\frac{3}{8}$ sq. units 4. 6 sq. units

Key

1-10	1	2	2	1	4
	4	2	1	1	4
11-20	1	2	1	1	3
	4	1	4	3	1
21-30	1	3	2	1	1
	1	4	2	1	1
31-40	2	1	3	2	2
	3	3	1	1	2
41-44	3	2	2	1	

LEVEL - III

- The area of the region bounded by $y = \tan x$ and tangent at $x = \frac{\pi}{4}$ and the x-axis is
 - $\log \sqrt{2} - \frac{1}{4}$ sq. units
 - $\log \sqrt{2} + \frac{1}{4}$ sq. units
 - $\log \sqrt{2}$
 - $\log 2$
- The area between the parabola $y^2 = 4x$, normal at one end of latusrectum and X-axis in sq. units is
 - $\frac{1}{3}$
 - $\frac{2}{3}$
 - $\frac{10}{3}$
 - $\frac{4}{3}$
- The area lying in the first quadrant between the curves $x^2 + y^2 = \pi^2$ and $y = \sin x$ and y-axis is
 - $\frac{\pi^3 - 8}{4}$ sq. units
 - $\frac{\pi^3 + 8}{4}$ sq. units
 - $4(\pi^3 - 8)$ sq. units
 - $\frac{\pi - 8}{4}$ sq. units
- The area bounded by the curves $y = 2^x$, $y = 2x - x^2$ between the lines $x=0$, $x=2$ is
 - $\frac{3}{\log 2} - \frac{4}{3}$ sq. units
 - $\frac{3}{\log 2} + \frac{4}{3}$ sq. units
 - $3 - 4 \log 2$ sq. units
 - $\frac{4}{3} - \frac{3}{\log 2}$ sq. units

- The area of the region between the curve $y = x^3$ and the lines $y = -x$ and $y = 1$ is
 - 5 sq. units
 - $\frac{4}{5}$ sq. units
 - $\frac{5}{4}$ sq. units
 - $\frac{3}{5}$ sq. units
- The area of the part of the circle $x^2 + y^2 = 8a^2$ and the parabola $y^2 = 2ax$ through which positive x-axis passes in sq. units is
 - $\frac{4a^2(3\pi + 2)}{3}$
 - $\frac{2a^2(3\pi - 2)}{3}$
 - $\frac{a^2(3\pi - 2)}{3}$
 - $\frac{2a^2(3\pi + 2)}{3}$
- The area between the parabolas $y^2 = 4a(x + a)$ and $y^2 = -4a(x - a)$ in sq. units is
 - $\frac{4a^2}{3}$
 - $\frac{8a^2}{3}$
 - $\frac{12a^2}{3}$
 - $\frac{16a^2}{3}$
- Area of the region bounded by $y = e^x$, $y = e^{-x}$, $x = 0$ and $x = 1$ in sq. units is
 - $\left(e + \frac{1}{e}\right)^2$
 - $\left(e - \frac{1}{e}\right)^2$
 - $\left(\sqrt{e} + \frac{1}{\sqrt{e}}\right)^2$
 - $\left(\sqrt{e} - \frac{1}{\sqrt{e}}\right)^2$
- The area of the region bounded by the curves $y = xe^x$, $y = xe^{-x}$ and the line $x=1$ is
 - $\frac{4}{e}$
 - $\frac{3}{e}$
 - $\frac{2}{e}$
 - $\frac{1}{e}$
- The area of the region bounded by the curves $y = ex \log x$ and $y = \frac{\log x}{ex}$ is
 - $\frac{e^2 - 5}{4e}$
 - $e - \frac{5}{4}$
 - $\frac{e}{4} - 5$
 - $\frac{e}{4} - \frac{1}{4e}$
- The value of c for which the area bounded by the curve $y = 8x^2 - x^5$, the lines $x=1$, $x=c$ and X-axis is $\frac{16}{3}$ sq. units is
 - 1
 - 0
 - 2
 - 1

12. The slope of the tangent to the curve $y = f(x)$ at $(x, f(x))$ is $2x+1$. If the curve passes through the point $(1,2)$ then the area of the region bounded by the curve, the X-axis and the line $x=1$ is
1. $\frac{2}{3}$ 2. $\frac{1}{3}$ 3. $\frac{1}{6}$ 4. $\frac{5}{6}$
13. The positive value of the parameter "a" for which the area of the figure bounded by $y = \sin ax$, $y=0$, $x = \frac{\pi}{a}$, $x = \frac{\pi}{3a}$ is equal to 8,
1. 1 2. $\frac{1}{3}$ 3. $\frac{1}{2}$ 4. $\frac{1}{4}$
14. The area of the region bounded by $y = |x-1|$ and $y=1$ in sq. units is
1. 1 2. $\frac{1}{2}$ 3. 2 4. 3
15. Area of the region bounded by $y = |x-1|$ and $y = 3-|x|$ is
1. 1 sq. unit 2. 2 sq. unit
3. 3 sq. units 4. 4 sq. units
16. The area bounded by the curve $y = f(x)$, the coordinates axes and the line $x=t$ is given by te^t then $f(x) =$
1. $xe^x - e^x$ 2. $xe^x + e^x$
3. xe^x 4. $xe^x + 2e^x$
17. Area of the region bounded by $y = x - [x]$, $2x-1=0$ and X-axis is
1. $\frac{1}{2}$ 2. $\frac{1}{4}$ 3. $\frac{1}{8}$ 4. 1
18. Area of the region bounded by $y = x - [x]$, $y = [x]$ and x-axis in $[0,2]$ is
1. $\frac{5}{2}$ 2. $\frac{3}{2}$ 3. 1 4. 2
19. The area bounded by the curve $a^2 y^2 = x^3 (2a-x)$ is
1. $\frac{\pi a^2}{4}$ 2. $\frac{\pi a^2}{16}$ 3. $\frac{\pi a^2}{32}$ 4. πa^2
20. Area bounded by the curve $y^2 (2a-x) = x^3$ and the line $x=2a$ is
1. $3\pi a^2$ 2. 2π 3. $2\pi a$ 4. 3π

21. Area bounded by the curve $xy^2 = a^2(a-x)$ and Y-axis is
1. π 2. $\frac{\pi}{2}$ 3. $\frac{\pi a^2}{2}$ 4. πa^2
22. For which of the following values of m is the area of the region bounded by the curve $y = x - x^2$ and the line $y = mx$ equal to $\frac{9}{2}$
1. -4 2. 2 3. 1 4. -2
23. The area bounded by $y = x^2$, $y = [x+1]$, $x \leq 1$ and the y-axis is
1. $\frac{1}{3}$ 2. $\frac{2}{3}$ 3. 1 4. $\frac{7}{3}$

KEY

1-10	1	3	1	1	3
	4	2	4	3	1
11-20	4	4	3	1	4
	2	3	3	4	1
21-30	4	4	2		

LEVEL - IV

NEW PATTERN QUESTIONS

1. I: The area bounded by $x = 2 \cos \theta$, $y = 3 \sin \theta$ is 36π sq. units.
II: The area bounded by $x = 2 \cos \theta$, $y = 2 \sin \theta$ is 4π sq. units.
Which of the above statement is correct?
1. Only I 2. Only II
3. Both I and II 4. Neither I nor II.
2. I: The area bounded by the curve $y = x^3$ and the ordinates $x = -2$ and $x = 1$ with X-axis is $\frac{15}{4}$ sq. units.
II: The area bounded by the parabola $y^2 = x$ and the straight line $y = 4$ with Y-axis is $\frac{64}{3}$ sq. units.
Which of the above statement is correct?
1. Only I 2. Only II
3. Both I and II 4. Neither I nor II.

3. I: The area bounded by the curve $y = \log_e x$, X-axis and the line $x=e$ is 1 sq. units.
 II: The area bounded by X-axis, the curve $y=f(x)$ and the lines $x=1, x=b$ is $\sqrt{b^2+1} - \sqrt{2}$ for all $b>1$!

$$\text{then } f(x) = \frac{x}{\sqrt{x^2+1}}.$$

Which of the above statement is correct?

1. Only I 2. Only II
 3. Both I and II 4. Neither I nor II.
4. I: The area bounded by the curves $y = \sin x$, $y = \cos x$ and Y-axis is $\sqrt{2} - 1$ sq. units.

II: The area bounded by $y = \cos x$, $y = x + 1$, $y = 0$ is $3/2$ sq. units.

Which of the above statement is correct?

1. Only I 2. Only II
 3. Both I and II 4. Neither I nor II.
5. I: The area bounded by the line $y=x$ and the curve $y = x^3$ is $1/2$ sq. units.

II: The area bounded by the curves $y = x^3$ and $y = x^2$ and the ordinates $x=1, x=2$ is $\frac{7}{12}$ sq. units.

Which of the above statement is correct?

1. Only I 2. Only II
 3. Both I and II 4. Neither I nor II.

KEY

1-5 2 3 3 3 1

1. Match the following:

List - I

List - II

1. Area of the region bounded by

$$y = 2x - x^2 \text{ and X-axis}$$

a. $1/3$

2. Area of the region

$$\{(x, y) : x^2 \leq y \leq |x|\}$$

b. $1/2$

3. Area bounded by

$$y = x \text{ and } y = x^3$$

c. $2/3$

4. Area bounded by $y = x|x|$,

$$\text{x-axis and } x = -1, x = 1$$

d. $4/3$

The correct match is

1. b,c,d,a

2. c,d,a,b

3. d,a,b,c

4. a,b,c,d

2. Match the following:

List - I

List - II

1. Area bounded by $y^2 = 4ax$

$$\text{and } x^2 = 4ay \text{ is}$$

a. $\frac{8a^2}{3}$

2. Area bounded by $y^2 = 4ax$

and its latusrectum is

b. $\frac{a^2}{6}$

3. Area bounded by

$$x = 2 \cos \theta, y = 2 \sin \theta \text{ is}$$

c. $\frac{16a^2}{3}$

4. Area bounded by $\sqrt{x} + \sqrt{y} = \sqrt{a}$

is

d. 2π

The correct match is

1. c,a,d,b

2. b,d,a,c

3. a,b,c,d

4. c,d,b,a

3. Match the following:

List - I

List - II

1. Area bounded by $y = |x|$

$$\text{and } y=2 \text{ is}$$

a. 4

2. Area bounded by

$$\frac{|x|}{a} + \frac{|y|}{b} = 1, \text{ when } a, b > 0 \text{ is } b. \frac{(\pi - 2)ab}{4}$$

3. Area between the ellipse

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1 \text{ and the chord}$$

$$\frac{x}{a} + \frac{y}{b} = 1$$

c. 1

4. Area bounded by $y = [x]$,

$$\text{the x-axis and } x=1, x=2 \text{ is}$$

d. $2ab$

The correct match is

1. a,d,c,b

2. a,d,b,c

3. b,d,a,c

4. a,b,c,d

4. Match the following:

List - I

List - II

1. Area of the region

bounded by

$$y = |5 \sin x| \text{ from } x=0$$

a. $3/2$

$$\text{to } x = 4\pi \text{ and x-axis}$$

2. The area bounded by

$$y = \cos x \text{ in } [0, 2\pi] \text{ and}$$

the X-axis

b. $\sqrt{2} - 1$

3. The area bounded by $y = \sin x$, $y = \cos x$ and the y -axis c. 4

4. The area bounded by $y = \cos x$, $y = x + 1$, $y = 0$ d. 40

The correct match is

- | | |
|------------|------------|
| 1. a,b,c,d | 2. d,b,a,c |
| 3. d,c,b,a | 4. d,a,b,c |

KEY

1. 3 2. 1 3. 2 4. 3

- A: Area bounded by $x = 4 - y^2$ with Y-axis
B: Area bounded by $x = 6 + 5y - y^2$ with Y-axis
C: Area bounded by $2x = y^2 - 1$ with Y-axis
The ascending order of A,B,C is
1. A,B,C 2. B,C,A 3. A,C,B 4. C,A,B
- A: The area bounded by $x = 3$, $y^2 = 3x$
B: The area bounded by $y = 1 - |x|$ and X-axis.
C: The area enclosed between the curve $y = x^2$ and the line $y = 3x$
The descending order of A,B,C is
1. A,C,B 2. B,C,A 3. A,B,C 4. C,A,B
- Arrangement of the following areas between the curves is descending order:
A: $y^2 = 4x$, $x^2 = 4y$
B: $y = x$, $y = x^3$
C: $y^2 = 8x$, $y = 2x$
D: $y = \sqrt{x}$, $y = x^2$
1. A,B,C,D 2. A,C,B,D
3. D,B,C,A 4. D,C,B,A

KEY

1. 4 2. 1 3. 2

- Assertion(A): If $e = 2.72$, $e^2 = 7.39$,
 $e^3 = 20.09$, $e^4 = 54.6$ then $\int_0^4 e^x dx$ by
Simpson's rule is 53.873
Reason(R): Simpson's rule is $\int_a^b y dx = \frac{h}{2}$
 $[(y_0 + y_n) + 2(y_1 + y_2 + \dots + y_{n-1})]$.
1. Both A and R are true and R is the correct explanation of A.
2. Both A and R are true but R is not the correct explanation of A.
3. A is true but R is false.
4. A is false but R is true..

- Assertion(A): The area bounded by $y^2 = 4x$ and $x^2 = 4y$ is $\frac{16}{3}$ sq. units.

Reason(R): The area bounded by $y^2 = 4ax$ and

$x^2 = 4ay$ is $\frac{16ab}{3}$ sq. units

- Both A and R are true and R is the correct explanation of A.
 - Both A and R are true but R is not the correct explanation of A.
 - A is true but R is false.
 - A is false but R is true.
- Assertion(A): The area bounded by $y^2 = 4x$ and $y = x$ is $\frac{8}{3}$ sq. units.
Reason(R): The area bounded by $y^2 = 4ax$ and $y = mx$ is $\frac{8a^2}{3m^3}$ sq. units.
1. Both A and R are true and R is the correct explanation of A.
2. Both A and R are true but R is not the correct explanation of A.
3. A is true but R is false.
4. A is false but R is true.

KEY

1. 3 2. 1 3. 1

LEVEL -V

- The area enclosed between the two curves $y = f_1(x)$ and $y = f_2(x)$ and ordinates $x = a$, $x = b$ ($b > a$) is denoted by R. Then the area of the region. R = Area of the region covered by $f_1(x)$ - Area of the region covered by $f_2(x)$
- The area of the region bounded by the curve $y = x^2 + 1$ and $y = 2x - 2$ between $x = -1$ and $x = 2$
1. 9 Sq. Units 2. 12 Sq. Units
3. 15 Sq. Units 4. 14 Sq. Units
- The area bounded by the curve $y^2 = x$ and the line $x = 4$ is
1. $\frac{32}{3}$ Sq. Units 2. $\frac{16}{3}$ Sq. Units

$$\frac{8}{3} \text{ Sq. Units} \quad 4. \frac{4}{3} \text{ Sq. Units}$$

- II. Let $y = f(x)$ be given function and for equally spaced $y = f(x)$ arguments $x = a, a+h, a+2h \dots a+nh = b$ and

$$y_0 = f(x_0), y_1 = f(x_1), y_2 = f(x_2) \dots$$

$$y_n = f(x_n) \text{ in } [a, b]. \text{ Then}$$

$$\int_a^b y dx = \frac{h}{2} [(y_0 + y_n) + 2(y_1 + y_2 + \dots + y_{n-1})].$$

- The value of $\int_1^4 3x^2 dx$ taking 3 intervals is
1. 24.5 2. 34.5 3. 64.5 4. 74.5
- The value of $\int_1^5 (2x+1) dx$ taking 4 equal intervals.
1. 5 2. 8 3. 28 4. 28.2

KEY

- I 1) 2 2) 1 II 1) 3 2) 3

PREVIOUS EAMCET QUESTIONS

- The area in square units bounded by the curves $y^2 = 4x$ and $x^2 = 4y$ in the plane is (EAMCET 2005)
1. $\frac{8}{3}$ 2. $\frac{16}{3}$ 3. $\frac{32}{3}$ 4. $\frac{4}{3}$
- The area bounded by $y = x^2 + 2$, X-axis, $x=1$ and $x=2$ is (EAMCET 2004)
1. $\frac{16}{3}$ 2. $\frac{17}{3}$ 3. $\frac{13}{3}$ 4. $\frac{20}{3}$
- If $[2,6]$ is divided into 4 intervals of equal length then approximate value of $\int_2^6 \frac{1}{x^2 - x} dx$ using Simpson's rule (EAMCET 2003)
1. 0.3222 2. 0.2333
3. 0.5222 4. 0.2555
- The approximate value of $\int_1^9 x^2 dx$ by using Trapezoidal rule with 4 equal intervals is (EAMCET 2002)

- 248 2. 242.5 3. 242.8 4. 243
- The area of the region bounded by $x^2 = 8y$, $x = 4$ and the x-axis is (EAMCET 2001)
1. $\frac{2}{3}$ 2. $\frac{4}{3}$ 3. $\frac{8}{3}$ 4. $\frac{10}{3}$
- x: 1 2 3 4
y: 0.7111 0.7222 0.7333 0.7444
Using above table and Trapezoidal rule, the approximate value of $\int_1^4 y dx$ is (EAMCET 2001)
1. 0.1833 2. 1.1833
3. 2.1883 4. 3.183
- The area in square units of the region bounded by the curve $x^2 = 4y$, the line $x=2$ and the X-axis is (EAMCET 2000)
1. 1 2. $\frac{2}{3}$ 3. $\frac{4}{3}$ 4. $\frac{8}{3}$
- The area in square units bounded by the curves $y = x^3$, $y = x^2$ and the ordinates $x=1$, $x=2$ is (EAMCET 2000)
1. $\frac{17}{12}$ 2. $\frac{12}{13}$ 3. $\frac{2}{7}$ 4. $\frac{7}{2}$
- The area bounded by the parabola $x = 4 - y^2$ and the Y-axis, in square units is (EAMCET 1999)
1. $\frac{3}{32}$ 2. $\frac{32}{3}$ 3. $\frac{33}{2}$ 4. $\frac{16}{4}$
- The approximate value of $\int_{-3}^3 x^2 dx$, using Trapezoidal rule and taking 6 equal intervals is (EAMCET 1999)
1. 11.5 2. 19 3. 115 4. 120
- The area bounded by $y = 3x$ and $y = x^2$ is (in square units) (EAMCET 1998)
1. 10 2. 5 3. 4.5 4. 9
- The area (in square units) bounded by the x-axis, part of the curve $y = 1 + \frac{8}{x^2}$ and the lines $x=2$ and $x=4$ is (EAMCET 1997)
1. 2 2. 3 3. 4 4. 5
- AOB is the positive quadrant of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ where $OA=a$, $OB=b$. Then area between the arc AB and chord AB of the ellipse is (EAMCET Re-exam 1996)

1. πab 2. $(\pi - 2)ab$

3. $\frac{ab(\pi + 2)}{2}$ 4. $\frac{ab(\pi - 2)}{4}$

14. Area of the segment cut off from the parabola $x^2 = 8y$ by the line $x - 2y + 8 = 0$ is

(EAMCET Re-exam 1996)

1. 12 2. 24 3. 48 4. 36

15. Area bounded by the curves $y = x$, $y = x^3$ is (EAMCET Re-exam 1996)

1. $\frac{1}{4}$ 2. $\frac{1}{6}$ 3. $\frac{1}{12}$ 4. $\frac{1}{2}$

16. The area in square units bounded by the X-axis, part of $y = 1 + \frac{8}{x^2}$ and the ordinates $x=2$ and $x=4$ is

(EAMCET Re-exam 1996)

1. 2 2. 3 3. 4 4. 5

17. The area bounded by the X-axis and the curve $y = 4x - x^2 - 3$ is (EAMCET - 1996)

1. $\frac{2}{3}$ 2. $\frac{8}{3}$ 3. $\frac{4}{3}$ 4. $\frac{1}{3}$

18. The area, in square units of the region bounded by the parabolas $y^2 = 4x$ and $x^2 = 4y$ is

(EAMCET - 1996)

1. $\frac{16}{3}$ 2. $\frac{32}{3}$ 3. $\frac{8}{3}$ 4. $\frac{4}{3}$

19. $f(x) = \frac{1}{1+x}$ for $0 \leq x \leq 1$ and the interval $[0,1]$ is divided into 2 equal subintervals. Us-

ing Trapezoidal rule, $\int_0^1 \frac{1}{1+x} dx =$

(EAMCET - 1996)

1. $\frac{17}{24}$ 2. $\frac{17}{14}$ 3. $\frac{17}{48}$ 4. $\frac{17}{12}$

20. Given $e=2.72$, $e^2 = 7.39$, $e^3 = 20.09$,

$e^4 = 54.60$, the approximate value of $\int_0^4 e^x dx$ using Simpson's rule and taking $h=1$ is

(EAMCET - 1995)

1. 57.325 2. 53.873

3. 58.873 4. 57.325

21. Area of the region enclosed by $y^2 = 8x$ and $y=2x$ is

(EAMCET - 1995)

1. $\frac{4}{3}$ 2. $\frac{3}{4}$ 3. $\frac{1}{4}$ 4. $\frac{1}{2}$

Eamcet-2007

22. The area (in square units) of the region enclosed by the curves $y = x^2$ and $y = x^3$ is **E-2007**

1) $\frac{1}{12}$ 2) $\frac{1}{6}$ 3) $\frac{1}{3}$ 4) 1

KEY

1-10 2 3 3 1 3

3 2 1 2 2

11-20 3 4 4 2 4

3 1 1 1 2

21-30 1 1

PREVIOUS AIEEE QUESTIONS

1. The area of the region bounded by $y = |x - 2|$, $x = 1$, $x = 3$ and x-axis is

1. 4 2. 2 3. 3 4. 1

2. The area of the region bounded by $y = |x - 1|$ and $y = 3 - |x|$ is

1. 6 2. 2 3. 3 4. 4

3. The area of the region bounded by $y = 2x - x^2$ and $y = -x$ is

1. $\frac{9}{2}$ 2. $\frac{43}{6}$ 3. $\frac{35}{6}$ 4. $\frac{10}{3}$

KEY

1. 4 2. 4 3. 1