

# MATHEMATICS

Class - 5



2019-20

---

State Council of Educational Research & Training Chhattisgarh, Raipur

---

For Free Distribution

**© S.C.E.R.T. C. G., Raipur**

**Publication Year - 2019**

**Guidance**

Rohit Dhankar (Digantar, Jaipur)

Hridaykant Dewan (Vidya Bhawan, Udaipur)

**Cordinator**

Dr. Sudhir Shrivastava

**Writing**

Dr. Sudhir Shrivastava, Nilesh Verma, R.K. Sengar,  
Hemant Panigrahi, Sachihidanand Patnaik, Chhaliya Vaishnav, Shankar Singh Rathor,  
Prem Prakash Shukla, Sanjay Dewangan, Harishanker Patel, Pramod Patel,  
Ashok Mahana, Madhugupta, Rajni Dwivedi, Inder Singh, Gajendra Raut

**Translator**

Vidya Bhawan Society, Udiapur

**Illustration**

Mohan Goswamy, Prashant Soni, Rekhraj Chouragadey

**Cover page and Layout Designing**

Rekhraj Chouragadey

**Published by**

**Chhattisgarh Text Book Corporation Raipur (C.G.)**

**Printed by**

## PREFACE

After the creation of Chhattisgarh state, the responsibility of creating new text books for children of the state has been assigned to State Council of Educational Research and Training. The books have been created by keeping in view the social, cultural and geographical background of the state.

It has also been kept in mind that the new vision which is being made in the context of the children at the national level can also benefit the children of the state.

These books were tested for two years in various areas of the state. As per the feedback of teachers, parents, children and academicians some changes were made.

At the time of creation of this mathematics text book the main thing that was put forward was that learning mathematics can be joy for children if they can relate our environment to it. Mathematics should not be confined to the text books. The knowledge of process of addition, subtraction, multiplication and division is not enough. The learner should also be able to apply these processes appropriately in real life situations. Pictorial representations have been used in the text book so that the learners easily relate mathematical concepts and process to their surroundings.

This book addresses children with easy language. It has been kept in mind while making the entire book that all the symbols and words are familiar to children. Wherever it is very necessary to use mathematical words, they are used with examples. To keep the learning process from being burdensome and boring several interesting activities have been given. By doing these activities individually or in groups, the learners will learn easily.

It has been kept in mind that the activities, examples and figures given in book are related to children's experience and interest.

According to the National Curriculum Framework-2005 the purpose of mathematics is not merely following the algorithm and getting the result. Hence in this text book, we have put emphasis on understanding, discussion and interaction of children. There are several such lessons in the book in which children have been asked to discuss many issues with their friends and teachers. We also recognize that if children use their own language to create logical framework their concepts will be strong and clear. Here the teachers are expected to create a rapport and let them speak openly about those issues. Teachers need to listen to them and if the children are having trouble to reach the conclusion then help them. Hope this text book will be helpful in keeping the environment of the school entertaining and exciting.

In preparing these books the council has got continuous cooperation from teachers, academicians and linguist of governmental and nongovernmental sector. The council is grateful to all of them.

It is our responsibility to make our future generation beautiful. We hope that we will all be able to do something good.

**Director**

State Council of Educational Research and  
Training Chhattisgarh, Raipur



## SUGGESTIONS FOR TEACHERS AND PARENTS

There have been continuous efforts to make teaching-learning processes interesting and effective. There have been efforts to understand the objects of having different disciplines in the school syllabus and to understand and explain nature of each subject. Yet in teachers and children a reflection on clarity and good understanding does seem to be evident. This is particularly true about mathematics.

If you were to pose the question, “What is mathematics?”, the answers would range from counting objects, displaying numbers, doing number operations, lines, making shapes and so on. A few answers might differ from the ones cited above, but these would be largely the things mentioned.

Before we go ahead, let us try and understand what all happens when we are attempting to solve a problem in mathematics. For example, “A bus travels a distance of 35 kilometers in 1 hour. How far will it travel in 6 hours?”

Here, time is an abstract concept. We have defined an interval as the unit of this abstract concept and expressed large time intervals in terms of these units. Similarly, for distance, we have defined a unit, which then helps us quantify it.

In the next step we explore the relationship between these two units of time and distance. We have stated, “The bus travels a distance of 35 kilometres in 1 hour”. This defines a relationship, which we translate in term of an operation-for instance, either addition or multiplication.

Let us consider another example. A kilogram of rice costs Rs. 16. How much will 54 kilograms of rice cost?

In this example, we have again defined a unit for quantity of rice, and expressed the total quantity in terms of the unit. The same can be observed while solving problems related to area, etc. It is clear from these examples that mathematics is not just limited to counting or operations on numbers. In the same way, mathematics of shapes and lines is about exploring and establishing the relationships between them. Further, while we include the concept of measurement for use, the sorting, classification searching for and establishing their properties, constitute important facets of mathematics.



When a child begins learning mathematics, in order to express abstract ideas understand operations as well as simple problems faced in daily life, it becomes necessary to use concrete (real physical) objects. However, this dependence on real objects progressively decreases as mathematical skills develop.

Children then begin to build arguments. Their ability to deal with abstractions increases. They begin to abstract arguments from their daily life, and translate abstractions into reality. They also begin to seek solutions to problems of their own accord using various methods. This whole process helps children understand how and where available information can be used to solve problems.

Therefore, it is imperative that in the teaching of mathematics children be allowed to have maximum opportunity to think and work independently. This will only happen if children are not provided with ready-made solutions, and are instead encouraged to think on their own, with guidance towards the right direction. This might seem strange in the beginning, but it is difficult to teach mathematics without developing the ability to think independently and take decisions on the basis of this thought. The development of this ability will make the children self-confident and reduce the fear of mathematics that is widely prevalent.

The class 1 textbook has been developed keeping in mind that it could be used by teachers as a guide and for self-learning by children. We have also tried to provide many opportunities for students following this textbook to think and act independently.

Beginning mathematics using concrete objects and games generates interest amongst the children. Therefore, we have also begun the book with games. The first section develops the ability to focus and concentrate, develop, eye-hand coordination, learn to sort and classify objects, and make pairs. These are through games and would help develop the abilities for sorting, classification, understanding one to one correspondence and comparing quantities.

It is expected that children will be given sufficient time to use as concrete objects while working on the materials given in the book. We have given some examples of the concrete objects that can be used for this purpose but you have to think of some more. Some suggestions can also be seen from the teachers' guide which is being published separately. The purpose of having children engaged with activities

with concrete objects and for creation of supplementary materials for games is to ensure that they work with concrete objects while learning new concepts. They should work on their own, understand operations and slowly move towards greater abstractions. In this period they should be given opportunities to use language in the context of these concepts and operations. These occasions should be both in small groups and in common situations along with teachers so that they can build their self confidence. If there is an opportunity in each chapter to do this then many difficulties that arise in learning Mathematics would be destroyed from the root. Children would develop different attitudes towards mathematics there is a need to pose for a while and think about this point.

Children love stories. One sees children completely engrossed in a story being told to them, especially, if it being related well. In order to understand mathematics because of its abstraction it is useful to have it embedded in stories or contexts, understanding and enjoying stories is a prerequisite. Keeping this in mind, some characters have been created in the textbook. Children can be encouraged to name these characters imaginatively and a short story could be woven around them at the beginning of the lesson. Problems can be posed through play, activities with concrete objects and stories, which would help children form their own base for understanding mathematics better.

No lesson or activity is complete in itself. The materials in the text are just indicative. According to the needs of your classroom and the interest of the children, develop and use new materials, new interesting activities and new games. We have given some suggestions for this purpose. Wherever extra things can be thought of symbols at the bottom of the page show what is possible according to use. The key to the symbols is given at the beginning of the book. Children could be encouraged to interpret the symbols and complete the activities on their own.

**To summarise:-**

- ☐ Children must be given the opportunity to flip through their books, look at the pictures given and attempt to read in an independent manner
- ☐ Every page of the textbook contains interesting activities and practice exercises. Make more such tasks, ask children to develop them and also to solve them.



- ❑ Children must be given sufficient time to understand and learn a new concept. Children develop new techniques to understand concepts, and must be encouraged in these endeavors.
- ❑ The objective of solving problems is to understand the underlying mathematical concept. Solving a select set of questions or rote learning of select solutions is not the correct way to teach mathematics. Children must, therefore, be encouraged to solve problems as well as develop new problems.
- ❑ Mistakes are a natural process of learning while learning a concept or in solving problems. Children must not be discouraged on mistakes. Instead, they should be encouraged to develop new methods and ways to solve problems.
- ❑ Children learn from their peers, and therefore, must be encouraged to indulge in conversations and group work, and then to present the work that was done in the group.
- ❑ If children have difficulty in solving a problem guidance can be provided in the form of pointed questions that help students think along a certain direction.
- ❑ The materials mentioned in the book are indicative. Please develop and use new materials, innovative games, exercises, and activities depending on the needs, interest and background of the children. The use of symbols in the book indicates the areas where this is possible. Children should be encouraged to understand the symbols independently and work according to the instructions given.

This book is an attempt to dialogue with the teachers/parents and children. All suggestions to improve the book are invaluable and you must please send these to the SCERT.

**Director**

State Council of Educational Research and Training  
Raipur (Chattisgarh)



## Contents

Names of Lessons	Page No.
1. Numbers	1-15
2. Operations	16-29
3. Profit and Loss	30-35
4. Unitary Method	36-39
5. Average	40-43
6. Multiples and Factors	44-53
7. Fractions	54-78
8. Decimals	79-98
9. Symmetry	99-105
10. Angles	106-117
11. Geometrical Figures	118-126
12. Length	127-130
13. Weight	131-134
14. Capacity	135-139
15. Money	140-145
16. Time	146-153
17. Billing	154-156
18. Perimeter	157-162
19. Area	163-170
20. Data Handling	171-177
21. Pattern and Riddles	178-182
22. Devanagari Numerals	183-198
23. Vedic Maths	199-205

# CHAPTER-1

## Numbers

### You know that-

In the abacus, when the ones position reaches the tenth bead, we put one bead in the tens position instead.

Each bead in the tens position indicates 10 ones. Similarly when the tens position reaches the tenth bead, we add one bead in the hundred position instead.

That is  $10 \text{ tens} = 1 \text{ hundred}$

We similarly put one bead in a new place when the tenth bead gets added to the hundreds position.

This new place is the thousands position

$10 \text{ ones} = 1 \text{ ten}$

$10 \text{ tens} = 1 \text{ hundred}$

$10 \text{ hundreds} = 1 \text{ thousand}$

Now look at the given picture

What number is indicated by the beads in the abacus?

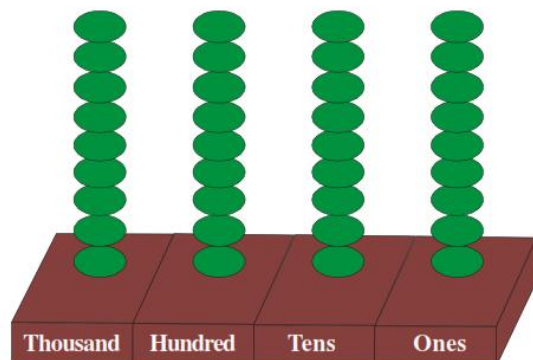
.....

Now if we were to add one more bead in the ones position what will you do?

Discuss it with your friends and teacher.

If you need an abacus take it and do it yourself.

You must remember that like before on reaching the 10 beads in any position you will create a new place. You are absolutely right!



## Maths - 5

The new position is known as the ten thousands position.

$$9999 + 1 = 10,000$$

**You are given some numerals in figures and words. Look at them and read the names.**

12,500	Twelve thousand five hundred
52,457	Fifty two thousand four hundred fifty seven
93,509	Ninety three thousand five hundred nine
94,060	Ninety four thousand sixty
10,325	Ten thousand three hundred twenty five
27,627	Twenty seven thousand six hundred twenty seven
20,005	Twenty thousand five
30,360	Thirty thousand three hundred sixty
04,252	Four thousand two hundred fifty two



**Write the given numerals in words:**

90,932	_____
76,180	_____
58,151	_____
65,839	_____
09,424	_____
18,381	_____
77,124	_____
45,864	_____
89,691	_____





## Numbers

Now try making some five digit numerals on your own. Write the numbers in words and show it to your friends and teacher.



Write the following numerals in figures:

Twenty five thousand three hundred and ninety \_\_\_\_\_

Ninety one thousand two hundred and fifty five \_\_\_\_\_

Forty thousand and seventy nine \_\_\_\_\_

Eighty nine thousand \_\_\_\_\_

Seventy two thousand and nine \_\_\_\_\_

## Place value

**Example 1 :** Write the place value of each digit of 48,567 and write it in the expanded form.

**Solution :**

Digit	position	place value
7	Ones	$7 \times 1 = 7$
6	Tens	$6 \times 10 = 60$
5	Hundreds	$5 \times 100 = 500$
8	Thousands	$8 \times 1000 = 8000$
4	Ten thousands	$4 \times 10,000 = 40,000$

The expanded form of 48,567 =  $40000 + 8000 + 500 + 60 + 7$

Write the place value of each digit of the given numerals and write the expanded form too :

(1) 25,462                      (2) 82,574                      (3) 34,016

(4) 40,710                      (5) 50,078                      (6) 93,509

Make some numerals of 5 digits and write the place value of the digits and write the expanded form of each.

## Maths - 5

**Write the numerals which come just before and just after:**

_____	98,297	_____
_____	50,932	_____
_____	49,291	_____
_____	15,817	_____
_____	14,509	_____



The numeral which comes just before is called the predecessor of the given numeral.  
The numeral which comes just after is called the successor of the given numeral.

**Now answer these:**



- (1) Successor of 99 is \_\_\_\_\_ (2) Predecessor of 100 is \_\_\_\_\_  
(3) Successor of 999 is \_\_\_\_\_ (4) Predecessor of 1000 is \_\_\_\_\_

The smallest 3 digit number comes just after the largest 2 digit number.  
The largest 2 digit number comes just before the smallest 3 digit number.

So can we say that the smallest 6-digit number comes just after the largest five-digit number? Find out.

**Write the following numerals in an increasing order:**

- |    |       |       |       |       |
|----|-------|-------|-------|-------|
| 1. | 15775 | 25525 | 20950 | 15975 |
| 2. | 77777 | 70777 | 77077 | 77707 |
| 3. | 45554 | 45545 | 45455 | 44555 |
| 4. | 90979 | 89979 | 79989 | 87979 |



**Write the following numerals in a decreasing order:**

- |    |       |       |       |       |
|----|-------|-------|-------|-------|
| 1. | 17426 | 27246 | 37642 | 47548 |
| 2. | 30636 | 35045 | 04545 | 40538 |
| 3. | 6978  | 786   | 81316 | 52374 |
| 4. | 33225 | 52233 | 11111 | 12345 |

## Lakh, Ten lakhs, Crore

Now you know how numbers increase. Whenever we reach the 10th beads in any position, we add one bead in the next position instead of 10 beads in that position. Each new position has a new name.

**We know that:**

$$\begin{array}{llll} 10 \text{ ones} & = & 1 \text{ ten} & 10 \text{ tens} & = & 1 \text{ hundred} \\ 10 \text{ hundreds} & = & 1 \text{ thousand} & 10 \text{ thousands} & = & 1 \text{ ten thousand} \end{array}$$

This continues even after the ten thousands, also. Let us know the number which come after ten thousand.

$$\begin{array}{llll} 10 \text{ ten thousand} & = & 1 \text{ lakh} & 10 \text{ lakhs} & = & 1 \text{ ten lakh} \\ 10 \text{ ten lakhs} & = & 1 \text{ crore} & 10 \text{ crores} & = & 1 \text{ ten crore} \end{array}$$

The numerals given in the table below are written in figures and words. Understand them properly and take the help of your teacher if required.

	Crores		Lakhs		Thousand		Hundred	Tens	Ones
	Ten crore	Crore	Ten lakh	Lakh	Ten thousand	Thousand			
7,25,420 Seven lakh twenty five thousand four hundred twenty				7,00 000	20 000	5000	400	20	0
25,04,562 Twenty five lakh four thousand five hundred sixty two			20 00 000	5 00 000	0	4000	500	60	2
10,27,985 Ten lakh Twenty seven thousand nine hundred eighty five			10 00 000	0	20 000	7000	900	80	5
3,15,34,859 Three crores fifteen lakh thirty four thousand eight hundred fifty nine		300 00 000	10 00 000	5 00 000	30 000	4000	800	50	9
94,24,15,378 Ninety four crores twenty four lakh fifteen thousand three hundred seventy eight	90 00 00 000	4 00 00 000	20 00 000	4 00 000	10 000	5000	300	70	8



Write the given numeral in figures or words as required

7,24,520 \_\_\_\_\_

\_\_\_\_\_ Five lakh twenty three thousand seven hundred twelve

25,54,399 \_\_\_\_\_

\_\_\_\_\_ Seventy two lakh six thousand three hundred ten

1,93,25,465 \_\_\_\_\_

\_\_\_\_\_ Three crores twenty two lakhs fourty six thousand

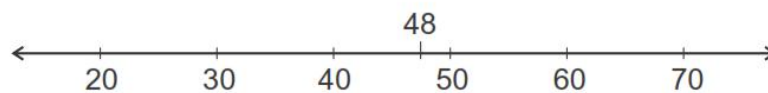
\_\_\_\_\_ Seven crores

90,00,00,000 \_\_\_\_\_

Which number is nearest -

48 is the number between 40 and 50.

48 is nearest to which number, 40 or 50 ?

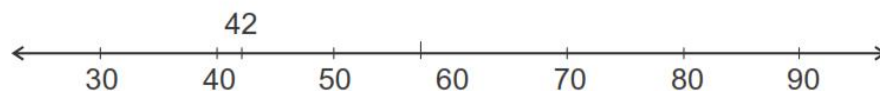


The number representation on number line we find that 48 is nearest to 50.

Which is nearest ten.

42 is the number between 40 and 50

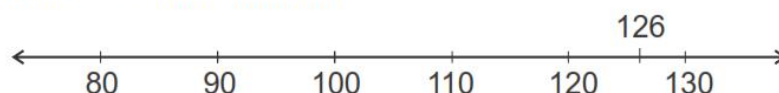
42 is nearest to which number?



The number representation on number line we find that 42 is nearest to 40.

Which is nearest ten.

126 is nearest to which number?

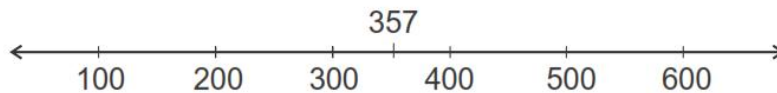


The number representation on number line we find that 126 is nearest to 130.

Which is nearest ten.

357 is between 300 and 400

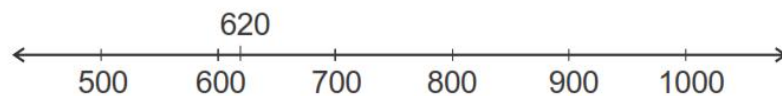
357 is nearest to which number?



The number representation on number line we find that 357 is nearest to 300.

Which is nearest hundred.

620 is nearest to which number?

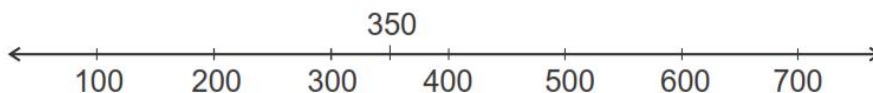


The number representation on number line we find that 620 is nearest to 600.

Which is nearest hundred.

**Special case :-** If a number is exactly between any two number, then how can we find its nearest number?

350 is nearest to which number?



350 is exactly between 300 and 400. In this condition we will take 400 as its nearest number. So 350 is nearest to 400

1. Find out the nearest tens of given numbers.

62, 95, 93, 459

2. Find out the nearest hundred of the given numbers.

249, 709, 698, 650

3. Find out the nearest ten and hundred of the given numbers.

245, 808, 976, 138

### Estimation of Addition –

**Example –** There are 63 coins in one bag and 39 coins in another bag. If we merge coins of both bags, then do the assessment of total coins.

Before assessment of  $(63 + 39)$  we have to find nearest ten of 63 and 39 and add them.

## Maths - 5

Number	Nearest ten
63	60
39	40

Estimated total

$$\begin{array}{r} 60 \\ + 40 \\ \hline 100 \end{array}$$

Actual total

$$\begin{array}{r} 63 \\ + 39 \\ \hline 102 \end{array}$$

By merging coins of both bags, we have to get 100 coins approximately. Like this, the difference between estimate total (100) and actual total (102) is 2 only.

Example – There are 375 mangoes in one box and 216 mangoes in another box. Do the estimation of total number of mangoes.

Before estimation of  $(375 + 216)$  we have to find nearest hundred of 375 and 216 and add them.

Number	Nearest hundred
378	400
216	200

Estimated Sum

$$\begin{array}{r} 400 \\ + 200 \\ \hline 600 \end{array}$$



$$\begin{array}{r} \text{Actual Sum (1)} \quad \quad \quad \begin{array}{r} 1 \\ 378 \\ + 216 \\ \hline 594 \end{array} \end{array}$$

The estimated number of total mangoes are 600, which is very nearer to actual number 594 of total mangoes.

Example – In a factory, 1789 female and 1436 male workers are working. Do the estimation of total number of workers.

Before estimation of (1789 + 1436) we have to find nearest thousand of 1789 and 1436 and add them-

Number	Nearest Thousand
1789	2000
1436	1000

$$\begin{array}{r} \text{Estimated Sum} \quad \quad \quad \begin{array}{r} 2000 \\ + 1000 \\ \hline 3000 \end{array} \end{array}$$

$$\begin{array}{r} \text{Actual Sum} \quad \quad \quad \begin{array}{r} 111 \\ 1789 \\ + 1436 \\ \hline 3225 \end{array} \end{array}$$

Find out the estimated sum by rounding off to nearest ten and also find actual sum.

- (1) 46, 81                      (2) 96, 15                      (3) 72, 88                      (4) 34, 65

Find out the estimated sum by rounding off to nearest hundred and also find actual sum.

- (1) 436, 356                      (2) 164, 719                      (3) 506, 271                      (4) 632, 225

Find out the estimated sum by rounding off to nearest thousand and also find actual sum.

- (1) 4360, 5812      (2) 3756, 140      (3) 7015, 2512      (4) 3160, 6420

**Estimation of difference :-**

**Example** – The number of boys and girls in class 5<sup>th</sup> are 28 and 36 respectively. Do the estimation of difference of their numbers.

Before estimation of (36-28) we have to find nearest ten of 36 and 28 and subtract them -

Number	Nearest Ten
36	40
28	30

$$\begin{array}{r}
 \text{Estimated difference} \quad 4-0 \\
 - \quad 3-0 \\
 \hline
 1-0
 \end{array}$$

$$\begin{array}{r}
 \text{Actual difference} \quad 3-6 \\
 - \quad 2-8 \\
 \hline
 8
 \end{array}$$

The difference between estimated number of girls and boys is 10, which is very nearer to actual difference 8.

**Example** - Mangoes collected from two gardens are 356 and 125 respectively. Do the estimation of their difference.

We are rounding off 356 and 125 to their nearest hundred and subtract them-

Number	Nearest hundred
356	400
125	100

$$\begin{array}{r} \text{Estimated difference} \quad 400 \\ - 100 \\ \hline 300 \end{array}$$

$$\begin{array}{r} \text{Actual difference} \quad 356 \\ - 125 \\ \hline 231 \end{array}$$

Example – The cost of a TV and a bicycle is 5680 and 3140 respectively. Do the estimation of their price difference.

Number	Nearest Thousand
5680	6000
3140	3000

$$\begin{array}{r} \text{Estimated difference} \quad 6000 \\ - 3000 \\ \hline 3000 \end{array}$$

$$\begin{array}{r} \text{Actual difference} \quad \text{—5—6—8—0} \\ - 3\text{—}1\text{—}4\text{—}0 \\ \hline 2\text{—}5\text{—}4\text{—}0 \end{array}$$

Find out the actual difference and estimated difference by rounding off to their nearest ten.

$$\begin{array}{r} 5-8 \\ - 4-3 \\ \hline \\ \hline \end{array}$$

$$\begin{array}{r} 9-2 \\ - 5-7 \\ \hline \\ \hline \end{array}$$

$$\begin{array}{r} 4-7-6 \\ - 1-5-1 \\ \hline \\ \hline \end{array}$$

$$\begin{array}{r} 5-7-6 \\ - 2-3-7 \\ \hline \\ \hline \end{array}$$



## Maths - 5

Find out the actual difference and estimated difference by rounding off to their nearest hundred.

$$\begin{array}{r} 6-3-7 \\ - 3-5-8 \\ \hline \end{array}$$

$$\begin{array}{r} 3-6-5 \\ - 1-5-1 \\ \hline \end{array}$$

$$\begin{array}{r} 9-2-6 \\ - 5-7-6 \\ \hline \end{array}$$

$$\begin{array}{r} 4-8-1-6 \\ - 1-3-8-1 \\ \hline \end{array}$$

Find out the actual difference and estimated difference by rounding off to their nearest thousand.

$$\begin{array}{r} 5-1-6-8 \\ - 2-7-1-3 \\ \hline \end{array}$$

$$\begin{array}{r} 8-6-5-3 \\ - 1-4-4-9 \\ \hline \end{array}$$

$$\begin{array}{r} 8-2-7-0 \\ - 4-1-5-9 \\ \hline \end{array}$$

### Estimation of multiplication –

#### Example –

Do the estimation of multiplication of 51 and 36

Number	Nearest Ten
51	50
36	40

Estimated multiplication

$$\begin{array}{r} 5-0 \\ \times 4-0 \\ \hline 0-0 \\ -2-0-0-0 \\ \hline \end{array}$$

Actual multiplication

$$\begin{array}{r} 5-1 \\ \times 3-6 \\ \hline -3-0-6 \\ -1-5-3-0 \\ \hline -1-8-3-6 \end{array}$$

**Example –**

Do the estimation of multiplication of 432 and 261

Number	Nearest hundred
432	400
261	300

Estimated multiplication

$$\begin{array}{r}
 4-0-0 \\
 \times 3-0-0 \\
 \hline
 0-0-0 \\
 \text{---}0-0-0-0 \\
 1-2-0-0-0-0 \\
 \hline
 1-2-0-0-0-0
 \end{array}$$

Actual multiplication

$$\begin{array}{r}
 4-3-2 \\
 \times 2-6-1 \\
 \hline
 4-3-2 \\
 \text{---}2-5-9-2-0 \\
 \text{---}8-6-4-0-0 \\
 \hline
 1-1-2-7-5-2
 \end{array}$$

Find out the estimated product and actual product by rounding off to their nearest ten.

$23 \times 58$

$46 \times 91$

$55 \times 21$

Find out the estimated product and actual product by rounding off to their nearest hundred.

$513 \times 156$

$263 \times 449$

**Estimation of division –**

**Example –**  $62 \div 26$

Number	Nearest Ten
62	60
26	30

Estimated division

$$\begin{array}{r} 2 \\ 30 \overline{)60} \\ \underline{60} \\ 00 \end{array}$$

Actual division

$$\begin{array}{r} 2 \\ 26 \overline{)62} \\ \underline{52} \\ 10 \end{array}$$

**Example –**

$$256 \div 26$$

256 is nearest to 300

26 is nearest to 30

So, divide 300 by 30

Estimated division

$$300 \div 30$$

$$\begin{array}{r} 10 \\ 30 \overline{)300} \\ \underline{300} \\ 000 \end{array}$$



Actual division -

$$\begin{array}{r} 13 \\ 26 \overline{) 356} \\ \underline{26} \phantom{6} \\ 96 \\ \underline{78} \\ 18 \end{array}$$

Estimated division result (10) is very nearest to actual division result (13)

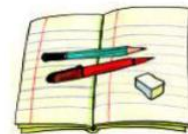
Do the estimation of Division

1.  $87 \div 28$

2.  $75 \div 21$

3.  $296 \div 31$

4.  $628 \div 24$



### Exercise

1. Make numbers of more than five digits. Then write all the numbers in words. Show them to your friends. Who made the maximum numbers ?
2. Make group of three digit numbers you have made. Now arrange them in ascending and descending order and show it to your teacher.
3. Write place value of the each digits of the numbers you have made and also write their expanded form.

## CHAPTER-2

### Operations

#### Addition & Subtraction

We have done addition and subtraction of numerals in 4 digits in the previous class. Let us revise :

A. Solve

$$\begin{array}{r} (1) \quad 3 \ 7 \ 2 \ 1 \\ + 2 \ 5 \ 1 \ 0 \\ \hline \\ \hline \end{array}$$

$$\begin{array}{r} (2) \quad 1 \ 5 \ 7 \\ 6 \ 8 \ 3 \ 2 \\ + 5 \ 3 \ 1 \ 8 \\ \hline \\ \hline \end{array}$$

$$\begin{array}{r} (3) \quad 9 \ 5 \\ 7 \ 2 \ 1 \\ 5 \ 3 \ 2 \ 8 \\ + \quad 3 \ 7 \\ \hline \\ \hline \end{array}$$

$$\begin{array}{r} (4) \quad 2 \ 7 \ 3 \ 1 \\ - 1 \ 5 \ 4 \ 2 \\ \hline \\ \hline \end{array}$$

$$\begin{array}{r} (5) \quad 6 \ 7 \ 1 \ 0 \\ - 5 \ 2 \ 8 \\ \hline \\ \hline \end{array}$$

$$\begin{array}{r} (6) \quad 5 \ 6 \ 3 \ 2 \\ - 3 \ 3 \ 0 \ 7 \\ \hline \\ \hline \end{array}$$

B. Fill in the boxes with the correct number:

$$\begin{array}{r} (1) \quad 6 \ 8 \ 8 \ 2 \\ + 2 \ \square \ 3 \ 8 \\ \hline \square \ 3 \ \square \ 0 \\ \hline \end{array}$$

$$\begin{array}{r} (2) \quad 4 \ 2 \ 4 \ 5 \\ + 3 \ 1 \ \square \ 8 \\ \hline 7 \ \square \ 3 \ \square \\ \hline \end{array}$$

$$\begin{array}{r} (3) \quad 5 \ 3 \ 0 \ \square \\ + \square \ 8 \ \square \ 8 \\ \hline 9 \ \square \ 0 \ 7 \\ \hline \end{array}$$

$$\begin{array}{r} (4) \quad 5 \ 8 \ 2 \ 0 \\ + 3 \ \square \ 3 \ 7 \\ \hline \square \ 0 \ 8 \ \square \\ \hline \end{array}$$

$$\begin{array}{r} (5) \quad 8 \ 3 \ 3 \ 8 \\ + \square \ 6 \ 2 \ \square \\ \hline 9 \ \square \ \square \ 9 \\ \hline \end{array}$$

$$\begin{array}{r} (6) \quad \square \ 7 \ \square \ 6 \\ + 2 \ 6 \ 8 \ \square \\ \hline 7 \ \square \ 1 \ 7 \\ \hline \end{array}$$

### Addition of numerals with 5 digits

See and understand

Example 1:

Tth	Th	H	T	O
3	2	7	8	5
+	1	3	2	1
4	5	9	9	8

Example 2 :

Tth	Th	H	T	O
6	5	8	6	5
+	2	6	0	2
9	1	8	9	1

Add :-

- (1) 56,784 and 48,765
- (2) 27,835 and 308
- (3) 20,312 and 5040 and 809
- (4) 6221 and 563 and 51,738
- (5) 53,817 and 37,405



### Subtraction of numerals with 5 digits

See and understand

Example 1 :

Tth	Th	H	T	O
6	8	9	3	5
-	4	7	8	1
2	1	1	2	1

Example 2 :

Tth	Th	H	T	O
3	3	9	1	8
-	1	4	7	0
1	9	2	0	9

Subtract:-

- (1) 59,726 from 80,780
- (2) 68,349 from 73,405
- (3) 4236 from 47,895
- (4) 23,562 from 78,354
- (5) 31,405 from 53,817





## Maths - 5

After having solved the above questions you will have realised that the subtraction and addition of a 5 digit number is exactly the same as you would do with a 4 digit, 3 digit or 2 digit number. In fact, the addition and subtraction of numbers with more than five digits is also the same.

### See and understand :

Example 1 :

Lakh	Tth	Th	H	T	O
7	5	3	4	2	8
+ 1	4	8	5	6	3
9	0	1	9	9	1

Example 2 :

Ten lakh	Lakh	Tth	Th	H	T	O
7	6	3	5	4	8	7
+ 2	0	8	3	8	0	6
9	7	1	9	2	9	3



## Exercise

(1) 
$$\begin{array}{r} 263703 \\ + 78395 \\ \hline \end{array}$$

(2) 
$$\begin{array}{r} 55007 \\ + 173860 \\ \hline \end{array}$$

(3) 
$$\begin{array}{r} 3783546 \\ + 6235627 \\ \hline \end{array}$$

(4) 
$$\begin{array}{r} 994255 \\ + 593509 \\ \hline \end{array}$$

$$\begin{array}{r} (5) \quad 6027627 \\ + \quad 94000 \\ \hline \hline \end{array}$$

$$\begin{array}{r} (6) \quad 83812 \\ + \quad 9194141 \\ \hline \hline \end{array}$$

$$\begin{array}{r} (7) \quad 6273904 \\ + \quad 406 \\ \hline \hline \end{array}$$

$$\begin{array}{r} (8) \quad 389 \\ + \quad 892313 \\ \hline \hline \end{array}$$

### Subtraction of six digit or seven digit numerals

See and understand-

Example 1 :

$$\begin{array}{r} 786538 \\ - 238715 \\ \hline 547823 \end{array}$$

Example 2 :

$$\begin{array}{r} 2447823 \\ - 1638715 \\ \hline 0809108 \end{array}$$

### Exercise

$$\begin{array}{r} (1) \quad 7850252 \\ - 6241049 \\ \hline \hline \end{array}$$

$$\begin{array}{r} (2) \quad 5124286 \\ - 2526214 \\ \hline \hline \end{array}$$

$$\begin{array}{r} (3) \quad 992646 \\ - 696627 \\ \hline \hline \end{array}$$

$$\begin{array}{r} (4) \quad 868223 \\ - 223104 \\ \hline \hline \end{array}$$

$$\begin{array}{r} (5) \quad 5593475 \\ - 58752 \\ \hline \hline \end{array}$$

$$\begin{array}{r} (6) \quad 4467895 \\ - 593251 \\ \hline \hline \end{array}$$

## Maths - 5

$$\begin{array}{r} (7) \quad 674868 \\ - 26789 \\ \hline \hline \end{array}$$

$$\begin{array}{r} (8) \quad 252457 \\ - 9509 \\ \hline \hline \end{array}$$

Now make numerals with 5 digits. Take them in groups of two and add them. Also from each group subtract the smaller numeral from the larger.

Similarly make numerals with 3 digits. Take them in groups of two and add them. Get them checked by your teacher.

Ask your friends and find out who made the maximum number of questions.

**Very nice!**

After solving the questions you must be eager to know whether your solutions are correct. Here we will tell you how you can check your solution. Let us understand the method.

$$\begin{array}{r} 25308 \\ +76397 \\ \hline 101705 \end{array}$$

Total is 101705

Subtract 25308 from this

$$\begin{array}{r} 101705 \\ -25308 \\ \hline 76397 \end{array}$$

Here we can say our answer is correct if we subtract from the total any one of the given numbers, we should get the other.

Now check your answer by this method.

### Statement sums

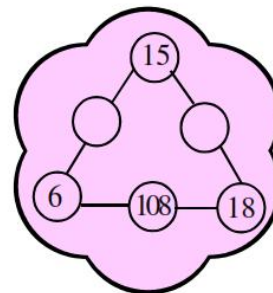
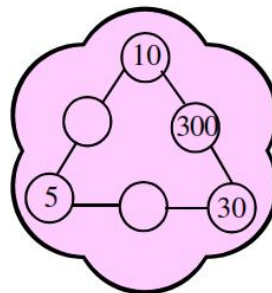
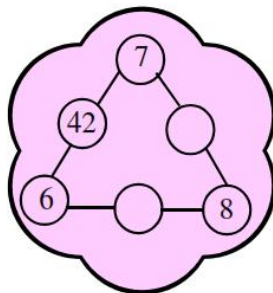
- (1) One businessman deposited Rs. 13,71,802 in his account in the first year and Rs. 12,18,625 in the second year. What is the total amount in his account in the two years?
- (2) Find the sum of the largest 6 digit number and the smallest 7 digit number.

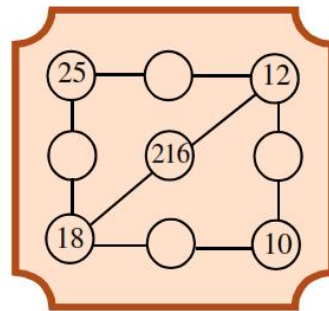
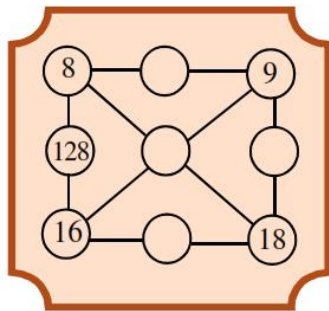


- (3) The population of one town is 6,52,561 and that of another town is 7,11,332. What is the total population of the two towns?
- (4) In a state there are 4,32,795 children studying in primary schools; 2,99,890 children in middle schools and 2,09,372 children in (secondary) schools. So how many total children are studying in this state?
- (5) The town has total population of 4,53,572 women and men, If 2,25,780 of them are men, what is the number of women?
- (6) The sum of two numbers is 2,30,560. If one of the number is 92,640, then what is the other number?
- (7) There are 3 candidates standing for election. The first candidate got 2,88,562 and the second candidate got 1,91,072 votes. If a total of 8,15,624 votes were cast, what number of votes did the third candidate get?
- (8) Ravi bought a house for Rs 6,80,000 and Rakesh bought another house for Rs. 5,50,000. What is the total cost of the two houses?
- (9) Find the difference between the smallest 4 digit number and the largest 3 digit number.
- (10) By subtracting 1 from the smallest 6 digit number, which number would you get? How many digits would it be?
- (11) Write two numbers whose sum is 9876.
- (12) Write two 5 digit numbers whose sum is 89,854.

## Multiplication

Observe, understand and complete the following-





Make some similar questions and give them to your friends to solve.

### Let us do and learn-

You have already learnt the method of multiplying a two digit number with another two digit number.

The examples given below will make it clear how you can multiply a three digit number with a two digit number.

**Example 1 :**  $463 \times 58 = ?$

**Solution :**

$$\begin{array}{r} 463 \\ \times 58 \\ \hline 3704 \\ +23150 \\ \hline 26854 \end{array}$$

$$\begin{aligned} &463 \times 58 \\ &= 463 \times (50+8) \\ &463 \times 8 = 3704 \\ &463 \times 50 = 23150 \\ &\quad \underline{26854} \end{aligned}$$

**Example 2 :**  $645 \times 273 = ?$

**Solution :**

$$\begin{array}{r} 645 \\ \times 273 \\ \hline 1935 \\ +45150 \\ 129000 \\ \hline 176085 \end{array}$$

$$\begin{aligned} &645 \times 273 \\ &= 645 \times (200+70+3) \\ &645 \times 3 = 1935 \\ &645 \times 70 = 45150 \\ &645 \times 200 = 129000 \\ &\quad \underline{176085} \end{aligned}$$

**Now try these :**

- |                       |                      |
|-----------------------|----------------------|
| (1) $735 \times 27$   | (2) $665 \times 51$  |
| (3) $513 \times 236$  | (4) $640 \times 70$  |
| (5) $867 \times 458$  | (6) $888 \times 222$ |
| (7) $306 \times 204$  | (8) $6438 \times 30$ |
| (9) $2284 \times 746$ |                      |

Make some similar questions on your own and show the solutions to your teacher.

### Statement sums

1. A cooler costs Rs. 4350. If a hostel purchases 15 coolers, what would the total cost of the coolers?
2. A cycle costs Rs. 1975. If there are 217 girls in a high school and each child is given one cycle. Find the total amount required for purchasing the cycles.
3. 4635 meter cloth is made in a factory in one day. What is the total length of cloth produced in the month of January?
4. A godown has 8734 sacks of grain. If each sack contains 75 kg. of grain, What is the total quantity of the grain in the godown?
5. Mohan saves Rs. 750 each month in his savings account. What amount would he save in 5 years?

### Division

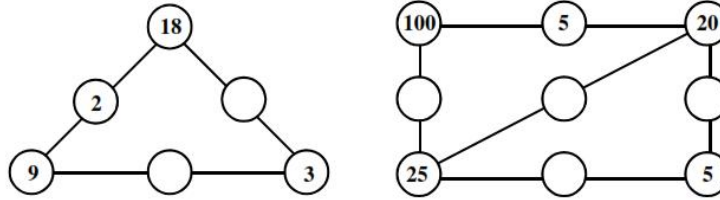
You have already learnt how to divide a three digit number by a one digit or a two digit number. Let us see some questions of this type:-

- |                   |                   |
|-------------------|-------------------|
| (1) $365 \div 5$  | (2) $816 \div 8$  |
| (3) $978 \div 7$  | (4) $735 \div 13$ |
| (5) $625 \div 12$ | (6) $432 \div 15$ |
| (7) $999 \div 11$ | (8) $384 \div 9$  |
| (9) $589 \div 19$ |                   |



## Maths - 5

Observe, understand and complete the following :-



### Checking your answer

Now we will let you know the method of checking your answer.

Look at the following example and understand:-

$$978 \div 7 = ?$$

**Solution :**

$$\begin{array}{r}
 139 \\
 7 \overline{) 978} \\
 \underline{- 7} \phantom{0} \\
 27 \\
 \underline{- 21} \\
 \phantom{0} 68 \\
 \underline{- 63} \\
 \phantom{00} 5
 \end{array}$$

you know that in the given question

$$\text{Dividend} = 978 \quad \text{Divisor} = 7$$

$$\text{Quotient} = 139 \quad \text{Remainder} = 5$$

$$\text{Dividend} = (\text{Quotient} \times \text{Divisor}) + \text{Remainder}$$

$$= 139 \times 7 + 5$$

$$= 973 + 5$$

$$= 978$$

which is the given dividend hence we can say that our solution is correct.

### Now you know that

If  $\text{Quotient} \times \text{Divisor} + \text{Remainder} = \text{Dividend}$   
then our solution is correct.

You can check your earlier solutions and see whether they were correct or not.

### Division of a four digit and five digit number

You have seen earlier that addition, subtraction and multiplication for a five digit number is same as that for a two, three or four digit number.

**Example 1:**

$$\begin{array}{r}
 264 \\
 27 \overline{) 7128} \\
 \underline{- 54} \phantom{00} \\
 172 \phantom{00} \\
 \underline{- 162} \phantom{00} \\
 108 \phantom{00} \\
 \underline{- 108} \phantom{00} \\
 000
 \end{array}$$

Quotient = 264

Remainder = 0

**Example 2:**

$$\begin{array}{r}
 1611 \\
 58 \overline{) 93456} \\
 \underline{- 58} \phantom{000} \\
 354 \phantom{00} \\
 \underline{- 348} \phantom{00} \\
 65 \phantom{00} \\
 \underline{- 58} \phantom{00} \\
 76 \phantom{00} \\
 \underline{- 58} \phantom{00} \\
 18
 \end{array}$$

Quotient = 1611

Remainder = 18

Before doing the division if you write the table of the divisor it will be easy for you to do the division.

Now find the solution of the given questions and check your answers:-

- |                      |                     |
|----------------------|---------------------|
| (1) $6531 \div 82$   | (2) $23671 \div 47$ |
| (3) $4035 \div 24$   | (4) $35152 \div 32$ |
| (5) $71839 \div 113$ | (6) $55679 \div 36$ |

Make some more questions, solve them and show them to your teacher.

### Statement Sums

- The daily wages of 25 labours is Rs. 1750. So what is the daily wage of each labour?
- On dividing 21,500 by a certain number we get 125 as the quotient. find the divisor?
- The product of two numbers is 1,15,625. If one of the numbers is 125, find the other?
- The total cost of 35 mobile sets is Rs. 37,825, then what is the cost of each mobile?

## Maths - 5

5. If the divisor is 48, the quotient is 403 and the remainder is 5, find the dividend.
6. Do this:

**Division method of more than 5 digit numbers is same as the division of 5 digit numbers.**

**So make some questions with more than five digits and find their solutions.**

**Find out who amongst your friends solved the maximum number of questions.**

## Now for some fun!

1. The given figure has 9 equal squares made with matchsticks.

Now remove only four matchsticks in such a way that you are left with five equal squares.

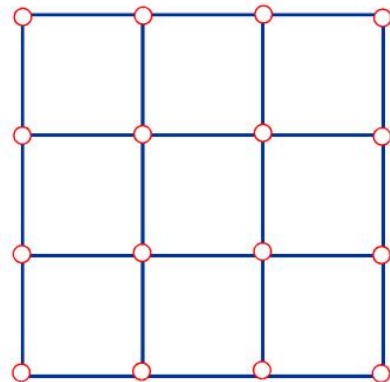
Make this figure using matchsticks and then

- a) Remove four matchsticks

Such that you are left with seven equal squares

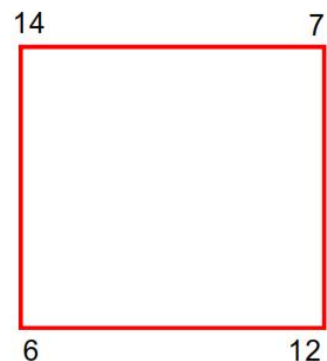
- b) Remove two matchsticks

Such that you are left with seven equal squares.



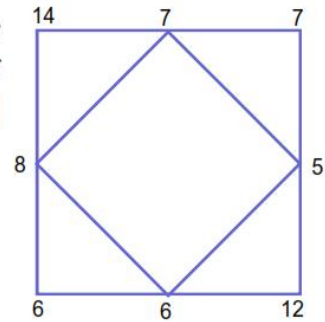
2. Do this also -

Step 1 : Make a square and write the numbers 14, 12, 6 and 7 at its edges.

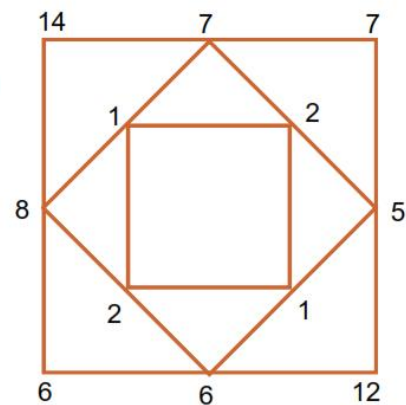




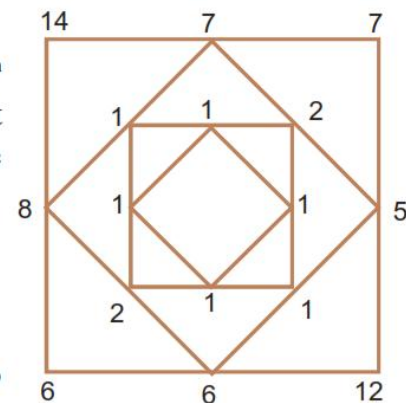
Step 2 : Join the mid points of this square to get another square. Write the difference of the numbers of the earlier square at the edges of the second square.



Step 3 : Repeat what you did in step 2 to get 3<sup>rd</sup> square in the centre.

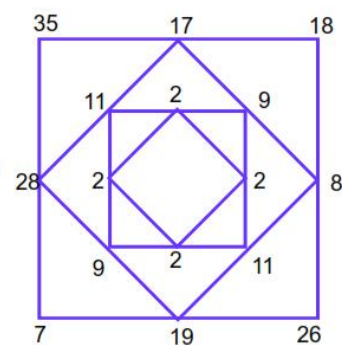


Step 4 : Repeat the same procedure to get 4<sup>th</sup> square, you will observe that you will get the same number at the edges of the fourth square. This is the last square.



Below given one figure. Observe it and try to understand.


**Note :-** While solving this type of squares the numbers of steps may be increased or decreased.



## Maths - 5

Now you can also make such squares on your own.

3. Given below are some magic squares. Fill the blank boxes with the correct digits as per the instructions given below.



		7
10		
		9

Total is 18

	13	
10		14

Total is 33

22		
		21
		28

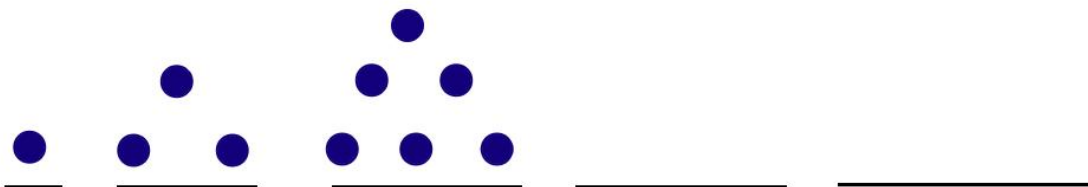
Total is 75

While solving the magic square see that the sum total of each line, each column and each diagonals is same.

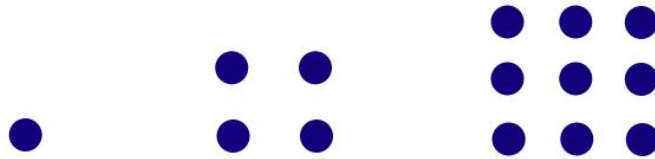
4. Look at the given pictures carefully.



Make at least two more pictures by moving this sequence forward.



The numbers taken in this order makes a long series. These numbers are called triangular numbers because points taken equal to these numbers make triangular figure.



Numbers taken in this order makes a long series. These numbers are called square numbers because points taken equal to these numbers make square figure.

5. Understand the given pattern and write at least three more terms in the given sequence:

- 1) 1, 1+2, 1+2+3, \_\_\_\_
- 2) 3, 7, 11, \_\_\_\_
- 3) 1, 4, 9, 16, \_\_\_\_
- 4) 1 2 4 \_\_\_\_
- 5) 3 9 27 \_\_\_\_

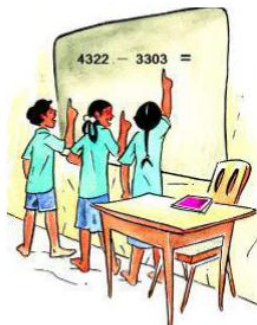


6. Some questions are given below. Understand them and answer carefully:

1. One child can see upto a distance of three kilometers, then how far 6 children can see?
2. Three children plucked 20 mangoes, so how many total mangoes did they pluck together ?
3. There were 20 birds sitting on a tree. A hunter fired a shot at a bird but missed, now how many birds are left on the tree?

Have you been able to answer these questions correctly?

Make some more questions of your own and ask your friends to solve them.



## CHAPTER-3

### Profit and Loss

Sanjay's father has a fruits shop. One day his father was writing some calculations on a piece of paper. Sanjay was watching it. The calculations were as shown below.

Item	Bought (in Rs.)	Sold at (in Rs.)
Apples	650	730
Bananas	300	380
Grapes	250	200
Oranges	300	300



His father said - Today, a profit was made on apples and Bananas and a loss on grapes.

Sanjay asked - How?

Father - I sold the apples and bananas at a price which was more than the price at which I bought them so there was a profit on those. But the grapes were sold at a price lower than the price at which I bought them. So there was a loss on those.

Sanjay - Why did you get less price for the grapes?

Father - Because some of the grapes were rotten.

Sanjay - You bought orange for Rs. 300 and sold them for the same price.

Father - Yes, so there was neither a profit nor a loss on the sale of oranges.

#### Now you know-

If a shopkeeper sells at a price higher than the buying price a profit is made and if he sells at a price lower than the buying price, a loss is made.

The price at which items are bought is known as cost price and the price at which it is sold is known as selling price.



## Profit & Loss

In the table below, are given the cost price and selling price of certain items. Understand and complete the table.

Cost price	Selling price	Profit, or Loss, ...	Amount in Rs.
145	165		
525	540		
330	330		
480	510		
640	635		



**Profit = selling price - cost price**

**Loss = cost price - selling price**

So if we have the cost price and selling price, we can get the profit or the loss incurred.

**Example 1 :** One shopkeeper bought a fan for Rs. 525 and sold it for Rs. 575, what is his profit or loss?

**Solution :**

Cost price of the fan = Rs. 525

Selling price of the fan = Rs. 575

The selling price is more than the cost price so there was a profit.

As profit = selling price - cost price

= 575 - 525

= Rs. 50

So the shopkeeper made a profit of Rs. 50

**Example 2 :** Balram bought a watch for Rs. 330 and sold it for Rs. 250, so what was his profit or loss?

**Solution :** The cost price of the watch = 330

The selling price of the watch = Rs. 250



Here the cost price is more than the selling price, So Balram incurred a loss.

$$\begin{aligned}\text{and as loss} &= \text{cost price} - \text{selling price} \\ &= 330 - 250 \\ &= \text{Rs. } 80\end{aligned}$$

Hence Balram had a loss of Rs. 80.



If we know the cost price of an item and its profit or loss, then could we calculate its selling price? Let us see how-

**Example 3 :** If the cost price of an item is Rs. 700 and the shopkeeper made a profit of Rs. 50 on selling it, what would be its selling price?

**Solution :** The cost price is Rs. 700.

Profit made Rs. 50.

Since a profit of Rs. 50 has been made, the selling price should be more than the cost price and we will get it by adding the cost price and profit-

$$\begin{aligned}\text{Selling price} &= \text{cost price} + \text{profit} \\ &= 700 + 50 \\ &= \text{Rs. } 750\end{aligned}$$

So the selling price is Rs. 750.



**Example 4 :** If an item was bought for Rs. 900 and on selling it a loss of Rs. 70 was incurred then find the selling price.

**Solution :** Cost price - Rs. 900

Loss - Rs. 70

Since an item of Rs. 900 was sold at a loss of Rs. 70 the selling price would be less than the cost price and we shall get it by subtracting the loss from the cost price.

$$\begin{aligned}\text{Selling price} &= \text{Cost price} - \text{Loss} \\ &= 900 - 70 \\ &= \text{Rs. } 830\end{aligned}$$

Thus, the selling price of the item would be Rs. 830

Now let us see how can we get the cost price if we are given the selling price along with the profit or loss.

**Example 5 :** On selling an item for Rs. 560, a shopkeeper makes a profit of Rs. 70, what would be its cost price?

**Solution :**

Here the selling price = Rs. 560

profit = Rs. 70

By selling at Rs. 560, a profit of Rs. 70 is made and the cost price will be lesser than the selling price which we would get by subtracting the profit from the selling price.

$$\begin{aligned}\text{Hence, cost price} &= \text{selling price} - \text{profit} \\ &= 560 - 70 \\ &= \text{Rs. 490}\end{aligned}$$

So the cost price of the item would be Rs. 490

**Example 6 :** If the selling price of an item is Rs. 480 and a loss of Rs. 56 is incurred, what would be its cost price be?

**Solution :**

By selling at Rs. 480, a loss of Rs. 56 is made which means the cost price would be more than the selling price.

To find the cost price we have to add the selling price and the loss.

$$\begin{aligned}\text{Hence, cost price} &= \text{Selling price} + \text{loss} \\ &= 480 + 56 \\ &= \text{Rs. 536}\end{aligned}$$

The cost price of the item is Rs. 536





### Exercise

#### 1. The amount of loss or profit :

1. Cost price Rs. 136, selling price Rs. 143, profit Rs. 7
2. Cost price Rs. 452, selling price Rs. 430, \_\_\_\_\_
3. Cost price Rs. 512, selling price Rs. 580, \_\_\_\_\_
4. Cost price Rs. 750, selling price Rs. 775, \_\_\_\_\_
5. Cost price Rs. 645, selling price Rs. 650, \_\_\_\_\_

#### 2. Fill in the blanks :

1. Selling price Rs. 725, cost price Rs. 650, so profit or loss \_\_\_\_\_
2. Cost price Rs. 980, loss Rs. 250, so selling price \_\_\_\_\_
3. Selling price Rs. 830, profit Rs. 125, so cost price \_\_\_\_\_
4. Selling price Rs. 675, loss Rs. 50, then cost price \_\_\_\_\_
5. Cost price Rs. 565, profit Rs. 35, so selling price \_\_\_\_\_

### Statement Sums

1. A trader bought 100 kg. of wheat for Rs. 850 and sold it at the rate of Rs. 95 for 10 kg. so how much profit or loss did he make?
2. Raju bought 20 litre milk for Rs. 200 and sold it for Rs. 12 per litre. What was his profit or loss?
3. Jamuna bought a fan and sold it for Rs. 690 at a loss of Rs. 180. Find the cost price of the fan.
4. Mona bought a clock for Rs. 435 and he wants sell it at a profit of Rs. 55, so what would its selling price be?
5. Sunil sold 5 chairs for Rs. 850. He made a profit of Rs. 100, so what was the cost price of the chairs.
6. Bharti bought a cow for Rs. 3750 and sold it after a few days at a profit of Rs. 150, so what was its selling price?



7. Suresh sold a fan for Rs. 895 at a loss of Rs. 52. What was the cost price of the fan?
8. Geeta bought 5 watches for Rs. 805 and sold three of them for Rs. 182 and two of them for Rs. 138. Did Gopal make profit or did he incur a loss?
9. Deepak bought 5 kg. sugar at the rate of Rs. 20.25 per kg. He sold 3 kg sugar at the rate of Rs. 20 per kg and 2 kg sugar at the rate Rs. 21.30 per kg. Did he make a profit or loss?
10. A shopkeeper bought a sack of rice for Rs. 1250 and sold it at a profit of Rs. 75. What was its selling price?



## CHAPTER- 4

### Unitary Method

You are given below a list of items and their unit cost.

**Look at it carefully-**

Pen	-	Rs. 5	Pencil	-	Rs. 2
Rubber	-	Rs. 1	Copy	-	Rs. 6
Box of chalk	-	Rs. 12	Slate	-	Rs. 15

From the above given rates, complete the table given below :-



S.No.	Item	Quantity	Cost
1.	Pen	08	
2.	Slate	05	
3.	Pencil	10	
4.	Rubber	10	
5.	Copy	06	
6.	Box of chalk	03	

What did you do to complete the table?

Ask your friends how they completed the table?

Have you used the same methods as your friend? Discuss this with your teacher.

**If the rate of each item is known and we want to find the cost of several items, we have to multiply the number of item bought with the rate of each item.**

## Unitary Method

**Example 1 :** If the rate of one copy is Rs. 8, then what would the price of 6 copies?

**Solution :** Given that the cost of one copy = Rs. 8  
We have to find the cost of 6 copies = ?

Number of copies	cost
1	Rs. 8
6	?

As the cost of each copy = Rs. 8

Therefore the cost of 6 copies =  $8 \times 6 = 48$

**Example 2 :** What would the cost of 5 watches, if the cost of each is Rs. 350?

**Solution :** Given that cost of one watch = Rs. 350

We need to find the cost of 5 watches = ?

Number of watches	Cost (in Rs.)
1	Rs. 350
5	?

Since the cost of one watch = Rs. 350

Therefore the cost of 5 watches =  $350 \times 5 = \text{Rs. } 1750$

Look at the table given below :

S.No.	Item	Quantity	Cost
1.	Pen	7	Rs. 28
2.	Register	5	Rs. 60
3.	Chalk	6 Boxes	Rs. 72
4.	Pencil	10	Rs. 20

On reading the table we get the cost of 7 pens, 5 registers, 10 pencils but not the cost of 1 pen, 1 register or 1 pencil.

- Can you use the information given in the table to find the cost of 1 pen?
- Discuss with your friends.
- Before this we have found out the cost of many items when the cost of one item was given.

- Now we need to find the cost of one item when the cost of many items are given. The method we need to follow is exactly the opposite of the earlier method.
- You know that the operation opposite to multiplication is division. So when we want the cost of one item from the cost of many we have to divide the cost by the number of items.

**The mathematical symbol since is  $\therefore$  and for therefore is  $\therefore$ .**



## Maths -5

### Come let us find a solution-

We are given the cost of 7 pens = Rs. 28

We want to find the cost of 1 pen = ?

Number of pens	Cost
----------------	------

7	Rs. 28
---	--------

1	?
---	---

The cost of 7 pens = Rs. 28

The cost of 1 pen =  $28 \div 7 = \text{Rs. } 4$

Now use the information given in the above table and find the cost of one register, one pencil and one box of chalk sticks.

### Meeta's problem

Meeta's brother got some vegetables from the market. Meeta asked- 'How much did you pay for this bottle gourd?' Her brother said- 'I bought the 2 kg. bottle gourd for Rs. 12.' Her brother thought he would test Meeta's mathematical ability, so he asked- 'Meeta, can you tell me how much I have to give for 10 kg. bottle gourd?'

Meeta thought to herself- I know how to find the cost of one when the cost of many is given. I also know how to find the cost of many when the cost of one is given however here I have been given the cost of many and I have to find the cost of a different number. Let me write it down

Meeta wrote in her copy-

Quantity of gourd	Cost
-------------------	------

$\therefore 2 \text{ kg}$	Rs. 12
---------------------------	--------

$\therefore 1 \text{ kg}$	$12 \div 2 = \text{Rs. } 6$
---------------------------	-----------------------------

$\therefore 10 \text{ kg}$	$10 \times 6 = \text{Rs. } 60$
----------------------------	--------------------------------

Her brother looked at the solution and said- 'You are absolutely correct, Meeta. You are very clever.'

**Example 3 :** If the cost of 12 kg. tomatoes is Rs. 60, then what is the cost of 15 kg. of tomatoes?

**Solution :** Given that the cost of 12 kg. of tomatoes = Rs. 60

We have to find the cost of 15 kg. of tomatoes = ?



Kilogram	Cost (in Rs.)
----------	---------------

12	Rs. 60
----	--------

15	?
----	---

12 kg. tomatoes cost = Rs. 60

1 kg. tomatoes cost =  $60 \div 12 = \text{Rs. } 5$

15 kg. tomatoes cost =  $5 \times 15 = \text{Rs. } 75$

**Example 4 :** If the cost of 6 chairs is Rs. 642, what is the cost of 4 chairs?

**Solution :** Given that the cost of 6 chairs is Rs. 642

We have to find the cost of 4 chairs = ?

Number of chairs	Cost (in Rs.)
------------------	---------------

6	642
---	-----

4	?
---	---

$\therefore$  Cost of 6 chairs = Rs. 642

$\therefore$  Cost of 1 chair =  $642 \div 6 = \text{Rs. } 107$

$\therefore$  Cost of 4 chairs =  $107 \times 4 = \text{Rs. } 428$



1. If 1 kg. grapes are available for Rs. 35, how much would 7 kg grapes cost.
2. Find the cost of 1 cycle when 3 cycles cost Rs. 6360.
3. If a labour charges Rs. 385 for 7 days work, then what amount would he take for 12 days?
4. If 3 litre of petrol costs Rs. 156, what is the cost of 8 litre of petrol?
5. If the cost of 5 kg sugar is Rs. 60, how much sugar would you get for Rs. 120?
6. How many cups of capacity 200 ml. would be needed to fill 1600 ml. of milk?
7. 3 pens can be bought for Rs. 15; How much would you have to pay to buy 15 pens?
8. One packet containing 5 pencils is available for Rs. 13. Another packet containing 10 pencils is available for Rs. 25. Which packet has a lesser rate per pencil?

## CHAPTER- 5

### Average



Raju has a milkman living in his neighbourhood. One day Raju asked him how much milk do you get everyday? The milkman told him 30 liters. Raju said, “You have 5 cows which means each cow gives around 6 litre of milk.” The milkman said, “No, some cow gives more than 6 litre and some give less than 6 litre, but in all there is a total of 30 litre of milk.

Raju : How is that? I don't understand.

Milkman : The white cow gives 3 liters, the red one gives 4 litre, the brown cow gives 6 litre and both the black ones give 7 and 10 litre respectively. Does it not add to give 30 liters?

Raju could not understand this and he thought a lot about it, After going to school he asked his teacher if 5 cows give a total of 30 liters milk each cows would give 6 liters but the milkman told him that the cows gave 3,4,6,7 and 10 liters of milk.

Teacher : Raju what is the least amount of milk given by the cows.

Raju : 3litre.

Teacher : And the maximum amount?

Raju : 10 litre.

Teacher : The 6 litre you talked about is in the middle of these two. The measure of this middle value is known as an average.

Raju : How did we get this average?

Teacher : The very method by which you found it. Come let us do it on the blackboard and understand this properly.

## Average

The number of cows = 5

The amount of milk given by each = 3,4,6,7 and 10 litres

The total quantity of milk =  $3+4+6+7+10 = 30$  litres

If all the cows were to give same amount of milk then

each would give =  $30 \div 5 = 6$  litres

Hence each cow gives an average of 6 litres milk. Let us take another example to understand this.

One student measured the height of his classmates and wrote it down as follows:-

Name	Height (in cms)
Santosh	125
Mona	123
Anju	133
Salma	124
Vineet	140
Yash	131
Neha	120

Now let us find the average height of the students

Number of children = 7

The total of their heights =  $125+123+133+124+140+131+120$  cm

Average =  $896 \text{ cm} \div 7$

Hence the average height = 128 cm

From the examples given above we can see that the numbers are giving some information. These numbers are called observations.

The height of the students can be taken as observations.

$\therefore \text{Average} = \frac{\text{Sum of all the observations}}{\text{Total number of observations}}$
--



**Example 1 :** In a primary school in Navagaon, the attendance of the students of classes 1 to 5 on Tuesday was respectively 15,17,15,14 and 19. What was the average attendance in a class on Tuesday?

The attendance of classes 1 to 5 was 15,17,15,14 and 19

Number of observations = 5

Average attendance =  $\frac{\text{Sum of all the observations}}{\text{Total number of observations}}$

$$\begin{aligned}\text{Average attendance} &= \frac{15+17+15+14+19}{5} \\ &= 80 \div 5 \\ &= 16\end{aligned}$$

Hence the average attendance of students of classes 1 to 5 on Tuesday was 16

**Example 2 :** There are 6 rows in a mango grove. There are 10,15,12,10,11 and 14 trees respectively in the rows. So what is the average number of trees in each row?

Average =  $\frac{\text{Sum of the observations}}{\text{Total number of observations}}$

$$\begin{aligned}\text{Average} &= \frac{10+15+12+10+11+14}{6} \\ &= 72 \div 6 \\ &= 12\end{aligned}$$

Thus, there are 12 trees on an average in each row in the mango grove.



1. A vegetable vendor's earnings in 5 days were Rs. 45, Rs. 50, Rs. 43, Rs. 52 and Rs. 60 respectively. What was his average earning?
2. Ramlal has 3 cows which give 12 litre, 8 litre and 7litre of milk respectively. So what is the average milk given by Ramlal's cows?



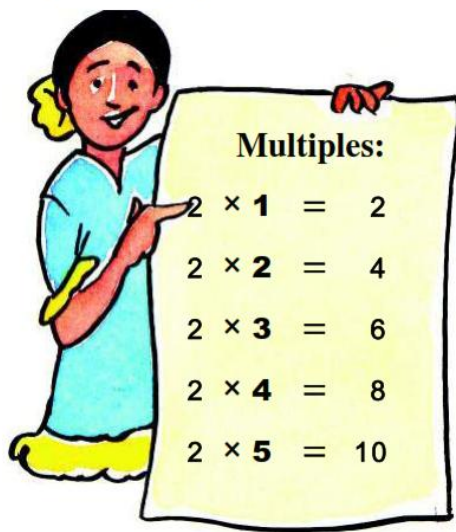
3. The weight of four students of class 4 is 27,23,28 and 30 kg respectively. Find the average weight.
4. Deepak secured 38 marks in Hindi, 42 in Mathematics, 41 in environmental science and 65 in English during quarterly examination. Find the average marks.
5. Rukhsana has 6 vessels of 25,27,24,32,33 and 15 litre respectively. Find the average capacity of the 6 vessels.
6. A family of five members have a monthly income of Rs. 1650, Rs. 2500, Rs. 2300, Rs. 2000 and 1900 respectively. What is their average income?
7. Amit paid Rs. 180, Rs. 140, Rs 210, Rs. 785, Rs. 205 and Rs. 208 respectively as the telephone bill for 6 months. So what was the average payment that he made each month?
8. A cricketer made 60, 75, 100, 25 and 50 runs respectively in five matches. So what was his average score in each match?
9. Niti, Riti, Ranu and Sweety, Paro and Shalu made respectively 24, 23, 15, 40, 25 and 35 chapattis. What was the average number of chapattis made by each?
10. One vegetable vender sold respectively 250, 275, 310, 280, 320, 300, 330 Rupees worth of vegetables in a week. So what was his average sale in that week ?



## CHAPTER- 6

### Multiples and Factors

You have learnt how to multiply by making use of tables. We shall talk more about the values you get when you make use of tables and multiply the number respectively by 1,2,3,...



By multiplying 2 with 1,2,3..... respectively we get 2,4,6,.... There are known as multiples of 2.

When we divide these numbers by 2

They get completely divided without a remainder.



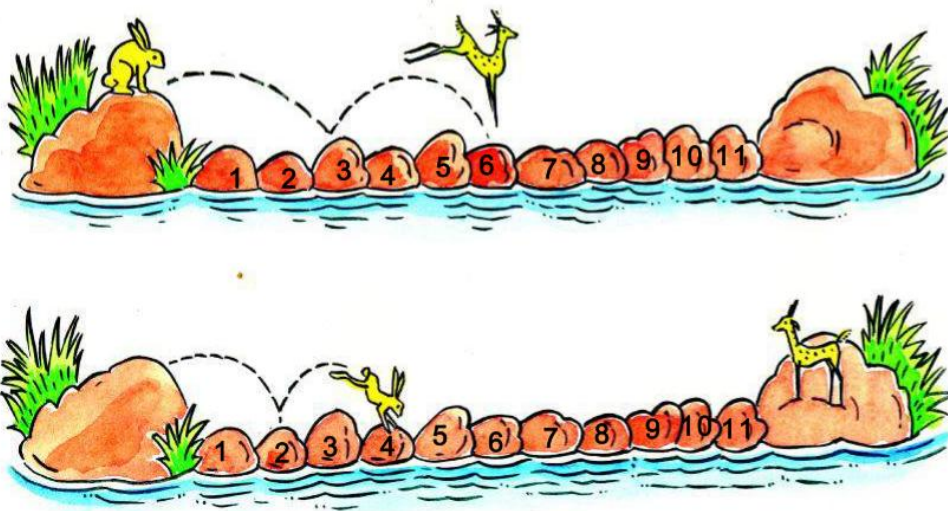
Now we will do the same with 3.

$3 \times 1$	$=$	3
$3 \times 2$	$=$	.....
$3 \times 3$	$=$	.....
$3 \times 4$	$=$	.....

On multiplying 3 by 1,2,3,4.... what numbers do we get? Write in the space given below:

.....

The numbers you have written here are all multiples of 3. On dividing these numbers by 3 they get completely divided without a remainder.



**Look at the picture and answer the questions:**

- The deer will jump on which rocks to reach the other side?
- The rabbit will jump on which rocks to reach the other side?

Now multiply the numbers given below by 1,2,3,..... and find their multiples

Multiples of 4 .....

Multiples of 5 .....

Multiples of 9 .....

**Look at the numbers given below and answer the given questions:**



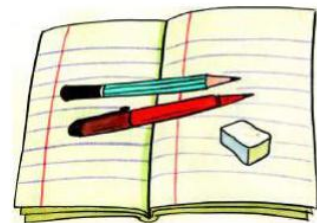


- Which of them are multiple of 2?  
.....
- Can you write four multiples of 2 which are not given?  
.....
- Which of them are multiples of 4?  
.....
- Can you write three multiples of 4 which are not given?  
.....
- Besides 2 and 4 which other numbers multiples are given here?  
.....
- Out of the given numbers which are not the multiples of 2?  
.....
- Which are the given numbers which are not the multiples of 5?  
.....
- List the numbers which are multiples of 2 and 3 both.  
.....

### The biggest multiple

Write as many multiples of 3 as you can.

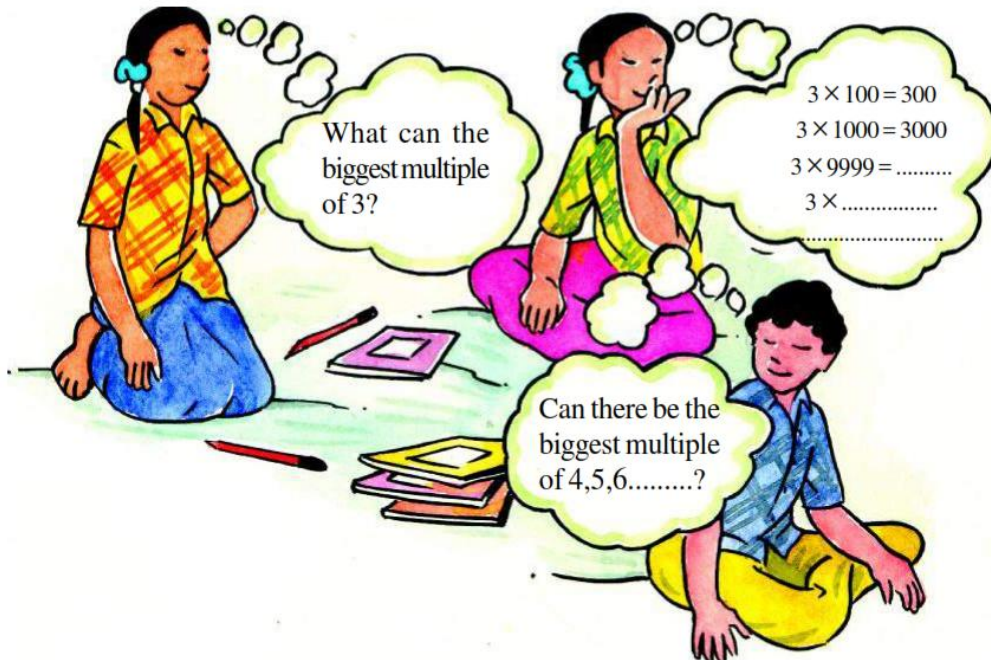
3,6,9, .....  
.....  
.....  
.....  
.....





Which of these is the biggest multiple? .....

Can there be a bigger multiple than this? .....



### Least common multiple

Try to identify the multiples of 2 and 3 from the table given below and colour the space given below as shown.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
Multiples of 2																	
Multiples of 3																	

**Observe the table and write:**

- The multiples of 3  
.....
- The multiples of 2  
.....
- Are there some numbers which are multiples of both 2 and 3? Note it down.  
.....

These numbers are the common multiples of 2 and 3 both.

Which of these is the smallest common multiple?

.....

This the least common multiple of 2 and 3.

Hence the least common multiple means it is that number which is a multiple both of the given numbers and the smallest of all the common multiples.

Let us find the least common multiple of 4 and 5:

The multiples of 4 : 4, 8, 12, 16, 20, 24, 28, 32, 36, 40, 44, .....

The multiples of 5 : 5, 10, 15, 20, 25, 30, 35, 40, 45, .....

The common multiples of 4 and 5 are

20, 40, .....

and the smallest common multiple = 20

Hence 20 is the smallest number which is divisible completely by both 4 and 5

**Now find the least common multiple of the numbers given below:**

**Example 1 :** 2 and 5

**Solution :** Multiples of 2 .....

Multiples of 5 .....

Common multiples of 2 and 5 .....

The smallest common multiple .....

Hence least common multiple of 2 and 5 is .....



**Try these:**

**(1) 8 and 12**

**Solution :** .....

.....

.....

.....

(2) Can you find the least common multiple of 3 numbers?



**Solution :**

To find this let us take 3 numbers 6, 10 and 15

Multiples of 6 .....

Multiples of 10 .....

Multiples of 15 .....

Common multiples of 6,10,15 .....







The smallest common multiple .....

Hence the least common multiple of 6,10,15 is .....

Now take two or three numbers and find the LCM and show it to your teacher.

### Factors

How can you write 12 as a product of two different numbers?

	$1 \times 12$	12
	$2 \times 6$	12
	$3 \times 4$	12
	$4 \times 3$	12
	$6 \times 2$	12
	$12 \times 1$	12

Can you write the number which completely divide 12 and leave no remainders?

.....

All these numbers are factors of 12.



Those number are known as factors of a given number if they completely divide the given number.

Find the factors of the numbers given below:

- Factors of 6 are 1, 2, 3, 6
- Factors of 8 are .....
- Factors of 12 are .....
- Factors of 15 are .....

You can also determine factors by dividing the given number respectively by 1,2,3..... and identifying those which divides the given numbers completely.

Give reasons to say whether the given statements are true or false.

**Example 2 :**

**3 is a factor of 8**

**False**

Because 3 does not divide 8 completely and gives a remainder 2 on dividing.

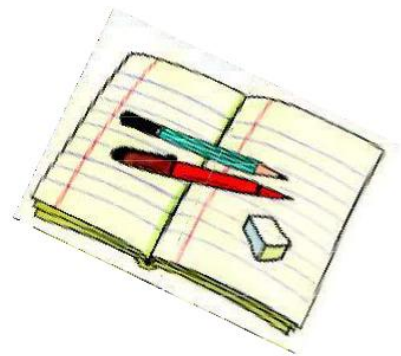
1. 6 is a factor of 36 .....
2. 8 is a factor of 8 .....
3. 5 is a factor of 12 .....
4. 7 is a factor of 25 .....



5. 6 is a factor of 48. ....
- .....
6. 12 is a factor of 96. ....
- .....

Write the factors of the numbers given below:

- Factors of 2 .....
- Factors of 3 .....
- Factors of 4 .....
- Factors of 5 .....
- Factors of 8 .....
- Factors of 12 .....
- Factors of 7 .....



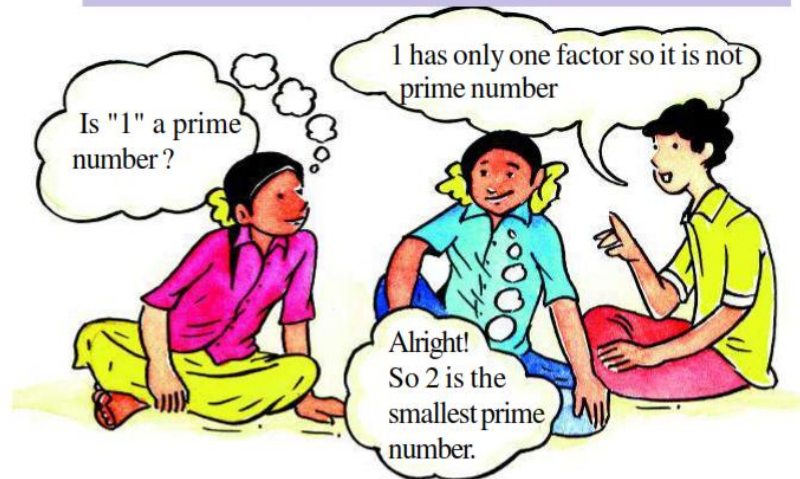
1. Which number is a factor of all the numbers?  
.....
2. Is there a number which is not a factor of itself?  
.....
3. Write down those numbers which have exactly two factors.  
.....

**Numbers which have exactly two factors  
are called prime numbers**

The numbers which you have written in which there are numbers which have more than two factors. List those numbers.

.....

**Numbers which have more than two factors are called composite numbers**



- circle the prime numbers-  
12, 22, 15, 23, 17, 25, 21, 19, 20, 35
- Write the prime numbers between 4 and 10.
- Which is the prime number nearest to 35?
- Write the prime numbers less than 4.
- Write the composite numbers between 1 and 10.

### Highest common factor

You know that the factors of a number completely divides that number.

Can you write all the factors of 12?

Let us see which numbers have 12 is their tables.

1,2,3,4,6 and 12

All of these numbers divide 12 completely and are therefore factor of 12

Now write all the factors of 18.

.....  
.....

Are there any factors of 18 which are also factors of 12?

Let us write the factors of both 12 and 18.

.....

**They are known as the common factors of 12 and 18**

**Now let us try to find the common factors of 16 and 20.**

Factors of 16 - 1, 2, 4, 8, 16

Factors of 20 - 1, 2, 4, 5, 10, 20

The common factors of 16 and 20 are 1, 2 and 4. 4 is the biggest common factor and is known as the highest common factor (HCF)

**So, the highest common factor of given numbers is the largest number of the common factors.**

**Let us find the highest common factor of 16 and 32.**

Factors of 16 - 1, 2, 4, 8, 16

Factors of 32 - 1, 2, 4, 8, 16, 32

The common factors are 1, 2, 4, 8 and 16 and the largest among these is 16, hence 16 is the highest common factor of 16 and 32.

**Find the HCF of-**

(1) 8 and 12                      (2) 10 and 20                      (3) 16 and 20

(4) 9 and 27                      (5) 13 and 39                      (6) 15 and 22

Now take any two numbers and find their HCF. Show the result to your teacher.

Take 12, 18 and 24 and find their HCF.

Now take any 3 numbers by yourselves and try finding their HCF. Confirm with your teacher.

**Think and answer-**

1. Can you find the smallest multiple of 8 and 12?
2. Can you find the largest multiple of 8 and 12? Discuss with your friends and teacher.
3. What will be the highest common factor of prime numbers like 5 and 7?



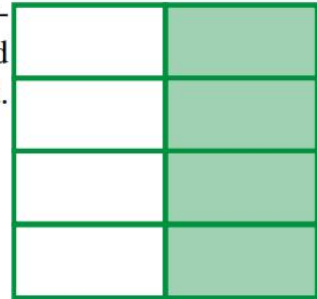


## Fractions

Abhay and Kittu were solving some questions of fractions. Kittu showed Abhay the adjacent picture and asked him to write down the fraction to represent the shaded part.

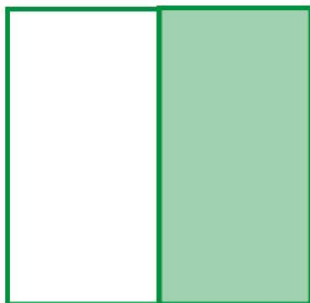
Abhay wrote  $\frac{1}{2}$

Kittu said, 'No', it is  $\frac{4}{8}$



They started arguing. Ultimately they decided to ask Laxmi Didi as to who was right.

'Laxmi Didi, I am saying that the shaded part representing a fraction is one by two, and Kittu says it is four by eight. Can you tell us who is correct?' Abhay asked.



Laxmi Didi smiled and said, "Both of you are right".

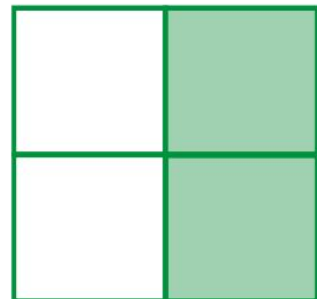
"Let us understand by folding a paper. I have taken a paper folded it through the centre and opened it. Now look at it and tell me how many parts are made? And what part is each part of the whole paper?"

"The paper is divided into two equal parts and each part is one by two of the whole", Abhay answered.

Laxmi didi coloured one half of the paper and again folded it horizontally and then asked, "Now what part is the shaded part of the whole?"

Kittu said - "Total parts are four and coloured parts are two, so the coloured part is two by four of the whole."

Kittu can we say this as  $\frac{1}{2}$  ?

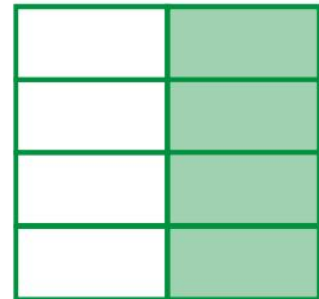




"Yes, we can say so, since one by two and two by four is the same coloured part of the paper."

Laxmi Didi again folded the paper horizontally and asked- "Now tell me what part is the coloured part of the whole?"

Abhay thought a little and answered, "The total parts of the paper are 8 and coloured parts are four so the coloured part is four by eight of the whole."



"Now think whether one by two, two by four and four by eight are all equal?" Laxmi asked.

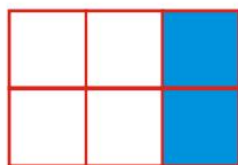
"Yes didi, all three of them are representing the same coloured part. So all three are equal." Abhay answered.

**All such fractions which represent the same part of a whole are called equivalent fractions.**

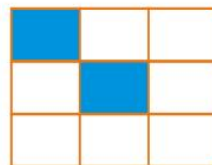
Now look at the pictures given below, write the fraction to represent the shaded parts and say which of them are equivalent fractions:



\_\_\_\_\_



\_\_\_\_\_



\_\_\_\_\_



\_\_\_\_\_



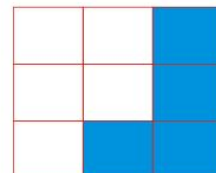
\_\_\_\_\_



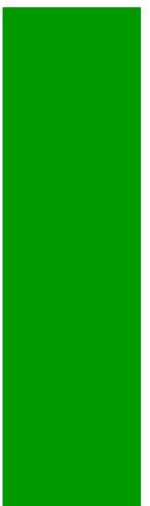
\_\_\_\_\_



\_\_\_\_\_



\_\_\_\_\_



Now write the fraction, represented by the shaded parts in the following pictures:



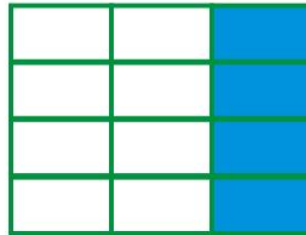
— — — — —



— — — — —



— — — — —



— — — — —

Is the shaded part the same in all the pictures? .....

Then, are  $\frac{1}{3}, \frac{2}{6}, \frac{3}{9}, \frac{4}{12}$  all equivalent fractions? .....

You are right  $\frac{1}{3}, \frac{2}{6}, \frac{3}{9}$  and  $\frac{4}{12}$  are all equivalent to each other.



Among these  $\frac{1}{3}$  is known as the fraction in the simplest form.

Now, if you were not given any pictures and you had to find equivalent fractions, what would you do?

Let us understand-

You have seen above that the equivalent fractions of  $\frac{1}{3}$  are  $\frac{2}{6}, \frac{3}{9}, \frac{4}{12}, \dots$  etc.

If we factorise the numerator and denominator, we get.

$$\frac{2}{6} = \frac{1 \times 2}{3 \times 2} \quad \frac{3}{9} = \frac{1 \times 3}{3 \times 3}$$

$$\frac{4}{12} = \frac{1 \times 4}{3 \times 4}$$

You can see that we are getting equivalent fractions of  $\frac{1}{3}$  by multiplying the numerator and denominator with 2,3,4 etc. respectively.

Let us find some equivalent fractions of  $\frac{3}{5}$

As mentioned above we would find equivalent fractions of given fraction by multiplying the numerator and denominator by 2,3,4..... respectively.

Hence the equivalent fractions of  $\frac{3}{5}$  are:

$$(i) \quad \frac{3}{5} \times \frac{2}{2} = \frac{6}{10}$$

$$(ii) \quad \frac{3}{5} \times \frac{3}{3} = \frac{9}{15}$$

$$(iii) \quad \frac{3}{5} \times \frac{4}{4} = \frac{12}{20}$$

$$(iv) \quad \frac{3}{5} \times \frac{5}{5} = \frac{15}{25}$$

$$(v) \quad \frac{3 \times 6}{5 \times 6} = \frac{18}{30}$$



Hence equivalent fractions of  $\frac{3}{5}$  are  $\frac{6}{10}, \frac{9}{15}, \frac{12}{20}, \frac{15}{25}, \dots$  etc.

### Exercise

Write equivalent fraction of the following -

1.  $\frac{2}{3}$

2.  $\frac{8}{10}$

3.  $\frac{3}{5}$

4.  $\frac{4}{6}$

5.  $\frac{1}{7}$

Can we get equivalent fraction by dividing the numerator and the denominator by any number?

Now if you want to write the simplest form of a fraction, what would you do?

**Let us understand-**

In the fraction  $\frac{8}{12}$ .

The common factor of numerator 8 and denominator 12, are 2 and 4.

## Maths - 5

Therefore, the numerator and denominator can be divided by 2 as well as by 4.

After dividing 2 from the numerator and denominator of  $\frac{8}{12}$ , we get

$$\frac{8}{12} = \frac{8 \div 2}{12 \div 2} = \frac{4}{6}$$

In the same way by dividing 4 from numerator and denominator, we get

$$\frac{8}{12} = \frac{8 \div 4}{12 \div 4} = \frac{2}{3}$$

$\therefore$  By dividing 2 and 4 from the numerator and denominator of  $\frac{8}{12}$ , we get  $\frac{4}{6}$  and  $\frac{2}{3}$

which are equivalent fraction of  $\frac{8}{12}$ , here  $\frac{2}{3}$  is the simplest form of  $\frac{8}{12}$ .

**Let us take another fraction  $\frac{6}{15}$**

The common factor of the numerator and denominator is 3

$$\text{Hence simplest form of } \frac{6}{15} = \frac{6 \div 3}{15 \div 3} = \frac{2}{5}$$

$$\therefore \text{ Simplest form of } \frac{6}{15} = \frac{2}{5}$$

Now write the following fractions in their simplest form:

(i)  $\frac{3}{9}$

(ii)  $\frac{36}{40}$

(iii)  $\frac{4}{12}$

(iv)  $\frac{56}{64}$

(v)  $\frac{8}{10}$

(vi)  $\frac{35}{45}$

(vii)  $\frac{12}{20}$

(viii)  $\frac{4}{10}$

(ix)  $\frac{15}{25}$

(x)  $\frac{22}{55}$

(xi)  $\frac{4}{5}$

(xii)  $\frac{3}{8}$

**Do this also:**

Write as many equivalent fractions as you can for the shaded part of given picture.



You can use a paper to obtain the different fractions-

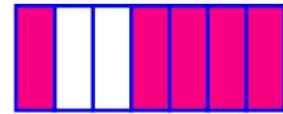


## Addition and subtraction of fraction -

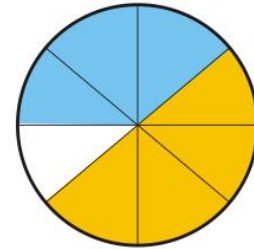
### Adding fractions with the same denominator:

**Example 1 :** Munnu had white washed  $\frac{4}{7}$  portion of the wall by the first day and the next day, he white washed the  $\frac{1}{7}$  portion. During these two days he white washed  $\frac{5}{7}$  portion of the wall.

$$\frac{1}{7} + \frac{4}{7} = \frac{5}{7} \text{ or } \frac{1+4}{7}$$



**Example 2 :** Add  $\frac{3}{8} + \frac{4}{8} = \frac{3}{8} + \frac{4}{8} = \frac{7}{8}$  or  $\frac{(3+4)}{8}$



Hence we can say-

**To add fractions with the same denominators we add the numerators and write it as a numerators and the denominator is written only once.**

**Solve these -**

1.  $\frac{5}{16} + \frac{7}{16} = \frac{5+7}{16} = \frac{12}{16}$

2.  $\frac{2}{7} + \frac{3}{7} = \dots\dots\dots =$

3.  $\frac{5}{8} + \frac{1}{8} = \dots\dots\dots =$

4.  $\frac{2}{9} + \frac{6}{9} = \dots\dots\dots =$

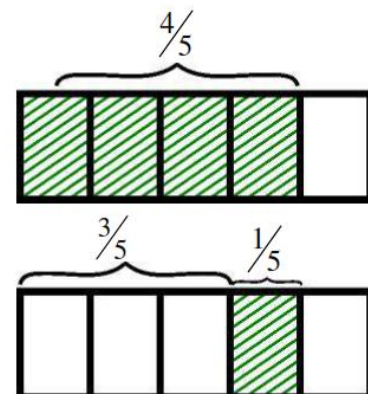
Let us now learn how to subtract such fractions:

A farmer planted  $\frac{4}{5}$  part of the farm

He then harvested  $\frac{3}{5}$  of it

So the part left with crops on it was  $\frac{1}{5}$

$$\frac{4}{5} - \frac{3}{5} = \frac{1}{5} \text{ or } \frac{4-3}{5}$$

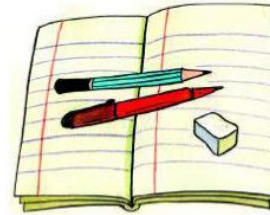


Hence we can say-

**To subtract fractions with same denominators we subtract the numerators and write it as the numerator and the denominator is written only once.**

**Subtract:**

1.  $\frac{2}{3} - \frac{1}{3} = \frac{2-1}{3} = \frac{1}{3}$
2.  $\frac{5}{8} - \frac{2}{8} = \dots\dots\dots = \dots\dots\dots$
3.  $\frac{4}{7} - \frac{3}{7} = \dots\dots\dots = \dots\dots\dots$
4.  $\frac{6}{13} - \frac{2}{13} = \dots\dots\dots = \dots\dots\dots$
5.  $\frac{7}{10} - \frac{3}{10} = \dots\dots\dots = \dots\dots\dots$



**Addition of fractions with the different denominator**

$$\frac{1}{3} + \frac{1}{4} = ?$$



Here denominator of both the fractions are different. We have added fractions with same denominators, so let us try to make the denominators of  $\frac{1}{3}$  and  $\frac{1}{4}$  the same. This can be done by obtaining equivalent fractions of both these fractions.

Equivalent fractions of  $\frac{1}{3}$  are  $\frac{2}{6}, \frac{3}{9}, \frac{4}{12}, \frac{5}{15}, \frac{6}{18} \dots\dots\dots$

Equivalent fractions of  $\frac{1}{4}$  are  $\frac{2}{8}, \frac{3}{12}, \frac{4}{16}, \frac{5}{20}, \frac{6}{24} \dots\dots\dots$

We see that the equivalent fraction  $\frac{4}{12}$  of  $\frac{1}{3}$  has same denomi-



nator as equivalent fraction  $\frac{3}{12}$  of  $\frac{1}{4}$

$$\text{So } \frac{1}{3} + \frac{1}{4} = \frac{4}{12} + \frac{3}{12}$$

Now these can be added as before  $\frac{1}{3} + \frac{1}{4} = \frac{4}{12} + \frac{3}{12}$

$$\frac{4+3}{12} = \frac{7}{12}$$

$$\text{So } \frac{1}{3} + \frac{1}{4} = \frac{7}{12}$$

**Let us understand again-**

$$\frac{1}{5} + \frac{1}{2} = ?$$



The denominators are not same. So we need to find equivalent fractions of  $\frac{1}{5}$  and  $\frac{1}{2}$  with same denominators:

Equivalent fractions of  $\frac{1}{5} = \frac{2}{10}, \frac{3}{15}, \frac{4}{20}, \frac{5}{25}, \dots$

Equivalent fractions of  $\frac{1}{2} = \frac{2}{4}, \frac{3}{6}, \frac{4}{8}, \frac{5}{10}, \frac{6}{12}, \dots$



Out of these the fractions with same denominator are  $\frac{2}{10}$  and  $\frac{5}{10}$ .

$$\text{Therefore } \frac{1}{5} + \frac{1}{2} = \frac{2}{10} + \frac{5}{10} = \frac{2+5}{10} = \frac{7}{10}$$

$$\text{Hence } \frac{1}{5} + \frac{1}{2} = \frac{7}{10}$$

**Now do this exercise:**

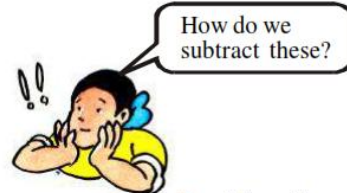
- |                                |                                |                                |
|--------------------------------|--------------------------------|--------------------------------|
| 1. $\frac{3}{5} + \frac{1}{4}$ | 2. $\frac{1}{2} + \frac{1}{3}$ | 3. $\frac{1}{5} + \frac{1}{6}$ |
| 4. $\frac{3}{4} + \frac{2}{8}$ | 5. $\frac{3}{7} + \frac{1}{3}$ | 6. $\frac{6}{7} + \frac{7}{8}$ |

### Subtraction of fractions with different denominators.

You have learnt how to add fractions with different denominators. Now see some examples of how to subtract fractions with different denominators.

#### Example:

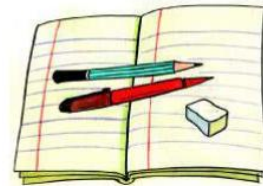
$$\frac{2}{3} - \frac{1}{4} = ?$$



To find fractions with same denominator, we will have to write equivalent fractions.

Equivalent fractions of  $\frac{2}{3}$  are  $\frac{4}{6}, \frac{6}{9}, \frac{8}{12}, \frac{10}{15}, \frac{12}{18}, \dots$

Equivalent fractions of  $\frac{1}{4}$  are  $\frac{2}{8}, \frac{3}{12}, \frac{4}{16}, \frac{5}{20}, \frac{6}{24}, \dots$



The fractions with same denominator are  $\frac{8}{12}$  and  $\frac{3}{12}$

$$\begin{aligned} \text{So } \frac{2}{3} - \frac{1}{4} &= \frac{8}{12} - \frac{3}{12} \\ &= \frac{8-3}{12} = \frac{5}{12} \\ \therefore \frac{2}{3} - \frac{1}{4} &= \frac{5}{12} \end{aligned}$$



Now do these exercise:

- |                                |                                |                                |
|--------------------------------|--------------------------------|--------------------------------|
| 1. $\frac{2}{3} - \frac{1}{6}$ | 2. $\frac{1}{2} - \frac{1}{4}$ | 3. $\frac{1}{3} - \frac{1}{6}$ |
| 4. $\frac{4}{5} - \frac{1}{2}$ | 5. $\frac{6}{7} - \frac{2}{3}$ | 6. $\frac{4}{9} - \frac{1}{3}$ |

**Note :** - Addition and subtraction of the fractions can be done by finding the L.C.M. of denominators. Get it confirmed with your teacher.

### Multiplication of fractions:

#### Multiplication of fraction by a whole number :-

You have multiplied two whole numbers. Let us how to multiply a fraction by a whole number?



$$1. \quad \frac{2}{10} \times 3 = \frac{2}{10} + \frac{2}{10} + \frac{2}{10}$$

$$= \frac{2+2+2}{10} = \frac{6}{10}$$

**Can we write this as?**

$$\frac{2}{10} \times 3 = \frac{2 \times 3}{10} = \frac{6}{10}$$

$$2. \quad \frac{3}{16} \times 4 = \frac{3}{16} + \frac{3}{16} + \frac{3}{16} + \frac{3}{16}$$

$$= \frac{3+3+3+3}{16} = \frac{12}{16}$$

**Can we write this as?**

$$\frac{3}{16} \times 4 = \frac{3 \times 4}{16} = \frac{12}{16}$$



**Do the questions given below by both these methods. Are the answers same?**

$$\frac{2}{8} \times 3 = \frac{2}{8} + \text{---} + \text{---} =$$

$$\text{or } \frac{2 \times 3}{8} = \text{---} = ( \quad )$$

$$\frac{3}{14} \times 2 = \frac{3}{14} + \text{---} =$$

$$\text{or } \frac{3 \times 2}{14} = \text{---} = ( \quad )$$

$$\frac{5}{21} \times 4 = \frac{5}{21} + \text{---} + \text{---} + \text{---} =$$

$$\text{or } \frac{5 \times 4}{21} = \text{---} = ( \quad )$$

$$\frac{3}{9} \times 2 = \text{---} =$$

$$\text{or } \text{---} = ( \quad )$$

### **Multiplying a fraction by a fraction -**

The sums you did above have a fraction as a multiplicand and a whole number as a multiplier. If both these were fractions, how would you multiply? Let us understand -

**Solve :-**  $\frac{1}{2} \times \frac{1}{3}$

We can say these as  $\frac{1}{3}$  of  $\frac{1}{2}$ .

Try to remember that what did you do when you wanted to get  $\frac{1}{3}$  of one.

By the same way we will get  $\frac{1}{3}$  of  $\frac{1}{2}$ .

First of all divide one unit into two equal parts. Each part shows  $\frac{1}{2}$  of 1 unit.

Dark any one part.



Now, we will find its  $\frac{1}{3}$  part. Mark 3 equal parts of the darkened part. Each part shows  $\frac{1}{3}$  of  $\frac{1}{2}$ .



Now put colours on any one of the darkened portion.

It is  $\frac{1}{2} \times \frac{1}{3}$



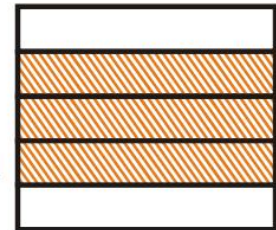
But each part is  $\frac{1}{6}$  of the whole

$$\therefore \frac{1}{2} \times \frac{1}{3} = \frac{1}{6}$$

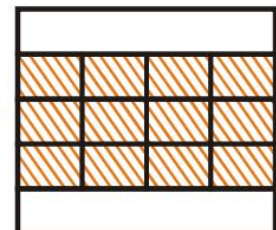


**Take one more example-**

Shade  $\frac{3}{5}$  th part of one whole.



Then to obtain  $\frac{2}{4}$  th part of this we divide it into 4 equal parts. Each part shows  $\frac{1}{4}$  of  $\frac{3}{5}$ .



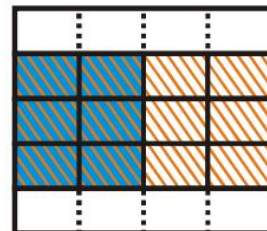
We need two such parts to get  $\frac{2}{4}$  of  $\frac{3}{5}$ . So those two parts represent  $\frac{2}{4} \times \frac{3}{5}$

But the whole is divided into 20 parts  $\frac{3}{5}$  and we have taken 6 parts out of those. So the shaded parts represents  $\frac{6}{20}$  of the whole.

$$\text{Hence } \frac{3}{5} \times \frac{2}{4} = \frac{6}{20}$$

Yes, so, this is same as

$$\frac{3}{5} \times \frac{2}{4} = \frac{3 \times 2}{5 \times 4} = \frac{6}{20}$$



*So, when two fractions are multiplied the resulting fraction is obtained by multiplying the respective numerators and the respective denominators. This resulting fraction is the product of the two given fractions.*

**Solve these:**

1.  $\frac{3}{7} \times \frac{2}{3}$

Product of numerators  $3 \times 2 = 6$   
Product of denominators  $7 \times 3 = 21$

Write 6 as the numerator and 21 as denominator so we get  $\frac{6}{21}$ .

$$\therefore \frac{3}{7} \times \frac{2}{3} = \frac{6}{21}$$

2.  $\frac{4}{5} \times \frac{3}{4} = \frac{4 \times 3}{5 \times 4} = \frac{12}{20}$

**Now you try these:**

1.  $\frac{3}{4} \times \frac{1}{5}$

2.  $\frac{2}{5} \times \frac{6}{7}$

3.  $\frac{1}{2} \times \frac{2}{9}$

4.  $\frac{2}{9} \times 5$

5.  $5 \times \frac{2}{9}$

6.  $\frac{10}{11} \times \frac{3}{8}$

**Division of fractions-**

Some questions related to division have been solved below try to understand them:

$6 \div 3 = ?$  means we have to divide 6 in group of 3. (or we see how many 3's are there in 6 ?) Let us see-





There are two group of 3 in 6  $\therefore 6 \div 3 = 2$

$6 \div 2 = ?$  means how many group of 2 are there in 6 ?



There are three group of 2 in 6 hence  $\therefore 6 \div 2 = 3$

$6 \div 1 = ?$  means how many ones can you take from 6 ?



We have 6 ones  $\therefore 6 \div 1 = 6$

Now let us see what we mean when we have  $6 \div \frac{1}{2} = ?$

$6 \div \frac{1}{2}$  means how many  $\frac{1}{2}$  are there in 6 ?



There are 12 pieces, each piece is  $\frac{1}{2}$

$$\therefore 6 \div \frac{1}{2} = 12$$

Or in other words one item has 2 halves

So 6 items have  $6 \times 2 = 12$  halves

$$\therefore 6 \div \frac{1}{2} = 12 \quad (= 6 \times 2)$$



Do we get the same result shown above when the division is a fraction? Let us find out-

$$6 \div \frac{1}{3} = ?$$

How many  $\frac{1}{3}$  are there in 6?



There are 18,  $\frac{1}{3}$  in 6

$$\therefore 6 \div \frac{1}{3} = 18 \quad \therefore 6 \times \frac{3}{1} = 18$$

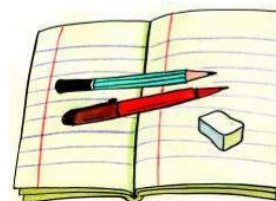
$$\therefore 6 \div \frac{1}{3} = 6 \times \frac{3}{1} = \frac{6 \times 3}{1} = 18$$

*So when you want to divide a fraction, write the numerator of divisor as denominator and denominator as numerator. (reciprocal) and multiply with the dividend.*

Understand this further-

**Example 4 :** Solve  $9 \div \frac{1}{2}$

**Solution :**  $9 \div \frac{1}{2} = \frac{9 \times 2}{1} = \frac{18}{1}$



**Example 5 :** Solve  $\frac{2}{3} \div \frac{3}{5}$

**Solution :**  $\frac{2}{3} \div \frac{3}{5} = \frac{2}{3} \times \frac{5}{3}$  [By interchanging the numerator and denominator of divisor and further multiplying it through dividend.]

$$= \frac{2 \times 5}{3 \times 3}$$

$$= \frac{10}{9}$$

Hence  $\frac{2}{3} \div \frac{3}{5} = \frac{10}{9}$

## Maths - 5

Now solve the questions given below :

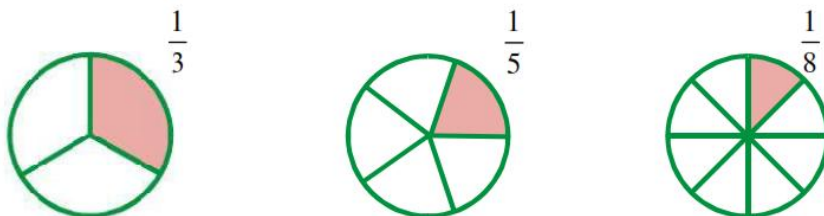
1.  $\frac{4}{6} \div 2$
2.  $6 \div \frac{1}{2}$
2.  $8 \div \frac{3}{4}$
4.  $\frac{3}{4} \div 6$
5.  $\frac{2}{5} \div \frac{3}{9}$
6.  $5 \div \frac{4}{5}$

### Statement sums

1. Raju plucked two papayas. One of them weighed  $\frac{1}{4}$  kg. and the other weighed  $\frac{1}{2}$  kg, so what is their total weight?
2. Ritesh drank  $\frac{1}{3}$  litre of milk daily and Seema drank  $\frac{1}{4}$  litre of milk. So how many litres of milk did they consume?
3. Ajay daily jogs  $\frac{2}{5}$  km. and Sheelu jogs  $\frac{1}{3}$  km. How many km. more than Ajay does Sheelu jog?
4. If a rectangular tile has  $\frac{3}{5}$  metre as the length and  $\frac{1}{2}$  metre as its breadth, What is its area? (Area of a rectangle = length  $\times$  breadth)
5. Sarita had  $\frac{8}{10}$  kg. of sweet. She gave  $\frac{1}{2}$  of this to Radha. How many kg. of sweet is left for ?

### Comparing fractions-

Look at these pictures given below:



These three circles are of the same size.

First circle has been divided into 3 equal parts.

$$\text{Each part} = \frac{1}{3}$$

Second circle has been divided into 5 equal parts

$$\text{Each part} = \frac{1}{5}$$

Third circle has been divided into 8 equal parts  $= \frac{1}{8}$

The total parts of the first circle is less.

So the size of the parts of this circle are bigger than the other two.

$$\text{Or } \frac{1}{3} > \frac{1}{8} \text{ similarly } \frac{1}{5} > \frac{1}{8}$$

**If the numerator of the fractions is same then the fraction with a smaller denominator is bigger, and the fraction with a bigger denominator is smaller.**

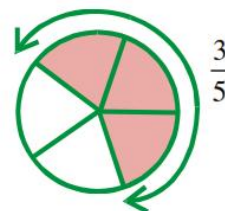
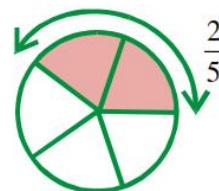
Which of the fractions  $\frac{2}{5}$  or  $\frac{3}{5}$  is bigger?

$\frac{2}{5}$  means 2 parts of the 5 equal parts

$\frac{3}{5}$  Means 3 parts of the 5 equal parts

So obviously 3 parts are more than 2

$$\therefore \frac{3}{5} > \frac{2}{5}$$



**Now write the fraction for the following:**



Arrange the fractions in an increasing order.

Are the numerators of these fractions the same?

Are the denominator of these fractions the same?

When the denominators are same, the fractions with bigger numerators are bigger or smaller?

When the denominators are same, the fractions with smaller numerators are bigger or smaller?

**If the denominators of the fractions are same, the ones with bigger numerators is big.**

Fill the blanks with <, > :-

1.  $\frac{3}{7}$  -----  $\frac{6}{7}$

2.  $\frac{3}{5}$  -----  $\frac{3}{9}$

3.  $\frac{4}{5}$  -----  $\frac{2}{5}$

4.  $\frac{20}{29}$  -----  $\frac{2}{29}$

5.  $\frac{5}{13}$  -----  $\frac{5}{8}$

6.  $\frac{4}{9}$  -----  $\frac{4}{15}$

7.  $\frac{11}{17}$  -----  $\frac{12}{17}$

8.  $\frac{3}{8}$  -----  $\frac{5}{8}$

Write the following fractions in an ascending (increasing) order -

1.  $\frac{1}{4}, \frac{3}{4}, \frac{2}{4}, \frac{4}{4}$

2.  $\frac{3}{5}, \frac{1}{5}, \frac{2}{5}, \frac{4}{5}$

3.  $\frac{5}{11}, \frac{7}{11}, \frac{4}{11}, \frac{8}{11}$



4.  $\frac{3}{8}, \frac{3}{5}, \frac{3}{16}, \frac{3}{14}$  .....
5.  $\frac{8}{9}, \frac{5}{9}, \frac{7}{9}, \frac{4}{9}$  .....
6.  $\frac{1}{2}, \frac{1}{10}, \frac{1}{8}, \frac{1}{9}$  .....

**Write the following fractions in the descending (decreasing) order:**

1.  $\frac{7}{10}, \frac{5}{10}, \frac{1}{10}, \frac{9}{10}$  .....
2.  $\frac{2}{7}, \frac{2}{25}, \frac{2}{13}, \frac{2}{17}$  .....
3.  $\frac{4}{7}, \frac{6}{7}, \frac{5}{7}, \frac{1}{7}$  .....
4.  $\frac{3}{6}, \frac{5}{6}, \frac{1}{6}, \frac{2}{6}$  .....
5.  $\frac{6}{9}, \frac{6}{14}, \frac{6}{13}, \frac{6}{7}$  .....
6.  $\frac{3}{14}, \frac{3}{19}, \frac{3}{25}, \frac{3}{16}$  .....

**To be able to compare two fractions, we need to have either equal numerators or equal denominators. If we get two fractions which have different numerators and denominators what would we do?**

Let us see whether  $\frac{2}{3}$  is bigger or smaller than  $\frac{4}{5}$

Since both the numerators and denominators are different we shall try to find equivalent fractions of both and see whether we can get one with same denominators.

Equivalent fractions of  $\frac{2}{3}$  are  $\frac{4}{6}, \frac{6}{9}, \frac{8}{12}, \frac{10}{15}, \frac{12}{18}, \dots$

Equivalent fractions of  $\frac{4}{5}$  are  $\frac{8}{10}, \frac{12}{15}, \frac{16}{20}, \frac{20}{25}, \frac{24}{30}, \dots$

The equivalent fractions of  $\frac{2}{3}$  and  $\frac{4}{5}$  with same denominators are  $\frac{10}{15}$  and  $\frac{12}{15}$  respectively.

$$\therefore 12 > 10$$

$$\therefore \frac{12}{15} > \frac{10}{15}$$

$$\therefore \frac{4}{5} > \frac{2}{3}$$

$$\therefore \frac{12}{15} = \frac{4}{5} \text{ and } \frac{10}{15} = \frac{2}{3}$$



Encircle the smaller fraction:

1.  $\frac{1}{2}$  and  $\frac{2}{3}$       2.  $\frac{3}{4}$  and  $\frac{1}{3}$

3.  $\frac{5}{6}$  and  $\frac{7}{8}$       4.  $\frac{1}{4}$  and  $\frac{6}{7}$

5.  $\frac{4}{5}$  and  $\frac{5}{6}$

**To write the fractions with different denominators in an ascending (increasing) or (descending) decreasing order.**

Write the following fractions in ascending and descending order-

$$\frac{2}{3}, \frac{3}{4}, \frac{1}{3} \text{ and } \frac{5}{6}$$

The denominators are different. Hence write the equivalent fractions of all the given fractions.

$$\text{Equivalent fractions of } \frac{2}{3} = \frac{4}{6}, \frac{6}{9}, \frac{8}{12}, \frac{10}{15}, \frac{12}{18}, \frac{14}{21}, \dots$$

$$\text{Equivalent fractions of } \frac{3}{4} = \frac{6}{8}, \frac{9}{12}, \frac{12}{16}, \frac{15}{20}, \frac{18}{24}, \dots$$

$$\text{Equivalent fractions of } \frac{1}{3} = \frac{2}{6}, \frac{3}{9}, \frac{4}{12}, \frac{5}{15}, \frac{6}{18}, \dots$$

$$\text{Equivalent fractions of } \frac{5}{6} = \frac{10}{12}, \frac{15}{18}, \frac{20}{24}, \frac{25}{30}, \dots$$

The equivalent fraction with same denominator = 12

Therefore, the equivalent fractions of  $\frac{2}{3}, \frac{3}{4}, \frac{1}{3}$  and  $\frac{5}{6}$  are  $\frac{8}{12}, \frac{9}{12}, \frac{4}{12}, \frac{10}{12}$ . If we arrange the numerators in an ascending order we would have-

$$\therefore 4 < 8 < 9 < 10$$

$$\therefore \frac{4}{12} < \frac{8}{12} < \frac{9}{12} < \frac{10}{12}$$

$$\text{or } \frac{1}{3} < \frac{2}{3} < \frac{3}{4} < \frac{5}{6}$$

And if we write them in the descending order we would have-

$$\therefore 10 > 9 > 8 > 4$$

$$\therefore \frac{10}{12} > \frac{9}{12} > \frac{8}{12} > \frac{4}{12}$$

$$\therefore \frac{5}{6} > \frac{3}{4} > \frac{2}{3} > \frac{1}{3}$$



Now write the given fractions in an ascending and descending order:

$$1. \quad \frac{1}{2}, \frac{3}{4}, \frac{3}{8}, \frac{1}{4} \text{ -----} \quad 2. \quad \frac{5}{6}, \frac{1}{3}, \frac{3}{4}, \frac{3}{8} \text{ -----}$$

$$3. \quad \frac{2}{9}, \frac{1}{2}, \frac{2}{3}, \frac{4}{6} \text{ -----} \quad 4. \quad \frac{2}{5}, \frac{3}{6}, \frac{1}{3}, \frac{3}{10} \text{ -----}$$

$$5. \quad \frac{1}{2}, \frac{4}{5}, \frac{3}{4}, \frac{7}{10} \text{ -----}$$

**Types of fraction-** Encircle the fractions whose numerator is less than the denominator:

$$1. \quad \frac{1}{2}, \frac{5}{6}, \frac{7}{2}, \frac{4}{9}, \frac{10}{3}, \frac{8}{5}, \frac{10}{10}, \frac{3}{4} \quad 2. \quad \frac{9}{4}, \frac{5}{7}, \frac{2}{5}, \frac{11}{8}, \frac{7}{4}, \frac{6}{15}$$

Write down the fractions you have encircled.

.....  
 .....

These are called proper fractions.

What is the speciality of these fractions?

.....  
 .....  
 .....

## Maths - 5

The fractions which have numerators which are smaller than their denominators are called proper fractions or the denominator of a proper fraction is bigger than their numerators.

The fractions which were left out in the above lists are called improper fractions. What is the speciality of improper fractions?

.....

.....

Those fractions whose numerators are bigger than their denominators are called improper fractions or the denominators of improper fractions are smaller than their numerators.

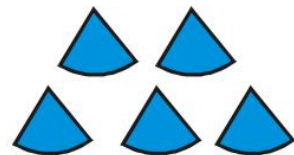
Now let us think about the improper fraction  $\frac{7}{5}$ .

5 is the denominator and 7 is the numerator of  $\frac{7}{5}$ .

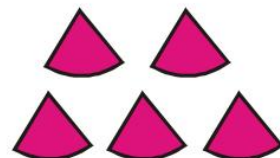
It means one whole is divided in 5 equal parts, similar 7 parts are the  $\frac{7}{5}$  of that whole. Here it is important to know that we had only 5 parts then how we will get 7 parts?

**Let us understand this :-**


One whole is divided into 5 equal parts. Out of these each part is  $\frac{1}{5}$  part of the whole.

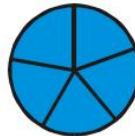


If the similar parts have been taken from another whole, that part will also be  $\frac{1}{5}$  part of the first whole.





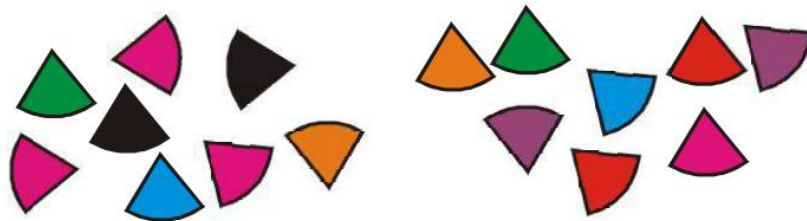
One part  is  $\frac{1}{5}$  of the whole



Another part  is  $\frac{1}{5}$  of the whole





Now imagine that we have collected several parts from different wholes.



Out of these each part is  $\frac{1}{5}$  of the whole



**Any two parts**

 ,  are  $\frac{2}{5}$  of the whole



**Any three parts**

 ,  ,  are  $\frac{3}{5}$  of the whole



**Any 5 parts**

     are  $\frac{5}{5}$  of the whole



**Any 7 parts**

       are  $\frac{7}{5}$  of the whole



**Similarly any 10 parts**

        are  $\frac{10}{5}$  of the whole



In the same way we can go further,

Think again about  $\frac{7}{5}$  and arrange all that seven parts on the unit circular portion of the given circle.



You can see, that  $\frac{7}{5}$  is equal to a complete whole and to  $\frac{2}{5}$ .

Therefore,  $\frac{7}{5} = 1 + \frac{2}{5}$  or

$$\frac{7}{5} = \frac{5+2}{5} = \frac{5}{5} + \frac{2}{5} = 1 + \frac{2}{5} = 1\frac{2}{5}$$

We can read  $1\frac{2}{5}$  as one whole two by five.

Similarly

$$\frac{5}{3} = \frac{3+2}{3} = \frac{3}{3} + \frac{2}{3}$$

$$\text{or } \frac{5}{3} = 1 + \frac{2}{3} \text{ or } 1\frac{2}{3}$$

Similarly

$$\frac{7}{2} = \frac{2+2+2+1}{2} = \frac{2}{2} + \frac{2}{2} + \frac{2}{2} + \frac{1}{2}$$

$$\text{or } \frac{7}{2} = 1+1+1+\frac{1}{2} = 3+\frac{1}{2} \text{ or } 3\frac{1}{2}$$

So you saw how improper fraction  $\frac{7}{5}$ ,  $\frac{5}{3}$  and  $\frac{7}{2}$  can be written as  $1\frac{2}{5}$ ,  $1\frac{2}{3}$  and  $3\frac{1}{2}$  respectively.

Out of these one is whole number and one is proper fraction. Such numbers are called mixed fractions.

**When we write an improper fraction as a combination of whole numbers and proper fractions. We call these as mixed fraction.**

We have seen how to write an improper fraction as a mixed fraction. If we were given a mixed fraction, how could this be written as an improper fraction?

Let us understand this with an example:

**Example : 5** Write the improper fraction of the mixed fraction  $1\frac{3}{5}$

**Solution :**  $1\frac{3}{5} = 1 + \frac{3}{5}$

Since the proper fraction here  $\frac{3}{5}$  has 5 as denominator we write 1 as  $\frac{5}{5}$

$$\begin{aligned} &= \frac{5}{5} + \frac{3}{5} \\ &= \frac{5+3}{5} = \frac{8}{5} \\ \therefore 1\frac{3}{5} &= \frac{8}{5} \end{aligned}$$

**Example : 6** Write the improper fraction of the mixed fraction  $3\frac{4}{9}$ .

**Solution :**  $3\frac{4}{9} = 3 + \frac{4}{9}$

Here the proper fraction has 9 as the denominator, so we will write the equivalent fraction of  $\frac{3}{1}$  which has 9 as denominator.

$$\begin{aligned} \therefore \frac{3}{1} &= \frac{3 \times 9}{1 \times 9} = \frac{27}{9} \\ \therefore 3\frac{4}{9} &= \frac{27+4}{9} \\ &= \frac{31}{9} \\ \therefore 3\frac{4}{9} &= \frac{31}{9} \end{aligned}$$

**Write the mixed fraction of the given improper fractions:**

- |                   |                   |
|-------------------|-------------------|
| 1. $\frac{10}{7}$ | 2. $\frac{10}{7}$ |
| 3. $\frac{13}{6}$ | 4. $\frac{8}{5}$  |
| 5. $\frac{9}{4}$  | 6. $\frac{7}{3}$  |

Represent the given mixed fractions pictorially:

1.  $1\frac{1}{3}$

2.  $2\frac{1}{2}$

3.  $1\frac{3}{4}$

4.  $2\frac{1}{5}$

5.  $3\frac{2}{3}$

6.  $1\frac{4}{5}$



Change the given mixed fractions to improper fractions-

1.  $1\frac{1}{3}$

2.  $1\frac{1}{2}$

3.  $4\frac{3}{4}$

4.  $5\frac{3}{7}$

5.  $2\frac{1}{5}$

6.  $3\frac{5}{6}$





## CHAPTER- 8

### Decimals

Write the place value of 1 in the given number.

12375 .....

21227 .....

20127 .....

22521 .....

**What did you observe?**

As the position of 1 moves to the right, the place value becomes a tenth part of the previous.

For example. The place value of 1 in the thousands place - 1000

The place value of 1 in the hundred place - 100

100 is tenth part of 1000. Similarly the place value of 1 in the tens place is 10 which is the tenth part of 100 and the 1 in the units place has a place value 1 which is the tenth part of 10.

Now think what would be the place value of 1 to the right of the ones place?

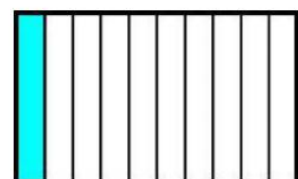
It would definitely be a tenth part of 1

**You know that if.**

One unit is represented as a box



One tenth of this would be the shaded portion as shown



We also know that this is represented as  $\frac{1}{10}$ .

So if we could write a 1 to the right of ones place, it would represent  $\frac{1}{10}$  th part.

Let us see what would happened when we write 1 to the right side of unit.

Thousand	Hundred	Tens	Ones	10th part	(One thousand one hundred eleven and one tenth)
1	1	1	1	1	

Would we be able to write such place value chart every time, when we write a number?

It would be difficult, wouldn't it?

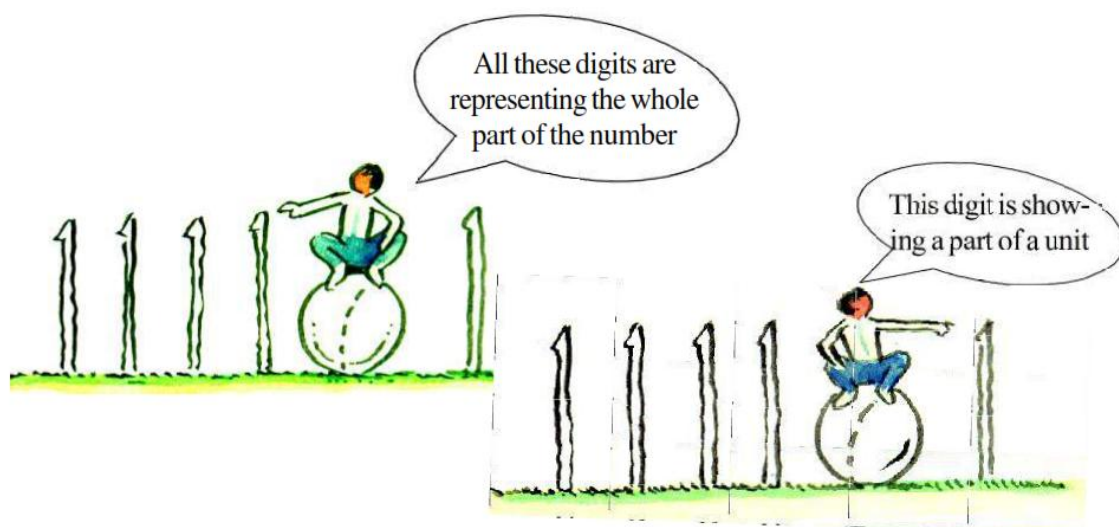
Let us write the number without the place value chart we will write. 11111

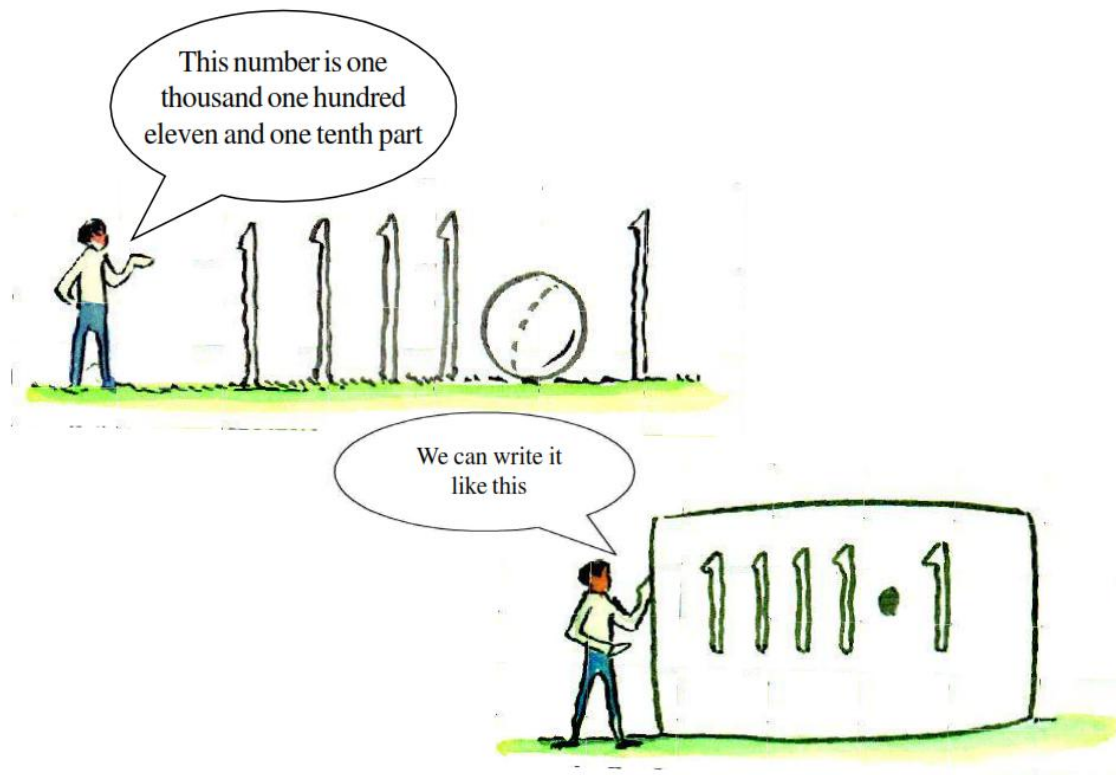
Now if we were to read this number what would we say?

Eleven thousand one hundred eleven, isn't it?

This is what would happen as every person knows that the digit to the extreme right represents ones digit.

Come, let us take the help of some one who would help anyone reading a number realise which is the ones digit? See what this great person is saying.





You can see that by putting a dot between the ones digit and the tenth part, we realise that to the left of this lies the ones, tens, hundreds.... position and to the other side lies the tenth part.

It is advisable to note here that the part which is to the left of the dot representing ones, tens, hundreds... position is actually a whole number and the tenth part is a part of a whole.

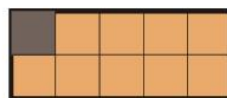
This shows that the dot separates the whole number from the part of a whole.

This dot is known as the decimal point.

You have also seen that the '1' which lies to the right of the decimal point is a tenth part of one



One unit



Shaded part . 1

Which is equal to  $\frac{1}{10}$

**.1** is read as 'point one'

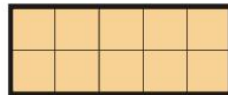
In the picture shown above one whole unit has been divided into 10 equal parts, out of which one is shaded and the remaining 9 are not.

Can you say what number each of these equal parts represent?

You are right, each of these represents .1 (point one) Now let us think of something new.

**.2** would represent how many part of a whole unit?

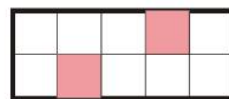
Consult your friends and shade .2 in the given unit.



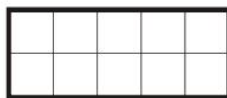
You are right,

**.2** represents 2 tenth parts of a unit.

The pictures given below all represent .2.



The units given below are all divided into ten equal parts shade each of them for the decimal part given below.



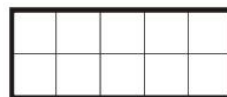
.1



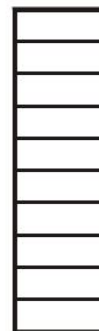
.2



.1



.3

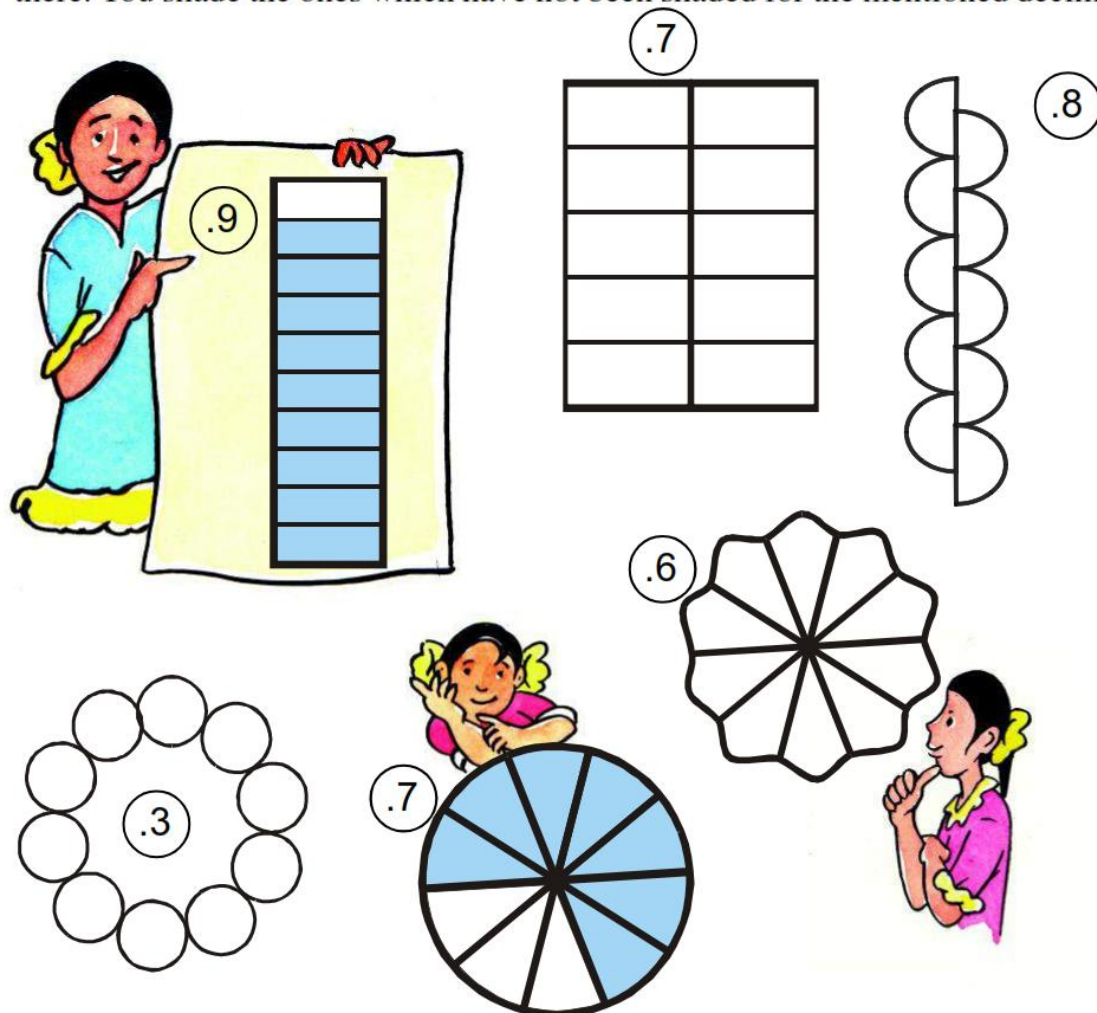


.2

Can you similarly represent .4, .5,... etc?



Some of the units given below have been shaded for the decimal part mentioned there. You shade the ones which have not been shaded for the mentioned decimal.

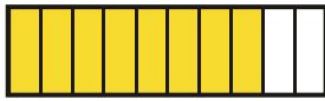


Here you have written the decimal representation using the decimal point for the mentioned number. You also know how to write these parts as a fraction.

Given below are some units whose parts are shaded, let us write the number in the form of decimal as well as a fraction:

Parts of a unit	Fraction	Decimal	What part of one
	$\frac{3}{10}$	$.3$	Three tenth parts
	$\frac{1}{10}$	$.1$	One tenth part

## Maths - 5



$$\frac{8}{10}$$

.8

Eight tenth parts



.....

.4

.....



$$\frac{7}{10}$$

.....

.....



.....

.....

.....



.....

.....

Ten tenth parts

### What after the tenth parts?

Observe the place value of the digits of the number 1.1.

1.1

→ One ones

→ One tenth part (a tenth part of unit)

If there were another 1 to the right of this tenth part, what would its place value be?

1.11

→ One ones

= 1

→ One tenth

= .1

→ One tenth of one tenth

= .01

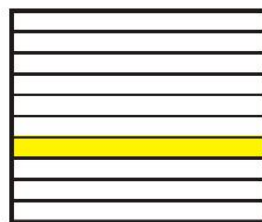
Tenth part of one tenth means hundredth part of a unit.

### Smaller parts of a unit.

Look at this pictures.



One unit



Tenth part

First picture shows a unit

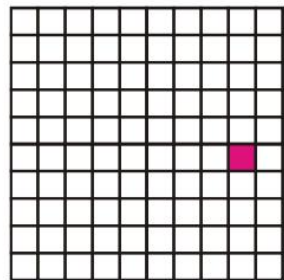
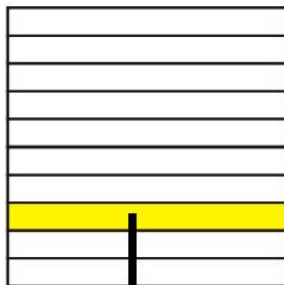
This unit has been divided into ten equal parts in the second picture. Each part as you know represents one tenth part.

In fraction we write this as  $\frac{1}{10}$  and in decimal as .1

Now, can we make smaller parts of  $\frac{1}{10}$  or .1

If you can, then how would we write these.

**Look at this picture**



This picture shows a complete unit. The coloured portion represents one tenth of the unit or tenth part of one.

This can be represented by  $\frac{1}{10}$  or .1.

If we divide  $\frac{1}{10}$  into ten equal part then the smallest part will be represented by .01 .

In the form of fraction  $\frac{1}{10}$  of  $\frac{1}{10}$  or  $\frac{1}{10} \times \frac{1}{10}$  or  $\frac{1}{100}$  .

Therefore part of one tenth = .01

$= \frac{1}{100}$  = hundredth part of unit (hundredth of unit)

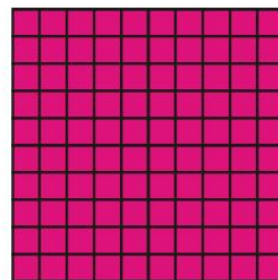
10  boxes =  (like a stripe)

$$\frac{1}{100} \times 10 = \frac{1}{10}$$



10 equal strips =

$$\frac{1}{10} \times 10 = 1$$



one unit

**See more numbers .**

Each small square represents .01 or  $\frac{1}{100}$

Let us see the value of the shaded parts

.01 = One hundredth part =  $\frac{1}{100}$

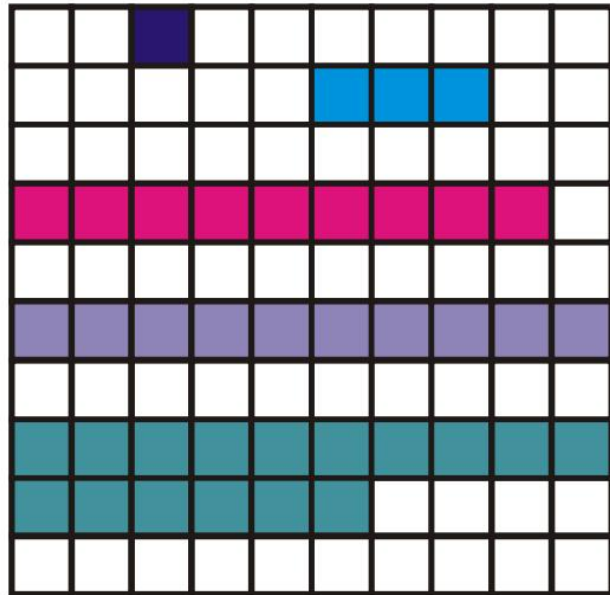
.03 = Three hundredth parts =  $\frac{3}{100}$

.09 = Nine hundredth parts =  $\frac{9}{100}$

.10 = Ten hundredth parts =  $\frac{10}{100}$

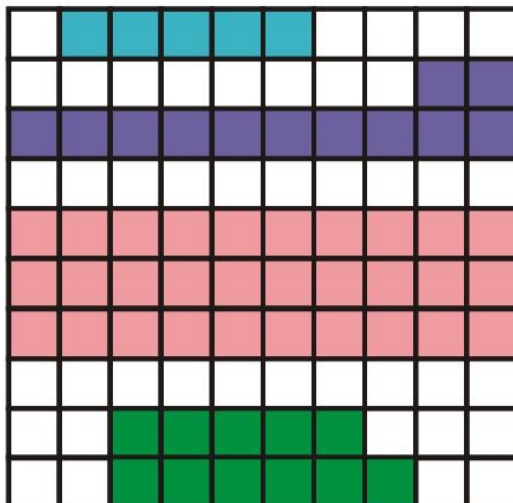
or one tenth part =  $\frac{1}{10}$

.16 = sixteen hundredth parts =  $\frac{16}{100}$



Or one tenth part and six hundredth part.

Now you write the value for the following coloured squares.



.05 = Five hundredth parts = .....

..... = Twelve hundredth parts = .....

.30 = ..... = .....

or = Three tenth parts = .....

..... = ..... =  $\frac{11}{100}$



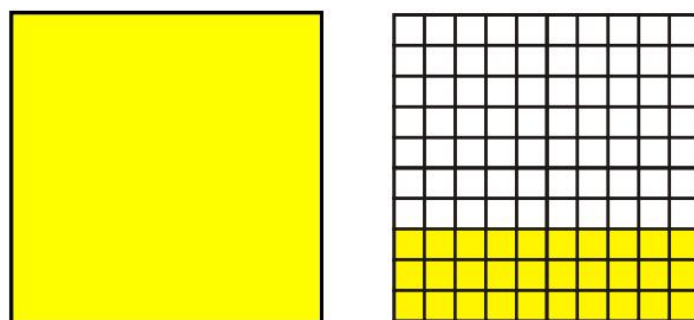
Complete the following table given below .

Decimal Numbers	Way of reading	Place value	Fraction from
.5	point five	5 tenth	$\frac{5}{10}$
.05	point zero five	.....	.....
.7	.....	.....	.....
.09	.....	.....	.....
.34	.....	3 tenth 4 hundredth	.....
.99	point nine.nine	.....	.....
.56	.....	.....	.....

### Decimal numbers greater than one .

The e×ample we have seen till now represents some part of 1. That's why these numbers are less than 1. Now let us see what is the meaning of numbers greater than 1, and how do we write it?

If small squares are there with a complete unit then how we will write it?

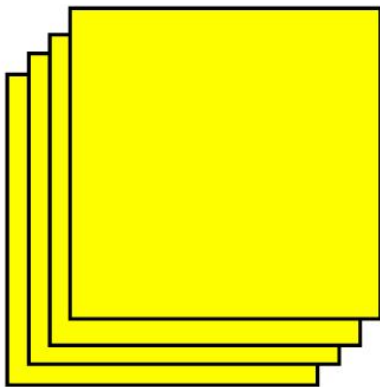


1 unit  
1

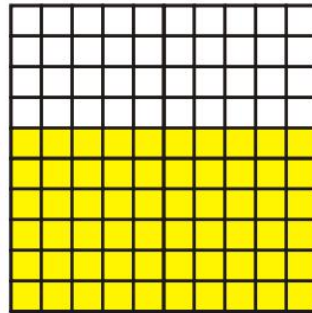
+  
+

three tenth parts  
.3

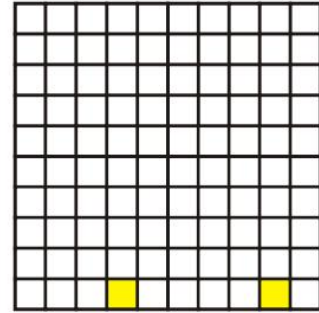
Adding these, we write it as 1.3.



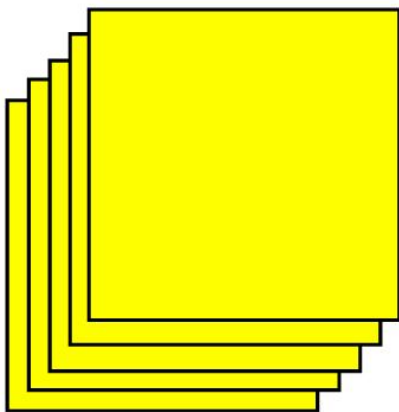
4 Units  
4



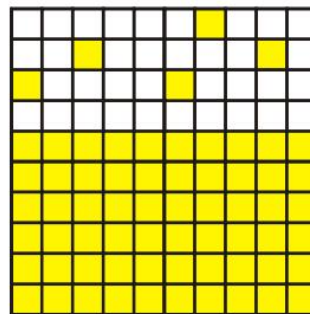
6 tenth parts  
.6



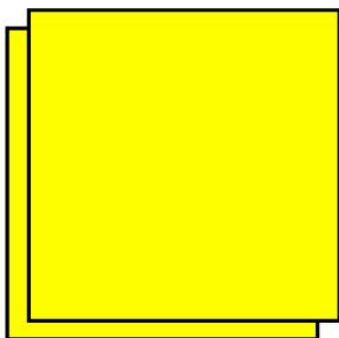
2 hundredth parts  
.02 = 4.62



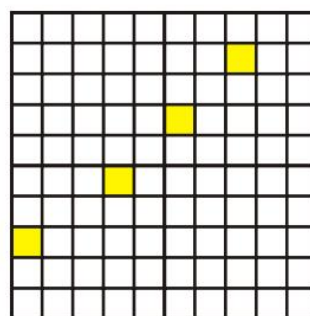
5 Units  
5



65 hundredth parts  
.65 = 5.65



2 Units  
2



4 hundredth parts  
.04 = 2.04

## Different ways of writing a number .

If you are asked to write twenty three, then you will write 23. Have you ever thought it can also be represented in a different way?

Let us talk about this .

As you know that 23 is a two digit number, in which there are 3 units and 2 tens. If you are asked that how many hundreds are in 23? Then you will say that there is no hundred in it or zero hundred. If we write .

023 (zero hundreds, 2 tens and 3 units)

Yet 023 represents 23. Similarly, 0023 (zero thousands, zero hundreds, two tens and three units) then also it is equal to 23. Now think if we write 230 in place of 23? You may think that it is “two hundred thirty”, because now zero is in units place, three is in tens and two is in hundreds place.

You are right, we can't write 230 in place of 23. Now think can we write it as 23.0?

There are 3 units, 2 tens and 0 tenths. It means it is equal to 23. Therefore, 23 can be written as 23.0. Similarly, it can also be written as 23.00 or 23.000.

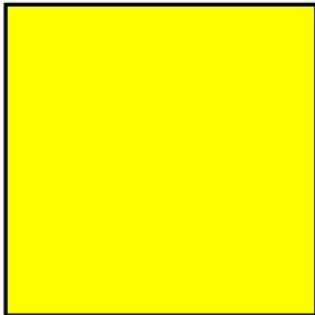
Some numbers are given below in different ways, look at them carefully.

Numbers	Numbers in different ways
2	02, 2.0, 2.00, 02.00 .....
12.5	12.5, 15.50, 12.500 .....
.7	0.7, .70, .700, 0.70 .....
.35	0.35, 00.35, 0.350, 0.3500 .....
.01	0.01, 0.010, 0.100 .....

Here we have seen how we can write zero before or after any number. We can do so when it is necessary. Further you will get some examples of it.

### Comparison of decimal numbers .

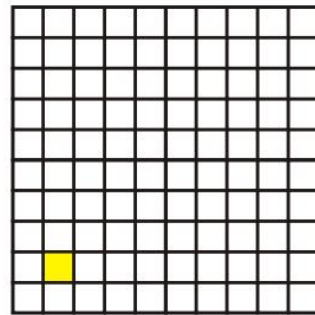
Write down the numbers represented by coloured portions, below the given figures .



.....



.....



.....

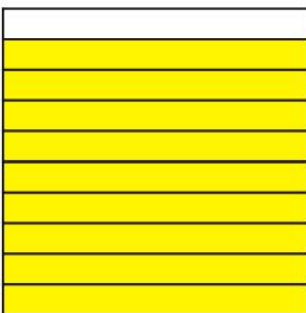
Out of these figures the first figure represents the whole unit, second represents the tenth part and the third represents the hundredth part of unit. Now we can write it in descending order as .

$$1 > 0.1 > 0.01$$

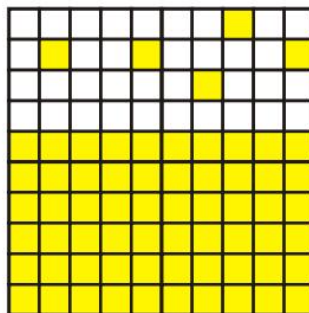
And in ascending order as .

$$0.01 < 0.1 < 1$$

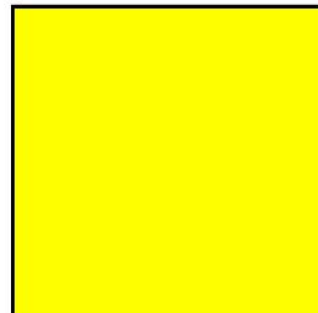
Now look at the following figures and write the numbers represented by them.



.....



.....



.....

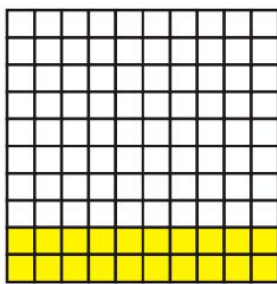
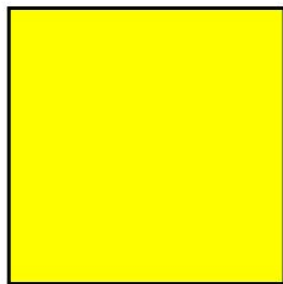
Write these numbers in ascending order . .....

Write these numbers in descending order . .....

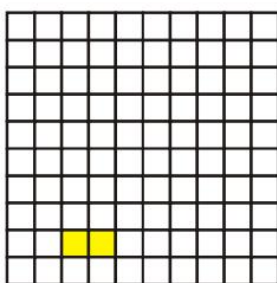
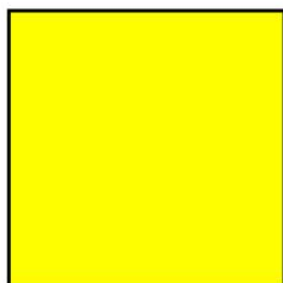


## Comparison of the number greater than one .

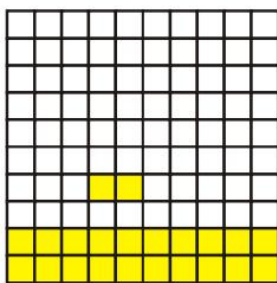
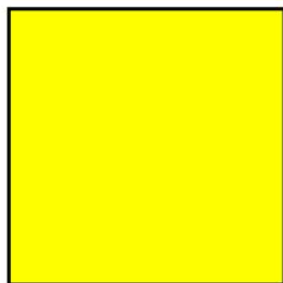
Write the numbers represented by the given figures and arrange them in ascending and descending order .



1.2 (or 1.20)



.....



.....

Numbers in ascending order - .....

Numbers in descending order - .....



### Exercise

Arrange in ascending order .

1. .2, .22, .02 .....
2. .03, .32, .03 .....
3. 1.3, .30, .03 .....
4. 2.5, 3.01, 2.99 .....

5. .04, .44, .14 .....

### Addition of decimals

**Example :** Anjana has participated in the marathon race on the sports day celebration in her school. She practices running 10.58 Kms. in the morning and 9.30 Kms. in the evening daily. How much does she run daily?

**Solutions :**  $10.58 + 9.30 = ?$

The addition of decimal numbers is same as the addition of whole numbers.

In 10.58, there are two digits after decimal. 5 is in tenth and 8 is in hundredth place. In 9.30, there is only a single digit after decimal that is 3 in tenth place and 0 in hundredth place.

$$\begin{array}{r} 10.58 \\ + 9.30 \\ \hline \end{array}$$

10.58 + 9.30 will be written in such a way that hundredth comes below hundredth, tenth comes below tenth and unit comes below unit.

The addition of decimal numbers is same as the addition of whole numbers.

$$\begin{array}{r} 10.58 \\ + 9.30 \\ \hline 19.88 \end{array}$$

**Answer :** Anjana runs 19.88 km daily.



### Exercise

**Add.**

1.  $\begin{array}{r} 23.11 \\ + 3.24 \\ \hline \end{array}$

2.  $\begin{array}{r} 41.25 \\ + 12.35 \\ \hline \end{array}$

3.  $\begin{array}{r} 0.1 \\ + 0.12 \\ \hline \end{array}$

4.  $\begin{array}{r} 17.01 \\ + 11.19 \\ \hline \end{array}$

5.  $\begin{array}{r} 6.78 \\ + 5.43 \\ \hline \end{array}$