

Lecture 15
10/11/19

CHAPTER-10

Stability of slope

① Stability of slope

→ Slopes for embankment are provided in road ways, rail ways, earthen dam, river training work (GHAT)

→ Slopes are of two types

1) Infinite slope

2) Finite slope

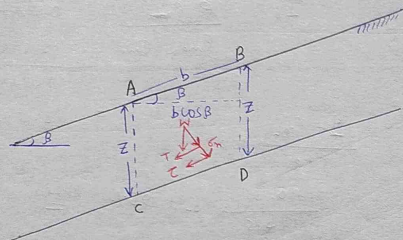
1) Infinite slope - If the slope represent the boundary surface of semi infinite soil mass then the properties of soil at all the similar depth below the surface will be same then the soil is termed as infinite slope.

→ Failure of infinite slope takes place due to sliding and failure surface is $\parallel$ (parallel) to ground slope surface

Stability Analysis of infinite slope

① Let AB represent infinite slope having slope angle of β with the Horizontal, failure of which takes place along critical sec CD which is $\parallel$ to ground slope surface and is at the depth of (z) below the surface. Consider unit

length of slope



For Wedge ABCD

- Area = $b \cos \beta \cdot z$
- Volume (V) = $A \cdot 1 = b \cos \beta \cdot z$
- Weight (W) = $V \cdot \gamma = (b \cos \beta \cdot z \cdot 1) \gamma = b \gamma z \cos \beta$
- Normal component of Wt (N) = $W \cos \beta = b \gamma z \cos \beta \cdot \cos \beta$
- Tangential component of Wt (T) = $W \sin \beta = b \gamma z \cos \beta \cdot \sin \beta$
- Normal stress (σ_n) = $\frac{N}{\text{Area}} = \frac{b \gamma z \cos^2 \beta}{b \cdot 1}$

$$\sigma_n = \gamma z \cos^2 \beta \quad \text{***}$$

- Tangential stress (τ) = $\frac{T}{\text{Area}} = \frac{b \gamma z \cos \beta \sin \beta}{(b \cdot 1)}$

$$\tau = \gamma z \cos \beta \sin \beta \quad \text{***}$$

Note ① If Water is present, then normal component of water pressure will be $\gamma_w z \cos^2 \beta$

Note ② Tangential stress will induce shear failure on the critical tech CD, which is being resisted by shear strength of soil

F.O.S = $\frac{\text{Shear strength on soil}}{\text{Shear stress on that plane}}$

$$F.O.S = \frac{S}{\tau} = \frac{c + \sigma_n \tan \phi}{\tau}$$

stability analysis for cohesionless soil ($c=0$)

Case ① Dry / Moist soil slope

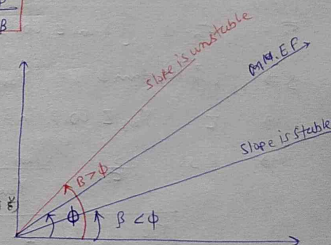
- Shear strength $S = c + \sigma_n \tan \phi = \sigma_n \tan \phi$
 $S = \gamma z \cos^2 \beta \cdot \tan \phi$
- Shear strength $\tau = \gamma z \cos \beta \sin \beta$
- F.O.S = $\frac{S}{\tau} = \frac{\gamma z \cos^2 \beta \tan \phi}{\gamma z \cos \beta \sin \beta} = \cot \beta \cdot \tan \phi$

$$F.O.S = \frac{\tan \phi}{\tan \beta}$$

- If $\beta < \phi \rightarrow F.O.S > 1$
(slope is stable)

- $\beta = \phi \rightarrow F.O.S = 1$
(slope is critical)
(असत संतुलन की अवस्था)

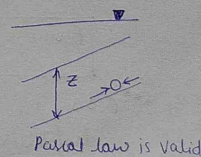
- $\beta > \phi \rightarrow F.O.S < 1$
(slope is unstable)



Case ② Submerge slope with no flow cond [G.W.T is above the h.L.]

- Shear strength $S = c + \sigma_n \tan \phi$
 $S = \gamma' z \cos^2 \beta \tan \phi$
- Shear stress $\tau = \gamma' z \cos \beta \sin \beta$
- F.O.S = $\frac{S}{\tau} = \frac{\gamma' z \cos^2 \beta \tan \phi}{\gamma' z \cos \beta \sin \beta} = \cot \beta \cdot \tan \phi$

$$F.O.S = \frac{\tan \phi}{\tan \beta}$$



Pascal law is valid

(Important moos)

Case ③ Submerge slope with steady seepage of height (h) above the critical sect

$$\gamma_{avg} = \frac{\gamma_s (Z-h) + \gamma_{sat} h}{Z}$$

$$\Rightarrow \sigma_n = \{ \gamma_s (Z-h) + \gamma_{sat} h \} \cos^2 \beta$$

$$= \gamma_{avg} \cdot Z \cdot \cos^2 \beta$$

$$u = \gamma_{wh} \cos^2 \beta$$

$$\sigma_n = \sigma_n - u = [(\gamma_{avg} Z \cos^2 \beta) - \gamma_{wh} \cos^2 \beta] = (\gamma_{avg} Z - \gamma_{wh}) \cos^2 \beta$$

$$S \Rightarrow \sigma_n \tan \phi = (\gamma_{avg} Z - \gamma_{wh}) \cos^2 \beta \cdot \tan \phi$$

$$\Rightarrow \tau = \gamma_{avg} Z \cos \beta \sin \beta$$

$$\Rightarrow F.O.S = \frac{S}{\tau} = \frac{(\gamma_{avg} Z - \gamma_{wh}) \cos^2 \beta \tan \phi}{\gamma_{avg} Z \cos \beta \sin \beta} = \left\{ \frac{\gamma_{avg} Z - \gamma_{wh}}{\gamma_{avg} Z} \right\} \frac{\tan \phi}{\tan \beta}$$

$$F.O.S = \left\{ 1 - \frac{\gamma_{wh}}{\gamma_{avg} Z} \right\} \frac{\tan \phi}{\tan \beta} \quad ***$$

Special case: If seepage takes place at h.L i.e (h=Z)

$$\Rightarrow \gamma_{avg} = \gamma_{sat}$$

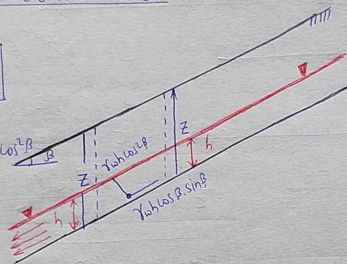
$$\Rightarrow S = (\gamma_{sat} Z - \gamma_{wh}) \cos^2 \beta \tan \phi = \gamma' Z \cos^2 \beta \tan \phi$$

$$\Rightarrow \tau = \gamma_{sat} Z \cos \beta \sin \beta = \underbrace{\gamma' Z \cos \beta \sin \beta}_{\text{Sub wt}} + \underbrace{\gamma_{wh} Z \cos \beta \sin \beta}_{\text{L due to seepage}}$$

$$\Rightarrow F.O.S = \frac{S}{\tau} = \frac{\gamma' Z \cos^2 \beta \tan \phi}{\gamma_{sat} Z \cos \beta \sin \beta}$$

$$F.O.S = \frac{\gamma' \tan \phi}{\gamma_{sat} \tan \beta} \quad *** = \frac{1 \tan \phi}{2 \tan \beta}$$

$\Rightarrow ***$ F.O.S is reduced to half in comparison to F.O.S of dry/moist / submerged slope. F.O.S should always be greater than 1



Stability Analysis for Cohesive soil

Case ① dry / moist soil slope

$$\# \text{ shear strength } S = c + \sigma_n \tan \phi = c + \sigma_n \tan \phi$$

$$S = c + \gamma Z \cos \beta \tan \phi$$

$$\# \text{ Shear stress } (\tau) = \gamma Z \cos \beta \sin \beta$$

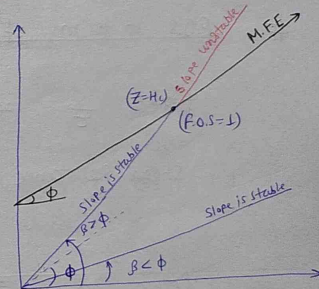
$$\# F.O.S = \frac{S}{\tau} = \frac{c + \gamma Z \cos^2 \beta \tan \phi}{\gamma Z \cos \beta \sin \beta} \quad (Z \text{ depth } \tau \text{ F.O.S depend on } Z)$$

$H_c \rightarrow$ critical depth

at $Z = H_c : F.O.S = 1$

$$F.O.S = \frac{c + \gamma H_c \cos^2 \beta \tan \phi}{\gamma H_c \cos \beta \sin \beta} = 1$$

$$\# \left[F.O.S = \frac{S}{\tau} \right] =$$



$$\gamma H_c \cos \beta \sin \beta = c + \gamma H_c \cos^2 \beta \tan \phi \text{ if } \beta < \phi \rightarrow \text{slope is stable}$$

$$(\gamma H_c \cos \beta \sin \beta - \gamma H_c \cos^2 \beta \tan \phi = c) \text{ if } \beta > \phi \rightarrow \text{slope is stable upto the depth of } (Z = H_c)$$

$$\gamma H_c \cos^2 \beta [\tan \beta - \tan \phi] = c$$

$$H_c = \frac{c}{\gamma \cos^2 \beta (\tan \beta - \tan \phi)}$$

If depth $Z > H_c$ then slope is unstable $\therefore (\tau > S)$

Taylor's Stability Number

$$\frac{c}{\gamma H_c} = \cos^2 \beta (\tan \beta - \tan \phi) = \text{unitless No.}$$

$$S_n = \frac{c}{\gamma H_c} \quad ***$$

F.O.S in terms of depth / height

1) If critical depth of slope is H_c and H is the depth of plan over which F.O.S is required then

$$F.O.S = \frac{H_c}{H} \quad ***$$

$$S_n = \frac{C}{\gamma H_c} = \frac{C}{\gamma (F.O.S) H} \quad ***$$

F.O.S in terms of mobilised shear stability

$$F.O.S = \frac{S}{C} = \frac{\text{Shear Strength}}{\text{Shear Resistance mobilized}}$$

$$\text{Shear Resistance mobilized} = \frac{S}{F.O.S} = \frac{C + \bar{\sigma}_n \tan \phi}{F.O.S}$$

$$= \frac{C}{F.O.S} + \frac{\bar{\sigma}_n \tan \phi}{F.O.S}$$

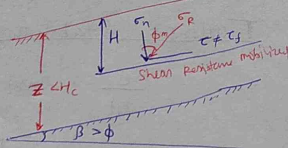
$$F.O.S = \frac{S}{C} = \frac{C + \bar{\sigma}_n \tan \phi}{C_m + \bar{\sigma}_n \tan \phi_m} \quad *$$

Mobilised cohesion

$$C_m = \frac{C}{F.O.S} \quad *$$

Mobilised friction angle

$$\tan \phi_m = \frac{\tan \phi}{F.O.S} \quad *$$



② Submerge slope with no flow

$$F.O.S = \frac{S}{C} = \frac{C + \bar{\sigma}_n \tan \phi}{C} = \frac{C + \gamma' Z \cos \beta \tan \phi}{\gamma' Z \cos \beta \sin \beta}$$

③ Submerge slope with steady seepage at G.L

$$S = C + \bar{\sigma}_n \tan \phi = C + \gamma' Z \cos \beta \tan \phi$$

$$C = \gamma' Z \cos \beta \sin \beta + \gamma_w Z \cos \beta \sin \beta$$

$$F.O.S = \frac{C + \gamma' Z \cos \beta \tan \phi}{\gamma_{sat} Z \cos \beta \sin \beta}$$

Note Unit wt used in stability No.

⇒ In submerged cond $\gamma = \gamma'$

⇒ In case of sudden drawdown $\gamma = \gamma_{sat}$ and w/friction angle is used to find stability No

$$\phi_m = \frac{\gamma'}{\gamma_{sat}} \times \phi$$

Swedish slip circle

Method of slices

- ① Slices & independent body
- ② forces b/w slices are neglected
- ③ Directional angle are used to locate critical circle
- ④ $F.O.S = \frac{\text{Resisting moment}}{\text{Rotating moment}}$

friction circle method

Radius of friction circle = $R \sin \phi$
cohesion is partially mobilised
and friction is fully utilized

Resultant Re_{an} makes angle ϕ with normal and tangential to friction circle.

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Solution- ⑧

$$C = 55 \text{ kN/m}^2$$

$$\phi = 0$$

$$\text{Radius of slip circle} = 19 \text{ m}$$

$$\text{wt of Wedge ABD} = 2050 \text{ kN}$$

$$\text{Distance of W from A is } 9 \text{ m}$$

$$\begin{aligned} \text{F.O.S. against sliding} &= \frac{M_R}{M_o} = \frac{C(L \times r)}{W \cdot g} \\ &= \frac{55(8 \cdot 0 \cdot r)}{W \cdot g} \\ &= \frac{55 \times [19 \cdot (\frac{64.5}{180}) \cdot 19]}{2050 \times 9} \\ &= 1.21 \text{ Ans} \end{aligned}$$

Solution ⑤

$$Z = 10 \text{ m}$$

$$\phi_0 = 15^\circ$$

$$C_0 = 12 \text{ kPa}$$

$$e = 1$$

$$G_{15} = 2.65$$

$$S_n = 0.08$$

F.O.S to cohesion

$$S_n = \frac{C}{\gamma H_c} = \frac{C}{\gamma(F.O.S)H}$$

$$0.08 = \frac{12}{\gamma(F.O.S) \times 10}$$

$$\gamma' =$$

Solution ⑥

$$0.126 = \frac{12}{\gamma_{sat} \times (F.O.S) \times 10}$$

Solution ⑩

$$H = ?$$

In soil ① at 5m

$$\begin{aligned} \tau &= \gamma z \cos \beta \sin \beta \\ &= 16 \times 5 \cos 25^\circ \sin 25^\circ \\ &= 30.6 \end{aligned}$$

$$\tau(30.6) < s(40) \text{ No failure in soil ①}$$

for failure in soil ②

$$s = \tau$$

$$60 = (\gamma H_1 + \gamma_2 x) \cos \beta \sin \beta$$

$$60 = (16 \times 5 + 20x) \cos 25^\circ \sin 25^\circ \quad x = 3.83 \text{ m}$$

depth 8.83 m

Solution ⑮

$$C = 15 \text{ kN/m}^2$$

$$e = 0.9$$

$$\phi = 20^\circ$$

$$G = 2.67$$

side slope is 1:1

$$\text{F.O.S} = ?$$

$$\gamma_{sat} = \frac{(G + e) \gamma_w}{1 + e}$$

$$S_n = \frac{C}{\gamma H_c} \quad \gamma_{sat} = \frac{(2.67 + 0.9)}{1 + 0.9}$$

$$S_n = \frac{C}{\gamma H_c} \quad \times 9.81 = 18.42$$

$$\phi_0 = \frac{\gamma'}{\gamma_{sat}} \phi = \left(\frac{18.42 - 9.81}{18.42} \right) 20^\circ = 9.35^\circ$$

$$S_n = 0.108 + \left(\frac{0.114 - 0.108}{12 - 6} \right) \times (3.35 - 6)$$

$$S_n = \frac{C}{\gamma_{sat}(F.O.S)H} = 0.111$$

$$= \frac{15}{18.42 \times (F.O.S) \times 6} \quad \text{F.O.S} = 1.22 \text{ Ans}$$

