

Chapter 17. Pythagoras Theorem

Ex 17.1

Answer 1.

Base = 5cm, Hypotenuse = 13cm

By Pythagoras theorem,

$$(\text{perpendicular})^2 = (13\text{cm})^2 - (5\text{cm})^2$$

$$(\text{perpendicular})^2 = 169\text{cm}^2 - 25\text{cm}^2$$

$$(\text{perpendicular})^2 = 144\text{cm}^2$$

$$(\text{perpendicular})^2 = (12\text{cm})^2$$

$$\therefore \text{perpendicular} = 12\text{cm}$$

$$\text{Area of the triangle} = \frac{1}{2} \times (\text{Base} \times \text{Perpendicular})$$

$$= \frac{1}{2} \times 5\text{cm} \times 12\text{cm}$$

$$= 30\text{cm}^2$$

Answer 2.

The two sides (excluding hypotenuse) of a right - angled triangle are given as 24cm and 7cm

$$(\text{hypotenuse})^2 = (24\text{cm})^2 + (7\text{cm})^2$$

$$(\text{hypotenuse})^2 = 576\text{cm}^2 + 49\text{cm}^2$$

$$(\text{hypotenuse})^2 = 625\text{cm}^2$$

$$(\text{hypotenuse})^2 = (25\text{cm})^2$$

Thus, the length of the hypotenuse of the triangle is 25cm.

Answer 3.

Hypotenuse = 65cm

One side = 16cm

Let the other side be of length x cm

By Pythagoras theorem,

$$(65\text{cm})^2 = (16\text{cm})^2 + (x \text{ cm})^2$$

$$(x \text{ cm})^2 = 4225\text{cm}^2 - 256\text{cm}^2$$

$$= 3969\text{cm}^2$$

$$= (63\text{cm})^2$$

$$\Rightarrow x = 63\text{cm}$$

$$\text{Area of the triangle} = \frac{1}{2} \times (\text{Base} \times \text{Height})$$

$$= \frac{1}{2} \times 16\text{cm} \times 63\text{cm}$$

$$= 504\text{cm}^2$$

Answer 4.

Let O be the original position of the man.

From the figure, it is clear that B is the final position of the man.

$\triangle AOB$ is right – angled at A.

By Pythagoras theorem,

$$OB^2 = OA^2 + AB^2$$

$$OB^2 = (10\text{m})^2 + (24\text{m})^2$$

$$OB^2 = 100\text{m}^2 + 576\text{m}^2$$

$$OB^2 = 676\text{m}^2$$

$$OB^2 = (26\text{m})^2$$

$$OB = 26\text{m}$$

Thus, the man is at a distance of 26m from the starting point.

Answer 5.

Let AC be the ladder and A be the position of the window.

Then, $AC = 25\text{m}$, $AB = 20\text{m}$

Using Pythagoras theorem,

$$AC^2 = AB^2 + BC^2$$

$$\Rightarrow (25\text{m})^2 = (20\text{m})^2 + BC^2$$

$$\Rightarrow BC^2 = 625\text{m}^2 - 400\text{m}^2$$

$$BC^2 = 225\text{m}^2$$

$$BC^2 = (15\text{m})^2$$

$$\Rightarrow BC = 15\text{m}$$

Thus, the distance of the foot of the ladder from the building is 15m.

Answer 6.

Hypotenuse = p cm

One side = q cm

Let the length of the third side be x cm.

Using Pythagoras theorem,

$$x^2 = p^2 - q^2 = (p + q)(p - q)$$

$$= (p + q) \times 1 \quad [\because p - q = 1, \text{ given}]$$

$$= p + q$$

$$\therefore x = \sqrt{p + q}$$

Thus, the length of the third side of the triangle is $\sqrt{p + q}$ cm.

Answer 7.

Let O be the foot of the ladder. Let AO be the position of the ladder when it touches the window at A which is 9m high and CO be the position of the ladder when it touches the window at C which is 12m high.

Using Pythagoras theorem,

In $\triangle AOB$,

$$BO^2 = AO^2 - AB^2$$

$$BO^2 = (15\text{m})^2 - (9\text{m})^2$$

$$BO^2 = 225\text{m}^2 - 81\text{m}^2$$

$$BO^2 = 144\text{m}^2$$

$$BO^2 = (12\text{m})^2$$

$$BO = 12\text{m}$$

Using Pythagoras theorem in $\triangle COB$,

$$DO^2 = CO^2 - CD^2$$

$$DO^2 = (15\text{m})^2 - (12\text{m})^2$$

$$DO^2 = 225\text{m}^2 - 144\text{m}^2$$

$$DO^2 = 81\text{m}^2$$

$$DO = 9\text{m}$$

$$\text{Width of the street} = DO + BO = 9\text{m} + 12\text{m} = 21\text{m}$$

Answer 8.

Let AC be the ladder and A be the position of the window which is 8m above the ground.

Now, the ladder is shifted such that its foot is at point D which is 8m away from the wall.

$$\therefore BD = 8\text{m}$$

At this instance, the position of the ladder is DE.

$$\therefore AC = DE$$

Using Pythagoras theorem in $\triangle ABC$,

$$AC^2 = AB^2 + BC^2$$

$$= (8\text{m})^2 + (6\text{m})^2$$

$$= 64\text{m}^2 + 36\text{m}^2$$

$$= 100\text{m}^2$$

$$= (10\text{m})^2$$

$$\therefore AC = DE = 10\text{m}$$

Using Pythagoras theorem in $\triangle DBE$,

$$BE^2 = DE^2 - BD^2$$

$$\Rightarrow BE^2 = (10\text{m})^2 - (8\text{m})^2$$

$$= 100\text{m}^2 - 64\text{m}^2$$

$$= 36\text{m}^2$$

$$= (6\text{m})^2$$

$$\Rightarrow BE = 6\text{m}$$

Thus, the required height up to which the ladder reaches is 6m above the ground.

Answer 9.

Let AB and CD be the two poles of height 14m and 9m respectively.

It is given that $BD = 12\text{m}$

$$\therefore CE = 12\text{m}$$

Now, $AE = AB - BE$

$$= 14\text{m} - 9\text{m} = 5\text{m}$$

Using Pythagoras theorem in $\triangle ACE$,

$$AC^2 = AE^2 + CE^2$$

$$= (5\text{m})^2 + (12\text{m})^2$$

$$= 25\text{m}^2 + 144\text{m}^2$$

$$= 169\text{m}^2$$

$$= 13\text{m}^2$$

$$\Rightarrow AC = 13\text{m}$$

Thus, the distance between the tops of the poles is 13m

Answer 10.

It is given that the diagonals of a rhombus are of length 14cm and 10cm respectively

$$\therefore d_1 = 14\text{cm}, d_2 = 10\text{cm}$$

The diagonals of a rhombus bisect each other

$$\therefore \left(\frac{d_1}{2}\right)^2 + \left(\frac{d_2}{2}\right)^2 = \text{side}^2$$

$$\Rightarrow \text{side}^2 = 7^2 + 5^2 = 49 + 25 = 74$$

$$\Rightarrow \text{Side} = \sqrt{74}$$

Thus, each side of the rhombus is of length $\sqrt{74}$ cm

Answer 11.

Side of the rhombus = 10cm

One diagonal, $d_1 = 16$ cm

Let d_2 be the other diagonal of the rhombus

The diagonals of a rhombus bisect each other

$$\therefore \left(\frac{d_1}{2}\right)^2 + \left(\frac{d_2}{2}\right)^2 = \text{side}^2$$

$$8^2 + \left(\frac{d_2}{2}\right)^2 = 100$$

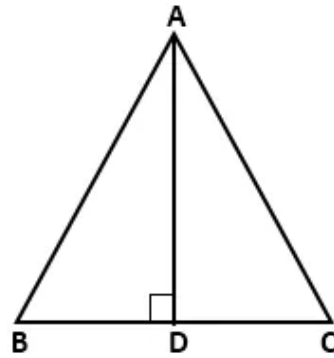
$$\Rightarrow \left(\frac{d_2}{2}\right)^2 = 100 - 64 = 36$$

$$\Rightarrow \frac{d_2}{2} = 6$$

$$\Rightarrow d_2 = 12$$

Thus, the other diagonal of the rhombus is of length 12cm

Answer 12.



Since triangles ABD and ACD are right triangles right-angled at D,

$$AB^2 = AD^2 + BD^2 \quad \dots(i)$$

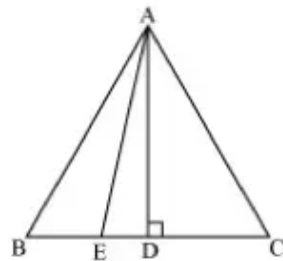
$$AC^2 = AD^2 + CD^2 \quad \dots(ii)$$

Subtracting (ii) from (i), we get

$$AB^2 - AC^2 = BD^2 - CD^2$$

$$\Rightarrow AB^2 + CD^2 = AC^2 + BD^2$$

Answer 13.



Let side of equilateral triangle be a . And AE be the altitude of $\triangle ABC$

$$\text{So, } BE = EC = \frac{BC}{2} = \frac{a}{2}$$

$$\text{And, } AE = \frac{a\sqrt{3}}{2}$$

$$\text{Given that } BD = \frac{1}{3}BC = \frac{a}{3}$$

$$\text{So, } DE = BD - BE = \frac{a}{2} - \frac{a}{3} = \frac{a}{6}$$

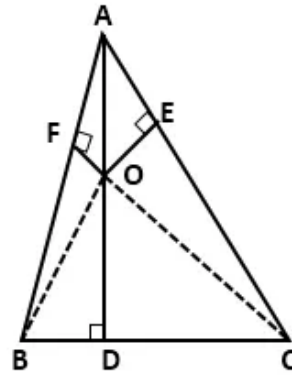
Now, in $\triangle ADE$ by applying Pythagoras theorem

$$AD^2 = AE^2 + DE^2$$

$$\begin{aligned} AD^2 &= \left(\frac{a\sqrt{3}}{2}\right)^2 + \left(\frac{a}{6}\right)^2 \\ &= \left(\frac{3a^2}{4}\right) + \left(\frac{a^2}{36}\right) = \frac{28a^2}{36} \end{aligned}$$

$$\text{Or, } 9 AD^2 = 7 AB^2.$$

Answer 14.



- a. In right triangles OFA, ODB and OEC, we have

$$OA^2 = AF^2 + OF^2$$

$$OB^2 = BD^2 + OD^2$$

$$OC^2 = CE^2 + OE^2$$

Adding all these results, we get

$$OA^2 + OB^2 + OC^2 = AF^2 + BD^2 + CE^2 + OF^2 + OD^2 + OE^2$$

$$\Rightarrow AF^2 + BD^2 + CE^2 = OA^2 + OB^2 + OC^2 - OD^2 - OE^2 - OF^2$$

- b. In right triangles ODB and ODC, we have

$$OB^2 = OD^2 + BD^2$$

$$OC^2 = OD^2 + CD^2$$

$$\therefore OB^2 - OC^2 = (OD^2 + BD^2) - (OD^2 + CD^2)$$

$$\Rightarrow OB^2 - OC^2 = BD^2 - CD^2 \quad \dots(i)$$

Similarly, we have

$$OC^2 - OA^2 = CE^2 - AE^2 \quad \dots(ii)$$

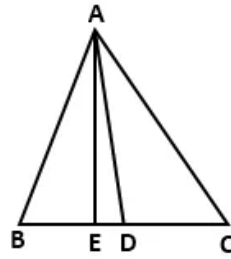
$$OA^2 - OB^2 = AF^2 - BF^2 \quad \dots(iii)$$

Adding (i), (ii) and (iii), we get

$$(OB^2 - OC^2) + (OC^2 - OA^2) + (OA^2 - OB^2) = (BD^2 - CD^2) + (CE^2 - AE^2) + (AF^2 - BF^2)$$

$$\Rightarrow (BD^2 + CE^2 + AF^2) - (AE^2 + CD^2 + BF^2) = 0$$

$$\Rightarrow AF^2 + BD^2 + CE^2 = AE^2 + CD^2 + BF^2$$

Answer 15.

We have $\angle AED = 90^\circ$,

$\therefore \angle ADE < 90^\circ$ and $\angle ADC > 90^\circ$

i.e. $\angle ADE$ is acute and $\angle ADC$ is obtuse.

a. In $\triangle ADC$, $\angle ADC$ is an obtuse angle.

$$\therefore AC^2 = AD^2 + DC^2 + 2 \times DC \times DE$$

$$\Rightarrow AC^2 = AD^2 + \left(\frac{1}{2}BC\right)^2 + 2 \times \frac{1}{2}BC \times DE$$

$$\Rightarrow AC^2 = AD^2 + \frac{1}{4}BC^2 + BC \times DE$$

$$\Rightarrow AC^2 = AD^2 + BC \times DE + \frac{1}{4}BC^2 \quad \dots (i)$$

b. In $\triangle ABD$, $\angle ADE$ is an acute angle.

$$\therefore AB^2 = AD^2 + BD^2 - 2 \times BD \times DE$$

$$\Rightarrow AB^2 = AD^2 + \left(\frac{1}{2}BC\right)^2 - 2 \times \frac{1}{2}BC \times DE$$

$$\Rightarrow AB^2 = AD^2 + \frac{1}{4}BC^2 - BC \times DE$$

$$\Rightarrow AB^2 = AD^2 - BC \times DE + \frac{1}{4}BC^2 \quad \dots (ii)$$

c. Adding (i) and (ii), we have

$$AC^2 + AB^2 = AD^2 + BC \times DE + \frac{1}{4}BC^2 + AD^2 - BC \times DE + \frac{1}{4}BC^2$$

$$\Rightarrow AB^2 + AC^2 = 2AD^2 + \frac{1}{2}BC^2 \quad \dots (iii)$$

d. Subtracting (ii) from (i), we have

$$AC^2 - AB^2 = AD^2 + BC \times DE + \frac{1}{4}BC^2 - AD^2 + BC \times DE - \frac{1}{4}BC^2$$

$$\Rightarrow AC^2 - AB^2 = 2BC \times DE$$

e. From (iii), we have

$$AB^2 + AC^2 = 2AD^2 + \frac{1}{2}BC^2$$

$$\Rightarrow AB^2 + AC^2 = 2AD^2 + \frac{1}{2}(2 \times CD)^2$$

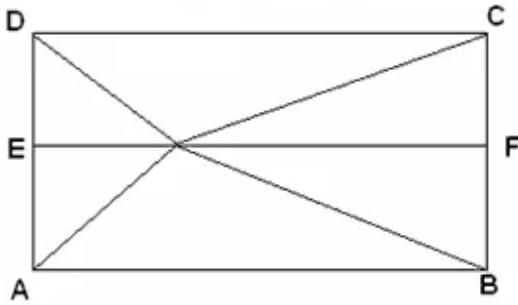
$$\Rightarrow AB^2 + AC^2 = 2AD^2 + \frac{1}{2} \times 4CD^2$$

$$\Rightarrow AB^2 + AC^2 = 2AD^2 + 2CD^2$$

$$\Rightarrow AB^2 + AC^2 = 2(AD^2 + CD^2)$$

Answer 16.

Let ABCD be the given rectangle and let O be a point within it.
Join OA, OB, OC and OD.



Through O, draw EOF \parallel AB. Then, ABFE is a rectangle.

In right triangles $\triangle OEA$ and $\triangle OFC$, we have

$$OA^2 = OE^2 + AE^2 \text{ and } OC^2 = OF^2 + CF^2$$

$$\Rightarrow OA^2 + OC^2 = (OE^2 + AE^2) + (OF^2 + CF^2)$$

$$\Rightarrow OA^2 + OC^2 = OE^2 + OF^2 + AE^2 + CF^2 \quad \dots\dots(i)$$

Now, in right triangles $\triangle OFB$ and $\triangle ODE$, we have

$$OB^2 = OF^2 + FB^2 \text{ and } OD^2 = OE^2 + DE^2$$

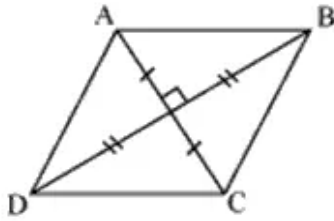
$$\Rightarrow OB^2 + OD^2 = (OF^2 + FB^2) + (OE^2 + DE^2)$$

$$\Rightarrow OB^2 + OD^2 = OE^2 + OF^2 + DE^2 + BF^2$$

$$\Rightarrow OB^2 + OD^2 = OE^2 + OF^2 + CF^2 + AE^2 \quad [\because DE = CF \text{ and } AE = BF] \dots\dots(ii)$$

From (i) and (ii), we get

$$OA^2 + OC^2 = OB^2 + OD^2$$

Answer 17.

In $\triangle AOB$, $\triangle BOC$, $\triangle COD$, $\triangle AOD$

Applying Pythagoras theorem

$$AB^2 = AO^2 + OB^2$$

$$BC^2 = BO^2 + OC^2$$

$$CD^2 = CO^2 + OD^2$$

$$AD^2 = AO^2 + OD^2$$

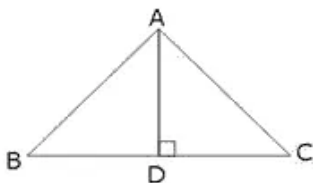
Adding all these equations,

$$AB^2 + BC^2 + CD^2 + AD^2 = 2(AO^2 + OB^2 + OC^2 + OD^2)$$

$$= 2\left(\left(\frac{AC}{2}\right)^2 + \left(\frac{BD}{2}\right)^2 + \left(\frac{AC}{2}\right)^2 + \left(\frac{BD}{2}\right)^2\right) \quad (\text{diagonals bisect each other.})$$

$$= 2\left(\frac{(AC)^2}{2} + \frac{(BD)^2}{2}\right)$$

$$= (AC)^2 + (BD)^2$$

Answer 18.

In equilateral triangle $AD \perp BC$.

$$\Rightarrow BD = DC = \frac{BC}{2} \quad (\text{In equilateral triangle altitude bisects the opposite side})$$

In right triangle ABD,

$$AB^2 = AD^2 + BD^2$$

$$= AD^2 + \left(\frac{BC}{2}\right)^2$$

$$= \frac{4AD^2 + BC^2}{4}$$

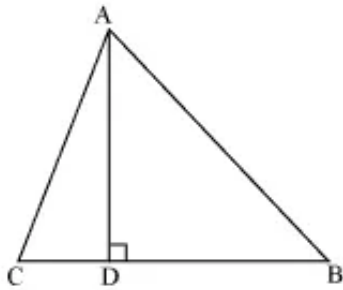
$$= \frac{4AD^2 + AB^2}{4} \quad (\text{Since } AB = BC)$$

$$\Rightarrow 4AB^2 = 4AD^2 + AB^2$$

$$\Rightarrow 3AB^2 = 4AD^2$$

Hence proved.

Answer 19.



In $\triangle ACD$

$$AC^2 = AD^2 + DC^2$$

$$AD^2 = AC^2 - DC^2 \quad (1)$$

In $\triangle ABD$

$$AB^2 = AD^2 + DB^2$$

$$AD^2 = AB^2 - DB^2 \quad (2)$$

From equation (1) and (2)

$$\text{Therefore } AC^2 - DC^2 = AB^2 - DB^2$$

since given that $3DC = DB$

$$DC = \frac{BC}{4} \text{ and } DB = \frac{3BC}{4}$$

$$AC^2 - \left(\frac{BC}{4}\right)^2 = AB^2 - \left(\frac{3BC}{4}\right)^2$$

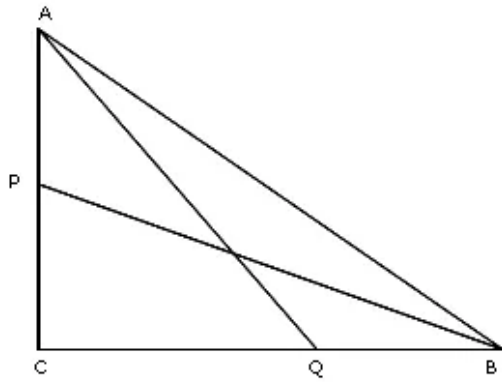
$$AC^2 - \frac{BC^2}{16} = AB^2 - \frac{9BC^2}{16}$$

$$16AC^2 - BC^2 = 16AB^2 - 9BC^2$$

$$\Rightarrow 16AB^2 - 16AC^2 = 8BC^2$$

$$\Rightarrow 2AB^2 = 2AC^2 + BC^2$$

Answer 20.



P divides AC in the ratio 2 : 1

$$\text{So } CP = \frac{2}{3} AC \dots\dots(i)$$

Q divides BC in the ratio 2: 1

$$QC = \frac{2}{3} BC \quad \dots\dots (ii)$$

(i) In $\triangle ACQ$

Using Pythagoras Theorem we have,

$$AQ^2 = AC^2 + CQ^2$$

$$\Rightarrow AQ^2 = AC^2 + \frac{4}{9} BC^2 \quad (\text{using (ii)})$$

$$\Rightarrow 9AQ^2 = 9AC^2 + 4BC^2 \quad \dots\dots(iii)$$

(ii) Applying Pythagoras theorem in right triangle BCP, we have

$$BP^2 = BC^2 + CP^2$$

$$\Rightarrow BP^2 = BC^2 + \frac{4}{9} AC^2 \quad (\text{Using (i)})$$

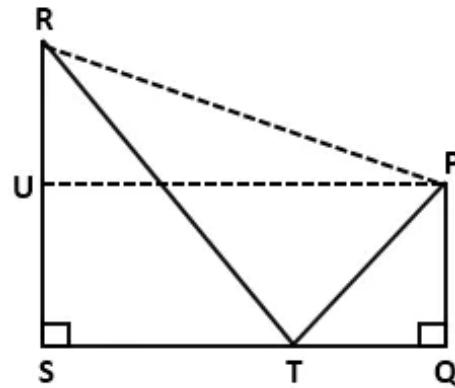
$$\Rightarrow 9BP^2 = 9BC^2 + 4AC^2$$

Adding (iii) and (iv), we get

$$9(AQ^2 + BP^2) = 13(BC^2 + AC^2)$$

$$\Rightarrow 9(AQ^2 + BP^2) = 13 AB^2$$

Answer 21.



$$PQ = \frac{RS}{3} = 8 \text{ cm}$$

$$\Rightarrow PQ = 8 \text{ cm and } RS = 3 \times 8 = 24 \text{ cm}$$

$$3ST = 4QT = 48 \text{ cm}$$

$$\Rightarrow ST = \frac{48}{3} = 16 \text{ cm and } QT = \frac{48}{4} = 12 \text{ cm}$$

In $\triangle PTQ$,

$$PT^2 = PQ^2 + QT^2 = 8^2 + 12^2 = 64 + 144 = 208$$

In $\triangle RTS$,

$$RT^2 = RS^2 + ST^2 = 24^2 + 16^2 = 576 + 256 = 832$$

$$\text{Now, } PT^2 + RT^2 = 208 + 832 = 1040 \quad \dots(i)$$

Draw $PU \perp RS$ and Join PR .

$$PU = SQ = ST + TQ = 16 + 12 = 28 \text{ cm}$$

$$RU = RS - US = RS - PQ = 24 - 8 = 16 \text{ cm}$$

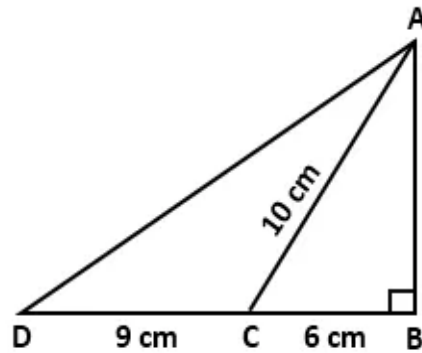
In $\triangle RUP$,

$$PR^2 = RU^2 + PU^2 = 16^2 + 28^2 = 256 + 784 = 1040 \quad \dots(ii)$$

From (i) and (ii), we get

$$PT^2 + RT^2 = PR^2$$

Thus, $\angle RTP = 90^\circ$

Answer 22.

In $\triangle ABC$, $\angle B = 90^\circ$

$$\therefore AC^2 = AB^2 + BC^2 \quad \dots(\text{Pythagoras Theorem})$$

$$\Rightarrow 10^2 = AB^2 + 6^2$$

$$\Rightarrow AB^2 = 10^2 - 6^2 = 100 - 36 = 64$$

$$\text{Now, } BD = BC + CD = 6 + 9 = 15 \text{ cm}$$

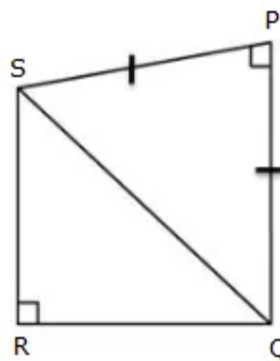
$$\Rightarrow BD^2 = 225$$

In $\triangle ABD$, $\angle B = 90^\circ$

$$\therefore AD^2 = AB^2 + BD^2$$

$$\Rightarrow AD^2 = 64 + 225 = 289$$

$$\Rightarrow AD = 17 \text{ cm}$$

Answer 23.

In $\triangle SRQ$, $\angle R = 90^\circ$

$$\therefore QS^2 = RS^2 + QR^2 \quad \dots(\text{Pythagoras Theorem})$$

$$= 20^2 + 21^2$$

$$= 400 + 441$$

$$= 841$$

Now, in $\triangle QSP$, $\angle P = 90^\circ$

$$\therefore QS^2 = PQ^2 + PS^2 \quad \dots(\text{Pythagoras Theorem})$$

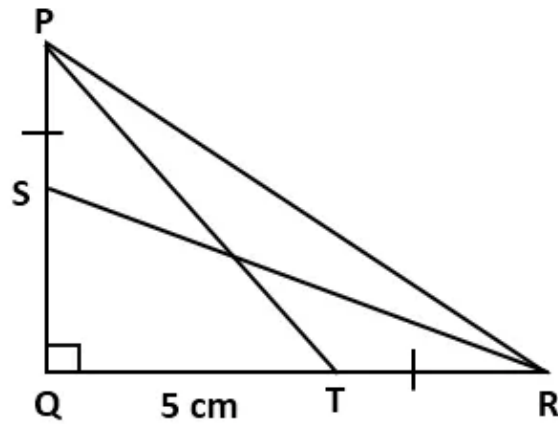
$$\Rightarrow QS^2 = PQ^2 + PQ^2 \quad \dots(\text{Given } PQ = PS)$$

$$\Rightarrow QS^2 = 2PQ^2$$

$$\Rightarrow PQ^2 = \frac{QS^2}{2} = \frac{841}{2} = 420.5$$

$$\Rightarrow PQ = 20.50 \text{ cm}$$

Answer 24.



In $\triangle PQT$, $\angle Q = 90^\circ$

$\therefore PT^2 = PQ^2 + QT^2$ (By Pythagoras Theorem)

$$\Rightarrow PQ^2 = PT^2 - QT^2 = 13^2 - 5^2 = 169 - 25 = 144$$

$$\Rightarrow PQ = 12 \text{ cm}$$

Now, $PS = TR = a$ (say)

In $\triangle SQR$, $\angle Q = 90^\circ$

$\therefore SR^2 = QS^2 + QR^2$ (By Pythagoras Theorem)

$$\Rightarrow SR^2 = (PQ - PS)^2 + (QT + TR)^2$$

$$\Rightarrow SR^2 = (PQ - PS)^2 + (QT + PS)^2 \quad \dots(\text{Since } PS = TR)$$

$$\Rightarrow SR^2 = PQ^2 - 2 \times PQ \times PS + PS^2 + QT^2 + 2 \times QT \times PS + PS^2$$

$$\Rightarrow 13^2 = 12^2 - 2 \times 12 \times a + a^2 + 5^2 + 2 \times 5 \times a + a^2$$

$$\Rightarrow 169 = 144 - 24a + a^2 + 25 + 10a + a^2$$

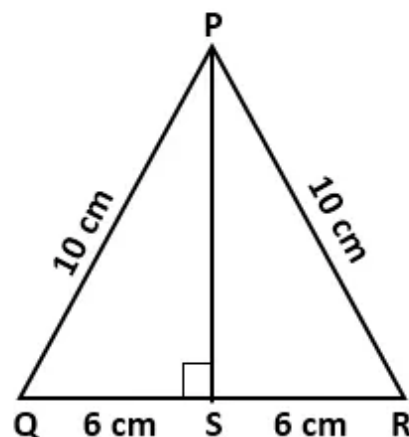
$$\Rightarrow 169 = 169 - 14a + 2a^2$$

$$\Rightarrow 2a^2 = 14a$$

$$\Rightarrow a = 7$$

Hence, $PS = 7 \text{ cm}$

Answer 25.



Since, PQR is an isosceles triangle and $PS \perp QR$,
therefore it divides QR into two equal parts.

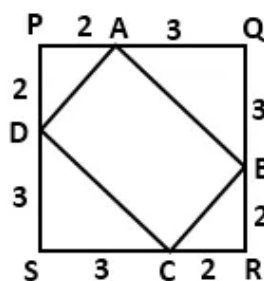
In $\triangle PSQ$, $\angle S = 90^\circ$

$$\therefore PQ^2 = PS^2 + QS^2 \quad \dots (\text{By Pythagoras Theorem})$$

$$\Rightarrow PS^2 = PQ^2 - QS^2 = 10^2 - 6^2 = 100 - 36 = 64$$

$$\Rightarrow PS = 8 \text{ cm}$$

Answer 26.



In $\triangle APD$, $\angle P = 90^\circ$

$$\therefore AD^2 = AP^2 + PD^2 = 2^2 + 3^2 = 4 + 9 = 13$$

$$\Rightarrow AD = \sqrt{13} \text{ cm}$$

Similarly, we can prove that in $\triangle BRC$,

$$BC = \sqrt{13} \text{ cm}$$

$$\therefore AD = BC \quad \dots (i)$$

In $\triangle AQB$, $\angle Q = 90^\circ$

$$\therefore AB^2 = AQ^2 + BQ^2 = 3^2 + 2^2 = 9 + 4 = 13$$

$$\Rightarrow AB = \sqrt{13} \text{ cm}$$

Similarly, we can prove that in $\triangle CSD$,

$$CD = \sqrt{13} \text{ cm}$$

$$\therefore AB = CD \quad \dots (ii)$$

Again, in $\triangle APD$,

$$AP = PD$$

$$\Rightarrow \angle PAD = \angle PDA = 45^\circ$$

Also, in $\triangle AQB$,

$$AQ = BQ$$

$$\Rightarrow \angle QAB = \angle QBA = 45^\circ$$

$$\text{Now, } \angle PAD + \angle DAB + \angle QAB = 180^\circ$$

$$\Rightarrow 45^\circ + \angle DAB + 45^\circ = 180^\circ$$

$$\Rightarrow \angle DAB = 90^\circ$$

Similarly, we can prove that $\angle ABC$, $\angle BCD$ and $\angle ADC$ are 90° each.

Thus, ABCD is a rectangle as opposite sides are equal and each angle is 90° .

Now,

$$\text{Area of a rectangle ABCD} = AD \times AB = 2\sqrt{2} \times 3\sqrt{2} = 12 \text{ cm}^2$$

$$\begin{aligned} \text{Perimeter of a rectangle ABCD} &= AB + BC + CD + AD \\ &= 2\sqrt{2} + 3\sqrt{2} + 2\sqrt{2} + 3\sqrt{2} \\ &= 10\sqrt{2} \text{ cm} \end{aligned}$$