

CBSE Test Paper 01
Chapter 9 Some Applications of Trigonometry

1. The _____ of an object is the angle formed by the line of sight with the horizontal when the object is above the horizontal level. **(1)**
 - a. angle of projection
 - b. angle of depression
 - c. angle of elevation
 - d. none of these

2. From a point on the ground which is 15m away from the foot of a tower, the angle of elevation is found to be 60° . The height of the tower is **(1)**
 - a. $15\sqrt{3}$ m
 - b. $20\sqrt{3}$ m
 - c. $10\sqrt{3}$ m
 - d. 10 m

3. From a point P on the level ground, the angle of elevation of the top of a tower is 30° . If the tower is 100m high, the distance between P and the foot of the tower is **(1)**
 - a. $300\sqrt{3}$ m
 - b. $150\sqrt{3}$ m
 - c. $200\sqrt{3}$ m
 - d. $100\sqrt{3}$ m

4. An electric pole is $10\sqrt{3}$ m high and its shadow is 10 m in length, then the angle of elevation of the sun is **(1)**
 - a. 45°
 - b. 15°
 - c. 30°
 - d. 60°

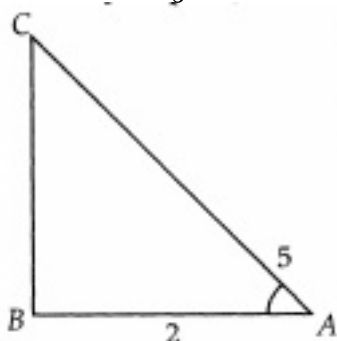
5. If the shadow of a boy 'x' metres high is 1.6m and the angle of elevation of the sun is

45° , then the value of 'x' is **(1)**

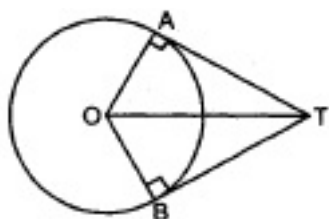
- a. 0.8 m
- b. 1.6 m
- c. 3.2 m
- d. 2 m

6. The angle of depression of car parked on the road from the the top of a 150 m hightower is 30° . Find the distance of the car from the tower. **(1)**

7. If $\cos A = \frac{2}{5}$, find the value of $4 + 4\tan^2 A$. **(1)**



8. In figure if $\angle ATO = 40^\circ$, find $\angle AOB$. **(1)**



9. A ladder 15 m long leans against a wall making an angle of 60° with the wall. Find the height of the wall from the point the ladder touches the wall. **(1)**

10. A pole 6 m high casts a shadow $2\sqrt{3}$ long on the ground, then find the Sun's elevation. **(1)**

11. A boy observes that the angle of elevation of a bird flying at a distance of 100 m is 30° . At the same distance from the boy, a girl finds the angle of elevation of the same bird from a building 20 m high is 45° . Find the distance of the bird from the girl. **(1)**

12. Find the angle of elevation of the sun when the shadow of a pole h m high is $\sqrt{3} h$ m long. **(2)**

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13. A 7 m long flagstaff is fixed on the top of a tower standing on the horizontal plane. From point on the ground, the angles of elevation of the top and bottom of the flagstaff are 60° and 45° respectively. Find the height of the tower correct to one place of decimal. **(2)**
14. The tops of two towers of height x and y , standing on level ground, subtend angles of 30° and 60° respectively at the centre of the line joining their feet, then find $x : y$. **(3)**
15. The length of a string between a kite and a point on the ground is 85 m. If the string makes an angle θ with the ground level such that $\tan \theta = 15/8$ then find the height of the kite from the ground. Assume that there is no slack in the string. **(3)**
16. A man standing on the deck of a ship which is 10 m above the water level observes the angle of elevation of the top of a hill as 60° and the angle of depression of the base of the hill as 30° . Calculate the distance of the hill from the ship and the height of the hill. **(3)**
17. The angle of elevation of the top Q of a vertical tower PQ from a point X on the ground is 60° . At a point R, 40 m vertically above X, the angle of elevation of the top Q of tower is 45° . Find the height of the tower PQ and the distance PX. **(3)**
18. The angle of depression of the top and bottom of a building 50 metres high as observed from the top of a tower are 30° and 45° respectively. Find the height of the tower and also the horizontal distance between the building and the tower. **(4)**
19. A vertically straight tree, 15 m high, is broken by the wind in such a way that its top just touches the ground and makes an angle of 60° with the ground. At what height from the ground did the tree break? **(4)**
20. A round balloon of radius r subtends an angle α at the eye of the observer while the angle of elevation of its centre is β . Prove that the height of the centre of the balloon is $r \sin \beta \operatorname{cosec} \frac{\alpha}{2}$. **(4)**

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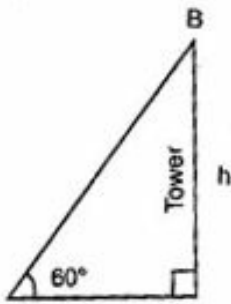
Solution

1. c. angle of elevation

Explanation: The angle of elevation of an object is the angle formed by the line of sight with the horizontal when the object is above the horizontal level.

2. a. $15\sqrt{3}$ m

Explanation: Let the height of the tower be h metres.



In triangle AOB, $\tan 60^\circ = \frac{AB}{OA}$

$$\Rightarrow \tan 60^\circ = \frac{h}{15}$$

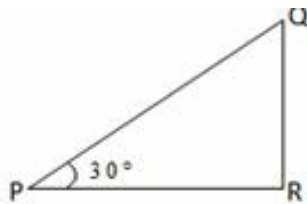
$$\Rightarrow \sqrt{3} = \frac{h}{15}$$

$$\Rightarrow h = 15\sqrt{3} \text{ m}$$

Therefore, the height of the tower is $15\sqrt{3}$ meters.

3. d. $100\sqrt{3}$ m

Explanation:



Let QR be the height of the tower, then $QR = 100$ m

And the angle of elevation of the top of the tower be $\angle QPR = 30^\circ$

$$\therefore \tan 30^\circ = \frac{QR}{PR}$$

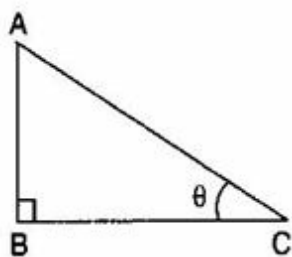
$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{100}{PR} \text{ m}$$

$$\Rightarrow PR = 100\sqrt{3} \text{ meters}$$

Therefore, the distance between P and the foot of the tower is $100\sqrt{3}$ meters.

4. d. 60°

Explanation:

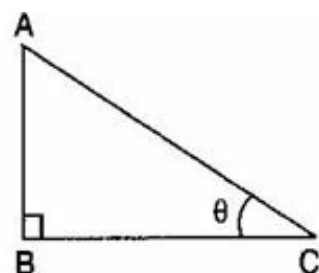


Let AB be the electric pole of height $10\sqrt{3}$ m and its shadow be BC of length 10 m. And the angle of elevation of the sun be θ .

$$\begin{aligned}\therefore \tan \theta &= \frac{AB}{BC} \\ \Rightarrow \tan \theta &= \frac{10\sqrt{3}}{10} \\ \Rightarrow \tan \theta &= \sqrt{3} \\ \Rightarrow \tan \theta &= \tan 60^\circ \\ \Rightarrow \theta &= 60^\circ\end{aligned}$$

5. b. 1.6 m

Explanation:



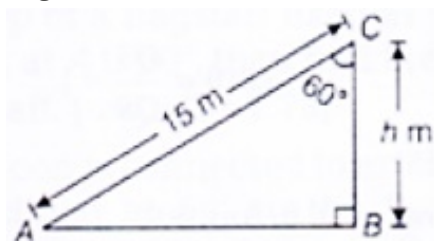
Given: Height of the boy = AB = x meters

And the length of the shadow of the boy = BC = 1.6 m

And angled of elevation $\theta = 45^\circ$

$$\begin{aligned}\therefore \tan 45^\circ &= \frac{AB}{BC} \Rightarrow 1 = \frac{x}{1.6} \\ \Rightarrow x &= 1.6 \text{ m}\end{aligned}$$

6. The angle of depression of car parked on the road from the the top of a 150 m hightower is 30° .



Let $AB = 150 \text{ m}$ be the height of the tower and angle of depression is $\angle DAC = 30^\circ$.

Therefore, $\angle ACB = \angle DAC = 30^\circ$ [\because alternate angles]

Now, in right-angled $\triangle ABC$, $\angle B = 90^\circ$

$$\tan 30^\circ = \frac{P}{B} = \frac{AB}{BC}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{150}{BC} \quad [\because \tan 30^\circ = \frac{1}{\sqrt{3}}]$$

$$\Rightarrow BC = 150\sqrt{3} \text{ m}$$

Therefore, Distance of car from tower = $150\sqrt{3} \text{ m}$

7. Given, $\cos A = \frac{5}{2}$

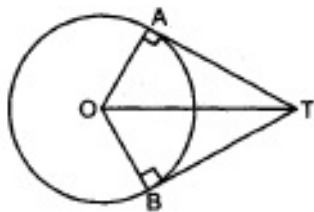
$$= 4 + 4 \tan^2 A$$

$$= 4(1 + \tan^2 A)$$

$$= 4 \sec^2 A = \frac{4}{\cos^2 A} = 4 \times \frac{25}{4} = 25$$

8. According to the question,

$$\angle ATO = 40^\circ$$



In $\triangle OAT$, $\angle OAT = 90^\circ$

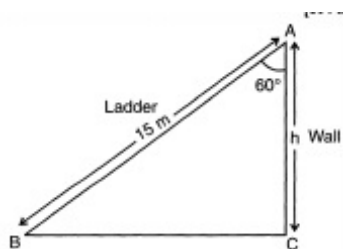
$$\angle AOT = 50^\circ \text{ [Angle sum property]}$$

Now $\angle BTO = 40^\circ$ as OT bisects $\angle ATB$

Similarly, $\angle BOT = 50^\circ$

$$\angle AOB = \angle AOT + \angle BOT = 50^\circ + 50^\circ = 100^\circ$$

9.



Let ABC be a right angled triangle where AB is ladder = 15m and angle $a = 60^\circ$

Let AC be the height of the wall

Therefore by Pythagoras theorem

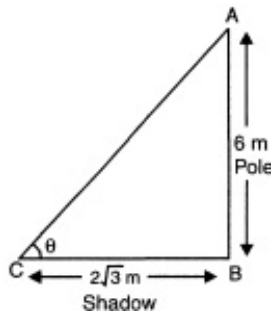
$$\frac{h}{15} = \cos 60^\circ$$

$$\Rightarrow h = 15 \times \cos 60^\circ$$

$$= 15 \times \frac{1}{2}$$

$$= 7.5 \text{ m}$$

10.



Let the Sun's elevation be θ

Length of pole = 6 m, length of shadow = $2\sqrt{3}$ m

From $\triangle ABC$, $\frac{AB}{BC} = \tan \theta$ (using Pythagoras theorem)

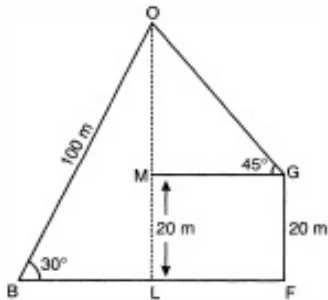
$$\Rightarrow \frac{6}{2\sqrt{3}} = \tan \theta$$

$$\Rightarrow \tan \theta = \frac{3}{\sqrt{3}} = \sqrt{3} = \tan 60^\circ$$

$$\Rightarrow \theta = 60^\circ$$

Hence sun's elevation is 60°

11.



Let O be the position of the bird and B be the position of the boy. Let FG be the building and G be the position of the girl.

In $\triangle OLB$,

$$\frac{OL}{OB} = \sin 30^\circ$$

$$\Rightarrow \frac{OL}{100} = \frac{1}{2}$$

$$\Rightarrow OL = 50 \text{ m}$$

$$OM = OL - ML$$

$$= OL - FG$$

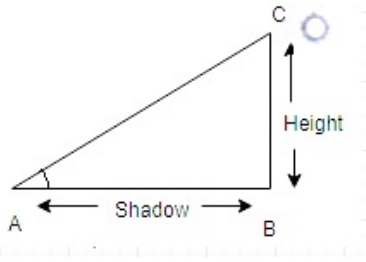
$$= 50 - 20 = 30 \text{ m}$$

In $\triangle OMG$

$$\frac{OM}{OG} = \sin 45^\circ = \frac{1}{\sqrt{2}}$$

$$OG = OM\sqrt{2} = 30\sqrt{2} = 42.3 \text{ meter}$$

12.



Let BC be the height and BA be the shadow of a man.

According to the question, $AB = BC$

The shadow of a pole $AB = h$ m high $BC = \sqrt{3} h$ m long.

Again, let the angle of elevation of the Sun be θ .

In right-angled $\triangle ABC$

$$\tan \theta = \frac{P}{B} = \frac{BC}{AB}$$

$$\Rightarrow \tan \theta = \frac{h}{\sqrt{3}h} \{ \because AB = h \text{ m and } BC = \sqrt{3} h \}$$

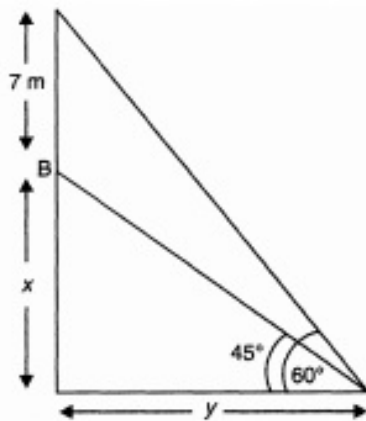
$$\Rightarrow \tan \theta = \frac{1}{\sqrt{3}}$$

$$\Rightarrow \tan \theta = \tan 30^\circ (\because \tan 30^\circ = \frac{1}{\sqrt{3}})$$

$$\Rightarrow \theta = 30^\circ$$

Therefore, Angle of elevation of Sun is 30°

13.



$$\frac{x}{y} = \tan 45^\circ = 1$$

$$\Rightarrow x = y$$

Now in big triangle

$$\tan 60^\circ = \frac{x+7}{x}$$

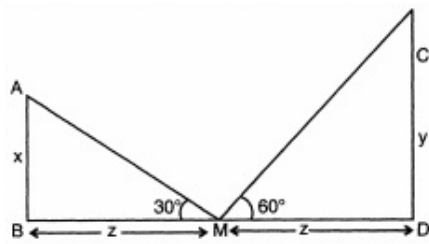
$$\sqrt{3} = \frac{x+7}{x}$$

$$x(\sqrt{3} - 1) = 7$$

So height of the tower

$$x = \frac{7}{\sqrt{3}-1} = 9.58$$

14.



Let M be the centre of the line joining their feet.

Let $BM = MD = z$

$$\therefore \tan \theta = \frac{\text{perpendicular}}{\text{base}}$$

$$\text{In } \triangle ABM, \therefore \frac{x}{z} = \tan 30^\circ$$

$$\Rightarrow x = z \times \frac{1}{\sqrt{3}} \dots (i)$$

In $\triangle MCD$ we have

$$\frac{y}{z} = \tan 60^\circ = \sqrt{3}$$

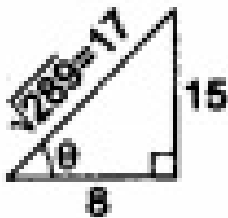
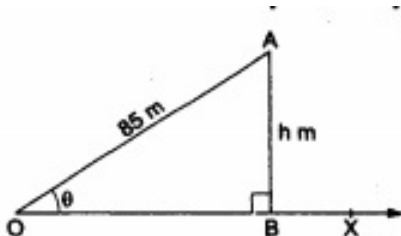
$$y = z\sqrt{3} \dots (ii)$$

From (i) and (ii) we get

$$\frac{x}{y} = \frac{z}{\sqrt{3}} \times \frac{1}{\sqrt{3}z} = \frac{1}{3}$$

Hence $x : y = 1 : 3$

15. Let OX be the horizontal ground and let A be the position of the kite. Let O be the position of the observer and OA be the string. Draw $AB \perp OX$.



Then, $\angle BOA = \theta$ such that $\tan \theta = \frac{15}{8}$, $OA = 85m$ and $\angle OBA = 90^\circ$.

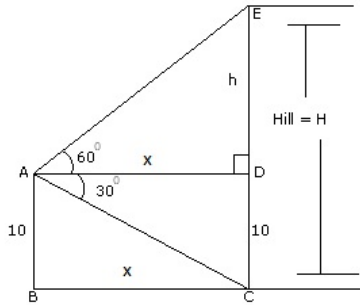
Let $AB = h$ m.

From right $\triangle OBA$, we have

$$\frac{AB}{OA} = \sin \theta = \frac{15}{17} \left[\because \tan \theta = \frac{15}{8} \Rightarrow \sin \theta = \frac{15}{17} \right]$$

$$\Rightarrow \frac{h}{85} = \frac{15}{17} \Rightarrow h = \frac{15}{17} \times 85 = 75.$$

16.



Let H = Height of hill

Let $AD = BC = x$ meters

$CE = CD + DE = 10 + h$

In right $\triangle ADE$, $\tan 30^\circ = \frac{AD}{DE}$

$$\frac{x}{h} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow x = \frac{h}{\sqrt{3}}$$

In right $\triangle ADC$, $\frac{x}{10} = \cot 30^\circ = \sqrt{3}$

$$\Rightarrow x = 10\sqrt{3}$$

Equating the values of x , we get

$$\frac{h}{\sqrt{3}} = 10\sqrt{3} \Rightarrow h = 30 \text{ m}$$

\therefore From $H = 10 + h = 10 + 30 = 40 \text{ m}$

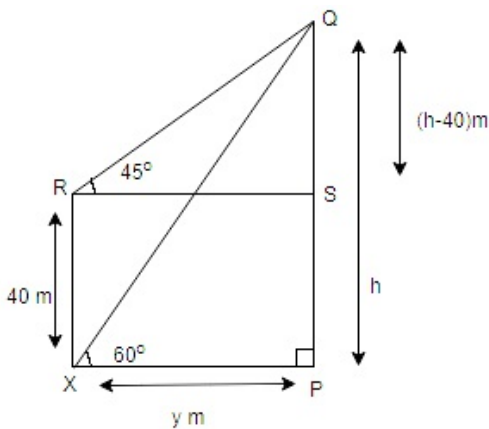
And x = distance of hill from ship = $10\sqrt{3} \text{ m}$

17. Let h be the height of the tower.

i.e, $PQ = h \text{ m}$ and let $PX = y \text{ m}$

Now, draw $RS \parallel XP$,

Then, we have $RX = SP = 40 \text{ m}$, $\angle QXP = 60^\circ$ and $\angle QRS = 45^\circ$



In right angled $\triangle XPQ$,

$$\tan 60^\circ = \frac{PQ}{XP} = \frac{h}{y}$$

$$\Rightarrow \frac{\sqrt{3}}{1} = \frac{h}{y} [\because \tan 60^\circ = \sqrt{3}]$$

$$\Rightarrow y = \frac{h}{\sqrt{3}} \dots (i)$$

In right angled $\triangle RSQ$,

$$\tan 45^\circ = \frac{P}{B} = \frac{QS}{RS}$$

$$\Rightarrow \tan 45^\circ = \frac{PQ-SP}{XP}$$

$$\Rightarrow 1 = \frac{h-40}{y}$$

$$\Rightarrow y = h - 40 \dots (ii)$$

Now, solve Eq(i) and Eq(ii), to find h and y.

$$\frac{h}{\sqrt{3}} = h - 40$$

$$(\sqrt{3} - 1)h = 40\sqrt{3}$$

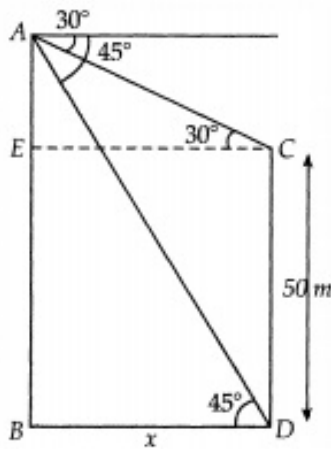
$$h = \frac{40\sqrt{3}}{\sqrt{3} - 1} = \frac{40(1.732)}{1.732 - 1} = \frac{68.28}{0.732} = 94.64$$

$$\Rightarrow y = 94.64 - 40$$

$$\Rightarrow y = 54.64$$

$$\Rightarrow PQ = 94.64 \text{ m and } PX = 54.64 \text{ m}$$

18.



Let the height of the tower be $AB = h$ m

Let the building be $CD = 50$ m

and let distance between $BD = x$

Now, In $\triangle ABD$

$$\frac{AB}{BD} = \tan 45^\circ$$

$$\Rightarrow \frac{h}{x} = 10$$

$$h = x \dots (i)$$

In $\triangle AEC$, $\frac{AE}{EC} = \tan 30^\circ$

$$\Rightarrow \frac{h-50}{x} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow x = h\sqrt{3} - 50\sqrt{3} \text{ ..(ii)}$$

From (i) and (ii) we get

$$h = \sqrt{3}(h - 50)$$

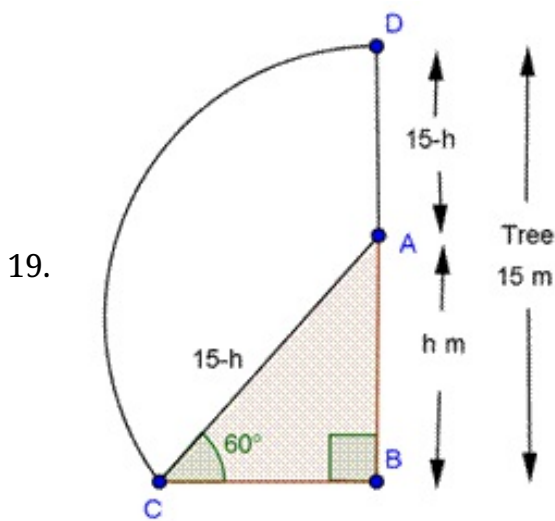
$$h(\sqrt{3} - 1) = 50$$

$$h = \frac{50}{\sqrt{3}-1} = \frac{50(\sqrt{3}+1)}{(\sqrt{3}-1)(\sqrt{3}+1)} = \frac{50(\sqrt{3}+1)}{3-1} = 25(1.73 + 1)$$

$$= 25 \times 2.73 = 68.25 \text{ meter}$$

Hence the height of tower = 68.25 meter

and distance between the building and tower $x = h = 68.25$ meter



The height of the tree (DB) = 15 m

Suppose it broke at A and its top D touches the ground at C.

Suppose AB = h Then AD = AC = (15 - h) m

In $\triangle ABC$

$$\sin 60^\circ = \frac{AB}{AC}$$

$$\Rightarrow \frac{\sqrt{3}}{2} = \frac{h}{15-h}$$

$$\Rightarrow 2h = 15\sqrt{3} - \sqrt{3}h$$

$$\Rightarrow 2h + \sqrt{3}h = 15\sqrt{3}$$

$$\Rightarrow h(2 + \sqrt{3}) = 15\sqrt{3}$$

$$\Rightarrow h = \frac{15\sqrt{3}}{2+\sqrt{3}}$$

$$\Rightarrow h = \frac{15\sqrt{3}}{2+\sqrt{3}} \times \frac{2-\sqrt{3}}{2-\sqrt{3}}$$

$$\Rightarrow h = \frac{30\sqrt{3}-45}{4-3}$$

$$\Rightarrow h = 15(2\sqrt{3} - 3)$$

$$\Rightarrow h = 15[2 \times 1.73 - 3]$$

$$\Rightarrow h = 15 [3.46 - 3]$$

$$\Rightarrow h = 15 \times 0.46$$

$$\Rightarrow h = 6.9m$$

\therefore Height above the ground from where the tree broke is 6.9 meter.

20. Let O be the centre of the balloon of radius r and P the eye of the observer. Let PA, PB be tangents from P to the balloon. Then, $\angle APB = \alpha$.

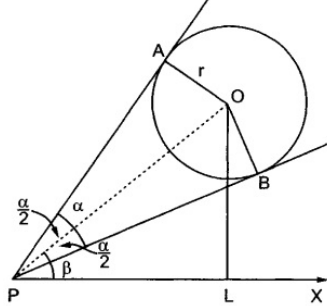
$$\therefore \angle APO = \angle BPO = \frac{\alpha}{2}$$

Let OL be perpendicular from O on the horizontal PX. We are given that the angle of the elevation of the centre of the balloon is β i.e, $\angle OPL = \beta$.

In $\triangle OAP$, we have

$$\sin \frac{\alpha}{2} = \frac{OA}{OP}$$

$$\Rightarrow \sin \frac{\alpha}{2} = \frac{r}{OP}$$



$$\Rightarrow OP = r \operatorname{cosec} \frac{\alpha}{2}$$

In $\triangle OPL$, we have

$$\sin \beta = \frac{OL}{OP}$$

$$\Rightarrow OL = OP \sin \beta = r \operatorname{cosec} \frac{\alpha}{2} \sin \beta \text{ [Using equation (i)]}$$

Hence, the height of the centre of the balloon is $r \sin \beta \operatorname{cosec} \frac{\alpha}{2}$