

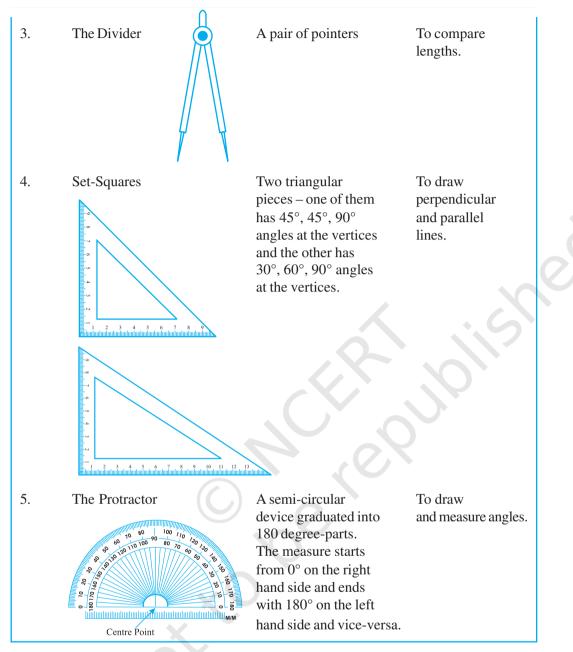
14.1 Introduction

We see a number of shapes with which we are familiar. We also make a lot of pictures. These pictures include different shapes. We have learnt about some of these shapes in earlier chapters as well. Why don't you list those shapes that you know about alongwith how they appear?

In this chapter we shall learn to make these shapes. In making these shapes we need to use some tools. We shall begin with listing these tools, describing them and looking at how they are used.

S.No.	Name and figure	Description	Use
1.	The Ruler [or the straight edge]	A ruler ideally has no markings on it. However, the ruler in your instruments box is graduated into centimetres along one edge (and sometimes into inches along the other edge).	To draw line segments and to measure their lengths.
2.	The Compasses Pencil Pointer	A pair – a pointer on one end and a pencil on the other.	To mark off equal lengths but not to measure them. To draw arcs and circles.





We are going to consider "**Ruler and compasses constructions**", using ruler, only to draw lines, and compasses, only to draw arcs.

Be careful while doing these constructions.

Here are some tips to help you.

- (a) Draw thin lines and mark points lightly.
- (b) Maintain instruments with sharp tips and fine edges.
- (c) Have two pencils in the box, one for insertion into the compasses and the other to draw lines or curves and mark points.

14.2 The Circle

Look at the wheel shown here. Every point on its boundary is at an equal distance from its centre. Can you mention a few such objects and draw them? Think about five such objects which have this shape.

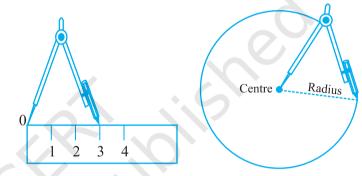


14.2.1 Construction of a circle when its radius is known

Suppose we want to draw a circle of radius 3 cm. We need to use our compasses. Here are the steps to follow.

Step 1 Open the compasses for the required radius of 3cm.

Step 2 Mark a point with a sharp pencil where we want the centre of the circle to be. Name it as O.



Step 3 Place the pointer of the compasses on O.

Step 4 Turn the compasses slowly to draw the circle. Be careful to complete the movement around in one instant.

Think, discuss and write

How many circles can you draw with a given centre O and a point, say P?

EXERCISE 14.1

- 1. Draw a circle of radius 3.2 cm.
- 2. With the same centre O, draw two circles of radii 4 cm and 2.5 cm.
- 3. Draw a circle and any two of its diameters. If you join the ends of these diameters, what is the figure obtained? What figure is obtained if the diameters are perpendicular to each other? How do you check your answer?
- 4. Draw any circle and mark points A, B and C such that
 - (a) A is on the circle. (b) B is in the interior of the circle.
 - (c) C is in the exterior of the circle.
- 5. Let A, B be the centres of two circles of equal radii; draw them so that each one of them passes through the centre of the other. Let them intersect at C and D.

Examine whether AB and CD are at right angles.

14.3 A Line Segment

Remember that a line segment is bounded by two end-points. This makes it possible to measure its length with a ruler.

If we know the length of a line segment, it becomes possible to represent it by a diagram. Let us see how we do this.

14.3.1 Construction of a line segment of a given length

Suppose we want to draw a line segment of length 4.7 cm. We can use our ruler and mark two points A and B which are 4.7 cm apart. Join A and B and

get \overline{AB} . While marking the points A and B, we should look straight down at the measuring device. Otherwise we will get an incorrect value.

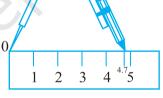
Use of ruler and compasses

A better method would be to use compasses to construct a line segment of a given length.

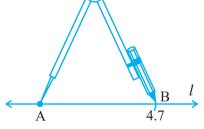
Step 1 Draw a line *l*. Mark a point A on a line *l*.



Step 2 Place the compasses pointer on the zero mark of the ruler. Open it to place the pencil point upto the 4.7cm mark.



Step 3 Taking caution that the opening of the compasses has not changed, place the pointer on A and swing an arc to cut l at B.

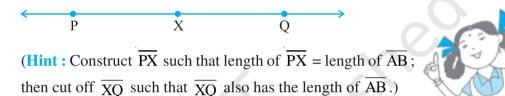


Step 4 \overline{AB} is a line segment of required length.





- 1. Draw a line segment of length 7.3 cm using a ruler.
- 2. Construct a line segment of length 5.6 cm using ruler and compasses.
- 3. Construct \overline{AB} of length 7.8 cm. From this, cut off \overline{AC} of length 4.7 cm. Measure \overline{BC} .
- 4. Given \overline{AB} of length 3.9 cm, construct \overline{PQ} such that the length of PQ is twice that of \overline{AB} . Verify by measurement.



5. Given \overline{AB} of length 7.3 cm and \overline{CD} of length 3.4 cm, construct a line segment \overline{XY} such that the length of \overline{XY} is equal to the difference between the lengths of \overline{AB} and \overline{CD} . Verify by measurement.

14.3.2 Constructing a copy of a given line segment

Suppose you want to draw a line segment whose length is equal to that of a given line segment \overline{AB} .

A quick and natural approach is to use your ruler (which is marked with centimetres and millimetres) to measure the length of \overline{AB} and then use the same length to draw another line segment \overline{CD} .

A second approach would be to use a transparent sheet and trace \overline{AB} onto another portion of the paper. But these methods may not always give accurate results.

A better approach would be to use ruler and compasses for making this construction.

To make a copy of \overline{AB} .

Step 1 Given AB whose length is not known.

A B

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Step 2 Fix the compasses pointer on A and the pencil end on B. The opening of the instrument now gives the length of \overline{AB} .

Step 3 Draw any line *l*. Choose a point C on *l*. Without changing the compasses setting, place the pointer on C.

Step 4 Swing an arc that cuts *l* at a point, say, D. Now \overline{CD} is a copy of \overline{AB} .

С

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EXERCISE 14.3

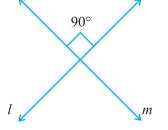
C

- 1. Draw any line segment \overline{PQ} . Without measuring \overline{PQ} , construct a copy of \overline{PQ} .
- 2. Given some line segment \overline{AB} , whose length you do not know, construct \overline{PQ} such that the length of \overline{PQ} is twice that of \overline{AB} .

14.4 Perpendiculars

You know that two lines (or rays or segments) are said to be perpendicular if they intersect such that the angles formed between them are right angles.

In the figure, the lines *l* and *m* are perpendicular.



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The corners of a foolscap paper or your notebook indicate lines meeting at right angles.

Do This 🐋

Where else do you see perpendicular lines around you?

Take a piece of paper. Fold it down the middle and make the crease. Fold the paper once again

down the middle in the other direction. Make the crease and open out the page. The two creases are perpendicular to each other.

14.4.1 Perpendicular to a line through a point on it

Given a line l drawn on a paper sheet and a point P lying on the line. It is easy to have a perpendicular to l through P.

We can simply fold the paper such that the lines on both sides of the fold overlap each other.

Tracing paper or any transparent paper could be better for this activity. Let us take such a paper and draw any line l on it. Let us mark a point P anywhere on l.

Fold the sheet such that l is reflected on itself; adjust the fold so that the crease passes through the marked point P. Open out; the crease is perpendicular to l.

Think, discuss and write

How would you check if it is perpendicular? Note that it passes through P as required.

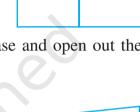
A challenge : Drawing perpendicular using ruler and a set-square (An optional activity).

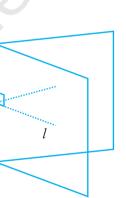
Step 1 A line *l* and a point P are given. Note that P is on the line *l*.



Step 2 Place a ruler with one of its edges along *l*. Hold this firmly.







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Step 3 Place a set-square with one of its edges along the already aligned edge of the ruler such that the right angled corner is in contact with the ruler.

Step 4 Slide the set-square along the edge of ruler until its right angled corner coincides with P.





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Step 5 Hold the set-square firmly in this position. Draw \overline{PQ} along the edge of the set-square.

 \overline{PQ} is perpendicular to *l*. (How do you use the \perp symbol to say this?).

Verify this by measuring the angle at P.

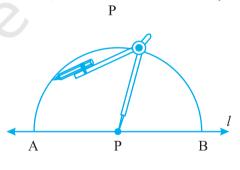
Can we use another set-square in the place of the 'ruler'? Think about it.

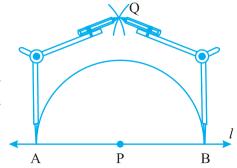
Method of ruler and compasses

As is the preferred practice in Geometry, the dropping of a perpendicular can be achieved through the "ruler-compasses" construction as follows :

Step 1 Given a point P on a line *l*.

Step 2 With P as centre and a convenient radius, construct an arc intersecting the line l at two points A and B.





Step 3 With A and B as centres and a radius greater than AP construct two arcs, which cut each other at Q.

Step 4 Join PQ. Then PQ is perpendicular to *l*.

We write PQ $\perp l$.

14.4.2 Perpendicular to a line through a point not on it

Do This 🐋

(Paper folding)

If we are given a line l and a point P not lying on it and P we want to draw a perpendicular to l through P, we can again do it by a simple paper folding as before.

Take a sheet of paper (preferably transparent).

Draw any line *l* on it.

Mark a point P away from *l*.

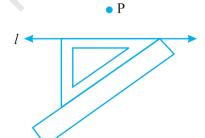
Fold the sheet such that the crease passes through P. The parts of the line l on both sides of the fold should overlap each other.

Open out. The crease is perpendicular to l and passes through P.

Method using ruler and a set-square (An optional activity)

Step 1 Let *l* be the given line and P be a point l outside *l*.

Step 2 Place a set-square on *l* such that one arm of its right angle aligns along *l*.



Step 3 Place a ruler along the edge opposite to the right angle of the set-square.

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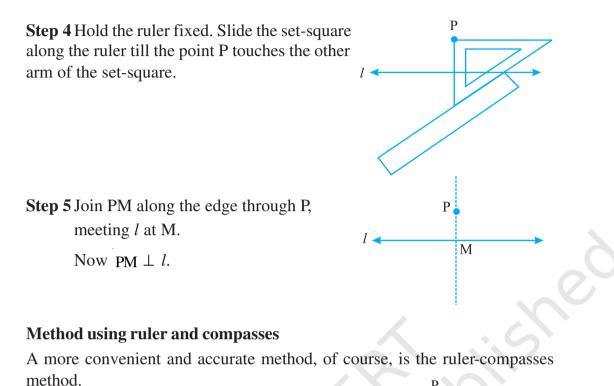
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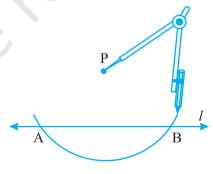
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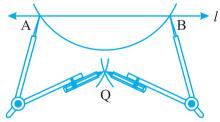


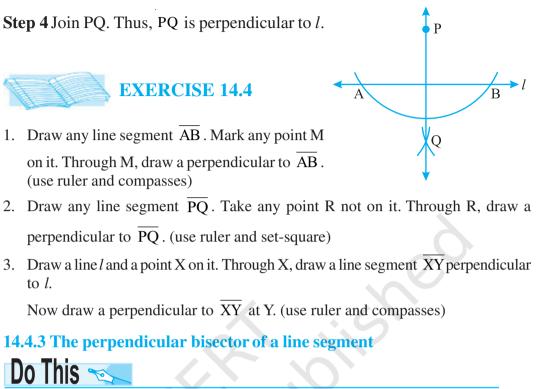
Step 1 Given a line *l* and a point P not on it.

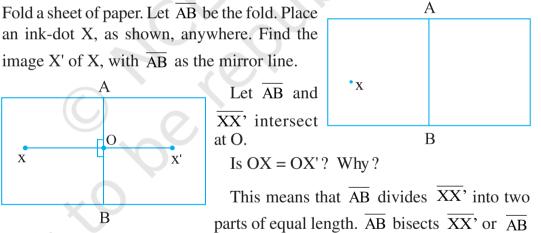
Step 2 With P as centre, draw an arc which intersects line l at two points A and B.



Step 3 Using the same radius and with A and B as centres, construct two arcs that intersect at a point, say Q, on the other side.







is a bisector of \overline{XX} '. Note also that $\angle AOX$ and $\angle BOX$ are right angles. (Why?).

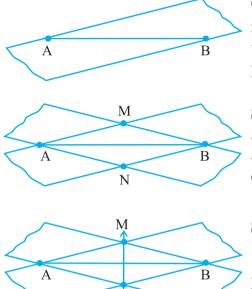
Hence, \overline{AB} is the perpendicular bisector of \overline{XX} '. We see only a part of \overline{AB} in the figure. Is the perpendicular bisector of a line joining two points the same as the axis of symmetry?



Α

(Transparent tapes)

Step 1 Draw a line segment \overline{AB} .



Step 2 Place a strip of a transparent rectangular tape diagonally across \overline{AB} with the edges of the tape on the end points A and B, as shown in the figure.

Step 3 Repeat the process by placing another tape over A and B just diagonally across the previous one. The two strips cross at M and N.

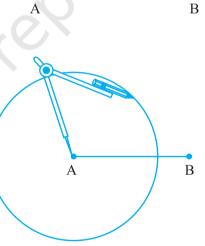
Step 4 Join M and N. Is \overline{MN} a bisector of \overline{AB} ? Measure and verify. Is it also the perpendicular bisector of \overline{AB} ? Where is the mid point of \overline{AB} ?

Construction using ruler and compasses

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Step 1 Draw a line segment \overline{AB} of any length.

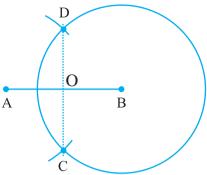
Step 2 With A as centre, using compasses, draw a circle. The radius of your circle should be more than half the length of \overline{AB} .



Step 3 With the same radius and with B as centre, draw another circle using compasses. Let it cut the previous circle at C and D.

Step 4 Join \overline{CD} . It cuts \overline{AB} at O. Use your divider to verify that O is the midpoint of \overline{AB} . Also verify that $\angle COA$ and $\angle COB$ are right angles. Therefore, \overline{CD} is the perpendicular bisector of \overline{AB} .

In the above construction, we needed the two points C and D to determine \overline{CD} . Is it necessary to draw the whole circle to find them? Is it not enough if we draw merely small arcs to locate them? In fact, that is what we do in practice!



Try These Q

In Step 2 of the construction using ruler and compasses, what would happen if we take the length of radius to be smaller than half the

length of \overline{AB} ?

1. Draw \overline{AB} of length 7.3 cm and find its axis of symmetry.

EXERCISE 14.5

- 2. Draw a line segment of length 9.5 cm and construct its perpendicular bisector.
- Draw the perpendicular bisector of XY whose length is 10.3 cm.
 (a) Take any point P on the bisector drawn. Examine whether PX = PY.
 - (b) If M is the mid point of \overline{XY} , what can you say about the lengths MX and XY?
- 4. Draw a line segment of length 12.8 cm. Using compasses, divide it into four equal parts. Verify by actual measurement.
- 5. With PQ of length 6.1 cm as diameter, draw a circle.
- 6. Draw a circle with centre C and radius 3.4 cm. Draw any chord \overline{AB} . Construct the perpendicular bisector of \overline{AB} and examine if it passes through C.
- 7. Repeat Question 6, if AB happens to be a diameter.
- 8. Draw a circle of radius 4 cm. Draw any two of its chords. Construct the perpendicular bisectors of these chords. Where do they meet?
- 9. Draw any angle with vertex O. Take a point A on one of its arms and B on another such that OA = OB. Draw the perpendicular bisectors of \overline{OA} and \overline{OB} . Let them meet at P. Is PA = PB ?

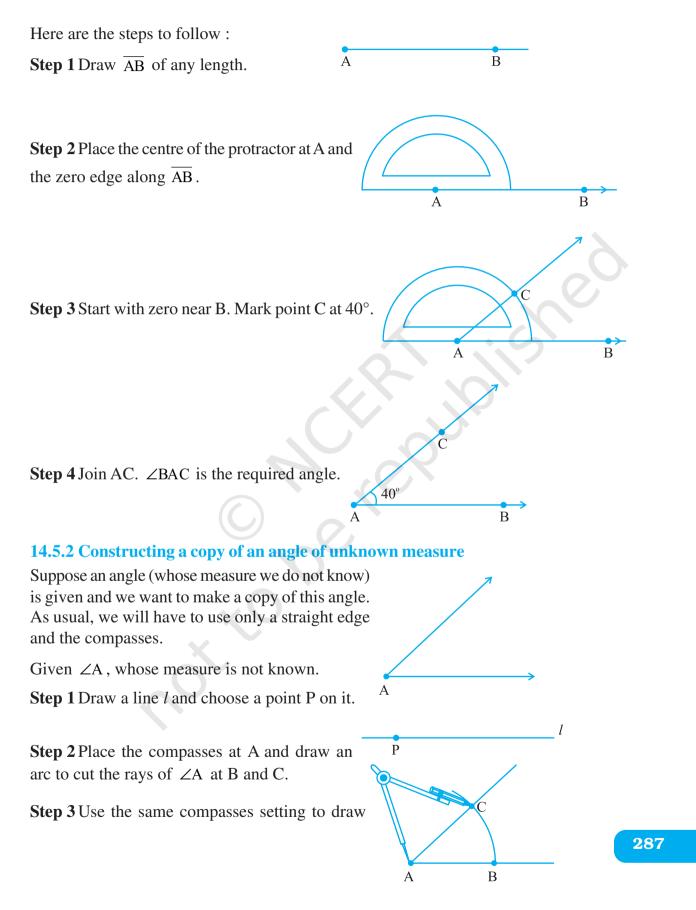
14.5 Angles

14.5.1 Constructing an angle of a given measure

Suppose we want an angle of measure 40°.



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an arc with P as centre, cutting l in Q.

Step 4 Set your compasses to the length BC with the same radius.

Step 5 Place the compasses pointer at Q and draw the arc to cut the arc drawn earlier in R.

Step 6 Join PR. This gives us $\angle P$. It has the same measure as $\angle A$.

This means $\angle QPR$ has same measure as $\angle BAC$.

14.5.3 Bisector of an angle

Do This er. Mark a point O

on it. With O as initial point, draw two

rays \overrightarrow{OA} and \overrightarrow{OB} . You get $\angle AOB$. Fold the sheet through O such that the

rays \overrightarrow{OA} and \overrightarrow{OB} coincide. Let OC be the crease of paper which is obtained after unfolding the paper.

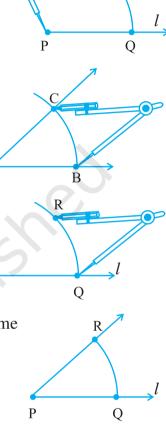
OC is clearly a line of symmetry for $\angle AOB$.

Measure $\angle AOC$ and $\angle COB$. Are they equal? OC the line of symmetry, is therefore known as the angle bisector of $\angle AOB$.

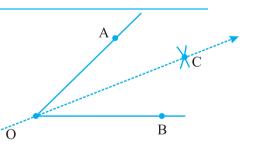
Construction with ruler and compasses

Let an angle, say, $\angle A$ be given.

Step 1 With A as centre and using compasses, draw an \swarrow arc that cuts both rays of $\angle A$. Label the points A



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of intersection as B and C.

Step 2 With B as centre, draw (in the interior of $\angle A$) an arc whose radius is more than half the length BC.

Step 3 With the same radius and with C as centre, draw another arc in the interior of $\angle A$. Let the two arcs intersect at D. Then \overline{AD} is the required bisector of $\angle A$.

Try These In Step 2 above, what would happen if we take radius to be smaller than half the length BC? 14.5.4 Angles of special A measures

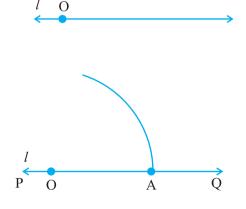
There are some elegant and accurate methods to construct some angles of special sizes which do not require the use of the protractor. We discuss a few here.

Constructing a 60° angle

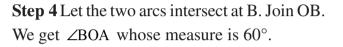
Step 1 Draw a line *l* and mark a point O on it.

Step 2 Place the pointer of the compasses at O and draw an arc of convenient radius which cuts the line PQ at a point say, A.

Step 3 With the pointer at A (as centre),



now draw an arc that passes through O.



Constructing a 30° angle

Construct an angle of 60° as shown earlier. Now, bisect this angle. Each angle is 30° , verify by using a protractor.

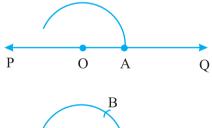
Constructing a 120° angle

An angle of 120° is nothing but twice of an angle of 60° . Therefore, it can be constructed as follows :

Step 1 Draw any line PQ and take a point O on it.

Step 2 Place the pointer of the compasses at O O and draw an arc of convenient radius which cuts the lir

O and draw an arc of convenient radius which cuts the line at A.



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B

B

A

A

Try These How will you construct a

 15° angle?

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Q

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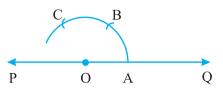
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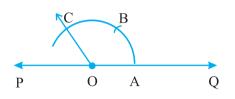
Step 3 Without disturbing the radius on the compasses, draw an arc with A as centre which cuts the first arc at B.

Step 4 Again without disturbing the radius on the compasses and with B as centre, draw an arc which cuts the first arc at C.



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Step 5 Join OC, \angle COA is the required angle whose measure is 120°.



Constructing a 90° angle

Construct a perpendicular to a line from a point lying on it, as discussed earlier. This is the required 90° angle.



EXERCISE 14.6

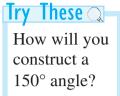
- 1. Draw $\angle POQ$ of measure 75° and find its line of symmetry.
- 2. Draw an angle of measure 147° and construct its bisector.
- 3. Draw a right angle and construct its bisector.
- 4. Draw an angle of measure 153° and divide it into four equal parts.
- 5. Construct with ruler and compasses, angles of following measures: (a) 60° (b) 30° (c) 90° (d) 120° (e) 45° (f) 135°
- 6. Draw an angle of measure 45° and bisect it.
- 7. Draw an angle of measure 135° and bisect it.
- 8. Draw an angle of 70°. Make a copy of it using only a straight edge and compasses.
- 9. Draw an angle of 40°. Copy its supplementary angle.

What have we discussed ?

This chapter deals with methods of drawing geometrical shapes.

- 1. We use the following mathematical instruments to construct shapes:
 - (i) A graduated ruler (ii) The compasses
 - (iii) The divider (iv) Set-squares (v) The protractor
- 2. Using the ruler and compasses, the following constructions can be made:
 - (i) A circle, when the length of its radius is known.
 - (ii) A line segment, if its length is given.
 - (iii) A copy of a line segment.
 - (iv) A perpendicular to a line through a point
 - (a) on the line (b) not on the line.

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Try These How will you construct a 45° angle?

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- (v) The perpendicular bisector of a line segment of given length.
- (vi) An angle of a given measure.
- (vii) A copy of an angle.
- (viii) The bisector of a given angle.
- (ix) Some angles of special measures such as
 - (a) 90° (b) 45° (c) 60° (d) 30° (e) 120° (f) 135°

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