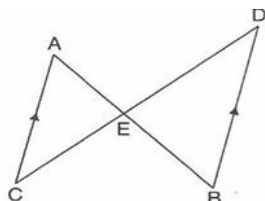


CBSE Test Paper 04
Chapter 6 Triangles

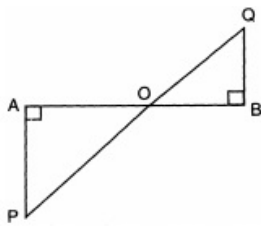
1. In the adjoining figure $AC \parallel BD$. If, $EB = 4$ cm, $ED = 8$ cm, $AC = 6$ cm, $AE = 3$ cm then CE and BD are respectively **(1)**



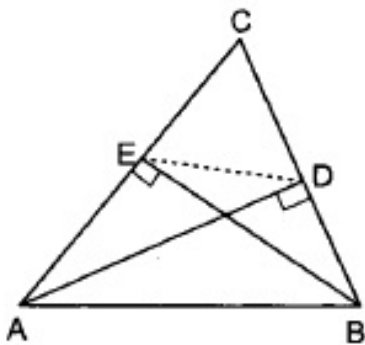
- a. 5 cm, 7 cm.
b. 7.5 cm, 9.5 cm.
c. 6 cm, 8 cm.
d. 4 cm, 6 cm.
2. A street light is fixed on a pole 6 m above the ground. If a woman of height 1.5 m casts a shadow of 3, then distance between her and the base of the pole is _____. **(1)**
- a. 12 m
b. 9 m
c. 8 m
d. 10 m
3. In an equilateral $\triangle ABC$, $AD \perp BC$ and $AD^2 = p \cdot BC^2$, then p is equal to **(1)**
- a. $\frac{1}{2}$
b. $\frac{3}{4}$
c. $\frac{2}{3}$
d. $\frac{1}{3}$
4. A street light is fixed on a pole 6 m above the ground. If a woman of height 1.5 m casts a shadow of 3, then distance between her and the base of the pole is **(1)**
- a. 12 m.
b. 8 m.
c. 9 m.
d. 10 m.
5. ABCD is a trapezium in which $AB \parallel DC$ and $AB = 2DC$. Diagonals AC and BD intersect at O. If $ar(\triangle AOB) = 84 \text{ cm}^2$, then $ar(\triangle COD)$ is equal to **(1)**

- a. 24 cm^2
- b. 42 cm^2
- c. 28 cm^2
- d. 21 cm^2

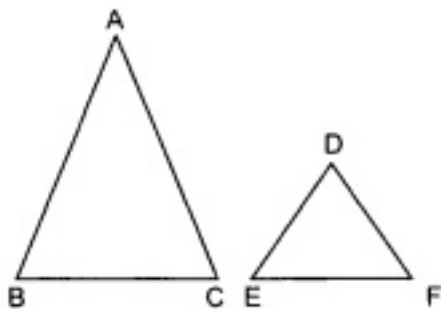
6. In the given figure, if $\angle A = 90^\circ$, $\angle B = 90^\circ$, $OB = 4.5 \text{ cm}$, $OA = 6 \text{ cm}$ and $AP = 4 \text{ cm}$, then find QB . **(1)**



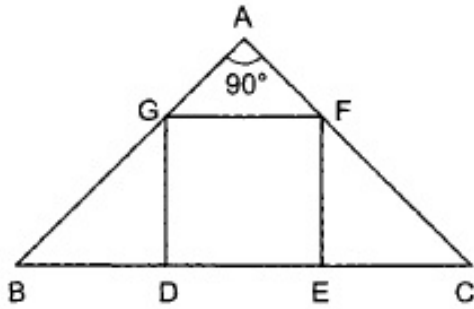
7. In Fig. AD and BE are respectively perpendiculars to BC and AC. Show that $\triangle ADC \sim \triangle BEC$ **(1)**



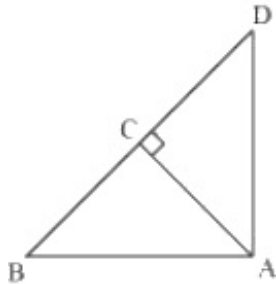
8. If $\triangle ABC \sim \triangle DEF$ such that $2AB = DE$ and $BC = 6 \text{ cm}$, find EF . **(1)**
9. In the given figure, $\triangle ABC \sim \triangle DEF$. If $AB = 2DE$ and area of $\triangle ABC$ is 56 sq. cm , find the area of $\triangle DEF$. **(1)**



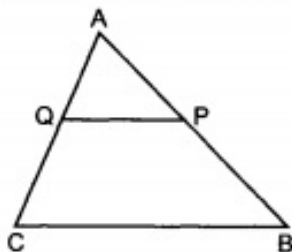
10. In Fig. DEFG is a square and $\angle BAC = 90^\circ$. Prove that $\triangle AGF \sim \triangle DBG$ **(1)**



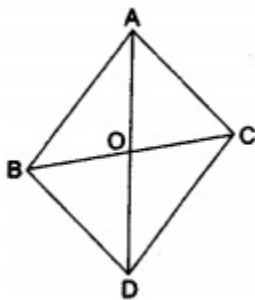
11. $\triangle ABD$ is a right triangle right-angled at A and $AC \perp BD$. Show that $AB^2 = BC \times BD$ (2)



12. In $\triangle ABC$, P and Q are points on sides AB and AC respectively such that $PQ \parallel BC$. If $AP = 4$ cm, $PB = 6$ cm and $PQ = 3$ cm, determine BC. (2)
13. In the fig., P and Q are points on the sides AB and AC respectively of $\triangle ABC$ such that $AP = 3.5$ cm, $PB = 7$ cm, $AQ = 3$ cm and $QC = 6$ cm. Find BC. (2)



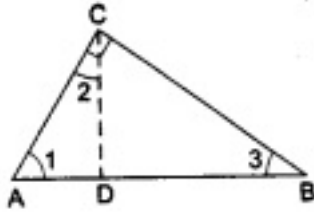
14. In the given figure, $\triangle ABC$ and $\triangle DBC$ are on the same base BC. If AD intersects BC at O, Prove that $\frac{\text{ar}(\triangle ABC)}{\text{ar}(\triangle DBC)} = \frac{AO}{DO}$. (3)



15. In a quadrilateral ABCD, P, Q, R, S are the mid-points of the sides AB, BC, CD and DA

respectively. Prove that PQRS is a parallelogram. **(3)**

16. In the given figure, $\angle ACB = 90^\circ$ and $CD \perp AB$. Prove that $CD^2 = BD \cdot AD$. **(3)**



17. From an airport, two aeroplanes start at the same time. If speed of first aeroplane due North is 500 km/h and that of other due East is 650 km/h then find the distance between the two aeroplanes after two hours. **(3)**

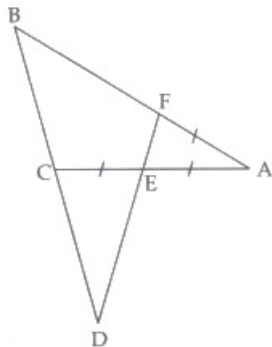
18. ABCD is a trapezium in which $AB \parallel DC$ and P and Q are points on AD and BC, respectively such that $PQ \parallel DC$. If $PD = 18$ cm, $BQ = 35$ cm and $QC = 15$ cm, find AD. **(4)**

19. Prove that the sum of the squares of the diagonals of a parallelogram is equal to the sum of the squares of its sides. **(4)**

20. In the given figure, line segment DF intersect the side AC of a triangle $\triangle ABC$ at the point E such that E is the mid-point of CA and $\angle AEF = \angle AFE$. Prove that: **(4)**

$$\frac{BD}{CD} = \frac{BF}{CE}.$$

[Hint: Take point G on AB such that $CG \parallel DF$.]



CBSE Test Paper 04
Chapter 6 Triangles

Solution

1. c. 6 cm, 8 cm.

Explanation: Given: $AC \parallel BD$ and $AC = 6$ cm, $AE = 3$ cm, $EB = 4$ cm, $ED = 8$ cm,
In triangles ACE and DEB, $\angle AEC = \angle DEB$ [Vertically opposite angles] $\angle ECA = \angle EDB$ [Alternate angles as $AC \parallel BD$]

$\therefore \triangle ACE \sim \triangle DEB$ [AA similarity]

$$\therefore \frac{EB}{AE} = \frac{ED}{EC}$$

$$\Rightarrow \frac{4}{3} = \frac{8}{EC}$$

$$\Rightarrow EC = \frac{8 \times 3}{4} = 6 \text{ cm}$$

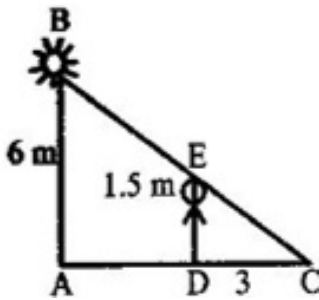
$$\text{Also } \frac{EB}{AE} = \frac{BD}{AC}$$

$$\Rightarrow \frac{4}{3} = \frac{BD}{6}$$

$$\Rightarrow BD = \frac{4 \times 6}{3} = 8 \text{ cm}$$

2. b. 9 m

Explanation: In triangles ABC and DEC,



$$\angle A = \angle D \text{ [Each } 90^\circ]$$

$$\angle C = \angle C \text{ [Common]}$$

Therefore, $\triangle ABC \sim \triangle DEC$ [AA similarity]

$$\Rightarrow \frac{AB}{DE} = \frac{AC}{DC}$$

$$\Rightarrow \frac{6}{1.5} = \frac{AC}{3} \Rightarrow AC = 12 \text{ m}$$

Therefore, the distance between the woman and pole is $12 - 3 = 9$ m

3. b. $\frac{3}{4}$

Explanation: In an equilateral triangle, ABC, if $AD \perp BC$,

$$\text{Then } AB^2 = AD^2 + BD^2$$

$$\Rightarrow AB^2 = AD^2 + \left(\frac{BC}{2}\right)^2$$

$$\Rightarrow BC^2 = AD^2 + \frac{BC^2}{4}$$

$$\Rightarrow AD^2 = BC^2 - \frac{BC^2}{4}$$

$$\Rightarrow AD^2 = \frac{3}{4}BC^2$$

Comparing with $AD^2 = p \cdot BC^2$

$$p = \frac{3}{4}$$

4. c. 9 m.

Explanation: AB - Lamp post and DE - Woman

In triangles ABC and DEC,

$$\angle A = \angle D \text{ [Each } 90^\circ]$$

$$\angle C = \angle C \text{ [Common]}$$

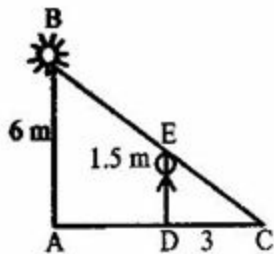
$\therefore \triangle ABC \sim \triangle DEC$ [AA similarity]

$$\therefore \frac{AB}{DE} = \frac{AC}{DC}$$

$$\Rightarrow \frac{6}{1.5} = \frac{AC}{3}$$

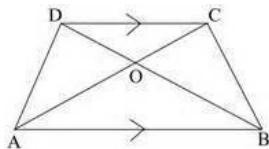
$$\Rightarrow AC = 12 \text{ m}$$

Therefore, distance between woman and pole = $AC - DC = 12 - 3 = 9 \text{ m}$



5. d. 21 cm^2

Explanation: In triangles, AOB and COD,



$$\angle AOB = \angle COD \text{ [vertically opposite angles]}$$

$$\angle ABO = \angle CDO \text{ [Alternate angles]}$$

Therefore, $\triangle AOB \sim \triangle COD$ [AA similarity]

$$\Rightarrow \frac{\text{area}(\triangle AOB)}{\text{area}(\triangle COD)} = \frac{AB^2}{DC^2} = \frac{(2DC)^2}{DC^2} = \frac{4}{1}$$

$$\Rightarrow \text{area}(\triangle COD) = \frac{84 \times 1}{4} = 21 \text{ cm}^2$$

6. In $\triangle PAO$ and $\triangle QBO$

$$\angle A = \angle B = 90^\circ$$

$$\angle POA = \angle QOB \text{ (Vertically Opposite Angle)}$$

$$\triangle PAO \sim \triangle QBO, \text{ (by AA criteria)}$$

$$\frac{OA}{OB} = \frac{PA}{QB}$$

$$\text{or, } \frac{6}{4.5} = \frac{4}{QB}$$

$$\text{or, } QB = \frac{4 \times 4.5}{6}$$

$$\text{Therefore, } QB = 3 \text{ cm}$$

7. In \triangle 's ADC and BEC, we have

$$\angle ADC = \angle BEC = 90^\circ \text{ [Given]}$$

$$\angle ACD = \angle BCE \text{ [Common]}$$

So, by AA-criterion of similarity, we obtain

$$\triangle ADC \sim \triangle BEC$$

8. Given that $\triangle ABC \sim \triangle DEF$

We know that when two triangles are similar, then the ratios of the lengths of their corresponding sides are equal.

$$\Rightarrow \frac{AB}{DE} = \frac{BC}{EF}$$

$$\Rightarrow \frac{1}{2} = \frac{6}{EF}$$

$$\Rightarrow EF = 12 \text{ cm}$$

9. $\triangle ABC \sim \triangle DEF$

Since for similar triangles, the ratio of the areas is the square of the ratio of their corresponding sides.

$$\therefore \frac{\text{Area } \triangle ABC}{\text{Area } \triangle DEF} = \frac{AB^2}{DE^2}$$

$$\Rightarrow \frac{56}{\text{area } \triangle DEF} = \frac{(2DE)^2}{DE^2}$$

$$\Rightarrow \frac{56}{\text{area } \triangle DEF} = 4$$

$$\Rightarrow \text{area } \triangle DEF = \frac{56}{4} = 14 \text{ cm}^2$$

10. In $\triangle AGF$ and $\triangle DBG$, we have

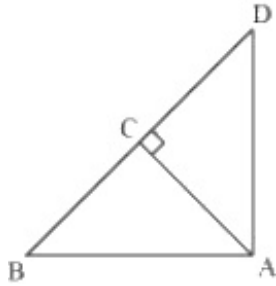
$$\angle GAF = \angle BDG \text{ [Each equal to } 90^\circ]$$

$$\text{and, } \angle AGF = \angle DBG \text{ [Corresponding angles]}$$

$$\therefore \triangle AGF \sim \triangle DBG \text{ [By AA-criterion of similarity]}$$

11. Given: $\triangle ABD$ is a right triangle right-angled at A and $AC \perp BD$.

To Prove: $AB^2 = BC \times BD$



Proof: In $\triangle ADB$ and $\triangle CAB$

$$\angle DAB = \angle ACB = 90^\circ$$

$$\angle ABD = \angle CBA \text{ [common angle]}$$

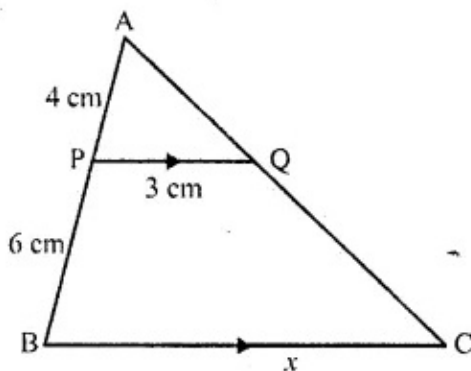
$$\angle ADB = \angle CAB \text{ [remaining angle]}$$

So, $\triangle ADB \sim \triangle CAB$ (by AAA similarity)

$$\text{Therefore } \frac{AB}{CB} = \frac{BD}{AB}$$

$$\Rightarrow AB^2 = CB \times BD$$

12. Let $BC = x$ cm



In \triangle 's APQ and ABC, we have,

$$\angle A = \angle A$$

$$\angle APQ = \angle ABC$$

Therefore, by AA criteria of similar \triangle 's, we have,

$$\therefore PQ \parallel BC$$

$$\therefore \triangle APQ \sim \triangle ABC$$

$$\therefore \frac{AP}{AB} = \frac{AQ}{AC} = \frac{PQ}{BC}$$

$$\Rightarrow \frac{AP}{AP+PB} = \frac{PQ}{BC}$$

$$\Rightarrow \frac{4}{4+6} = \frac{3}{x} \Rightarrow \frac{4}{10} = \frac{3}{x}$$

$$\Rightarrow x = \frac{10 \times 3}{4} = \frac{15}{2}$$

$$\therefore BC = \frac{15}{2} \text{ cm} = 7.5 \text{ cm}$$

13. According to question it is given that P and Q are points on the sides AB and AC respectively of $\triangle ABC$ such that AP = 3.5 cm, PB = 7 cm, AQ = 3 cm and QC = 6 cm.

$$\frac{AP}{PB} = \frac{3.5}{7} = \frac{1}{2} \dots\dots(\text{i})$$

$$\frac{AQ}{QC} = \frac{3}{6} = \frac{1}{2} \dots\dots(\text{ii})$$

from (i) and (ii), we have

$$\frac{AP}{PB} = \frac{AQ}{QC}$$

$$\therefore PQ \parallel BC$$

$$\therefore \angle AQP = \angle ACB$$

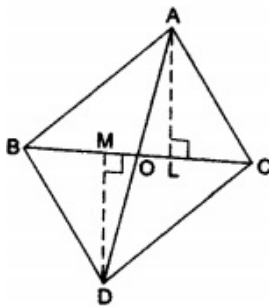
and $\angle APQ = \angle ABC$ (corresponding angles)

$$\therefore \triangle AQP \sim \triangle ACB \text{ (AA similarity)}$$

$$\Rightarrow \frac{PQ}{BC} = \frac{AQ}{AC} = \frac{AQ}{AQ+QC} \text{ (By definition of SSS similarity)}$$

$$\Rightarrow \frac{4.5}{BC} = \frac{3}{9} \Rightarrow BC = 13.5 \text{ cm}$$

14. Given: $\triangle ABC$ and $\triangle DBC$ are on the same base BC and AD intersects BC at O.



$$\text{To Prove } \frac{\text{ar}(\triangle ABC)}{\text{ar}(\triangle DBC)} = \frac{AO}{DO}.$$

Construction Draw $AL \perp BC$ and $DM \perp BC$.

Proof: In $\triangle ALO$ and $\triangle DMO$, we have

$$\angle ALO = \angle DMO = 90^\circ$$

and $\angle AOL = \angle DOM$ (vertical opposite angles)

$$\therefore \triangle ALO \sim \triangle DMO \text{ [by AA-similarity]}$$

$$\Rightarrow \frac{AL}{DM} = \frac{AO}{DO}$$

$$\therefore \frac{\text{ar}(\triangle ABC)}{\text{ar}(\triangle DBC)} = \frac{\frac{1}{2} \times BC \times AL}{\frac{1}{2} \times BC \times DM} = \frac{AL}{DM} = \frac{AO}{DO} \text{ [using (i)]}$$

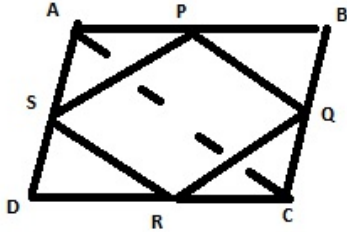
$$\text{Hence, } \frac{\text{ar}(\triangle ABC)}{\text{ar}(\triangle DBC)} = \frac{AO}{DO}$$

15. To Prove: PQRS is a parallelogram

Construction: Join AC

Proof: In $\triangle DAC$

$$\frac{DS}{SA} = \frac{DR}{RC} = 1$$



[\because S and R are mid-points of AD and DC]

$\Rightarrow SR \parallel AC$ (i) [by converse of B.P.T]

In $\triangle BAC$, $\frac{PB}{AP} = \frac{BQ}{QC} = 1$ [\because P and Q are midpoints of AB and BC]

$\Rightarrow PQ \parallel AC$ (ii) [By converse of B.P.T]

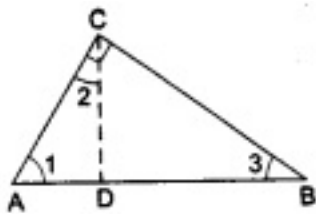
From (i) and (ii), we get

$SR \parallel PQ$ (iii)

Similarly, join B to D and PS \parallel QR

$\Rightarrow \therefore$ PQRS is a parallelogram.

16. It is given that in $\triangle ABC$, $\angle ACB = 90^\circ$ and $CD \perp AB$.



To Prove: $CD^2 = BD \cdot AD$

Proof: In right $\triangle ADC$, we have

$$\angle 1 + \angle 2 = 90^\circ \text{(i)}$$

In right $\triangle ACB$, we have

$$\angle 1 + \angle 3 = 90^\circ \text{(ii)}$$

From (i) and (ii) we have

$$\angle 1 + \angle 2 = \angle 1 + \angle 3$$

$$\Rightarrow \angle 2 = \angle 3$$

In $\triangle ADC$ and $\triangle CDB$, we have

$$\angle 2 = \angle 3 \quad (\text{proved})$$

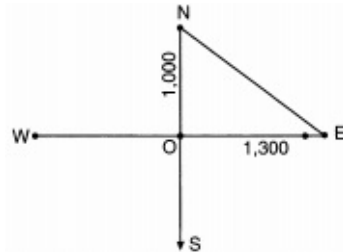
$$\text{and } \angle ADC = \angle CDB = 90^\circ$$

$$\therefore \triangle ADC \sim \triangle CDB \quad [\text{by AA-similarity}]$$

$$\therefore \frac{AD}{CD} = \frac{CD}{BD}$$

$$\text{Hence, } CD^2 = BD \cdot AD.$$

17.



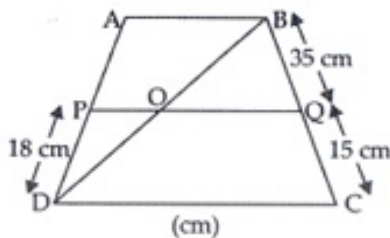
Distance covered by first aeroplane due North after two hours = $ON = 500 \times 2 = 1000$ km

Distance covered by second aeroplane due East after two hours $OE = 650 \times 2 = 1300$ km

As per shown in the figure the distance between the aeroplane will be equal to NE, Now in $\triangle ONE$

$$\begin{aligned} NE &= \sqrt{ON^2 + OE^2} \\ &= \sqrt{1000^2 + 1300^2} = \sqrt{2690000} = 1640.12 \text{ km} \end{aligned}$$

18. In trapezium ABCD



$AB \parallel CD$ (Given)

$PQ \parallel DC$ (Given)

and $PD = 18$ cm, $BQ = 35$ cm and $QC = 15$ cm

To find: AD

$$\therefore AB \parallel CD \parallel PQ \dots\dots(i)$$

In $\triangle BCD$,

$OQ \parallel CD$ [From (i)]

$$\therefore \frac{BO}{OD} = \frac{BQ}{QC} \text{ (ii) [By BPT]}$$

Similarly, in $\triangle DAB$,

$PO \parallel AB$ [From (i)]

$$\therefore \frac{BO}{OD} = \frac{AP}{PD} \text{ (iii) [By BPT]}$$

From (ii) and (iii)

$$\frac{AP}{PD} = \frac{BQ}{QC}$$

$$\Rightarrow \frac{AP}{18} = \frac{35}{15}$$

$$\Rightarrow AP = \frac{35}{15} \times 18 = 7 \times 6$$

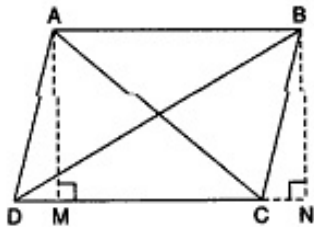
$$\Rightarrow AP = 42 \text{ cm}$$

$$\therefore AD = AP + PD = 42 \text{ cm} + 18 \text{ cm} = 60 \text{ cm}.$$

19. Given: ABCD is a parallelogram whose diagonals are AC and BD.

To prove: $AB^2 + BC^2 + CD^2 + DA^2 = AC^2 + BD^2$

Construction: Draw $AM \perp DC$ and $BN \perp D(\text{Produced})$



Proof: In right triangle AMD and BNC.

$AD = BC$ Opp.sides of a || gm

$AM = BN$ Both are altitudes of the same parallelogram to the same base

$\therefore \triangle AMD \cong \triangle BNC$ RHS congruence criterion

$\therefore MD = NC$ (1).....CPCT

In right triangle BND,

$$\therefore \angle N = 90^\circ$$

$$\therefore BD^2 = BN^2 + DN^2 \text{By Pythagoras theorem}$$

$$= BN^2 + (DC + CN)^2$$

$$= BN^2 + DC^2 + CN^2 + 2DC.CN$$

$$= (BN^2 + CN^2) + CN^2 + 2DC.CN$$

$$= BC^2 + DC^2 + 2DC.CN \text{(2)}$$

In right triangle BNC with $\angle N = 90^\circ$

$$BN^2 + CN^2 = BC^2 \text{By Pythagoras theorem}$$

In right triangle AMC

$$\therefore \angle M = 90^\circ$$

$$\therefore AC^2 = AM^2 + MC^2$$

$$\begin{aligned}
&= AM^2 = (DC - DM)^2 \\
&= AM^2 + DC^2 + DM^2 - 2DC.DM \\
&= (AM^2 + DC^2) + DC^2 - 2DC.DM \\
&= AD^2 + DC^2 - 2DC.DM
\end{aligned}$$

\therefore In right triangle AMD with $\angle M=90^\circ$

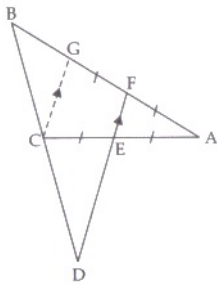
$$AD^2 = AM^2 + DM^2 \dots\dots\dots[\text{By Pythagoras theorem}]$$

$$= AD^2 + AB^2 - DC.CN \dots\dots\dots\text{From(1)}$$

Adding (3) and (2), we get

$$AC^2 + BD^2 = (AD^2 + AB) + (BC^2 + DC) = AB^2 + BC^2 + BC^2 + CD^2 + DA^2$$

20. To Prove: $\frac{BD}{CD} = \frac{BF}{CE}$



Construction: Draw $CG \parallel EF$.

Proof: In $\triangle AGC$ $CG \parallel EF$

\therefore E is the mid point of AC

\therefore F will be the mid point of AG.

$$\Rightarrow FG = FA$$

But, $EC = EA = AF$ [Given]

$$\therefore FG = FA = EA = EC \dots\dots(i)$$

In $\triangle BCG$ and $\triangle BDF$

$EF \parallel CG$. (By construction)

$$\therefore \frac{BC}{CD} = \frac{BG}{GF} \text{ [By BPT]}$$

$$\Rightarrow \frac{BC}{CD} + 1 = \frac{BG}{GF} + 1 \Rightarrow \frac{BC+CD}{CD} = \frac{BG+GF}{GF}$$

$$\Rightarrow \frac{BD}{CD} = \frac{BF}{GF}$$

But, $FG = CE$ [From (i)]

$$\Rightarrow \frac{BD}{CD} = \frac{BF}{CE} \text{ Hence, proved.}$$