

MANUAL

FOR

SECONDARY

MATHEMATICS KIT

PREFACE

One of the most significant recommendations of the National Curriculum Framework (NCF)-2005 is the mathematisation of the child's thought processes. In achieving this goal, concrete mathematical experiences play a major role. A child is motivated to learn mathematics by getting involved in handling various concrete manipulants in various activities. In addition to activities, games in mathematics also help the child's involvement in learning by strategising and reasoning. For learning mathematical concepts through the above-mentioned approach, a child-centred Mathematics kit has been developed for the students of Secondary stage based on some of the concepts from the newly developed NCERT mathematics textbooks. The kit includes various kit items along with a manual for performing activities. The kit broadly covers the activities in the areas of geometry, algebra, trigonometry and mensuration. The kit has the following advantages :

- Availability of necessary materials at one place
- Multipurpose use of items
- Economy of time in doing the activities
- Portability from one place to another
- Provision for teacher's innovation
- Low-cost material and use of indigeneous resources

Here are some of the special features of the kit items :-

Two variety of plastic strips with slots and markings have been provided. They help in creating angles, triangles, quadrilaterals and determination of values of trigonometric ratios. The full or half protractor can be fixed on the strips for measuring the angles in the activities related to angles, triangles, and quadrilaterals.

A Circular Board is designed in such a manner that it can be used to verify results related to a circle as well as trigonometric ratios.

A Geoboard is a board of dimensions $19\text{cm} \times 19\text{cm} \times 1\text{cm}$ having holes drilled on side A of it at a distance of 1cm each. Geoboard pins can be fitted in the holes and with the help of rubber bands different geometrical shapes can be formed.

Cut-outs of corrugated sheets in the form of parallelogram, triangle, trapezium and circle help in learning concepts related to areas.

A cube with adjusting cut-outs of cuboid, cylinder, cone and hemisphere have been given to construct the concept of surface area and volume.

Cut-outs of plastic cardboard in the form of triangles, quadrilaterals and rectangle etc. have been given to verify Pythagoras theorem and algebraic identities like $a^2 - b^2 = (a - b)(a + b)$.

Another interesting item, Algebraic Tiles has also been provided. They are provided in two different colours and three different sizes. They can be used for concretisation of the concept of factorisation of quadratic equations.

The kit items, apart from being academically useful, are also designed in attractive manner. It is hoped that this kit will generate enough interest for learning mathematics at secondary stage. It will prove to be an important part of the mathematics resource room in the schools across the country.

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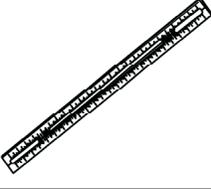
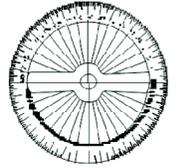
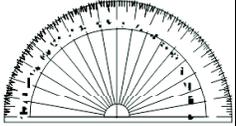
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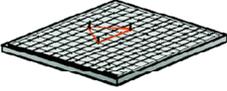
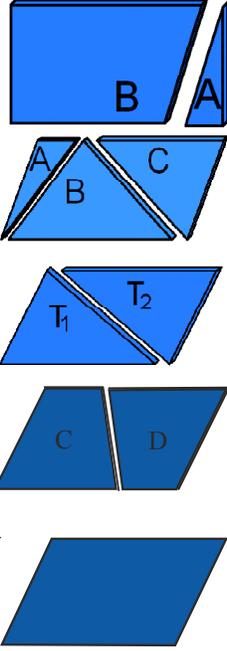
opposite angles of a non cyclic quadrilateral is not equal to 180°

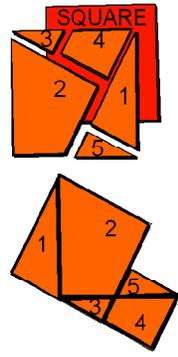
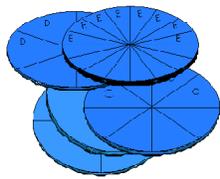
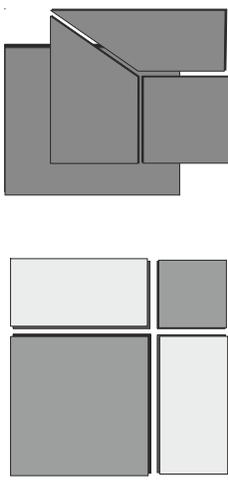
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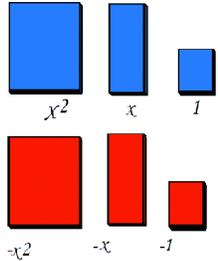
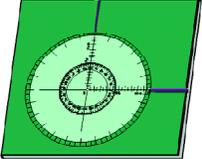
SECONDARY MATHEMATICS KIT

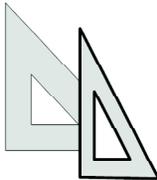
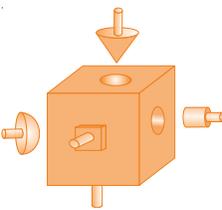
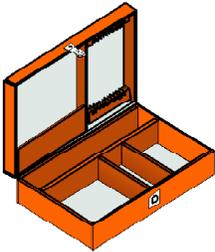
Technical Specification

S. No.	Item	Figure/Name	Specification Shapes	No.Off
1	Plastic Strip (A Type)		264 × 20 × 2mm ³ cuboidal perspex having 3 slots of 5mm width at (0-30)mm, (50-200)mm and (220-250)mm As per sample	08
2	Plastic Strip (B Type)		264 × 20 × 2mm ³ cuboidal perspex having 3 slots of 5mm width at (0-0.3)dm, (0.5-2.0)dm & (2.2-2.5)dm As per sample	03
3	Full Protractor (360°)		A 2mm thick circular transparent plastic sheet of dia 120 mm marked in (0-360) degrees. As per sample	04
4	Half Protractor (180°)		A 2mm thick semi circular transparent plastic sheet of dia 90 mm marked in (0-180) degrees As per sample	04
5	Fly nut and screw		It is a combination of nut with wing and chromium plated screw with metric thread (M ₄) of length 15mm made up of wild steel haing slotted round head or HDPE molded As per sample	15 Sets

6	Geo-board		190×190×10mm ³ A B S material board having grid of 10mm squares with a hole of 1mm dia. at the corners of each square except boundary corners of square. As per sample	01
7	Geo-board Pins		Solid cylindrical pins of length 18mm and dia 2mm made up of stainless steel. As per sample	10
8	Rubber bands		Small multicolours rubber band. standard item. As per sample	20
9	Cutouts (For area of polygons)		Different shapes cut-outs of a 3mm thick blue coloured corrugated sheets. The shapes are as follows. (1) A triangle and a trapezium marked as A and B respectively (2) Three triangles marked as A, B and C (3) Two triangles marked as T ₁ & T ₂ respectively (4) Two trapezium marked as C & D respectively (5) A parallelogram As per sample	01 Set each

10	<p>CutOuts (For Pythagoras Theorem)</p>		<p>Made up of 3mm thick cardboard and includes:-</p> <ol style="list-style-type: none"> (1) square of side 125 mm (2) 5 cut-outs of different shapes obtained from another square of side 125mm (3) Riangular cut-out of hypotenuse 125mm (4) Two squares of sides equal to height and base of triangular cut-out <p>As per sample</p>	<p>01 Set each</p>
11	<p>Cutouts (For area of a circle)</p>		<p>5 Blue coloured circular corrugated sheets having 3mm thickness and dia 160 mm. divided into 4, 6, 8, 12, and 16 equal sectors .</p> <p>As per sample</p>	<p>01 Set each</p>
12	<p>Cutouts (For Aigebraic identities)</p>		<p>Made up of 3mm thick cardboard and includes</p> <ol style="list-style-type: none"> (1) Square cut-out of side 76 mm (2) 3 cut-outs obtained from another square of side 76mm out of which one is a square of side 38mm and the remaining two are trapezium of dim. $38 \times 76 \text{ mm}^2$ (3) Square cut-outs of side 80 mm and 45 mm (4) Rectangular cut-out 	<p>01 set each</p>

			of dimension $80 \times 45 \text{ mm}^2$ As per sample	
13	Algebraic Tiles a) x^2 , x , 1 b) $-x^2$, $-x$, -1		<p>Made up of plastic cardboard in 3 different sizes:</p> <p>40 (20red+20blue) squares of side 10mm known as unit tiles.</p> <p>20 (10red+10blue) rectangles of $50 \times 10 \text{ mm}^2$ dimension know as x or -x tiles</p> <p>10 (5 red + 5 blue) squares of side 50mm known as x^2 or $-x^2$ tiles.</p> <p>As per sample</p>	01 set each
14	Trigonometric Circular Board		<p>A $260 \times 260 \times 10 \text{ mm}^3$ board having a 5mm wide and 6mm deep circular groove on its left side. The inner circle of circular groove has a 6mm hole at the centre and 200mm dia. with coordinate axis marked on it. It is also marked in degrees (1 unit=5). the board has 3 rectangular grooves touching the circular groove and has 14 holes of dia. 6mm.</p> <p>As per sample</p>	01
15	Connectors (For circular board)		<p>Stainless steel rubber sleeved screw having 25mm length, 5mm dia. and a round head.</p> <p>As per sample</p>	15

16	Connectors (For strip)		Flat round headed screw of length 20mm, dia. 4mm with split ends and rubber sleeve. As per sample	10
17	Set Square		As per standard medium size. As per sample.	01 set each
18	Rotating Needle		Steel rod of length 200mm and dia 3mm. with one 'L' band at one side of rod. As per sample	01
19	Cut-outs with Cube a) Cone b) Cuboids c) Cylinder d) Hemisphere		Solid Cube of side 60mm having following cut-outs fitted in it - (1) Cuboid of dimension $30 \times 30 \times 15 \text{ mm}^3$ (2) Cone of height 30mm dia. 30mm (3) Hemisphere of dia. 30mm. (4) Cylinder of height 20mm & dia. 20mm As per sample	01 set each
20	Kit Box along with carton		$425 \times 300 \times 125 \text{ mm}^3$ box with suitable hinges and lock system provided with pockets inside to keep the kit items. As per sample	01

Activity 1

MEASUREMENT OF ANGLES

OBJECTIVE:

To form different angles and measure them.

MATERIAL REQUIRED:

Two plastic strips, full protractor, fly screws.

HOW TO PROCEED?

1. Take two plastic strips and a full protractor.
2. Fix the strips along with the protractor at their end points with a fly screw.
3. Fix one of the strips along the 0° - 180° marked line of the protractor as shown below in Fig. 1.



Fig.1. Zero Angle

4. By moving the other strip [in anticlockwise direction], try to make angles of different measures [Fig.1, Fig.2, Fig.3, Fig.4, Fig.5, Fig.6 and Fig.7].

Fill in the blanks after observing the measure of various

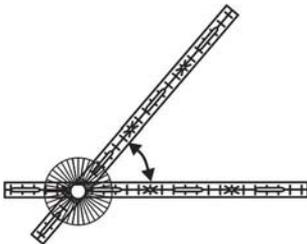


Fig. 2. Acute angle

Note:

1. All angles are to be measured in anticlockwise direction from first strip.
2. Use the markings of the scale of the protractor carefully.

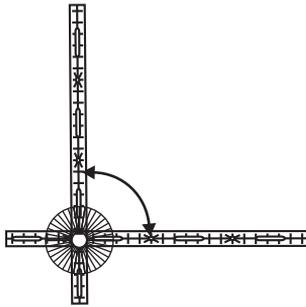


Fig. 3. Right angle

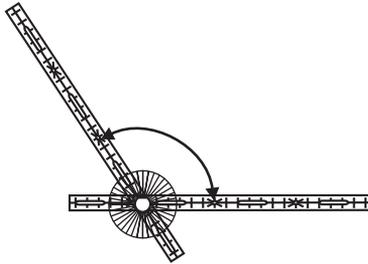


Fig. 4. Obtuse angle

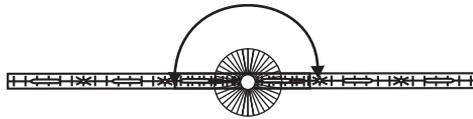


Fig. 5. Straight angle

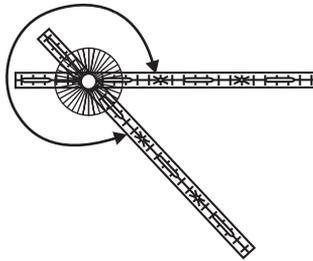


Fig. 6. Reflex angle

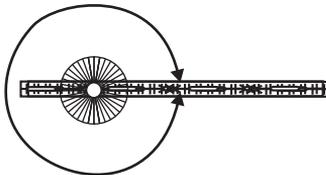


Fig. 7. Complete angle

Fill in the blanks after observing the measure of various angles so formed with protractor and plastic strips:

Right angle is formed when the measure is _____.

Straight angle is formed when the measure is _____.

Complete angle is formed when the measure is _____.

Acute angle is formed when the measure is _____.

Obtuse angle is formed when the measure is _____.

Reflex angle is formed when the measure is _____.

Measuring angles with starting point of any degree other than zero degree:

Now fix the first strip along with the 30° marked line of the protractor and second strip along with 70° marked line of the protractor.

- What is the measure of the angle formed?
- What type of angle is it?

The angle so formed is an acute angle of measure $70^\circ - 30^\circ = 40^\circ$. Similarly, take the two strips at different marked lines of the protractor and then complete the following table:

S. No.	Position of first strip (A)	Position of Second strip (B)	Measure of angle (B-A)	Type of angle
1.	10°	50°	40°	Acute
2.	25°	60°	-----	-----
3.	-----	170°	135°	-----
4.	50°	200°	-----	-----
5.	-----	115°	-----	Right
6.	-----	230°	180°	-----

Now, fix the first strip at 40° . Give measures of some more angles by which the second strip will be moved in anticlockwise direction to complete the following table:

S. No.	Position of first strip	Position of Second strip	Measure of angle	Type of angle
1.	40°			Acute
2.	40°			Obtuse
3.	40°			Right
4.	40°			Straight
5.	40°			Reflex

-----* * * * *-----

Activity 2

TWO PARALLEL LINES AND A TRANSVERSAL

OBJECTIVE:

To verify the relation of different pairs of angles formed by a transversal with two parallel lines.

MATERIAL REQUIRED:

3 plastic strips, two full protractors and fly screws.

HOW TO PROCEED?

1. Take three strips and two full protractors and fix them with the help of fly screws in such a manner that the two strips are parallel to each other and the third strip is a transversal to them as shown in Fig.1.

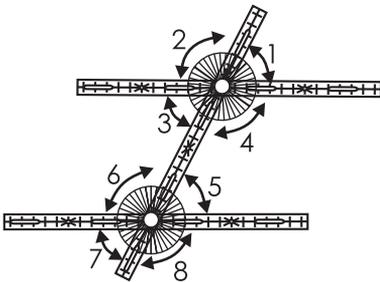


Fig 1

Think

How would you check whether two strips are parallel or not?

2. Measure all the angles so formed numbered from 1 to 8 and complete the following tables.

Table A: - Corresponding angles

S. No.	Name of the angle	Measure of the angle	Name of the angle	Measure of the angle	Observation (Relationship)
1.	$\angle 1$	52°	$\angle 5$	52°	Equal
2.	$\angle 2$		$\angle 6$		
3.	$\angle 3$		$\angle 7$		

Inference :

Table B:- Alternate interior and exterior angles

S. No.	Name of the angle	Measure of the angle	Name of the angle	Measure of the angle	Observation (Relationship)
1.	$\angle 3$	52°	$\angle 5$	52°	Equal
2.	$\angle 4$		$\angle 6$		
3.	$\angle 1$		$\angle 7$		
4.	$\angle 2$		$\angle 8$		

Inference :

Table C: - Interior angles on the same side of the transversal

S. No.	Name of the angle	Measure of the angle	Name of the angle	Measure of the angle	Observation
1.	$\angle 4$	128°	$\angle 5$	52°	$\angle 4 + \angle 5 = 180^\circ$
2.	$\angle 3$		$\angle 6$		

Inference :

- Now, fix these strips and two protractors in such a manner that the two strips are not parallel to each other

and the third strip is transversal to them as shown in Fig. 2.

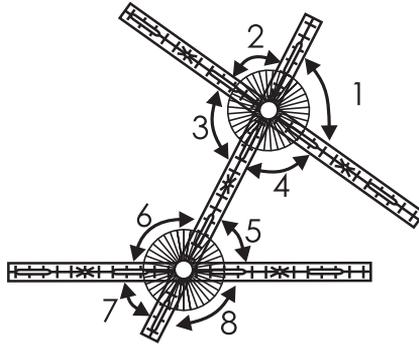
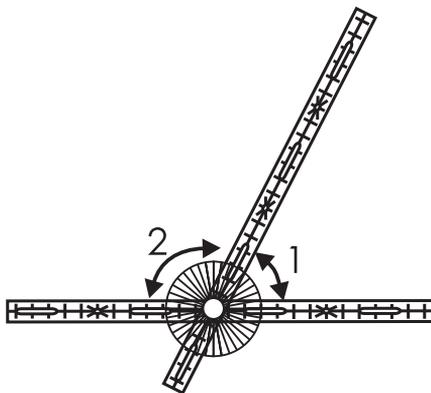


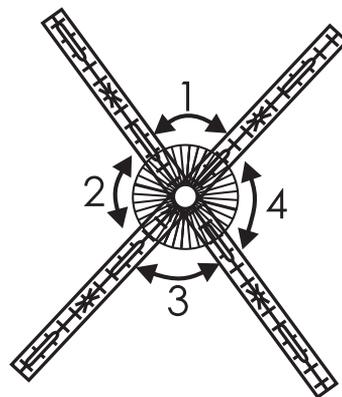
Fig. 2

Repeat the activity and fill the Tables A, B, and C given above.

You can also observe the properties of vertically opposite angles and linear pair using the set up as shown below.



(i) For linear pair.



(ii) For vertically opposite angle.

Q1: Verify the result for linear pair and vertically opposite angle using Fig.2.

Q2: Can you correlate this activity with 5th Euclids postulate?

Ans: If a straight line intersecting with two straight lines makes the interior angles on the same side of it, taken together are less than two right angles, then the two straight lines if produced indefinitely, meet on that side on which the sum of angles is less than two right angles.

-----* * * * *-----

Activity 3

PROPERTIES OF A TRIANGLE

OBJECTIVE:

To explore the properties of a triangle.

MATERIAL REQUIRED:

Three plastic strips, three half protractors or full protractors, fly screws.

HOW TO PROCEED?

1. Fix the strips along with protractors as shown in Fig. 1. Two strips can be joined, if needed.

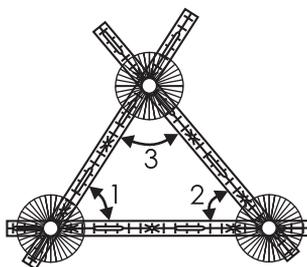


Fig.1

2. Form different triangles by moving the strips. Also measure the angles (interior as well as exterior taken in an order) and the sides of the triangles so formed and explore its properties.

Angle Sum Property of a Triangle

Vary the angles of the triangle, and note their measurement to find out the relationship between its angles.

S. No.	Angle1	Angle2	Angle3	$\angle 1 + \angle 2 + \angle 3$
1.				
2.				
3.				

Inference :

Exterior Angle Property

Look at the exterior angles formed by the extended side and the respective interior opposite angles of the triangle. Note down their measurements to find out the relationship.

S. No.	Exterior Angle	Interior Opposite Angle	Sum of interior opposite angles
1.			
2.			
3.			

Inference :

Isosceles Triangle

Form different triangles having two equal sides (Fig .2) by moving the strips and note down the measure of sides and angles of the triangles so formed.

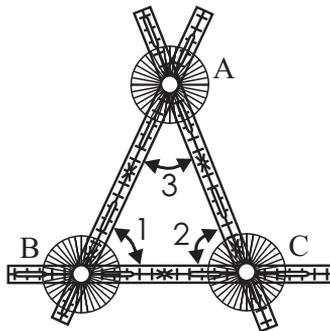


Fig.2

S. No.	Length of the side			Measure of the angle			Equal Sides	Equal angles
	AB	BC	AC	$\angle 1$	$\angle 2$	$\angle 3$		
1.								
2.								
3.								

Inference :

Equilateral Triangle

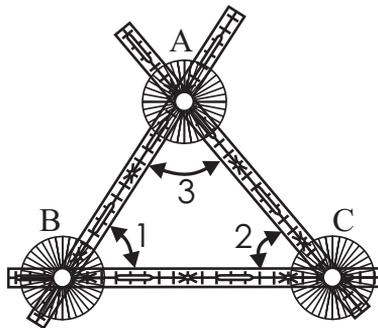


Fig.3

Form different triangles having all three sides equal (Fig.3) by moving the strips and note down the measure of sides and angles of the triangles so formed in the following table.

S. No.	Length of the side			Measure of the angle		
	AB	BC	AC	$\angle 1$	$\angle 2$	$\angle 3$
1.						
2.						
3.						

Inference :

Scalene Triangle

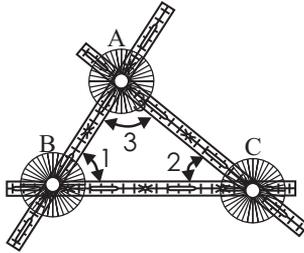


Fig.4

Form different scalene triangles (Fig.4) by moving the strips and note down the measure of sides and angles of the triangles so formed in the following table.

S. No.	Length of the side			Measure of the angle		
	AB	BC	AC	$\angle 1$	$\angle 2$	$\angle 3$
1.						
2.						
3.						

Inference :

Angle opposite to longest side in a triangle

Vary the length of one side so that it becomes longest. Measure sides, angles and note down in the table. Similarly vary the angle to make it biggest and note. Explore the relationship between two angle and side opposite to them.

S. No.	Length of the side			Measure of the angle			Longer side	Greater angle
	AB	BC	AC	$\angle 1$	$\angle 2$	$\angle 3$		
1.								
2.								
3.								

Inference :

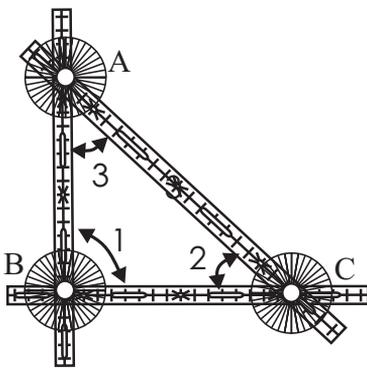
Sum of any two sides in a triangle

Make triangles of different side lengths and note their measurements in the table. Explore the relationship of sum of two sides with the third side.

S. No.	Length of the side			AB + BC	BC + AC	AB + AC
	AB	BC	AC			
1.						
2.						
3.						

Inference :

Right Triangle



Do the squares of the sides have some relationship

Fig.5

Make different right triangles (Fig.5) by moving the strips and complete the following table:

S. No.	Length of the side			Measure of the angle			Longest side	Square of the length of the sides		
	AB	BC	AC	$\angle 1$	$\angle 2$	$\angle 3$		AB^2	BC^2	AC^2
1.										
2.										
3.										

Inference :

-----* * * * *-----

Activity 4

MID-POINT THEOREM

OBJECTIVE:

To verify the mid-point theorem “A line joining the mid points of a triangle is parallel to the third side and half of it”.

MATERIAL REQUIRED:

Four plastic strips, two half protractors, fly screws.

HOW TO PROCEED?

1. Fix 3 strips to form a triangle ABC and one half protractor at one vertex (say B) as shown in Fig. 1

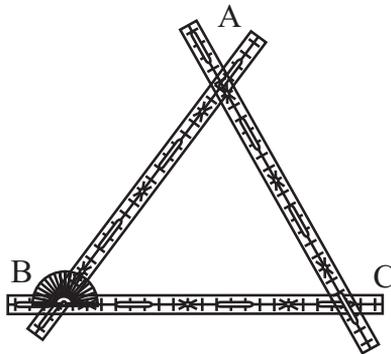


Fig.1

2. Fix one more strip at the mid-points say D of one of the side AB of the triangle alongwith a half protractor.
3. Now adjust this strip so that it also passes through the mid point say E of the other side AC as shown in Fig.2.

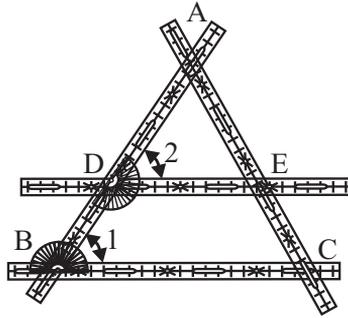


Fig.2

4. Now measure the angles shown by the two protractors.
5. Also measure length of the side BC and DE.
6. Repeat the above activity by forming different types of triangles with the help of strips in different orientations.
7. Now complete the following table:

S. No.	$\angle 1$	$\angle 2$	Is $\angle 1 = \angle 2$?	Length of BC	Length of DE	Is $DE = \frac{1}{2} BC$?
1.						
2.						
3.						

Inference : Since $\angle 1 = \angle 2$,

so $DE \dots\dots\dots BC$ and $DE = \frac{1}{2} \times \dots\dots\dots$

-----* * * * *-----

Activity 5

CONVERSE OF MID-POINT THEOREM

OBJECTIVE:

To verify that a line drawn through the mid point of one side and parallel to the second side bisects the third side.

MATERIAL REQUIRED:

Four plastic strips, two half protractors, fly screws.

HOW TO PROCEED?

1. Fix 3 strips to form a triangle ABC and a half protractor at one of the vertices say B as shown in the Fig 1.

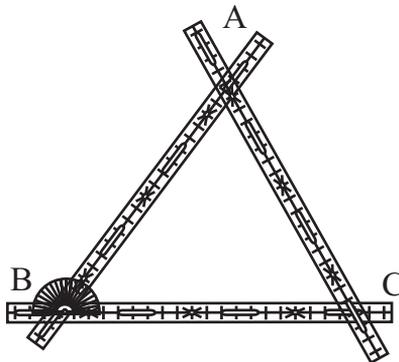


Fig.1

2. Fix another strip and a protractor at the mid-point say D of one of the sides say AB of the triangle so that it intersects the third side of triangle at E.
3. Now adjust this strip so that the angles shown on the two protractors are equal as shown in the Fig.2.

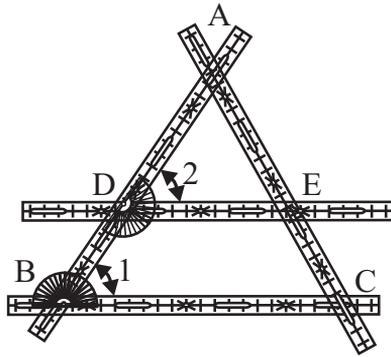


Fig. 2

4. These are corresponding angles so strip DE parallel BC.
5. Now measure the lengths AE and EC.
6. Repeat the above activity by forming different types of triangles and complete the following table:

S. No.	AE	EC	Is AE = EC?
1.			
2.			
3.			

Inference :

----- * * * * * -----

Activity 6

BASIC PROPORTIONALITY THEOREM

OBJECTIVE:

To verify the Basic Proportionality Theorem “If a line drawn parallel to one side of a triangle to intersects the other two sides than it divides them in same proportion”.

MATERIAL REQUIRED:

4 plastic strips, two half protractors, fly screws

HOW TO PROCEED?

1. Fix 3 strips to form a triangle ABC and one half protractor at one of the vertices say B as shown in Fig.1.

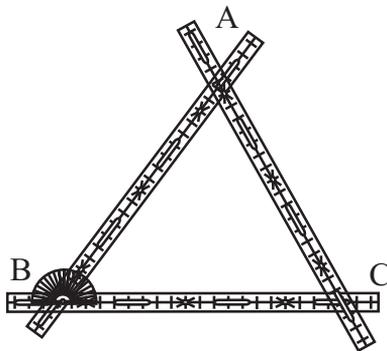


Fig. 1

2. Fix another strip at any convenient point say D on one of the sides of the triangle so that the ratio of AD and DB can be calculated easily.
3. Now adjust this strip so that the angles on the two protractors are equal as shown in the Fig.2.

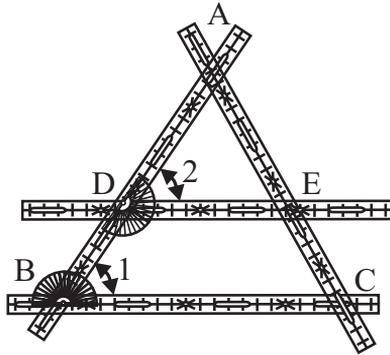


Fig. 2

4. Now measure the length of AD, DB, AE and EC.
5. Repeat the above activity by forming different types of triangles and complete the following table:

S. No.	AD	DB	AD : DB	AE	EC	AE : EC	Is $AB:DB=AE:EC$?
1.							
2.							
3.							

Inference :

Since $\angle 1 = \angle 2$

so $DE \parallel \dots\dots\dots$

If a line is drawn parallel to one side of a triangle to intersect the other two sides then it divided them $\dots\dots\dots$

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Activity 7

CONVERSE OF BASIC PROPORTIONALITY THEOREM

OBJECTIVE:

To verify that a line dividing two sides of a triangle in the same ratio is parallel to the third side.

MATERIAL REQUIRED:

4 plastic strips, two half protractors, fly screws

HOW TO PROCEED?

1. Fix 3 strips to form a triangle ABC having a half protractor at one of the vertices say B as shown in the fig. 1.

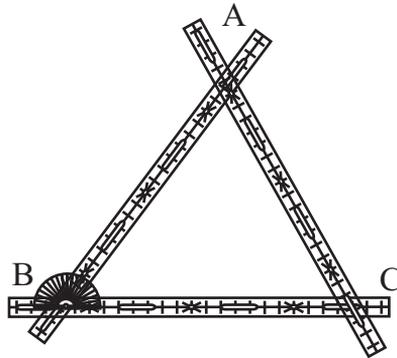


Fig. 1

2. Fix another strip at a convenient point say D on side AB and point say E on side AC, such that the ratios $AD : DB$ and $AE : EC$ are same. Also fix a half protractor at D as shown in Fig.2.

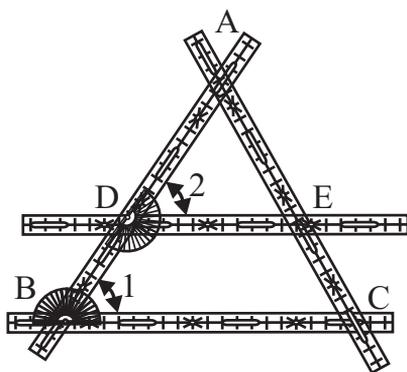


Fig.2

3. Now measure the angles at B and D as shown on the two half protractors.
4. Repeat the above activity by :-
 - Forming different types of triangles.
 - Keeping a triangle fixed and varying the positions of the strip on the two sides AB and AC of triangle ABC such that the ratio $AD : DB = AE : EC$.

S. No.	$\angle ABE$	$\angle ABC$	Is $\angle ABE = \angle ABC$
1.			
2.			
3.			

5. Now complete the following table:

Inference :

Since $\angle 1 = \angle 2$

so $DE \parallel$

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Activity 8

PROPERTIES OF QUADRILATERAL

OBJECTIVE:

To explore properties of different types of quadrilaterals.

MATERIAL REQUIRED:

Six plastic strips, four half protractors, one full protractors and fly screws.

HOW TO PROCEED?

Angle Sum Property of a Quadrilateral

1. Fix four strips along with the half protractors using fly screws as shown in fig. 1.

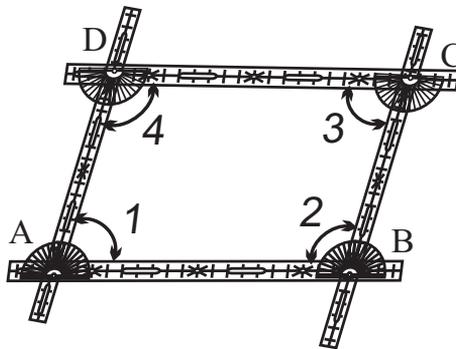


Fig.1

2. Similarly form different quadrilaterals by moving strips and measure the angles of each quadrilateral so formed in the table given below.

S. No.	$\angle 1$	$\angle 2$	$\angle 3$	$\angle 4$	$\angle 1 + \angle 2 + \angle 3 + \angle 4$
1.					
2.					
3.					

Inference :

Properties of a Parallelogram.

- Form different parallelograms by moving the strips as shown in Fig 2 and for each parallelogram measure the angles and the lengths of the sides.

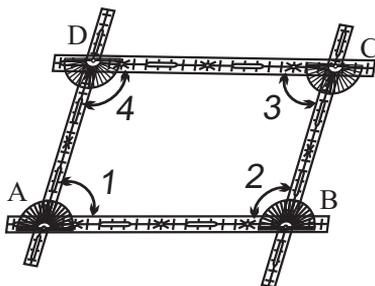


Fig.2

Now complete the following table.

S. No.	Length of the Sides				Measure of angles				$\angle 1$	$\angle 1$	$\angle 3$	$\angle 2$
	AB	BC	DC	AD	$\angle 1$	$\angle 2$	$\angle 3$	$\angle 4$	$+$ $\angle 2$	$+$ $\angle 4$	$+$ $\angle 4$	$+$ $\angle 3$
1.												
2.												
3.												

Inference :

- Opposite angles
- Opposite sides
- Adjacent angles

2. Take two strips and fix them as diagonal AC and BD as shown in Fig. 3.

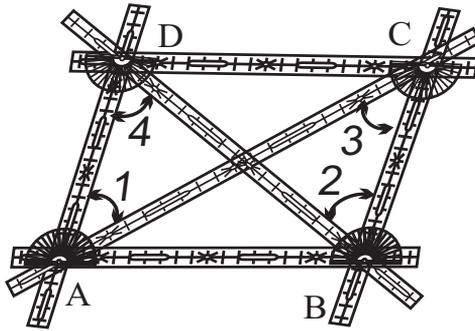


Fig.3

3. Similarly form different parallelograms with diagonals and note down the distance of vertices of each parallelogram from the point of intersection O in the following table.

S. No.	Measure of angle				Length along the diagonal				Measurement of angle					
	$\angle 1$	$\angle 2$	$\angle 3$	$\angle 4$	AC	AO	OC	BD	BO	OD	$\angle AOB$	$\angle BOC$	$\angle COD$	$\angle DOA$
1.														
2.														
3.														

- Inference :** 1. Diagonals
 2. Point of intersection of diagonals

Properties of a Rhombus

1. Make different rhombuses by moving the strips and measure the angles, length of sides of the each rhombus so formed as shown in Fig.4.

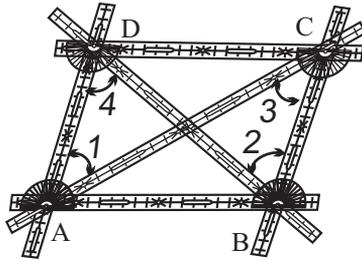


Fig.4

Now complete the following table.

S. No.	1	2	3	4	AB	BC	CD	DA
1.								
2.								
3.								

Inference :

1. Opposite angles
2. Opposite sides

2. Take two strips and fix them as diagonal AC and BD as shown in Fig.4. Hence measure the angles formed by the diagonals and the distance of the vertices from the point of the intersection O of the diagonals.

S. No.	Length along the diagonal		Distance from point O				Measure of angles			
	BD	AC	AO	OC	BO	OD	BOA	BOC	DOC	AOD
1.										
2.										
3.										

Inference :

1. Diagonals
2. Point of intersection of diagonals
3. Angles between the diagonals

Properties of a Rectangle

1. Make different rectangles by moving the strips and fix two strips as diagonals AC and BD of the rectangle so formed as shown in Fig.5

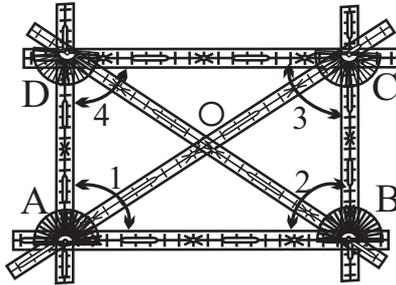


Fig.5

2. Now measure the angles, sides and diagonals of the rectangle so formed. Also measure the distance of vertices from the point of intersection O and the angles formed by diagonals of each rectangle so formed and complete the following table:

S. No.	Length of the side				Measure of angle				Length along the diagonal					
	AB	BC	DC	AD	1	2	3	4	AC	AO	OC	BD	BO	OD
1.														
2.														
3.														

Inference :

1. Opposite sides
2. Angles
3. Point of intersection of diagonals
4. Lengths of diagonals

Properties of a Square

Make different squares by moving the strips(Fig.6) and measure its angles, sides and different line segments .Complete the following table:

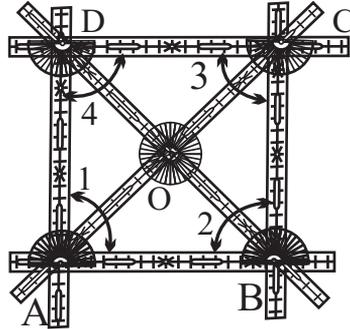


Fig.6

S. No.	Measure of angle				Distance from point O					Measure of angles				
	$\angle 1$	$\angle 2$	$\angle 3$	$\angle 4$	AC	AO	OC	BD	BO	OD	BOA	BOC	DOC	AOD
1.														
2.														
3.														

Inference :

1. Sides
2. Points of intersection of diagonals
3. Angles
4. Angles between diagonals
5. Lengths of diagonals

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Activity 9

QUADRILATERAL FORMED BY MID-POINT OF SIDE OF GIVEN QUADRILATERAL

OBJECTIVE:

To verify that a quadrilateral formed by joining the mid-points of the sides of a quadrilateral taken in order, is a parallelogram.

MATERIAL REQUIRED:

Eight plastic strips, two half protractors, fly screws.

HOW TO PROCEED?

1. Fix four plastic strips using fly screws to form a quadrilateral ABCD as shown in Fig.1

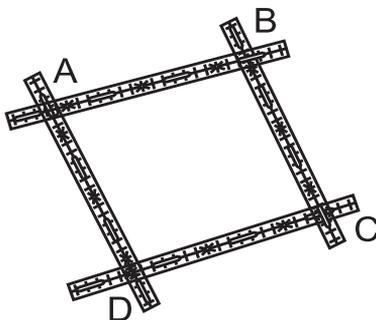


Fig.1

2. Fix the remaining four strips at the mid-points E, F, G and H of the sides of quadrilateral in such a manner that they will form a quadrilateral as shown in Fig.2

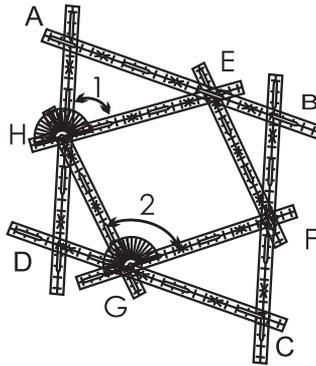


Fig.2

3. Now measure $\angle 1, \angle 2$ and length of sides HE and GF.
4. Repeat the above activity by forming different types of quadrilaterals and complete the following table :

S. No.	$\angle 1$	$\angle 2$	Is $\angle 1 = \angle 2$?	HE	GF	Is HE = GF?
1.						
2.						
3.						

Inference:

Since $\angle 1 = \angle 2$, so HE \parallel

Also HE and GF are

So quadrilateral EFGH is a

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Activity 10

EXPLORING AREA USING GEOBOARD

OBJECTIVE:

To form different shapes on a geoboard and explore their areas.

MATERIAL REQUIRED:

Geoboard, rubber bands, Geoboard pins

HOW TO PROCEED?

Area of Rectangles

1. Form shapes of different rectangles using geoboard pins and rubber bands on the geoboard as shown in Fig.1.

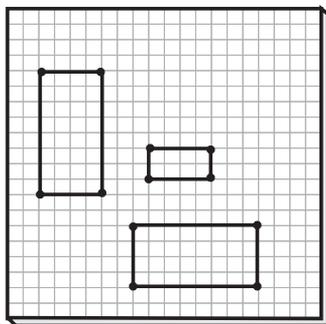


Fig.1

2. Now count the number of unit squares enclosed in each rectangle and complete the following table :

S. No.	Total number of unit squares in rectangle	Length of the rectangle	Breadth of the rectangle	Length \times Breadth
1.				
2.				
3.				

Inference: Area of the rectangle is

Area of Squares

- Form the shapes of different squares using geoboard pins and rubber bands on a geoboards as shown in the Fig 2.

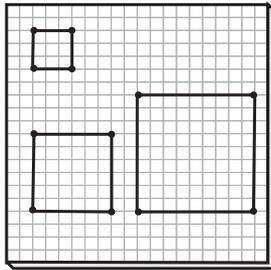


Fig.2

- Count the number of unit squares enclosed in each of the three square and complete the following table.

S. No.	Total number of unit squares in the square	Side of the square	Side \times Side
1.			
2.			
3.			

Inference : Area of Square is

Area of a Right Triangle

1. Form shapes of different right angled triangles with the help of geoboard pins and rubber bands on a geoboard as shown in Fig.3.

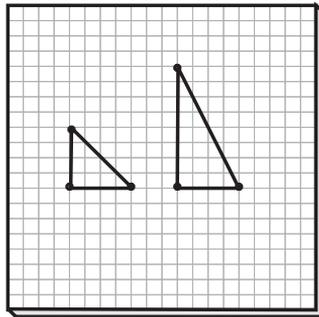


Fig.3

2. Now count the number of unit squares enclosed in each right angled triangle using the criterion for finding the area of any figure by counting the number of unit squares enclosed in it given in next page and complete the following table :

S. No.	Total number of unit squares in the right triangle	Height (h)	Base (b)	$\frac{1}{2} \times (b \times h)$
1.				
2.				
3.				

Inference: Approx. area of right angled triangle is

Area of Irregular Figures

1. Form an irregular figure on a Geoboard with the help of geoboard pins and rubber band as shown in Fig.4.

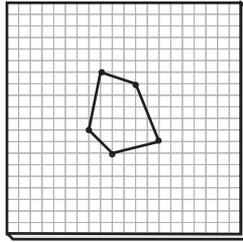


Fig.4

2. Find out the area of this figure by counting the number of unit squares enclosed in it in the following manner :
 - a) Count one complete unit square enclosed by the figure as 1 and take its area as 1 square unit.
 - b) Count the unit square which is more than half enclosed by the figure as 1 and take its area as 1 square unit.
 - c) Count the unit square which is half enclosed by the figure as $1/2$ and take its area as $1/2$ square unit.
 - d) Neglect the unit squares which are less than half enclosed by the figure.
3. The above Fig.4 enclosed 17 complete unit squares, 4 more than half unit squares and 5 half unit squares.

Inference: The Area of the above figure is

4. Now make more irregular figures on the geoboard and try to find out their areas.

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Activity 11

AREAS OF SIMILAR TRIANGLES

OBJECTIVE:

To verify that the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides.

MATERIAL REQUIRED:

Geoboard, rubber bands, geoboard pins

HOW TO PROCEED?

1. Make two similar triangles ABC and DEF by fixing 6 geoboard pins at suitable places on a geoboard and rubber band as shown in Fig.1

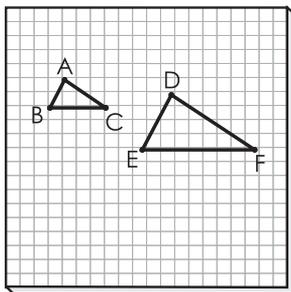


Fig.1

2. Using rubber bands and geoboard pins make squares on sides BC and EF as shown in Fig.2.

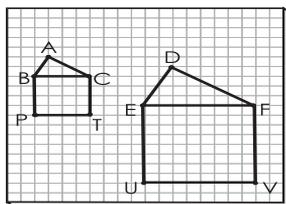


Fig.2

3. Find out the area of the two triangles and the two squares formed above by counting the number of unit squares enclosed in it as discussed earlier in Activity No. 10.
4. Also find out the length of sides BC and EF.
5. Repeat the above activity by forming different pairs of similar triangles by suitably changing the positions of the geoboard pins and complete the following table :

S. No.	$\frac{ar(\triangle ABC)}{ar(\triangle DEF)}$	Area of square on BC $(BC)^2$	Area of square on EF $(EF)^2$	$\frac{ar(\triangle ABC)}{ar(\triangle DEF)} = \frac{(BC)^2}{(EF)^2}$
1.				
2.				
3.				

Inference:

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Activity 12

MEDIAN AND AREA OF A TRIANGLE

OBJECTIVE:

To verify that median of a triangle divides it in two triangles of equal area.

MATERIAL REQUIRED:

Geoboard, rubber-bands, Geoboard pins

HOW TO PROCEED?

1. Fix three pins on a geoboard and use a rubber band to form the $\triangle ABC$ such that the length of base BC has even number of units.

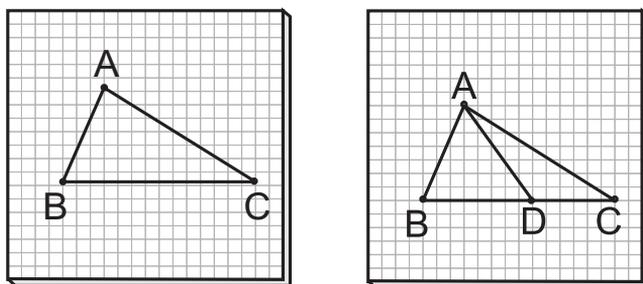


Fig.1.

2. From the mid point of BC say D , join A using a rubber band to form the median AD .
3. Find out the area of triangle ADC and triangle ADB by counting the number of unit squares enclosed in it as discussed earlier in Activity No. 10.

4. Repeat the above activity by forming different triangles by changing the positions of geoboard pins and complete the following table :

S. No.	$ar(\triangle ABD)$	$ar(\triangle ACD)$	Is $ar(\triangle ABD) = ar(\triangle ACD)$?
1.			
2.			
3.			

Inference : The median of a triangle divides it in two triangles having

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Activity 13

FIGURES ON THE SAME BASE AND BETWEEN THE SAME PARALLEL LINES.

OBJECTIVE:

To form different figures on a Geoboard satisfying the following conditions :

- lying on the same base
- lying between the same parallel lines but not on the same base.
- lying on the same base and between the same parallel lines.

MATERIAL REQUIRED:

Geoboard, Rubber-bands, Geoboard pins

HOW TO PROCEED?

Figures lying on the same base

- Fix 2 geoboard pins on a geoboard at two different points say A and B. and place 3 different coloured rubber bands between the two geoboard pins as shown in Fig.1.

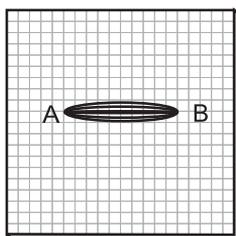


Fig.1

- Now with these 3 rubber bands make three different figures say a triangle, rectangle and trapezium by fixing geoboard pins at suitable places as shown in Fig.2.

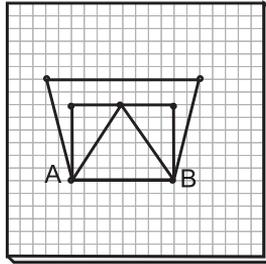


Fig.2

All these figures formed above in Fig.2 are lying on the same base i.e AB

Figures lying between the same parallels but not on the same base

- Fix 4 geoboard pins suitably in a line. Now fix 2 geoboard pins on a line parallel to the previous lines on the geoboard.
- Take 3 rubber bands and make three different figures say square, triangle and a trapezium such that they lie between the same parallel lines but not on the same base as shown in the Fig.3 given below.

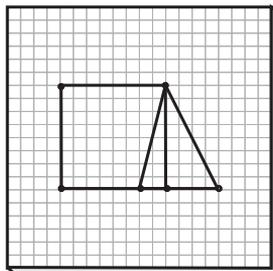


Fig.3

Figures lying on the same base and between the same parallel lines

1. Fix 2 geoboard pins on the geoboard at 2 points and place 3 different coloured rubber bands between these 2 pins.
2. Now with these rubber bands make three different figures say triangle, rectangle and trapezium in such a manner that they lie on the same base and between the same parallel lines as shown in the Fig.4.

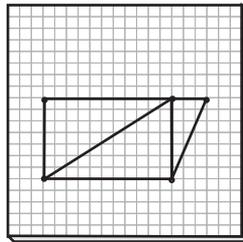


Fig.4

3. Repeat the above activities by making different shapes using geoboard pins and rubber bands satisfying any of the above three conditions.

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Activity 14

TRIANGLES ON THE SAME BASE AND BETWEEN THE SAME PARALLEL

OBJECTIVE:

To verify that triangles on the same base and between the same parallels are equal in area.

MATERIAL REQUIRED:

Geoboard, rubber-bands, Geoboard pins

HOW TO PROCEED?

1. Fix geoboard pins on the geoboard to make $\triangle ABC$ using rubber band as shown in Fig.1.

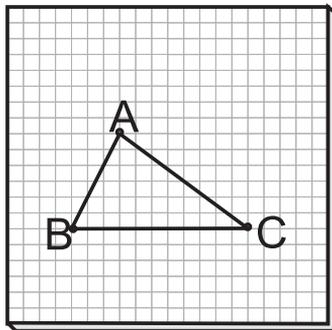


Fig.1

2. Fix more geoboard pins on the geoboard at suitable places to form another $\triangle ABC$ use different colour of rubber band) such that both the triangles are on the same base and between the same parallel lines as shown in Fig.2.

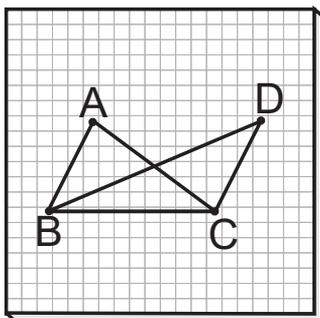


Fig.2

3. Find out the area of the two triangles by counting the number of unit squares enclosed in it as discussed earlier in Activity No.10.
4. Repeat the above activity by forming different pairs of triangles lying on the same base and between the same parallel lines by suitably changing the positions of geoboard pins and complete the following table :

S. No.	$ar(\triangle ABC)$	$ar(\triangle DBC)$	Is $ar(\triangle ABC) = ar(\triangle DBC)$?
1.			
2.			
3.			

Inference : Triangles on the same base and between same parallels are

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Activity 15

PARALLELOGRAMS ON THE SAME BASE AND BETWEEN SAME PARALLEL LINES

OBJECTIVE:

To verify that parallelograms on the same base and between the same parallels are equal in area.

MATERIAL REQUIRED:

Geoboard, rubber-bands, Geoboard pins

HOW TO PROCEED?

1. Fix geoboard pins on a geoboard to make the parallelogram ABCD using rubber band as shown in Fig.1.

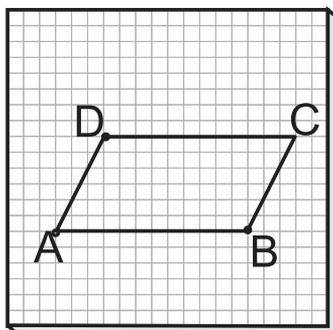


Fig.1

2. Fix more geoboard pins on the geoboard at suitable places to form another parallelogram ABEF (use different coloured rubber band) such that both the parallelograms are on the same base and between the same parallel lines as shown in Fig.2.

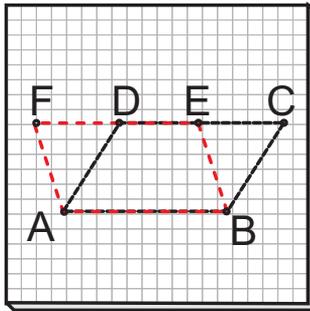


Fig.2

3. Find the area of the two parallelograms by counting the number of unit squares enclosed as done earlier in Activity No.10.
4. Repeat the above activity by forming different pairs of parallelograms by suitably changing the positions of geoboard pins and complete the following table :

S. No.	Area of $\parallel gm ABCD$	Area of $\parallel gm ABEF$	Is $ar(\parallel gm ABCD) = ar(\parallel gm ABEF)$?
1.			
2.			
3.			

Inference : Parallelograms on the same base and between same parallel lines are

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Activity 16

TRIANGLE AND PARALLELOGRAM ON THE SAME BASE AND BETWEEN SAME PARALLEL LINES

OBJECTIVE:

To verify that for a triangle and a parallelogram on the same base and between the same parallels, the area of triangle is half the area of parallelogram.

MATERIAL REQUIRED:

Geoboard, rubber-bands, Geoboard pins

HOW TO PROCEED?

1. Fix geoboard pins on a geoboard to make a parallelogram ABCD using rubber band as shown in Fig.1.

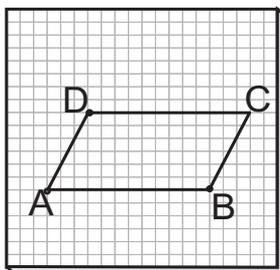


Fig.1

2. Fix more geoboard pins on the geoboard at suitable places to form a triangle ABE (use different colour of rubber band) such that the triangle and the parallelogram lie on the same base and between the same parallel lines as shown in Fig.2.

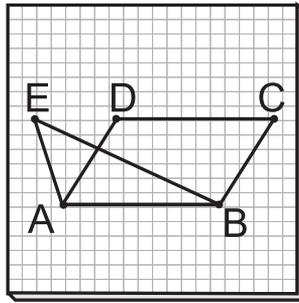


Fig.2

3. Find the area of parallelogram ABCD and $\triangle ABE$ by counting the number of unit squares enclosed as done earlier in Activity No.10.
4. Repeat the above activity by forming different pairs of triangles and parallelograms by suitably changing the positions of geoboard pins and complete the following table :

S. No.	Area of $\parallel gm$ ABCD	Area of $\triangle ABE$	Is $ar(\triangle ABE) = \frac{1}{2} ar(\parallel gm ABCD)$?
1.			
2.			
3.			

Inference : If a triangle and a parallelogram are on the same base and between the same parallel lines, then area of triangle is of the area of

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Activity 17

AREAS OF TRIANGLE, PARALLELOGRAM AND TRAPEZIUM

OBJECTIVE:

To explore area of triangle, parallelogram and trapezium.

MATERIAL REQUIRED:

Cut-outs of different shapes

HOW TO PROCEED?

Area of Parallelogram

1. Put cut-outs of a triangular piece 'A' and a trapezium piece 'B' together to form a parallelogram as shown in Fig.1.

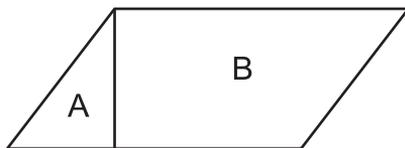


Fig.1

2. Remove cut-out A of triangular piece and attach it to the other side of cut out B of trapezium piece as shown in the Fig.2 given below. It will form a rectangle.



Fig.2

Inference:

Area of the Parallelogram = Area of
= Length \times of rectangle.
= Base \times of parallelogram.

Area of Triangle

1. Put the cut-outs of the two congruent triangles T_1 and T_2 together to form a parallelogram as shown in Fig.3.

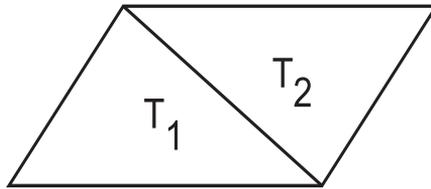


Fig.3

Inference :

Area of the triangle (T_1 or T_2) = $\frac{1}{2} \times$ Area of

2. Take a parallelogram and three triangular pieces A, B and C which exactly cover the parallelogram as shown in Fig.4 (I)

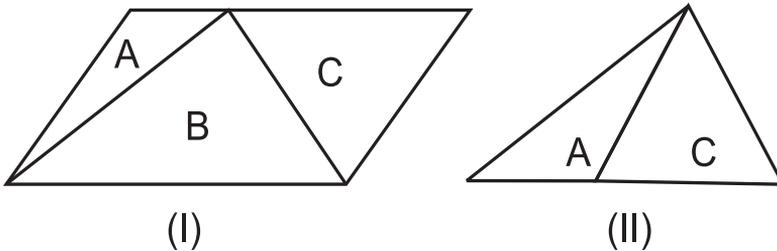


Fig.4

3. Put the triangular pieces A and C together. They will cover the triangular piece B completely as shown in Fig.4 (II).

Inference :

Area of B = Area of A + Area of C

Area of the parallelogram = 2 × Area of B

Area of B =

Area of Trapezium

1. Take cut-outs of two congruent trapeziums 'C' and 'D' having height 'h' and parallel sides 'a' and 'b'.
2. Put the cut-outs together to form a parallelogram as shown in Fig.5 given below.

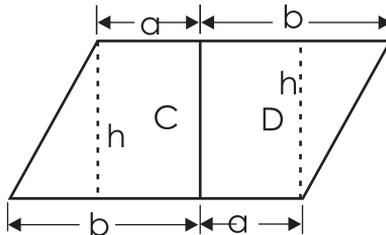


Fig.5

Inference :

Area of trapezium C = Area of trapezium D.

Area of parallelogram = Area of + Area of

$$\therefore \text{Area of trapezium} = \frac{1}{2} \times \text{Area of } \dots\dots\dots$$

$$= \frac{1}{2} \times (a + b) \times \dots\dots\dots$$

Note:

This activity may be repeated by using suitable cut-outs of triangles, trapeziums and parallelograms of different sizes and students may be encouraged to make more cut-outs of parallelogram, trapeziums and triangles to explore the inter-relationship of the areas of various shapes.



Activity 18

PHYTHAGORAS THEOREM

OBJECTIVE:

To verify Pythagoras theorem i.e. “In a right angled triangle the square of the hypotenuse is equal to the sum of the squares of the other two sides”.

MATERIAL REQUIRED:

Cut-outs of right angled triangle with sides a , b and c , Cut-outs of squares of sides a , b and c .

HOW TO PROCEED?

1. Arrange the cut-outs of three squares of sides a , b , c and right angled triangle as shown in Fig.1.

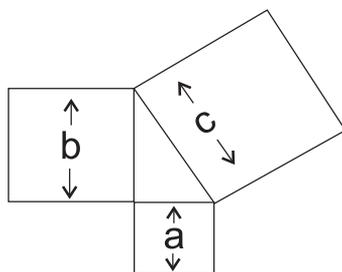


Fig.1

2. Put the squares of sides a and b together as shown in Fig.2.

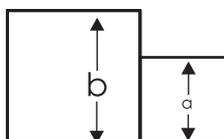


Fig.2

3. 3 cut-outs from square of side a and 2 cut-outs from square of side b (given in the kit) are prepared by marking the two right angled triangle with side a , b and c in Fig.2 and then cutting it along the dotted lines as shown in Fig.3.

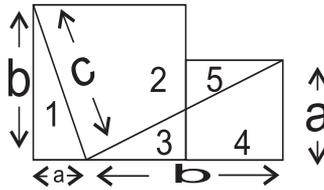


Fig.3

4. Now rearrange these 5 pieces on the square of side c as shown in Fig.4. The square of side c is exactly covered by the five cut-out pieces of squares of sides a and b respectively.

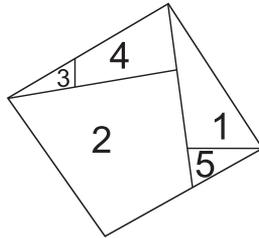


Fig.4

5. From step 4, we have $a^2 + b^2 = c^2$

Repeat this activity by taking different right angled triangles.

Inference: In a right angled triangle with sides a , b and c , where c is hypotenuse

$$a^2 + b^2 = \dots\dots\dots$$

In a right angled triangle, square of hypotenuse is

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Activity 19

ALGEBRAIC IDENTITIES

OBJECTIVE:

To verify the algebraic identities

(i) $(a+b)^2 = a^2 + 2ab + b^2$

(ii) $(a-b)^2 = a^2 - 2ab + b^2$

MATERIAL REQUIRED:

Cut-out of squares of side a and b units, two rectangular cut-outs of length a units and breadth b units.

HOW TO PROCEED?

$$(a+b)^2 = a^2 + 2ab + b^2$$

1. Arrange the four cut-outs on a table as shown in Fig.1.

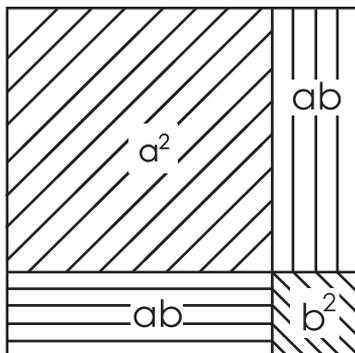


Fig.1.

2. Look at the shape obtained in Fig.1. It is a square of side $(a+b)$ units.

3. Find the area of the shape so formed in Fig.1 using the formula for area of square i.e. side \times side.

$$(a + b) \times (a + b) = (a + b)^2$$

4. Also find the area of the shape so formed by adding the areas of the four pieces as —

$$a^2 + ab + ab + b^2 = a^2 + 2ab + b^2$$

5. Repeat the activity by making squares and rectangles with different values of a and b using chart paper etc. and complete the following table :

S. No.	a	b	a ²	b ²	ab	2ab	a ² +2ab+b ²	(a+b)	(a+b) ²
1.									
2.									
3.									

Inference :

$$(a + b)^2 = a^2 + 2ab + b^2, \text{ for all values of } a \text{ and } b$$

$$(a - b)^2 = a^2 - 2ab + b^2$$

How to proceed :

1. Put cut-outs of two squares of side a and b units. Arrange the two square cut-outs on the table as shown in Fig.2.

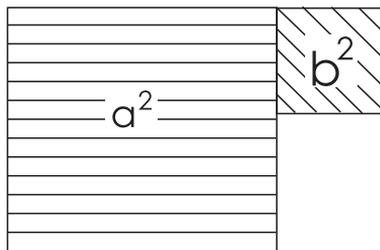


Fig.2

2. Now put one cut-out of rectangle of length a units and breadth b units on the shape which is obtained in Fig .2 as shown in Fig.3.

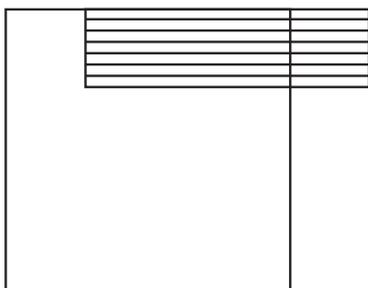


Fig.3

3. Put another rectangular piece of same dimension on the shape in Fig.3 as shown in Fig.4.

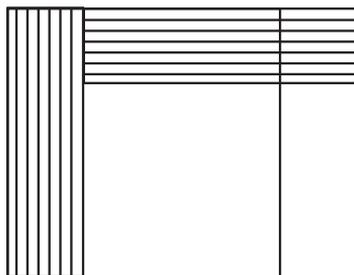


Fig.4

4. Look at uncovered portion in the Fig.4. Is it a square?
5. Find the length of its side. It is $(a - b)$ units.
6. Find the area of the shape given in Fig.2. It is $(a^2 + b^2)$ sq.units.
7. Find the area of shaded portion given in Fig.4. It is $2ab$ sq.units .
8. Find the area of uncovered portion given in Fig.4 from step 2 and step 3. It is $(a^2 + b^2 - 2ab)$ sq.units.
9. Now compute the area of uncovered portion in Fig.4 using formula for area of square .It is $(a - b) \times (a - b) = (a - b)^2$ sq.units.

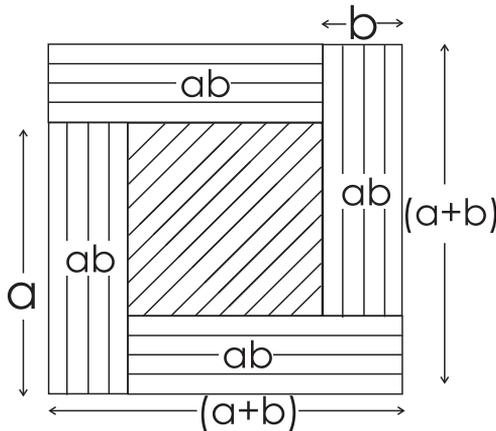
10. Repeat the above activity by taking squares and rectangles with different values of a and b and complete the following table :

Inference :

$$(a - b)^2 = a^2 - 2ab + b^2, \text{ for all values of } a \text{ and } b$$

S. No.	a	b	a ²	b ²	ab	2ab	a ² -2ab+b ²	(a-b)	(a-b) ²
1.									
2.									
3.									

Extension : Try verifying the identity $(a + b)^2 - 4ab = (a - b)^2$



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Activity 20

ALGEBRAIC IDENTITIES

OBJECTIVE:

To verify the algebraic identity

$$a^2 - b^2 = (a + b)(a - b)$$

MATERIAL REQUIRED:

Cut-outs of square of side a and b units, two cut-outs of congruent trapezium having parallel sides of length a and b units.

HOW TO PROCEED?

1. Arrange the two cut-outs of squares on a table as shown in Fig. 1.

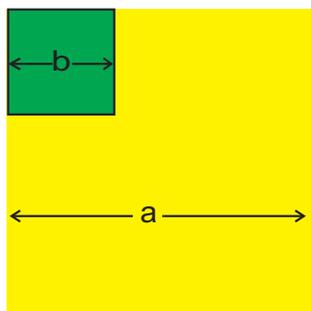


Fig.1

2. Arrange the cut-outs of two trapeziums on uncovered portion of square of side a units as shown in Fig.2 .They will cover the remaining portion of square completely.

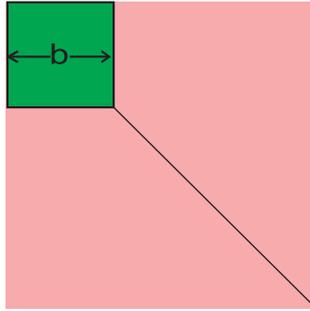


Fig.2

3. Now take out the cut-outs of trapeziums and arrange them. They will form a rectangle of length $(a+b)$ units and breadth $(a-b)$ units as shown in Fig.3.

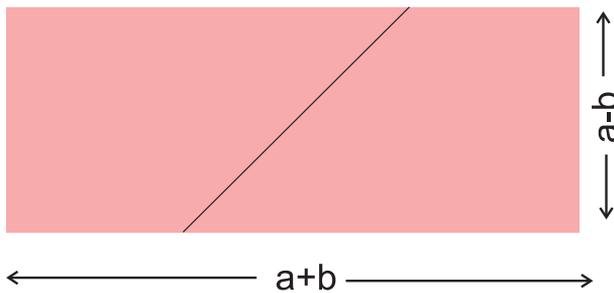


Fig.3

4. Look at Fig. 1 and find the area of uncovered portion. It is $(a^2 - b^2)$ sq. units
5. Find the area of two trapezium pieces in Fig.2. It is $(a^2 - b^2)$ sq. units
6. Look at Fig.3. It is a rectangle with sides $(a + b)$ and $(a - b)$ units. Its area is $(a + b)(a - b)$ sq. units.

7. Repeat the above activity by taking square and trapezium with different values of a and b and hence complete the following table :

S. No.	a	b	a ²	b ²	a+b	a-b	a ² -b ²	(a+b)(a-b)	Is a ² -b ² =(a+b)(a-b)?
1.									
2.									
3.									

Inference :

$$a^2 - b^2 = (a + b) (a - b), \text{ for all values of } a \text{ and } b.$$

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Activity 21

FACTORISATION OF A QUADRATIC POLYNOMIAL

OBJECTIVE:

To factorise expression of the type $Ax^2 + Bx + C$, say

- $x^2 + 5x + 6$
- $x^2 - x - 6$
- $2x^2 - 7x + 6$

MATERIAL REQUIRED:

Blue and Red coloured Algebraic tiles

HOW TO PROCEED?

To factorise x^2+5x+6

1. Take one x^2 tile, five x tiles and 6 unit tiles. Arrange them to form a rectangle as shown in Fig.1.

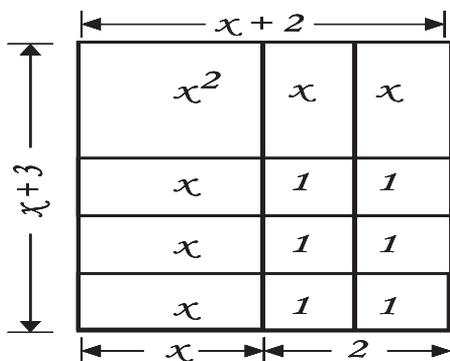


Fig.1

2. The rectangle obtained in Fig.1 has sides of length $(x + 3)$ and $(x + 2)$. So area of this rectangle is $(x + 2)(x + 3)$.

3. Also by adding the area of all the tiles enclosed by rectangle, we get

$$x^2 + x + x + x + x + x + 1 + 1 + 1 + 1 + 1 + 1 = x^2 + 5x + 6$$

Inference : This shows that :-

$$x^2 + 5x + 6 = (x + 2)(x + 3)$$

To factorise $x^2 - x - 6$

1. Take one x^2 tile, one $-x$ tile and six -1 tiles. Arrange these tiles in the form of a rectangle.
2. In this case the tiles will not form a rectangle. Now, we will take one x^2 tile, three $-x$ tiles, two x tiles and six -1 tiles to form a rectangle as shown in given Fig.2.

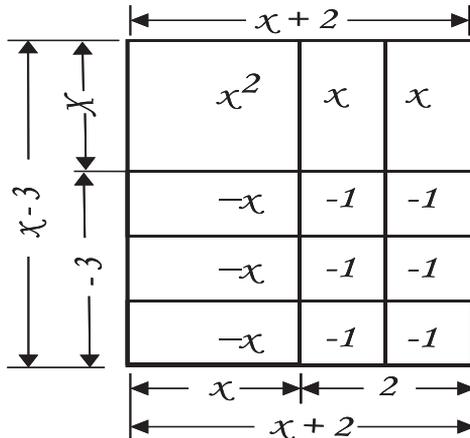


Fig.2

3. The rectangle obtained in Fig.2 has sides of length $(x + 2)$ and $(x - 3)$.

So area of this rectangle is $(x + 2)(x - 3)$.

4. Also by adding the area of all the tiles enclosed by the rectangle given in Fig.2, we get :-

$$x^2 + x + (-x) + (-x) + (-x) + (-1) + (-1) + (-1) + (-1) + (-1) + (-1) = x^2 - x - 6$$

Inference : This shows that :-

$$x^2 - x - 6 = (x + 2)(x - 3)$$

To factorise $2x^2 - 7x + 6$

1. Take two x^2 tiles, seven $-x$ tiles and six unit tiles. Arrange these tiles in the form of a rectangle as shown in Fig.3.

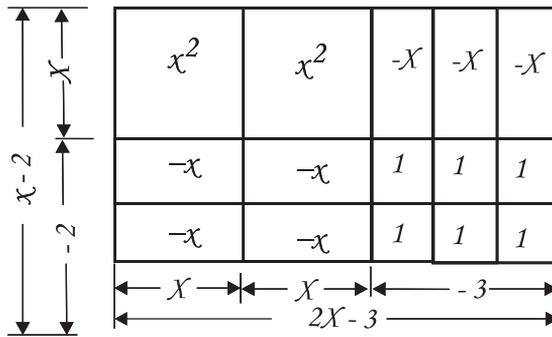


Fig.3

2. The rectangle obtained in Fig.3 has sides of length $(2x - 3)$ and $(x - 2)$. So area of this rectangle is $(x + 2)(x - 3)$.
3. Also by adding the area of all the tiles enclosed by the rectangle given in Fig.3, we get :-

$$x^2 + x^2 + (-x) + 1 + 1 + 1 + 1 + 1 + 1 = 2x^2 - 7x + 6$$

Inference : This shows that :-

$$2x^2 - 7x + 6 = (2x - 3)(x - 2)$$

Now using the similar process of factorisation by algebraic tiles complete the following table:

No. of tiles required for polynomials	x^2	x	$-x$	+1	-1	1 st factor	2 nd factor
$x^2 + 7x + 10$							
$-2x^2 - 3x + 5$							
$2x^2 + 10x$							
$x^2 - 7x + 12$							

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Activity 22

AREA OF A CIRCLE

OBJECTIVE:

To explore the area of a circle.

MATERIAL REQUIRED:

Cut-outs of Circle

HOW TO PROCEED?

1. Take a Circular cut-out which is divided into 4 cut-outs of equal sectors, half of which i.e. 2 are labelled as 'A' as shown in Fig. 1.

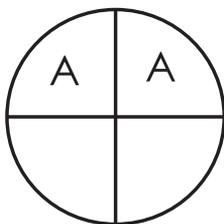


Fig.1

2. Now arrange these sectors to form a figure as shown below in Fig.2.

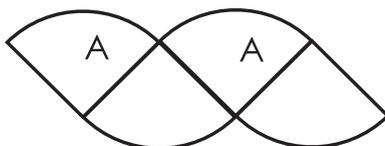


Fig.2

3. Take a Circular cut-out which is divided into 6 cut-outs of equal sectors, half of which i.e. 3 are labelled as 'B' as shown in Fig.3.

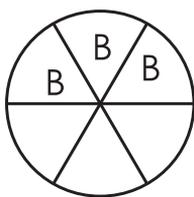


Fig.3

4. Arrange these sectors to form a shape as shown below in Fig.4.

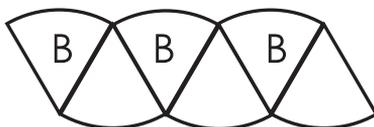


Fig.4

5. Take a Circular cut-out which is divided into 8 cut-outs of equal sectors, half of which i.e. 4 are labelled as 'C' as shown in Fig.5.

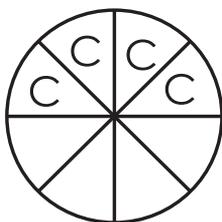


Fig.5

6. Arrange these sectors to form a shape as shown below in Fig.6.

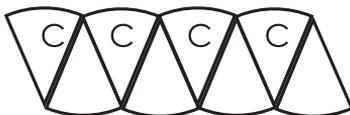


Fig.6

7. Take a Circular cut-out which is divided into 12 cut-outs of equal sectors, half of which i.e. 6 are labelled as 'D' as shown in Fig.7.

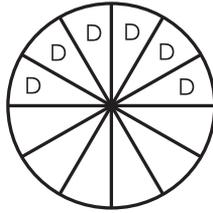


Fig.7

8. Arrange these sectors to form a shape as shown below in Fig.8.

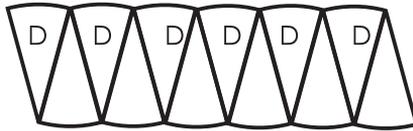


Fig.8

9. Take a Circular cut-out which is divided into 16 cut-outs of equal sectors, half of which i.e. 8 are labelled as 'E' as shown in Fig.9.

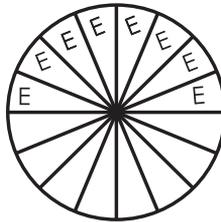


Fig.9

10. Rearrange these sectors to form a shape as shown below in Fig.10.



Fig.10

11. What do you observe in all the figures above?

Inference : The figures which is so formed above looks like a parallelogram having length equal to half of circumference of respective circular cut-out and height equal to radius of circular cut-out. Hence we get

$$\begin{aligned}\text{Area of circle} &= \text{Area of Parallelogram} \\ &= \text{Length of parallel sides} \times \text{Height of parallelogram} \\ &= \pi r^2\end{aligned}$$

Extension:

This activity may be repeated by taking 32 or 64 equal cut-outs of sectors of the circle.

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Activity 23

ANGLE SUBTENDED AT THE CENTRE OF A CIRCLE BY UNEQUAL CHORDS

OBJECTIVE:

To verify that a longer chord subtend greater angle at the centre of a circle.

MATERIAL REQUIRED:

Circular board, two plastic strips, rubber bands, connectors (for circular board), full protractor.

HOW TO PROCEED?

1. Take two plastic strips and fix them on the circular board with the help of connectors representing two chords AB and CD of the circle of different lengths as shown in Fig. 1.

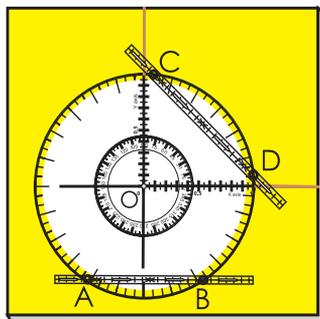


Fig.1

2. With the help of rubber bands of different colours make two angles at the centre O subtended by the two chords as shown in Fig.2.

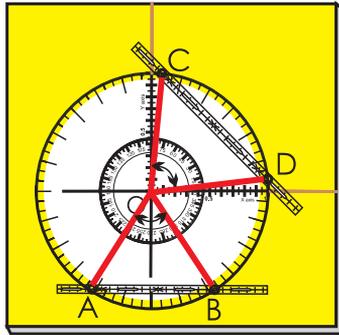


Fig.2

3. Measure $\angle AOB$ and $\angle COD$ at the centre of circle with the help of markings on the circular board or a full protractor.
4. Repeat the above activity by taking different lengths of the strips and complete the following table:

S. No.	AB	CD	$\angle AOB$	$\angle COD$	Larger chord	Larger angle
1.						
2.						
3.						

Inference :

Angle at centre of the circle of larger chord is

-----* * * * *-----

Activity 24

ANGLES SUBTENDED AT THE CENTRE OF A CIRCLE BY EQUAL CHORDS

OBJECTIVE:

To verify that equal chords subtend equal angles at the centre of the circle.

MATERIAL REQUIRED:

Circular board, two plastic strips, rubber bands, connectors (for circular board).

HOW TO PROCEED?

1. Take two plastic strips and fix them on the circular board with the help of connectors in such a manner that they will represent two equal chords AB and CD of the circle as shown in Fig.1.

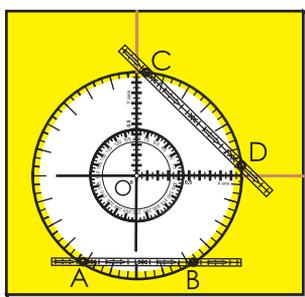


Fig.1

2. With the help of different coloured rubber bands make angles at the centre O of given circle subtended by the two chords as shown in Fig.2.

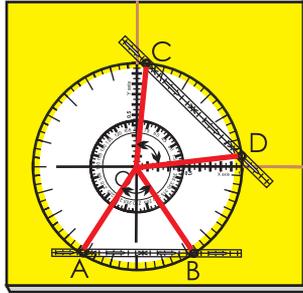


Fig.2

3. Measure $\angle AOB$ and $\angle COD$ with the help of markings on the circular board or a full protractor.
4. Repeat the above activity by taking different chords of equal lengths and complete the following table:

S. No.	AB	CD	$\angle AOB$	$\angle COD$	Is $\angle AOB = \angle COD$?
1.					
2.					
3.					

Inference :

If AB CD, then

$\angle AOB$ $\angle COD$

i.e. equal chords of a circle subtend

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Activity 25

CHORDS SUBTENDING EQUAL ANGLES AT THE CENTRE OF A CIRCLE

OBJECTIVE:

To verify that the chords subtending equal angles at the centre of a circle are equal.

MATERIAL REQUIRED:

Circular board, two plastic strips, rubber bands, connectors(for circular board)

HOW TO PROCEED?

1. Fix two plastic strips at suitable places with the help of connectors representing two chords AB and CD on the circular board such that the angles subtended by them at the centre of given circle are equal as shown in the Fig.1.

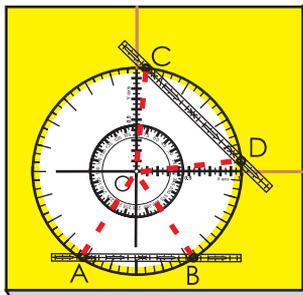


Fig.1

2. Measure the length of each strip between the two connectors representing the two chords AB and CD.

3. Repeat the above activity by taking other pairs of chords subtending equal angles at the centre of circle on circular board and complete the following table :

S. No.	AB	CD	$\angle AOB$	$\angle COD$	Is $AB = CD$?
1.					
2.					
3.					

Inference :

Chords subtending equal angles at the centre are

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Activity 26

PERPENDICULAR FROM THE CENTRE TO A CHORD IN A CIRCLE

OBJECTIVE:

To verify that the perpendicular drawn from the centre of a circle to a chord bisects the chord.

MATERIAL REQUIRED:

Circular board, set square, plastic strip, connectors (for circular board)

HOW TO PROCEED?

1. Fix a plastic strip on the circular board representing chord AB with the help of connectors.
2. Take a set square and place it on the circular board such that its one of the edges (other than the hypotenuse) coincides with the edge of the plastic strip as shown in the Fig.1.

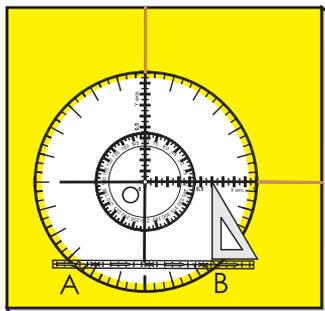


Fig.1

- Now slide the set square along the strip so that the other edge of the set square passes through the centre 'O' of the circle on the circular board and marked the meeting point of set square and plastic strip as 'M' as shown in the Fig.2.

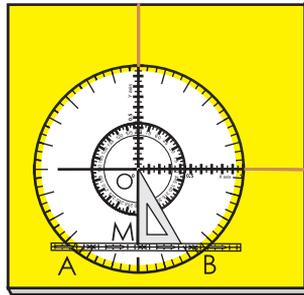


Fig.2

- Now measure the lengths of AM and BM of chord AB.
- Repeat the above activity by forming different chords of different lengths by using plastic strips and complete the following table:

S. No.	AM	BM	Is AM = BM?
1.			
2.			
3.			

Inference :

If $OM \perp AB$ then $AM = \dots\dots\dots$.

Think and discuss!!
Is $AM=BM$ when OM is not perpendicular to AB ?

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Activity 27

LINE THROUGH THE CENTRE OF A CIRCLE BISECTING A CHORD

OBJECTIVE:

To verify that a line drawn through the centre of a circle to bisect a chord is perpendicular to the chord.

MATERIAL REQUIRED:

Circular board, 1 plastic strip, connectors(for circular board), connectors(for strips), rubber band, one half protractor

HOW TO PROCEED?

1. Fix a plastic strip on the circular board at suitable points with the help of connectors to represent chord AB.
2. Fix a connector at the centre O of the circle and a connector (for strips) at the mid-point M of the chord. Now tie a rubber band on the two connectors to represent the line drawn through the centre of circle to bisect the chord AB as shown in the Fig.1.

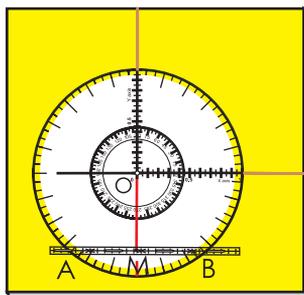


Fig.1

- Place a protractor such that its centre coincides with the mid-point M of the chord AB as shown in Fig.2.

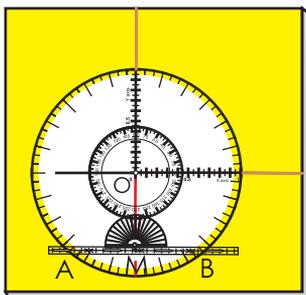


Fig.2

- Now measure $\angle OMA$ or $\angle OMB$
- Repeat the above activity by forming chords of different length by fixing strip at different positions and complete the following table :

S. No.	$\angle OMA$	$\angle OMB$
1.		
2.		
3.		

Inference :

$\angle OMA$ is a angle. So,

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Activity 28

EQUAL CHORDS OF A CIRCLE

OBJECTIVE:

To verify that equal chords of a circle are equidistant from the centre of a circle.

MATERIAL REQUIRED:

Circular board, 2 plastic strips, one set square, connectors(for circular board).

HOW TO PROCEED?

1. Take 2 plastic strips and suitably fix them with the help of connectors so that they represent two equal chords AB and CD of the circle on circular board with centre O as shown in the Fig.1.

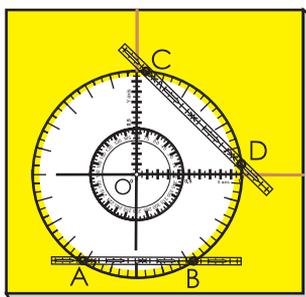


Fig.1

2. Take a set square and slide it along the strip so that the other edge of the set square passes through centre O of circle on the circular board and is perpendicular to AB . Marked the meeting point of set square and plastic strip as M as shown in Fig.2.

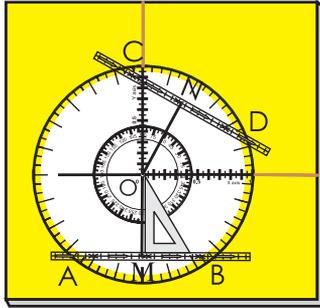


Fig.2

3. Measure the length OM. Now repeat step 2 for chord CD and measure the length of the perpendicular ON from centre O to chord CD.

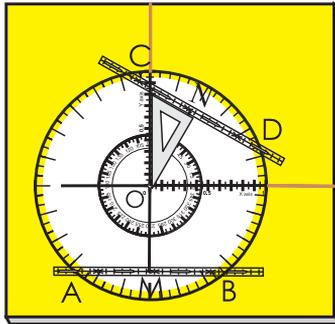


Fig.3

4. Repeat the same activity by varying lengths of equal chord AB and CD by fixing plastic strips at different positions and complete the following table:

S. No.	AB	CD	OM	ON	Is $OM = ON$?
1.					
2.					
3.					

Inference :

Equal chord of a circle are

Think and discuss:

- (i) Is $OM = ON$, if $AB \neq CD$?
- (ii) If $AB > CD$, Is $OM > ON$ or $OM < ON$?

-----* * * * *-----

Activity 29

CHORDS EQUIDISTANT FROM THE CENTER OF A CIRCLE

OBJECTIVE:

To verify that the chords equidistant from the centre of a circle are equal .

MATERIAL REQUIRED:

Circular board, 2 plastic strips, one set square, connectors(for circular board)

HOW TO PROCEED?

1. Take a plastic strip and fix it at a convenient distance OM (say 5cm) from centre O of circle on the circular board with the help of set square to represent a chord AB as shown in the Fig.1.

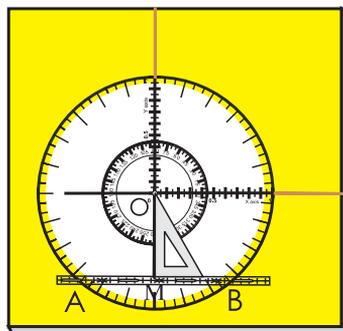


Fig.1

2. Now again with the help of set square place another plastic strip at the same distance ON (5cm) to represent another chord CD as shown in the Fig.2.

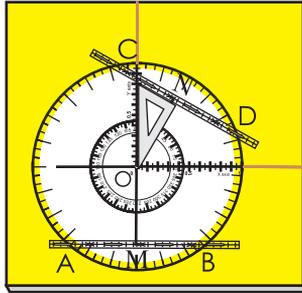


Fig.2

3. Now measure length of chords AB and CD using markings on plastic strips.
4. Repeat the above activity by fixing the plastic strips at different positions to represent other pairs of chords which are equidistant from the centre O of circle on circular board and complete the following table :

S. No.	AB	CD	OM	ON	Is AB = CD?
1.					
2.					
3.					

Inference : Chords equidistant from the centre of a circle are..... .

Think and discuss:

- (i) Is $AB = CD$, if $ON \neq OM$?
- (ii) If $ON > OM$, Is $AB > CD$ or $AB < CD$?

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Activity 30

EQUAL ARCS OF A CIRCLE

OBJECTIVE:

To verify that equal arcs of a circle subtend equal angles at the centre.

MATERIAL REQUIRED:

Circular board, connectors (for circular board), rubber bands

HOW TO PROCEED?

1. Fix four connectors at suitable positions on the boundary of circle on the circular board to represent two equal arcs AB and CD as shown in Fig.1.

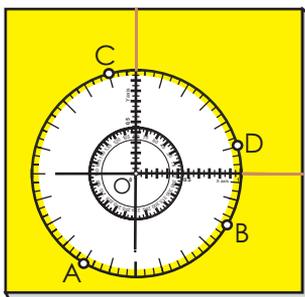


Fig.1

2. Fix a connector at the centre O of the circle on circular board and with the help of 2 different coloured rubber bands make $\angle AOB$ and $\angle COD$ subtended by these two arcs at the centre O as shown in the Fig.2.

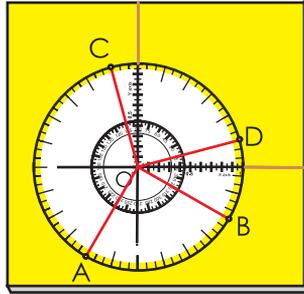


Fig.2

3. Now measure $\angle AOB$ and $\angle COD$ with the help of degree markings at centre of circle or by fixing a full protractor at centre of circle.
4. Repeat the above activity by taking different pairs of congruent arcs on the circular board and complete the following table :

S. No.	$\angle AOB$	$\angle COD$	Is $\angle AOB = \angle COD$?
1.			
2.			
3.			

Inference : Equal arcs of a circle subtend..... .

Think and discuss:

- (i) Is $\angle AOB = \angle COD$ when arc AB and arc CD are not congruent?
- (ii) If arc AB > arc CD, is $\angle AOB > \angle COD$?

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Activity 31

ANGLE SUBTENDED AT THE CENTRE AND AT ANY POINT ON THE CIRCUMFERENCE OF CIRCLE

OBJECTIVE:

To verify that an angle subtended by an arc of a circle at the centre, is double the angle subtended by it on any point on the circumference of circle.

MATERIAL REQUIRED:

Circular board, connectors (for circular board), rubber bands, one half protractor

HOW TO PROCEED?

1. Fix two connectors at two convenient places on the boundary of circle on the circular board to represent an arc AB as shown in Fig.1.

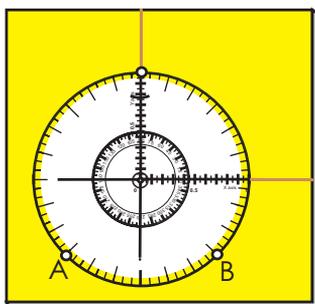


Fig.1

2. Fix a connector at the centre O of circle and make $\angle AOB$ subtended by this arc at the centre by using rubber band.

3. Now fix a connector at any point P on the remaining part of the boundary of circle on the circular board and show $\angle APB$ subtended by the same arc AB at point P with the help of another rubber band as shown in Fig.2.

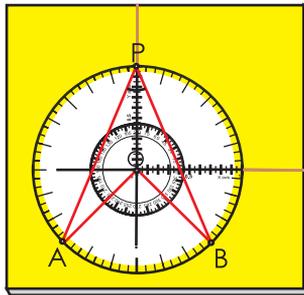


Fig.2

4. Measure $\angle AOB$ with the help of degree marking at the centre of circle on the circular board and measure $\angle APB$ by fixing a half protractor at P as shown in Fig.3.

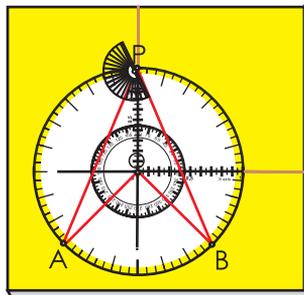


Fig.3

5. Repeat the activity by taking point P at different positions on the boundary of circle on circular board.
6. Also repeat the same activity by varying length of arc AB with the help of connectors and complete the following table :

S. No.	$\angle AOB$	$\angle APB$	Is $\angle AOB = \angle APB$
1.			
2.			
3.			

Inference: Angle subtended by an arc at the centre is..... .

Think and discuss:

- (i) If point P lies outside the circle,
Is $\angle AOB = 2 \angle APB$?
- (ii) If point P lies within the circle,
Is $\angle AOB = 2 \angle APB$?

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Activity 32

ANGLES IN THE SAME SEGMENT OF A CIRCLE

OBJECTIVE:

To verify that the angles in the same segment of a circle are equal.

MATERIAL REQUIRED:

Circular board, connectors (for circular board), rubber bands, one plastic strip, one half protractor

HOW TO PROCEED?

1. Fix a plastic strip with the help of connectors to represent a chord AB of the circle on circular board.
2. Fix two pins at two different points P and Q on the same side of AB, on the boundary of circle on the circular board.
3. Use two rubber bands of different colours to represent $\angle APB$ and $\angle AQB$ in the same segment of the circle as shown in Fig. 1.

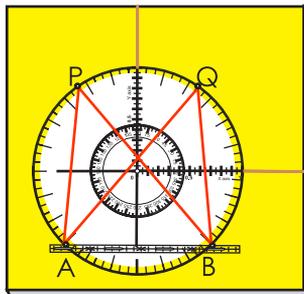


Fig.1

4. Measure $\angle APB$ and $\angle AQB$ using half protractor.
5. Repeat the activity by making different pairs of angles in the same segment of the circle and complete the following table :

S. No.	$\angle APB$	$\angle AQB$	Is $\angle APB = \angle AQB$?
1.			
2.			
3.			

Inference: Angles in the same segment of a circle are..... .

Think and discuss:

Is $\angle APB = \angle AQB$ if one of the points P and Q is not on the boundary of the circular board?

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Activity 33

ANGLE IN A SEMI CIRCLE

OBJECTIVE:

To verify that an angle in a semi circle is a right angle.

MATERIAL REQUIRED:

Circular board, connectors (for circular board), rubber bands, one plastic strip, one half protractor

HOW TO PROCEED?

1. Fix a plastic strip at a suitable place on the boundary of circle on the circular board with the help of connectors to represent diameter AB of the circle.
2. Fix a connector at any point P on the boundary of circle on the circular board.
3. Using rubber band make $\angle APB$ in the semi-circle as shown in Fig. 1.

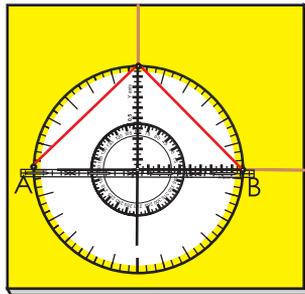


Fig.1

4. Measure $\angle APB$ using half protractor.

5. Repeat the activity by taking different positions of point P in the semi circle and complete the following table :

S. No.	$\angle APB$
1.	
2.	
3.	

Inference : Angle in a semicircle is

Think and discuss:

1. If AB is not a diameter then what will be the measure of $\angle APB$?
2. What can you say about an angle (i) in a major arc (ii) in a minor arc.

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Activity 34

PAIR OF OPPOSITE ANGLES OF A CYCLIC QUADRILATERAL

OBJECTIVE:

To verify that the sum of either pair of opposite angles of a cyclic quadrilateral is 180° .

MATERIAL REQUIRED:

Circular board, connectors (for circular board), rubber bands, two half protractor

HOW TO PROCEED?

1. Fix 4 connectors at suitable points A, B, C and D on the boundary of circle on the circular board and form a cyclic quadrilateral ABCD with the help of the rubber band as shown in the Fig.1.

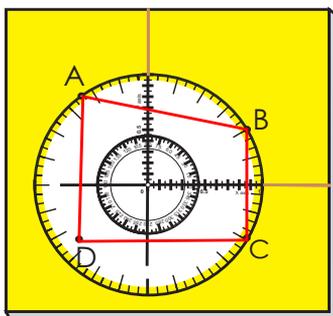


Fig.1

2. Measure $\angle ABC$ and $\angle ADC$ with the help of half protractor and find their sum.
3. Also measure $\angle BAD$ and $\angle BCD$ with the help of half protractor and find their sum.

4. Repeat the activity by forming other cyclic quadrilaterals by changing the position of connectors on the circular board and complete the following table :

S. No.	$\angle ABC$	$\angle ADC$	$\angle ABC + \angle ADC$	$\angle BCD$	$\angle BAD$	$\angle BCD + \angle BAD$
1.						
2.						
3.						

Inference : Sum of either pair of opposite angles of a cyclic quadrilateral is

Think and discuss:

If one of the points A, B, C and D is not on the boundary of circle on circular board, will $\angle ABC + \angle ADC = 180^\circ$ or $\angle BAD + \angle BCD = 180^\circ$?

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Activity 35

PAIR OF OPPOSITE ANGLES OF A NON CYCLIC QUADRILATERAL

OBJECTIVE:

To verify that the sum of either pair of opposite angles of a non-cyclic quadrilateral is not equal to 180° .

MATERIAL REQUIRED:

Circular board, plastic strips, connectors (for circular board), connectors (for strip), rubber bands, two half protractors.

HOW TO PROCEED?

1. Fix 4 connectors at points A, B, C and D on the circular board such that 3 connectors are on the boundary of circle and the fourth connector is outside the boundary of circle.
2. Form a quadrilateral ABCD, using rubber band as shown in Fig.1.

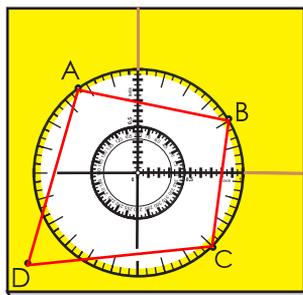


Fig.1

3. Measure $\angle ADC$ and $\angle ABC$ with the help of a half protractor and find their sum.

4. Similarly, measure $\angle DAB$ and $\angle DCB$ with the help of half protractor and find their sum. Repeat the activity by taking different positions of points and complete the following table :

S. No.	$\angle ADC$	$\angle ABC$	$\angle ADC + \angle ABC$	$\angle DAB$	$\angle DCB$	$\angle DAB + \angle DCB$
1.						
2.						
3.						

Inference: Is $\angle ADC + \angle ABC = 180^\circ$?

Is $\angle DAB + \angle DCB = 180^\circ$?

5. Now again fix four connectors on the circular board such that 3 connectors are on the boundary and the fourth connector is inside the boundary as shown in Fig.2.

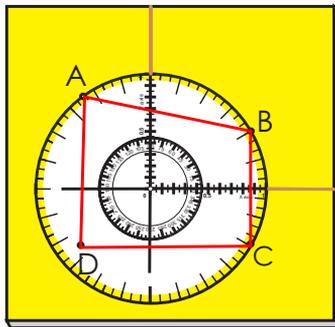


Fig.2

6. Measure $\angle ADC$ and $\angle ABC$ using a half protractor and find their sum.
7. Similarly, measure $\angle DAB$ and $\angle DCB$ by half protractor and find their sum. Repeat the activity by varying positions of points and complete the following table.

S. No.	$\angle DAC$	$\angle ABC$	$\angle DAC + \angle ABC$	$\angle DAB$	$\angle DCB$	$\angle DAB + \angle DCB$
1.						
2.						
3.						

Inference : The sum of either pair of opposite angles of a non cyclic quadrilateral is

Think and discuss:

In Fig.1 and Fig.2, slowly try to move point D towards the boundary of the circular board and find the sum of each pair of opposite angles accordingly. Is the sum coming closer and closer to 180° ?

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Activity 36

TANGENT AT A POINT ON A CIRCLE

OBJECTIVE:

To verify that a tangent at any point of circle is perpendicular to the radius through the point of contact.

MATERIAL REQUIRED:

Circular board, 1 plastic strip, one half protractor, rubber band, connector (for circular board)

HOW TO PROCEED?

1. Fix a plastic strip at a point say P on the boundary of circle on the circular board such that the strip touches the circle representing a tangent APB .
2. Fix a connector at the centre 'O' of circular board and join it with point P using a rubber band representing the radius OP of the circle as shown in the Fig.1.

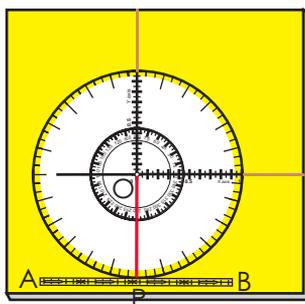


Fig.1

3. Measure $\angle OPA$ and $\angle OPB$ with the help of half protractor as shown in the Fig.2.

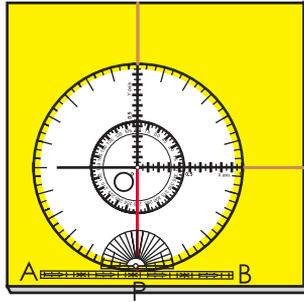


Fig.2

4. Repeat the activity by placing the strip at different points on the boundary of circle on the circular board and complete the following table :

S. No.	$\angle OPA$	$\angle OPB$
1.		
2.		
3.		

Inference : The tangent at any point of a circle is..... .

Think and discuss:

If Q is any point other than P on the strip. Is $OQ > OP$ or $OQ = OP$ or $OQ < OP$?

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Activity 37

TANGENTS TO A CIRCLE FROM AN EXTERNAL POINT

OBJECTIVE:

To verify that the length of two tangents drawn from an external point to a circle are equal.

MATERIAL REQUIRED:

Circular board, 2 plastic strips, connectors(for circular board)

HOW TO PROCEED?

1. Choose a convenient point P outside the boundary of circle on the circular board and fix 2 plastic strips at that point.
2. Now adjust the two strips in such a way that the two strips touch the boundary of circle on the circular board at two different points say 'A' and 'B' as shown in Fig.1.

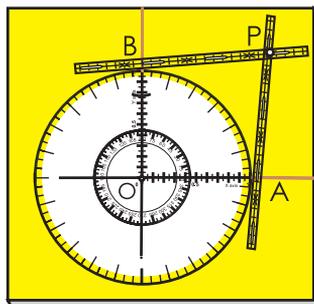


Fig.1

3. Measure the length of PA and PB using making on the plastic strips.
4. Repeat the activity by fixing the two strips at different positions outside the boundary of circle on the circular board and complete the following table:

S. No.	$\angle PA$	$\angle PB$	Is $\angle PA = \angle PB$?
1.			
2.			
3.			

Inference : Two tangents drawn from an external point to a circle are

Think and discuss:

What happens when P lies on the circle?

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Activity 38

TRIGONOMETRIC RATIOS-I

OBJECTIVE:

To understand the meaning of different trigonometric ratios using the circular board.

MATERIAL REQUIRED:

Circular board, wire needle, set square, plastic strips (B type), connectors(for circular board)

HOW TO PROCEED?

a) $\sin \theta, \cos \theta$

1. Fix the wire needle at the centre O of the circular board to make an angle POX with the horizontal line marked on the circular board as shown in Fig. 1.

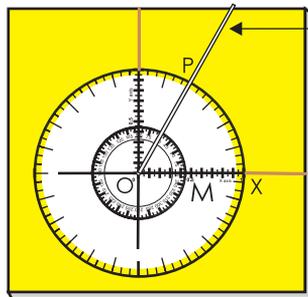


Fig.1

2. Place the set square such that one edge of the set square (other than the hypotenuse) coincides with the horizontal line.
3. Now slide the set square along the horizontal line so

that other edge of the set square forming the right angle passes through the point P (if necessary you may remove the needle temporarily to get the exact perpendicular) as shown in Fig.2.

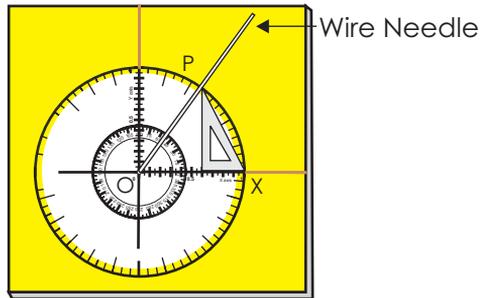


Fig.2

4. Place a plastic strip (B type) along this edge of the set square to represent a perpendicular PM on horizontal line OX as shown in Fig.3.

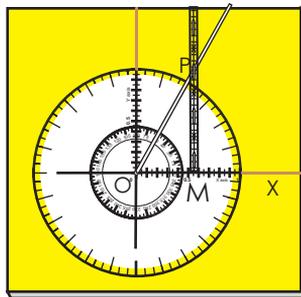


Fig.3

5. Now measure length of PM and OM

$$6. \quad \sin \theta = \frac{\text{Perpendicular}}{\text{Hypotenuse}} = \frac{PM}{OP} = \frac{PM}{1} = PM$$

$$\text{and } \cos \theta = \frac{\text{Base}}{\text{Hypotenuse}} = \frac{OM}{OP} = \frac{OM}{1} = OM$$

7. Repeat the activity by making different angles by varying the position of the needle and complete the following table:

S. No.	θ	PM	OM	$\sin \theta$	\cos
1.					
2.					
3.					

sine and cosine of complementary angles

8. In Fig.3 above, $\angle OPM = 90^\circ - \theta$

$$\sin(90^\circ - \theta) = \frac{\text{Perpendicular}}{\text{Hypotenuse}} = \frac{OM}{OP} = \frac{OM}{1} = OM = \cos \theta$$

$$\cos(90^\circ - \theta) = \frac{\text{Base}}{\text{Hypotenuse}} = \frac{PM}{OP} = \frac{PM}{1} = PM = \sin \theta$$

Thus, we have

$$\sin(90^\circ - \theta) = \cos \theta \text{ and } \cos(90^\circ - \theta) = \sin \theta$$

b) $\tan \theta, \sec \theta, \cot \theta, \operatorname{cosec} \theta$

HOW TO PROCEED:

1. Fix the wire needle at the centre O of circle on the circular board to make an angle POX with the horizontal line as shown in Fig.1.
2. Fix a plastic strip tangential to the circular board at point P and place another plastic strip along the horizontal line OX to meet first strip at point A as shown in Fig.4.

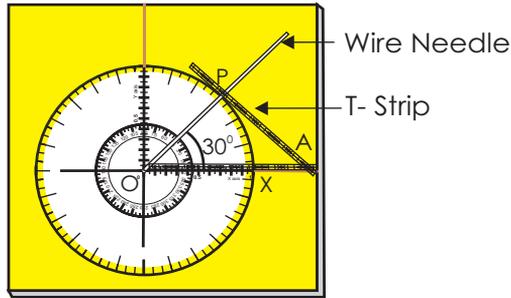


Fig.4

- Place another plastic strip along the vertical line passing through centre O to meet the first strip at point B as shown in Fig.5.

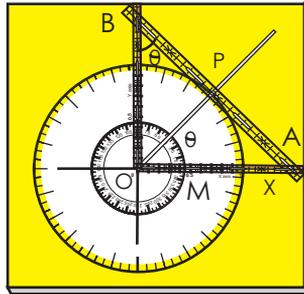


Fig.5

- From right triangle POA

$$\tan \theta = \frac{\text{Perpendicular}}{\text{Base}} = \frac{AP}{OP} = \frac{AP}{1} = AP$$

$$\text{and } \sec \theta = \frac{\text{Hypotenuse}}{\text{Base}} = \frac{OA}{OP} = \frac{OA}{1} = OA$$

- From right ΔPOB , $\angle PBO = \theta$

$$\cot \theta = \frac{\text{Base}}{\text{Perpendicular}} = \frac{BP}{OP} = \frac{BP}{1} = BP$$

$$\text{and } \operatorname{cosec} \theta = \frac{\text{Hypotenuse}}{\text{Perpendicular}} = \frac{OB}{OP} = \frac{OB}{1} = OB$$

6. Repeat the activity by making different angles by varying the position of needle and complete the following table :

S. No.	θ	$\tan \theta$	$\sec \theta$	$\operatorname{cosec} \theta$	$\cot \theta$
1.					
2.					
3.					

$\tan \theta, \sec \theta, \cot \theta, \operatorname{cosec} \theta$ of complementary angles

7. From triangle OAP given in Fig 5, $\angle OAP = 90^\circ - \theta$

$$\cot(90^\circ - \theta) = \frac{\text{Base}}{\text{Perpendicular}} = \frac{AP}{OP} = \frac{AP}{1} = AP = \tan \theta$$

$$\operatorname{cosec}(90^\circ - \theta) = \frac{\text{Hypotenuse}}{\text{Perpendicular}} = \frac{OA}{OP} = \frac{OA}{1} = OA = \sec \theta$$

Now, from POB given in Fig 5, $\angle BOP = (90^\circ - \theta)$

$$\tan(90^\circ - \theta) = \frac{\text{Perpendicular}}{\text{Base}} = \frac{BP}{OP} = \frac{BP}{1} = BP = \tan \theta$$

$$\sec(90^\circ - \theta) = \frac{\text{Hypotenuse}}{\text{Base}} = \frac{OB}{OP} = \frac{OB}{1} = OB = \operatorname{cosec} \theta$$

Thus, we have $\cot(90^\circ - \theta) = \tan \theta$

$$\operatorname{cosec}(90^\circ - \theta) = \sec \theta$$

$$\tan(90^\circ - \theta) = \cot \theta$$

$$\sec(90^\circ - \theta) = \operatorname{cosec} \theta$$

Think and discuss:

Can the trigonometric ratios \tan , \cot , \sec and cosec be obtained from Fig.3? Why are we using Fig.5?

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Activity 39

TRIGONOMETRIC RATIOS-II

OBJECTIVE:

To find the trigonometric ratios of some special angles such as 0° , 30° , 45° , 60° and 90°

MATERIAL REQUIRED:

Circular board, plastic strips(B type), connectors(for circular board), wire needle, set square

HOW TO PROCEED?

For sine and cosine of 0° , 30° , 45° , 60° and 90°

1. Fix a wire needle at the centre O of circle on the circular board such that it makes an angle $\angle POX = 30^\circ$ with the horizontal line OX as shown in Fig.1.

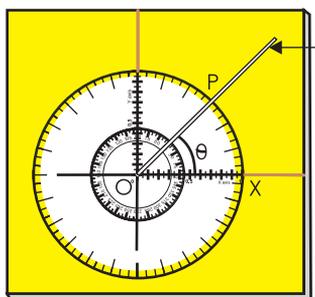


Fig.1

2. Now place a plastic strip passing through point P to represent a perpendicular PM on horizontal line OX using a set square (as done earlier in Activity No.39) as shown in Fig.2

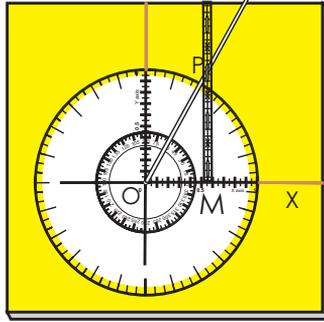


Fig.2

3. Now measure length of PM and OM.

$$4. \sin 30^\circ = \frac{PM}{OP} = \frac{PM}{1} = PM = 0.5$$

$$\cos 30^\circ = \frac{OM}{OP} = \frac{OM}{1} = OM = 0.9 \text{ (approx).}$$

5. The same activity can be repeated by taking $\angle POX$ as 45° and 60° .

6.1 For $\sin 0^\circ$ and $\cos 0^\circ$

- (i) Fix the wire needle to make any angle say $\angle POX = \theta$
- (ii) Fix a plastic strip to represent perpendicular PM on horizontal line OX using set square as explained earlier.
- (iii) Now rotate the wire needle in clockwise direction and accordingly change the position of the strip representing perpendicular PM.
- (iv) When the wire needle coincides with OX i.e. when $\theta = 0^\circ$, point P and M coincides. Then $OM = 1\text{dm}$ and PM becomes 0 as shown in Fig.3.

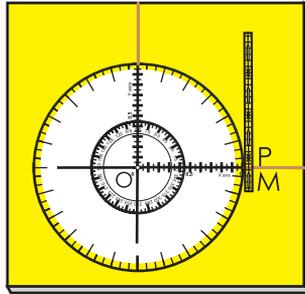


Fig.3

So, $\sin 0^\circ = PM = 0$ and $\cos 0^\circ = OM = 1$.

6.2 For $\sin 90^\circ$ and $\cos 90^\circ$

- (i) Fix a plastic strip to represent perpendicular PM on horizontal line OX as explained earlier in 6.1.
- (ii) Now rotate the wire needle in anticlockwise direction and accordingly change the position of strip representing PM.
- (iii) When the wire needle coincides with vertical line OY i.e. when $\theta = 90^\circ$ then point O and M coincides. Then $PM = 1$ dm and $OM = 0$ as shown in Fig.4.

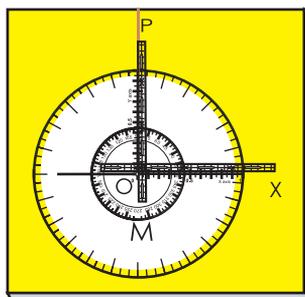


Fig.4

So, $\sin 90^\circ = PM = 1$ and $\cos 90^\circ = OM = 0$.

For tan, sec, cot and cosec of 30° , 45° and 60°

- (1) Fix the wire needle at the centre O of circle on the circular board to make an $\angle POX = 30^\circ$ with horizontal line OX (as explained earlier).
- (2) Fix a plastic strip tangential to the circular board at point P and place another strip along the OX to meet the first strip at point A as shown in Fig.5

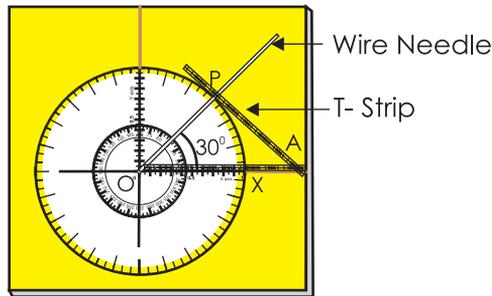


Fig.5

- (3) Place another plastic strip along the vertical line passing through the center O to meet the first strip at point B as shown in Fig.6

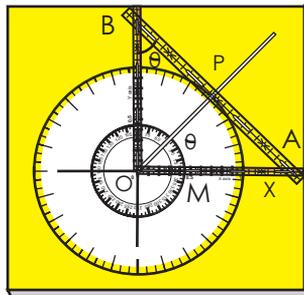


Fig.6

- (4) Now measure AP, OA, PB and OB

$$(5) \quad \tan 30^\circ = \frac{AP}{OP} = \frac{AP}{1} = AP$$

$$\sec 30^\circ = \frac{OA}{OP} = \frac{OA}{1} = OA$$

$$\cot 30^\circ = \frac{BP}{OP} = \frac{BP}{1} = BP$$

$$\operatorname{cosec} 30^\circ = \frac{OB}{OP} = \frac{OB}{1} = OB$$

(6) Same activity can be repeated by taking $\angle POX$ as 45° and 60°

7.1 For tan, sec, cot and cosec of 0°

- (i) Fix the wire needle to make any angle say $\angle POX = \theta$
- (ii) Fix a plastic strip to represent perpendicular PM on horizontal line OX using set square as explained earlier. Rotate the wire needle in clockwise direction and accordingly change the position of plastic strip, such that when wire needle coincides with OX i.e. when $\theta = 0^\circ$, AP becomes 0 as P and A coincides as shown in the Fig.7.

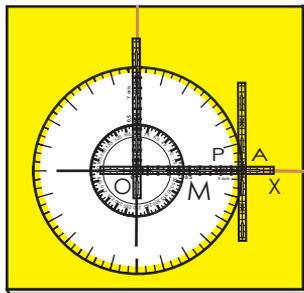


Fig.7

(iii) Now, $\tan 0^\circ = \frac{AP}{1} = \frac{0}{1} = 0$

(iv) Also, $\cot 0^\circ = PB$ where B is the point of intersection of the 2 plastic strips. Since the two strips are parallel, so PB is not defined. Thus, $\cot 0^\circ$ is not defined.

(v) $\operatorname{cosec} 0^\circ = OB$ where B is the point of intersection of the two plastic strips. Since the two strips are parallel so, OB is not defined. Thus, $\operatorname{cosec} 0^\circ$ is not defined.

7.2 For tan, sec, cot and cosec of 90°

(i) Arrange the strips as explained earlier in (7.1). Now rotate the wire needle anticlockwise and accordingly change the position of plastic strip such that when needle coincides with vertical line OY i.e. when $\theta = 90^\circ$, PB becomes 0 and points P & B coincides as shown in the Fig.8

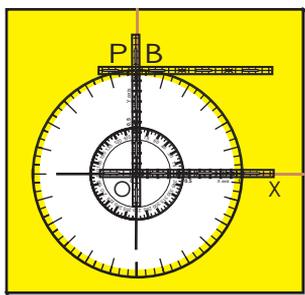


Fig.8

(ii) Now $\tan 90^\circ = \frac{AP}{1}$ where A is the intersection point of the two plastic strips. Since two strips are parallel. So AP is not defined.

(iii) $\sec 90^\circ = OA$ where A is the point of intersection of the two strips. But the two strips are parallel. So, OA is not defined. Thus $\sec 90^\circ$ is not defined

$$(iv) \text{ Also, } \cot 90^\circ = \frac{PB}{1} = \frac{0}{1} = 0$$

$$\text{and } \operatorname{cosec} 90^\circ = \frac{OB}{1} = \frac{1}{1} = 1$$

Think and discuss:

- (i) Is $\sin 30^\circ = \cos 60^\circ$
- (ii) Is $\tan 0^\circ = \cot 90^\circ$
- (iii) Is $\sin 45^\circ = \cos 45^\circ$
- (iv) Is $\sin 30^\circ = \operatorname{cosec} 30^\circ$
- (v) Is $\cos 60^\circ = \sec 60^\circ$

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Activity 40

TRIGONOMETRIC RATIOS AND SIDES OF RIGHT TRIANGLE

OBJECTIVE:

To verify that the values of trigonometric ratios of an angle do not vary with the lengths of the sides of the triangle.

MATERIAL REQUIRED:

Geoboard, rubber bands, ruler, Geoboard pins

HOW TO PROCEED?

1. Fix 5 geoboard pins on the geoboard at suitable points A, B, C, D and E and join them with 2 rubber bands of different colours to represent two similar right triangles as shown in the Fig.1.

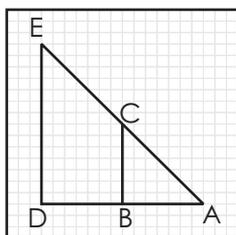


Fig1

2. Measure length of AB, BC, AD, DE, AC and AE using a ruler.
3. Find $\frac{BC}{AC}, \frac{AB}{AC}, \frac{BC}{AB}, \frac{DE}{AE}, \frac{AD}{AE}, \frac{DE}{AD}$

4. Repeat the activity by making other pairs of similar right triangles and complete the following table

S. No.	AB	BC	AC	$\frac{BC}{AC}$	$\frac{AB}{AC}$	$\frac{BC}{AB}$	AD	DE	AE	$\frac{DE}{AE}$	$\frac{AD}{AE}$	$\frac{DE}{AD}$
1.												
2.												
3.												

Inference:

(i) Since $\frac{BC}{AC} = \frac{DE}{AE}$

So, $\sin A$ does not vary with the change of the length of the sides of the .

(ii) $\frac{AB}{AC} = \dots\dots\dots$, So, $\cos A = \dots\dots\dots$

(iii) $\frac{BC}{AB} = \dots\dots\dots$, So, $\tan A = \dots\dots\dots$

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Activity 41

TRIGONOMETRIC IDENTITIES

OBJECTIVE:

To verify standard trigonometric identities.

MATERIAL REQUIRED:

Circular board, wire needle, set square, T-strips, connectors (for circular board)

HOW TO PROCEED?

(A) For identity $\sin^2\theta + \cos^2\theta = 1$

1. Fix the wire needle at the centre O of the circular board to make an angle POX as θ with the horizontal line as shown in Fig. 1.

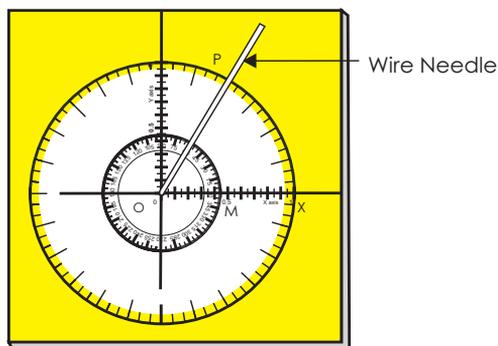


Fig.1

2. Place a T-strip to represent a perpendicular PM on OX using set square (as done in earlier activity) as shown in Fig .2.

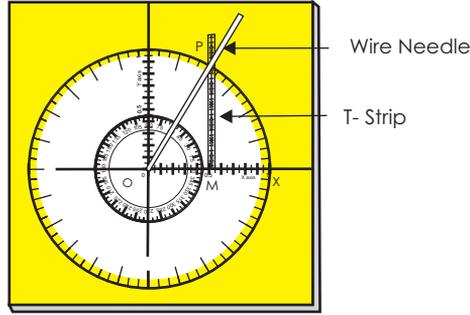


Fig.2

3. Now $\sin \theta = \frac{\text{Perpendicular}}{\text{Hypotenuse}} = \frac{PM}{1} = PM$

and $\cos \theta = \frac{\text{Base}}{\text{Hypotenuse}} = \frac{OM}{1} = OM$

Now, $\sin^2\theta + \cos^2\theta = (PM)^2 + (OM)^2$
 $= (OP)^2$ (Pythagoras theorem)

or $\sin^2\theta + \cos^2\theta = (1)^2 = 1$

(B) For identities $1 + \tan^2\theta = \sec^2\theta$ and $1 + \cot^2\theta = \text{cosec}^2\theta$

- (1) Fix the wire needle at the centre O of the circular board to make an angle POX as θ with horizontal line OX as shown in Fig 1 (done earlier)
- (2) Fix a T-strip tangential to circular board at point P and place another T-strip along horizontal line OX to meet first strip at point A as done earlier.
- (3) Now place another T-strip along the vertical line, passing through centre O to meet the T-strip at point B as shown in the Fig.3.

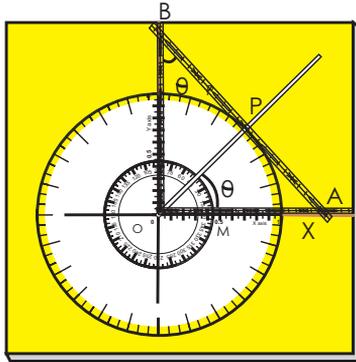


Fig.3

(5) From right ΔPOA

$$\tan \theta = \frac{\text{Perpendicular}}{\text{Base}} = \frac{AP}{1} = AP$$

$$\text{and } \sec \theta = \frac{\text{Hypotenuse}}{\text{Base}} = \frac{OA}{1} = OA$$

$$\text{so, } 1 + \tan^2 \theta = 1 + (AP)^2$$

$$= (OP)^2 + (AP)^2$$

$$= (OA)^2 \quad (\text{Pythagoras theorem})$$

$$= \sec^2 \theta$$

(6) From right ΔPOB

$$\cot \theta = \frac{\text{Base}}{\text{Perpendicular}} = \frac{BP}{1} = BP$$

$$\text{and } \operatorname{cosec} \theta = \frac{\text{Hypotenuse}}{\text{Perpendicular}} = \frac{OB}{1} = OB$$

$$\text{so, } 1 + \cot^2 \theta = 1 + (BP)^2$$

$$= (OP)^2 + (BP)^2$$

$$= (OB)^2 \quad (\text{Pythagoras theorem})$$

$$\text{so, } 1 + \cot^2\theta = \operatorname{cosec}^2\theta$$

Inference : values of $\sin q$, $\cos q$ and other trigonometric ratios can be identified for q being in different quadrants.

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Activity 42

SURFACE AREA AND VOLUME OF SOLIDS

OBJECTIVE:

- (i) To understand the concept of surface area and volume of solids.
- (ii) To verify the fact that increase/decrease in the volume of a solid may not result the same change in its surface area.

MATERIAL REQUIRED:

One solid wooden cube, cut out of a cuboid, right circular cylinder, right circular cone and hemisphere embedded in cube.

HOW TO PROCEED?

1. Take solid wooden cube (say of side a) along with all the cut-outs fitted in it as shown in Fig. 1.

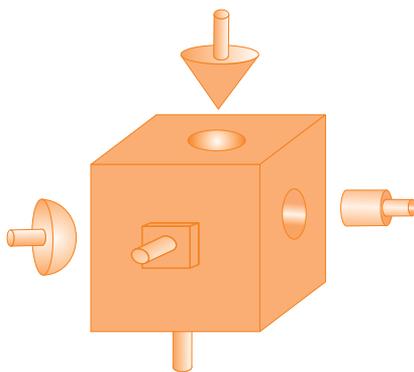


Fig.1

- Take out the cut out of cuboid say of dimension l , b & h from cube as shown in Fig.2.

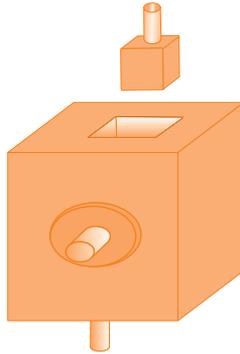


Fig.2

- Find the volume and surface area of the cut-out of cuboid.
- Find the volume and surface area of the remaining solid i.e. solid left after taking out cuboid from the given cube.
- Take different values of a , l , b & h and find the change in the volume and surface area of the original cube and the left out solid. Now complete the following table :

S. No.	Cube		Cuboid		Left out solid	
	Volume a^3	TSA $6a^2$	Volume lbh	TSA $2(lb+bh+lh)$	Volume a^3-lbh	TSA $6a^2+2h(l+b)$
1.						
2.						
3.						

- Repeat the same activity for cut-outs of a cylinder, a cone and an hemisphere as shown in following figures.

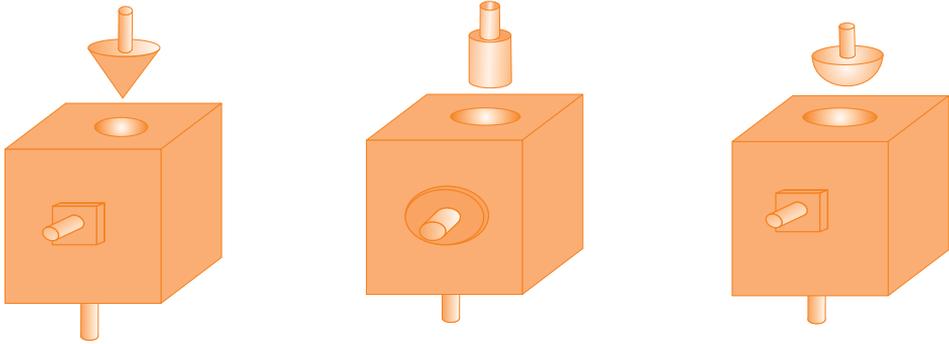


Fig 3

Cylinder

Let r be the base radius and h be the height of the cylinder
 Take different values of r & h to complete the following table :

S. No.	Cube		Cylinder		Left out solid	
	Volume	TSA	Volume	TSA	Volume	TSA
	a^3	$6a^2$	$\pi r^2 h$	$2\pi r(r+h)$	$a^3 - \pi r^2 h$	$6a^2 + 2\pi rh$
1.						
2.						
3.						

Cone

Let r be the base radius and h be the height and l be the slant height of given cut-out of cone. Take different values of r , l and h to complete the following table :

S. No.	Cube		Cone		Left out solid	
	Volume	TSA	Volume	TSA	Volume	TSA
	a^3	$6a^2$	$\frac{1}{3}\pi r^2 h$	$\pi r(l+r)$	$a^3 - \frac{1}{3}\pi r^2 h$	$6a^2 - \pi r(r-l)$
1.						
2.						
3.						

Hemisphere

Let r be the radius of given cut-out of hemisphere. Take different values of r to complete the following table :

S. No.	Cube		Hemisphere		Left out solid	
	Volume	TSA	Volume	TSA	Volume	TSA
	a^3	$6a^2$	$\frac{2}{3}\pi r^3$	$3\pi r^2$	$a^3 - \frac{2}{3}\pi r^3$	$6a^2 + \pi r^2$
1.						
2.						
3.						

Inference

- (i) Volume of left out solid decreases by the amount of volume of the cutout solid.
- (ii) Surface area of the left out solid increases in each case as compared to the original surface area of the solid.
- (iii) From the above observations, we conclude that decrease (increase) in the volume of a solid need not result in decrease (increase) in the surface area of the resulting solid.

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