

4<sup>th</sup> Sept,  
SATURDAY

# 11. ROOF TRUSSES

→ Selection criteria for  
Roof truss:

- Span of the truss.
- Pitch of the truss.

Pitch of the truss depends  
on:

(i) Type of roof covering  
material to be used for truss (like AC sheets, GI sheets,  
plastic sheets)

(ii) Lightening & ventilation requirement.

$$\text{Pitch} = \frac{\text{Rise}}{\text{Span}} = \frac{h}{L}$$

$$\text{Slope} = \tan \theta = \frac{\text{Rise}}{\text{Half span}} = \frac{h}{L/2} = \frac{2h}{L}$$

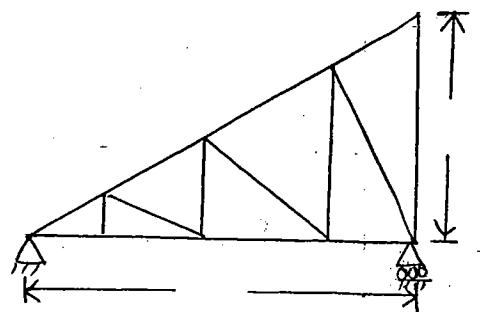
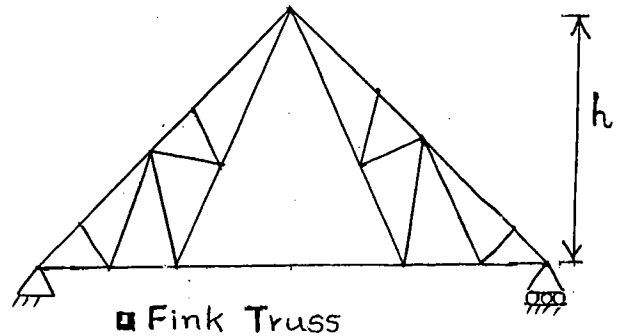
$$\boxed{\text{Slope} = 2 \times \text{pitch}} \quad (\text{for symmetric truss})$$

\* North Light Roof Truss

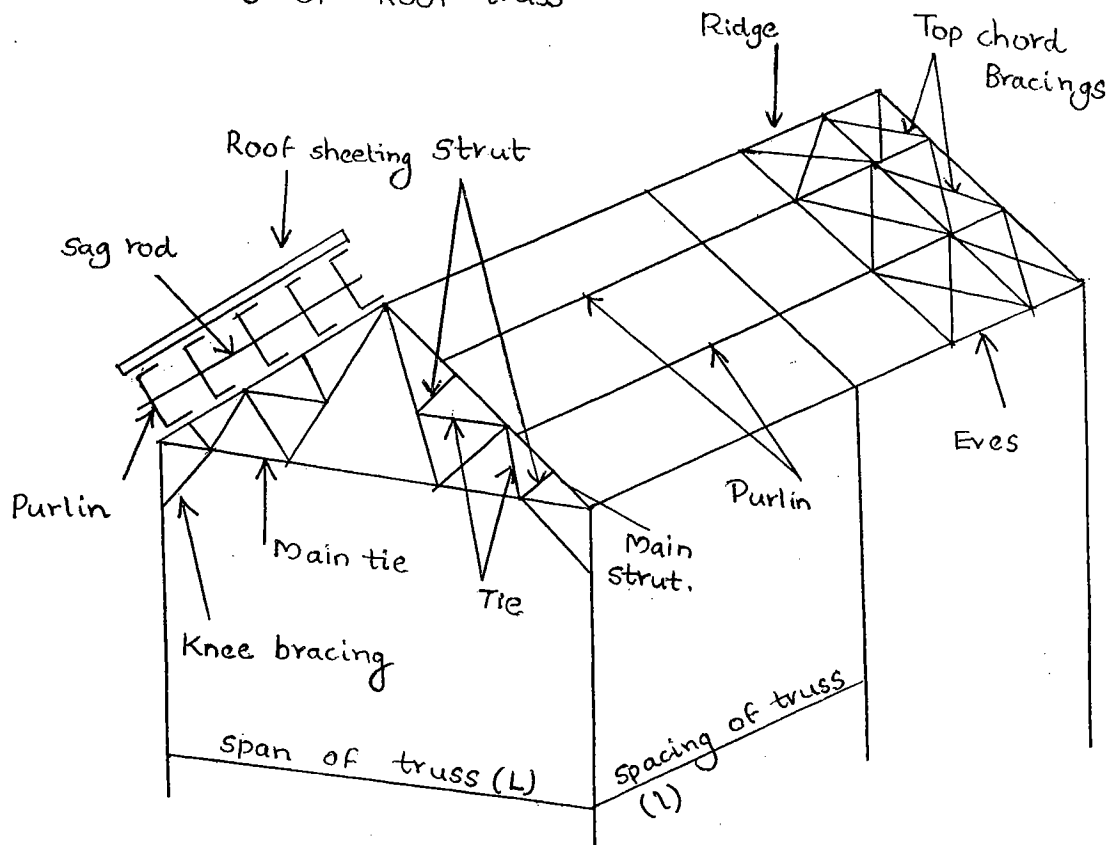
- Spans upto 10 m
- Day light is main criteria  
for selection of North light roof  
truss.

$$\text{Pitch} = \frac{h}{L}$$

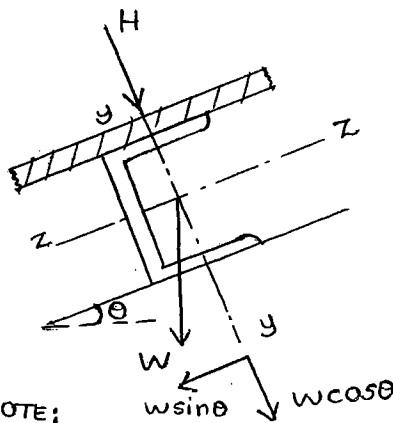
$$\text{Slope} = \tan \theta = \frac{h}{L} \Rightarrow \boxed{\text{Pitch} = \text{Slope}}$$



## → Elements of Roof truss



- Top Chord bracings are not required when masonry walls are provided.



NOTE:

$$M_{zz} = \frac{\gamma_L (H + W \cos \theta) l^2}{10}$$

$$M_{yy} = \frac{\gamma_L (W \sin \theta) l^2}{10}$$

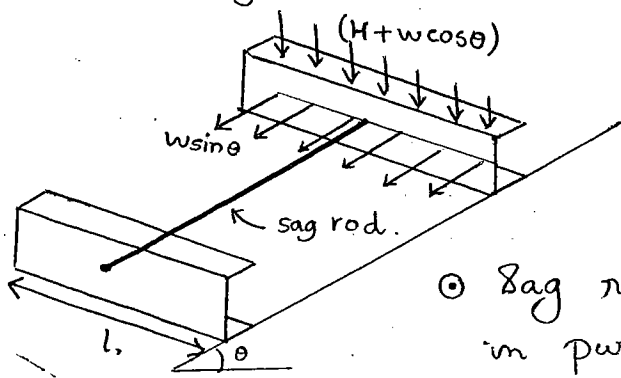
$W \rightarrow$  gravity load due to DL & LL (N/m or KN/m)

$H \rightarrow$  load due to wind pressure (N/m or KN/m)

$\gamma_L \rightarrow$  load factor.

- Purlin member may be designed as simply supported beam or cantilever beam or continuous beam. IS 800:2007 recommends to design as continuous beam subj to bi-axial bending moment

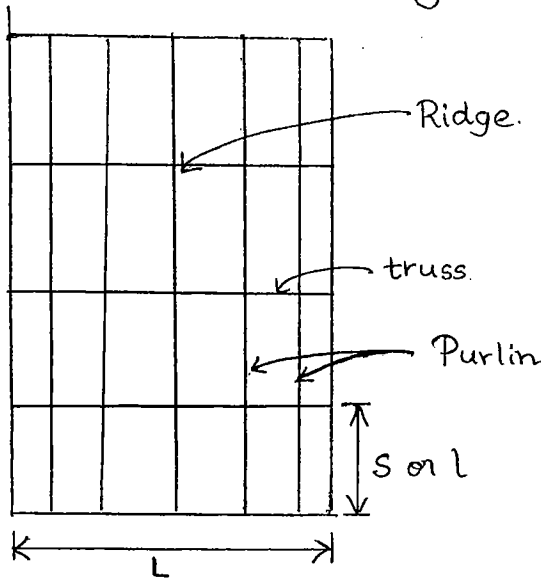
$$M_{yy} = \frac{\gamma_L W \sin \theta (l/2)^2}{10}$$



$$= \frac{1}{4} \gamma_L \frac{W \sin \theta l^2}{10}$$

- Sag rod will minimise deflection and BM in purlin member about minor principal axis

→ Economical spacing of truss (s or l)



$t \rightarrow$  cost of truss per unit area

$p \rightarrow$  cost of purlin per unit area

$r \rightarrow$  cost of roof sheeting per unit area.

$x \rightarrow$  total (or) overall cost of roof building per unit area.

$$x = t + p + r$$

$$\textcircled{1} \quad t \propto \frac{1}{s} \Rightarrow t = \frac{C_1}{s} \quad \therefore C_1 = ts$$

$$m = \frac{wl^2}{10} \Rightarrow p \propto s^2$$

$$\textcircled{2} \quad p = C_2 s^2 \Rightarrow C_2 = \frac{p}{s^2}$$

$\textcircled{3}$  As spacing increases, no. of joints b/w roofing sheets increase and as a result cost of erection increases.

$$r = C_3 s \Rightarrow C_3 = \frac{r}{s}$$

$$x = t + p + r$$

$$x = \frac{C_1}{s} + C_2 s^2 + C_3 s$$

To have minimum cost of roof building,

$$\frac{dx}{ds} = 0$$

$$\frac{d}{ds} \left( \frac{C_1}{s} + C_2 s^2 + C_3 s \right) = 0.$$

$$-\frac{C_1}{s^2} + 2C_2 s + C_3 = 0$$

$$\frac{C_1}{s^2} = 2C_2 s + C_3.$$

$$\frac{ts}{s^2} = \frac{2p}{s^2} s + \frac{r}{s} \Rightarrow \boxed{t = 2p + r}$$

G6 (55)

Cost of truss per unit area =  $2 \times$  cost of purlin per unit area  
+ cost of roof covering per unit area.

$$l \text{ or } s = \frac{L}{3} \text{ to } \frac{L}{5}$$

→ Design Loads on Roof truss

- design dead loads.
- design live (or) imposed loads.
- design wind loads.
- design snow loads.

\* Design Dead Loads (IS 875 : 1987 Part I)

- (i) Self weight of purlins.
- (ii) Self weight of bracings.
- (iii) Self weight of roof sheeting
- (iv) Self weight of truss.

$$\begin{aligned} \text{Self weight of truss} &= 100 \text{ N/m}^2 \text{ to } 150 \text{ N/m}^2 \text{ Plan area} \\ &= \left( \frac{L}{3} + 5 \right) \times 10 \text{ N/m}^2 \text{ Plan area.} \\ &\quad (L = \text{span of truss}) \end{aligned}$$

\* Design Live (or) Imposed loads (IS 875 : 1987 Part II)

- Slope of roof,  $\theta \leq 10^\circ$

$$LL = 1500 \text{ N/m}^2 \text{ (if access is provided for repair \& maintenance)}$$

$$= 750 \text{ N/m}^2 \text{ (if access is not provided for repair \& maintenance)}$$

- Slope of roof,  $\theta > 10^\circ$

$$LL = (750 - 20(\theta - 10)) \text{ N/m}^2 \neq 400 \text{ N/m}^2$$

\* Design Snow Load. (IS 875: 1987 Part IV)

$$\begin{aligned} SL &= 25 \text{ N/m}^2 \text{ per every 'cm' depth of snow.} \\ &= 2.5 \text{ N/m}^2 \text{ per every 'mm' depth of snow.} \end{aligned}$$

$\theta > 50^\circ$ ; Snow load need not to be considered.

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\* Design Wind Load. (IS 875: 1987 Part III)

$V_b$  = Basic wind speed in m/s at a height of 10m from MSL

$V_z$  = Design wind speed in m/s at a height  $z$ .

$$V_z = K_1 K_2 K_3 V_b$$

where  $K_1 \rightarrow$  probability (or) risk factor

$K_2 \rightarrow$  size, shape and structure factor.

$K_3 \rightarrow$  topography factor.

$P_z$  = Design wind pressure at a height  $z$  of a structure.

$$P_z = K \cdot V_z^2$$

$$P_z = 0.6 V_z^2 \quad (K = 0.6)$$

Design wind load =  $(C_{pe} - C_{pi}) P_z \cdot A_e$ .

where  $A_e \rightarrow$  exposed area.

$C_{pe} \rightarrow$  external wind pressure coefficient  
(depends on slope of roof)

$C_{pi} \rightarrow$  internal wind pressure coefficient  
(depends on degree of permeability (or)  
no. of openings in structure)

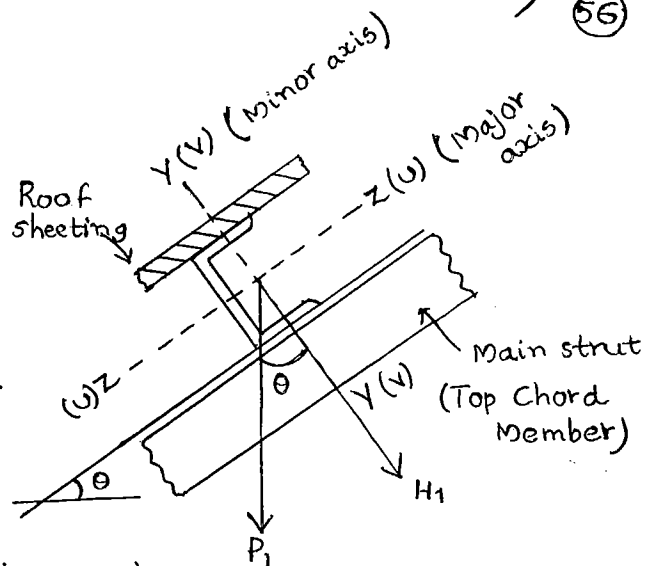
## → Design of Purlin

$P_1$  = Gravity load due to sheeting and live load.  
(in  $\text{KN/m}$ )

$H_1$  = load due to wind pressure  
in  $\text{KN/m}$ .

$l$  = span of purlin  
(spacing b/w two adjacent trusses).

$\theta$  = slope of roof.



IS 800:2007 recommends to design a purlin as a continuous beam subjected to biaxial (unsymmetrical) BMs.

Load along minor axis (YY axis)

$$P = \gamma_L (H_1 + P_1 \cos \theta) \rightarrow M_{zz}$$

Load along major axis (ZZ axis)

$$H = \gamma_L (P_1 \sin \theta) \rightarrow M_{yy}$$

Bending moment about major axis,  $M_{zz} = \frac{P l^2}{10}$ .

Bm about minor axis,  $M_{yy} = \frac{H l^2}{10}$ .

\* Deflection (or) Serviceability limits: (IS 800:2007)

(i) Brittle cladding (or sheet) =  $\frac{L}{180}$   
Eg: AC roofing sheet

(ii) Elastic cladding =  $\frac{L}{150}$   
Eg: GI, Plastic roofing sheet

- Design bending strength about major axis ( $M_{dz}$ ).

$$M_{dz} = Z_{pz} \cdot \frac{f_y}{\gamma_{mo}}$$

- Design bending strength about minor axis ( $M_{dy}$ ).

$$M_{dy} = Z_{py} \cdot \frac{f_y}{\gamma_{mo}}$$

$Z_{pz}$  &  $Z_{py}$  : Plastic section modulus of purlin about major & minor axis resptly.

- For safety of purlin, Interaction Equation as per IS 800 : 2007 must be satisfied:

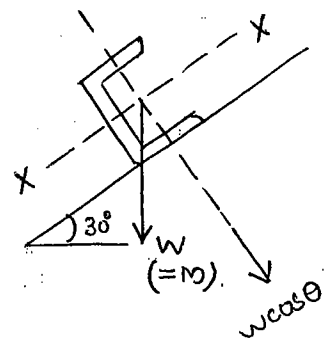
$$\textcircled{a} \quad \frac{M_{zz}}{M_{dz}} + \frac{M_{yy}}{M_{dy}} \leq 1.0 \quad \begin{array}{l} M_{dz} > M_{zz} \\ M_{dy} > M_{yy} \end{array}$$

$$\textcircled{b} \quad \Delta_{cal} \leq \Delta_{limit} ; \Delta_{limit} = \text{limiting deflection.}$$

2

For  $w$ ,  $M_{xx} = M$

$$\begin{aligned} \text{For } w \cos 30, M_{xx} &= M \cos 30 \\ &= \frac{\sqrt{3}}{2} M \end{aligned}$$



3.

$$M_{dz} = Z_{pz} \cdot \frac{f_y}{\gamma_{mo}}$$

$$M_{dy} = Z_{py} \cdot \frac{f_y}{\gamma_{mo}}$$



Section modulus ( $Z_{pz}$  &  $Z_{py}$ ) is independent of orientation of sections.

04. As per IS 800:1984, angle iron purlins were used

68  
(57)

\* Assumptions:

(i) Slope,  $\theta \leq 30$  (exposed area for wind force gets minimised).

(ii) Bending moment about minor axis neglected.

(iii)  $LL = 750 \text{ N/mm}^2$ .

08 Slope = 1

$$\tan \theta = 1 \Rightarrow \underline{\underline{\theta = 45^\circ}}$$