Quadratic Equations

Exercise 1.1 I. Very Short Answer Type Questions [1 Mark] 1. Multiple Choice Questions (MCQs) Choose the correct answer from the given options: (1) Which of the following is a quadratic equation? (b) $-2x^2 = (5-x)\left(2x-\frac{2}{5}\right)$ (a) $x^{2} + 2x + 1 = (4 - x)^{2} + 3$ (c) $(k+1)x^2 + \frac{3}{2}x = 7$ (where k = -1) (d) $x^3 - x^2 = (x-1)^3$ (2) Which of the following equations has 2 as a root? (a) $x^2 - 4x + 5 = 0$ (b) $x^2 + 3x - 12 = 0$ (c) $2x^2 - 7x + 6 = 0$ (d) $3x^2 - 6x - 2 = 0$ (3) The roots of the quadratic equation $x^2 - 0.04 = 0$ are [CBSE Standard 2020] (a) ± 0.2 (b) ± 0.02 (c) 0.4(d) 2 (4) The degree of quadratic equation is (c) 2(a) 0(b) 1 (d) 5 2. Assertion-Reason Type Questions In the following questions, a statement of assertion (A) is followed by a statement of reason (R). Mark the correct

In the following questions, a statement of assertion (A) is followed by a statement of reason (R). Mark the col choice as:

- (a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).
- (b) Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A).
- (c) Assertion (A) is true but reason (R) is false.
- (d) Assertion (A) is false but reason (R) is true.
- (1) Assertion (A): The equation $x^2 + 3x + 1 = (x 2)^2$ is a quadratic equation. Reason (R): Any equation of the form $ax^2 + bx + c = 0$ where $a \neq 0$, is a quadratic equation.
- (2) Assertion (A): $(2x-1)^2 4x^2 + 5 = 0$ is not a quadratic equation. Reason (R): x = 0, 3 are the roots of the equation $2x^2 - 6x = 0$.

3. Answer the following.

- [Delhi 2015]
- (1) If $x = -\frac{1}{2}$ is a solution of the quadratic equation $3x^2 + 2kx 3 = 0$, find the value of k. (2) Find the value of k for which $x = \sqrt{3}$ is a solution of the equation $kx^2 + \sqrt{3}x 4 = 0$.

II. Short Answer Type Questions -I

- 4. If $x = \frac{2}{3}$ and x = -3 are roots of the quadratic equations $ax^2 + 7x + b = 0$, find the values of a and b.
- 5. Show that x = -2 is a solution of the equation $3x^2 + 13x + 14 = 0$.

III. Short Answer Type Questions - II

Represent the following situations in the form of a quadratic equation (Q. 6 & Q.7):

- 6. John and Jivanti together have 45 marbles. Both of them lost 5 marbles each, and the product of the number of marbles they have now is 124. We would like to find out how many marbles they had to start with.
- 7. A cottage industry produces a certain number of toys in a day. The cost of production of each toy (in rupees) was found to be 55 minus the number of toys produced in a day. On a particular day, the total cost of production was ₹ 750. We would like to find out the number of toys produced on that day.
- 8. If one root of the quadratic equation $3x^2 + px + 4 = 0$ is $\frac{2}{3}$, then find the value of p and the other root of the equation.

Case Study Based Questions

I. Raj and Ajay are very close friends. Both the families decide to go to Ranikhet by their own cars. Raj's car travels at a speed of x km/h while Ajay's car travels 5 km/h faster than Raj's car. Raj took 4 hours more than Ajay to complete the journey of 400 km.



1. What will be the distance covered by Ajay's car in two hours?

(a)
$$2(x+5)$$
 km (b) $(x-5)$ km (c) $2(x+10)$ km (d) $(2x+5)$ km

2. Which of the following quadratic equations describes the speed of Raj's car?

(a)
$$x^2 - 5x - 500 = 0$$
 (b) $x^2 + 4x - 400 = 0$ (c) $x^2 + 5x - 500 = 0$ (d) $x^2 - 4x + 400 = 0$

3. The roots of the quadratic equation which describe the speed of Raj's car are

(a)
$$15, -20$$
 (b) $20, -15$ (c) $20, -25$ (d) $25, -25$

4. Which of the following quadratic equations has 2 as a root?

(a)
$$x^2 - 4x + 5 = 0$$
 (b) $x^2 + 3x - 12 = 0$ (c) $2x^2 - 7x + 6 = 0$ (d) $3x^2 - 6x - 2 = 0$

5. The positive root of
$$\sqrt{3x^2 + 6} = 9$$
 is
(a) 5 (b) -5 (c) 3 (d) -3

[Delhi 2016]

[3 Marks]

[2 Marks]

 \Rightarrow

1. (1) (d) $x^3 - x^2 = (x - 1)^3$ (1) (2) (c) $2x^2 - 7x + 6 = 0$ (1) (3) $(a) \pm 0.2$ (1)(4) (c) 2(1)**2.** (1) (*d*) Assertion (A) is false but reason (R) is true. (1) (2) (b) Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A). (1)3. (1) :: $x = \frac{-1}{2}$ is the solution of $3x^2 + 2kx - 3 = 0$ So, $3\left(\frac{-1}{2}\right)^2 + 2k\left(\frac{-1}{2}\right) - 3 = 0$ $\frac{3}{4} - k - 3 = 0$ \Rightarrow $k = \frac{3}{4} - 3$ \Rightarrow $k = -2\frac{1}{4}$ (1) \Rightarrow (2) We have $kx^2 + \sqrt{3}x - 4 = 0$ $\Rightarrow k\left(\sqrt{3}\right)^2 + \sqrt{3}\left(\sqrt{3}\right) - 4 = 0$ 3k + 3 - 4 = 0 \Rightarrow 3k - 1 = 0 \Rightarrow 3k = 1 \Rightarrow $k = \frac{1}{2}$ \Rightarrow Hence, the required value of k is $\frac{1}{2}$. (1)4. Given quadratic equation is $ax^2 + 7x + b = 0$...(*i*) $a\left(\frac{2}{3}\right)^2 + 7\left(\frac{2}{3}\right) + b = 0$ $[\because x = \frac{2}{3} \text{ is the root of eq. } (i)]$

$$\Rightarrow \frac{4a+42+9b}{9} = 0$$

$$\Rightarrow 4a+9b+42 = 0 \qquad \dots(ii)$$

Also, $a(-3)^2 + 7(-3) + b = 0$
[$\because x = -3$ is the root of eq. (i)]

$$\Rightarrow 9a+b-21 = 0$$

$$b = 21 - 9a$$
 ...(*iii*)(1)

Putting the value of b from (iii) in (ii), we get

$$4a + 9[21 - 9a] + 42 = 0$$

$$\Rightarrow 4a + 189 - 81a + 42 = 0$$

$$\Rightarrow a = 3$$

Putting $a = 3$ in (*iii*), we have
 $b = -6$
So $a = 3$, $b = -6$
(1)

So,
$$a = 3, b = -6.$$
 (1)
6. $x^2 - 45x + 324 = 0$ (3)

$$7 \quad r^2 - 55r + 750 = 0 \tag{3}$$

8.
$$3x^2 + px + 4 = 0$$
 (1/2)

x = 2

$$3\left(\frac{2}{3}\right)^{2} + p\left(\frac{2}{3}\right) + 4 = 0$$

$$4 - 2p - 4 = 0$$

$$\frac{4}{3} + \frac{2p}{3} + 4 = 0 \tag{1/2}$$

$$p = -8 (1/2)$$

$$2r^2 8r + 4 = 0$$

$$3x^2 - 6x - 2x + 4 = 0$$
 (½)

$$x = \frac{2}{3}$$
 or $x = 2$ (1/2)

Hence,

 $(\frac{1}{2})$

Case Study Based Questions

I. 1. (a)
$$2(x + 5)$$
 km2. (c) $x^2 + 5x - 500 = 0$ 3. (c) $20, -25$ 4. (c) $2x^2 - 7x + 6 = 0$ 5. (a) 5

Exercise 1.2

I. Very Short Answer Type Questions

- **1.** Multiple Choice Questions (MCQs) Choose the correct answer from the given options:
 - (1) The roots of the equation $\frac{4}{3}x^2 2x + \frac{3}{4} = 0$ are (a) $\frac{2}{3}, \frac{3}{2}$ (b) $\frac{3}{4}, \frac{3}{4}$ (c) $\frac{1}{2}, -\frac{1}{2}$ (d) None of these
 - (2) The required solution of $4x^2 25x = 0$ are

(a)
$$x = 0, x = \frac{12}{7}$$
 (b) $x = 0, x = \frac{25}{4}$ (c) $x = 1, x = \frac{5}{9}$ (d) $x = 1, x = \frac{12}{7}$

2. Assertion-Reason Type Questions

In the following questions, a statement of assertion (A) is followed by a statement of reason (R). Mark the correct choice as:

- (a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).
- (b) Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A).
- (c) Assertion (A) is true but reason (R) is false.

[1 Mark]

- (d) Assertion (A) is false but reason (R) is true.
- (1) Assertion (A): When the quadratic equation $6x^2 x 2 = 0$ is factorised, we get its roots as $\frac{2}{2}$ and $-\frac{1}{2}$ **Reason (R):** $6x^2 - x - 2 = 0 \implies 2x(3x - 2) + (3x - 2) = 0 \implies (3x - 2)(2x + 1) = 0 \implies x = \frac{2}{3}, -\frac{1}{2}$ (2) Assertion (A): If $x^2 - (\sqrt{3} + 1)x + \sqrt{3} = 0$, then $x^2 - \sqrt{3}x - x + \sqrt{3} = 0$

 $\Rightarrow \quad x(x-\sqrt{3})-1(x-\sqrt{3})=0 \quad \Rightarrow \quad (x-\sqrt{3})(x-1)=0 \quad \Rightarrow \quad x=\sqrt{3}, 1$

Reason (R): If we can factorise $ax^2 + bx + c$, $a \ne 0$ into a product of two linear factors, then the roots of the quadratic equation $ax^2 + bx + c = 0$ can be found by equating each factor to zero.

3. Answer the following.

Find the roots of the following quadratic equations by factorisation [(1) to (4)]:

(1) $\sqrt{3}x^2 + 10x + 7\sqrt{3} = 0$ [Imp.] (2) (x-3)(2x+3) = 0

(3)
$$3x^2 - 2ax - a^2 = 0$$
 (4) $3a^2x^2 + 8abx + 4b^2 = 0$

(5) Find the roots of the equation $x^2 + 7x + 10 = 0$.

II. Short Answer Type Questions -I

Find the roots of the following quadratic equations by factorisation (Q4 to Q10).

- 4. Solve for x: $4\sqrt{3}x^2 + 5x 2\sqrt{3} = 0$
- 5. Solve for x: $x^2 (\sqrt{2} + 1)x + \sqrt{2} = 0$ [Foreign 2013]
- 6. Solve for x: $\sqrt{2x+9} + x = 13$.

7. Solve for x:
$$\sqrt{6x+7-(2x-7)} = 0.$$
 [AI 2016]

- 8. Solve for x: $\sqrt{3}x^2 2\sqrt{2}x 2\sqrt{3} = 0$. [Foreign 2016]
- 9. Solve for x: $\frac{1}{x-3} \frac{1}{x+5} = \frac{1}{6}$, $x \neq 3, -5$. [Foreign 2016]
- **10.** Solve for x: $\sqrt{3}x^2 + 14x 5\sqrt{3} = 0$

III. Short Answer Type Questions - II

11. Solve for x: $\frac{x+1}{x-1} + \frac{x-2}{x+2} = 4 - \frac{2x+3}{x-2}$; $x \neq 1, -2, 2$.

12. The difference of two natural numbers is 3 and the difference of their reciprocals is $\frac{3}{28}$. Find the numbers.[Delhi 2014]

13. The difference of two natural numbers is 5 and the difference of their reciprocals is $\frac{5}{14}$. Find the numbers. [Delhi 2014]

IV. Long Answer Type Questions

- 14. Solve the equation for x: $\frac{3x-4}{7} + \frac{7}{3x-4} = \frac{5}{2}, x \neq \frac{4}{3}$. [Foreign 2010]
- **15.** Solve the equation for x: $\frac{1}{x+1} + \frac{2}{x+2} = \frac{5}{x+4}$, $x \neq -1, -2, -4$. [Foreign 2012]
- 16. Some students planned a picnic. The total budget for food was ₹2,000. But 5 students failed to attend the picnic and thus the cost of food for each member increased by ₹20. How many students attended the picnic and how much did each student pay for the food? [Foreign 2010]
- 17. A two-digit number is such that the product of its digits is 14. When 45 is added to the number, the digits interchange their places. Find the number. [Foreign 2011]
- 18. Two water taps together can fill a tank in 6 hours. The tap of larger diameter takes 9 hours less than the smaller one to fill the tank separately. Find the time in which each tap can separately fill the tank. [Foreign 2012]
- 19. Two pipes running together can fill a tank in $11\frac{1}{9}$ minutes. If one pipe takes 5 minutes more than the other to fill the tank separately, find the time in which each pipe would fill the tank separately. [AI 2016]

[3 Marks]

[2 Marks]

[Delhi 2013]

[AI 2016]

[CBSE Standard SP 2020-21]

[5 Marks]

- 20. A pole has to be erected at a point on the boundary of a circular park of diameter 17 m in such a way that the differences of its distances from two diametrically opposite fixed gates A and B on the boundary is 7 metres. Find the distances from the two gates where the pole is to be erected. [Foreign 2016]
- 21. A motorboat whose speed in still water is 18 km/h, takes 1 hour more to go 24 km upstream than to return downstream to the same spot. Find the speed of the stream.[CBSE Standard 2020, CBSE 2018, AI 2013]
- 22. At present Asha's age (in years) is 2 more than the square of her daughter Nisha's age. When Nisha grows to her mother's present age, Asha's age would be one year less than 10 times the present age of Nisha. Find the present ages of both Asha and Nisha.
 [NCERT Exemplar]
- 23. A train travels at a certain average speed for a distance of 63 km and then travels at a distance of 72 km at an average speed of 6 km/hr more than its original speed. If it takes 3 hours to complete total journey, what is the original average speed?
 [CBSE 2018]
- **24.** Solve the following equation:

 $\frac{1}{x} - \frac{1}{x - 2} = 3, x \neq 0, 2$

[CBSE Standard SP 2019-20]

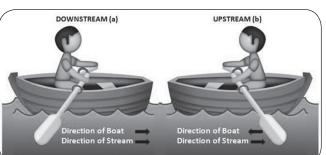
[CBSE Standard SP 2019-20]

- **25.** Find two consecutive positive integers sum of whose squares is 365.
- 26. A rectangular park is to be designed whose breadth is 3 m less than its length. Its area is to be 4 square metres more than the area of a park that has already been made in the shape of an isosceles triangle with its base as the breadth of the rectangular park and of altitude 12 m. Find the length and breadth of the park. [CBSE 2016]
- 27. In a flight of 600 km, an aircraft was slowed down due to bad weather. The average speed of the trip was reduced by 200 km/hr and the time of flight increased by 30 minutes. Find the duration of flight. [CBSE Standard 2020]

Case Study Based Questions

I. The speed of a motor boat is 20 km/hr. For covering the distance of 15 km the boat took 1 hour more for upstream than downstream.





1. Let speed of the stream be x km/hr, then speed of the motorboat in upstream will be

(a) 20 km/hr (b) (20 + x) km/hr (c) (20 - x) km/hr (d) 2 km/hr2. What is the relation between speed, distance and time? (b) distance = $\frac{\text{(speed)}}{\text{time}}$ (a) speed = $\frac{\text{(distance)}}{\text{time}}$ (c) time = speed \times distance (d) speed = distance \times time 3. Which is the correct quadratic equation for the speed of the stream? (a) $x^{2} + 30x - 200 = 0$ (b) $x^{2} + 20x - 400 = 0$ (c) $x^{2} + 30x - 400 = 0$ (d) $x^{2} - 20x - 400 = 0$ 4. What is the speed of stream? (a) 20 km/hour (b) 10 km/hour (c) 15 km/hour (d) 25 km/hour5. How much time boat took in downstream? (a) 90 minutes (b) 15 minutes (c) 30 minutes (d) 45 minutes

Answers and Hints

(1)

1. (1) (*b*)
$$\frac{3}{4}, \frac{3}{4}$$
 (1) (2) (*b*) $x = 0, x = \frac{25}{4}$

2. (1) (a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).
(1)

(2) (a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A). (1)

3. (1)
$$-\sqrt{3}, -\frac{7}{\sqrt{3}}$$
 (1) (2) $3, \frac{-3}{2}$ (1)

(3)
$$a, \frac{-a}{3}$$
 (1) (4) $\frac{-2b}{a}, \frac{-2b}{3a}$ (1)

(5)
$$x^{2} + 7x + 10 = 0$$

 $x^{2} + 5x + 2x + 10 = 0$ (1/2)
 $(x + 5)(x + 2) = 0$

$$x = -5, x = -2 \qquad (1/2)$$

4. Consider
$$4\sqrt{3}x^2 + 5x - 2\sqrt{3} = 0$$

 $\Rightarrow 4\sqrt{3}x^2 + 8x - 3x - 2\sqrt{3} = 0$ (1)
 $\Rightarrow 4x(\sqrt{3}x + 2) - \sqrt{3}(\sqrt{3}x + 2) = 0$

$$\Rightarrow \quad x = \frac{\sqrt{3}}{4} \text{ and } -\frac{2}{\sqrt{3}} \tag{1}$$

5. Consider:

 \Rightarrow

0

$$x^{2} - (\sqrt{2} + 1)x + \sqrt{2} = 0$$

$$x^{2} - \sqrt{2}x - x + \sqrt{2} = 0$$
(1)

$$\Rightarrow \qquad (x - \sqrt{2})(x - 1) = 0$$

$$\Rightarrow \qquad x = \sqrt{2} \text{ or } x = 1 \qquad (1)$$

6.
$$\sqrt{2x+9} + x = 13 \implies \sqrt{2x+9} = (13-x)$$

Squaring both sides, we get
 $\Rightarrow 2x+9 = 169 - 26x + x^2$ (1)
 $\Rightarrow x^2 - 28x + 160 = 0$
 $\Rightarrow (x-20)(x-8) = 0$
 $\Rightarrow x = 20 \text{ or } x = 8$
 $\Rightarrow x = 8$
[as $x = 20$ does not satisfy the equation] (1)

 $\sqrt{6x+7} - (2x-7) = 0$ 7.

$$\Rightarrow \sqrt{6x+7} = 2x-7$$

Squaring both sides, we get

$$\Rightarrow 6x+7 = 4x^2 - 28x + 49 \qquad (1)$$

$$\Rightarrow 4x^2 - 34x + 42 = 0$$

$$\Rightarrow 2x^2 - 17x + 21 = 0$$

$$\Rightarrow 2x^2 - 14x - 3x + 21 = 0$$

$$\Rightarrow (2x-3)(x-7) = 0$$

$$\Rightarrow x = 7 \text{ or } x = \frac{3}{2} \Rightarrow x = 7$$

$$[as x = \frac{3}{2} \text{ does not satisfy the equation}] \qquad (1)$$
8. $\sqrt{3}x^2 - 2\sqrt{2}x - 2\sqrt{3} = 0$

$$\Rightarrow \sqrt{3}x^2 + \sqrt{2}x - 3\sqrt{2}x - 2\sqrt{3} = 0 \qquad (1)$$

$$\Rightarrow \qquad (\sqrt{3}x + \sqrt{2})(x - \sqrt{6}) = 0$$

$$\therefore \qquad x = \frac{-\sqrt{2}}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{-\sqrt{6}}{3} \quad \text{and} \quad x = \sqrt{6} \qquad (1)$$

9.
$$\frac{1}{x-3} - \frac{1}{x+5} = \frac{1}{6} \implies \frac{x+5-x+3}{x^2+2x-15} = \frac{1}{6}$$
 (1)
 $\implies x^2 + 2x - 15 = 48 \implies x^2 + 2x - 63 = 0$

$$\Rightarrow (x+9)(x-7) = 0 \quad \Rightarrow \quad x = 7 \text{ or } x = -9 \tag{1}$$

 $\sqrt{3}x^2 + 14x - 5\sqrt{3} = 0$ 10. $\sqrt{3}x^2 + 15x - x - 5\sqrt{3} = 0$ \Rightarrow $\Rightarrow \sqrt{3}x(x+5\sqrt{3}) - (x+5\sqrt{3}) = 0$ $(x+5\sqrt{3})(\sqrt{3}x-1) = 0$ \Rightarrow $x + 5\sqrt{3} = 0$ Either (1) $\sqrt{3}x - 1 = 0$ or $r = -5\sqrt{3}$ \Rightarrow

$$x = -5\sqrt{3}$$
$$x = \frac{1}{\sqrt{3}}$$
(1)

11.
$$\frac{x+1}{x-1} + \frac{x-2}{x+2} = 4 - \frac{2x+3}{x-2}$$
$$\Rightarrow \qquad \frac{x+1}{x-1} + \frac{x-2}{x+2} + \frac{2x+3}{x-2} = 4$$
(1)

$$\Rightarrow \frac{(x+1)(x+2)(x-2) + (x-2)^{2}(x-1)}{(x+2)(x-2)} = 4$$

$$\Rightarrow \frac{(x+1)(x^{2}-4) + (x-1)(x^{2}+4-4x)}{(x+1)(x^{2}+x-2)} = 4(x-1)(x^{2}-4) \quad (1)$$

$$\Rightarrow \frac{5x^{2}+19x-30}{(x+5)(5x-6)} = 0 \Rightarrow x = -5$$

or
$$x = \frac{6}{5} \qquad (1)$$

14. Given that:
$$\frac{3x-4}{7} + \frac{7}{3x-4} = \frac{5}{2}, x \neq \frac{4}{3}$$

Let us consider: $\frac{3x-4}{7} = y$
 \Rightarrow The given equation becomes $y + \frac{1}{y} = \frac{5}{2}$ (1)
 $\Rightarrow 2y^2 - 5y + 2 = 0 \Rightarrow 2y^2 - 4y - y + 2 = 0$
 $\Rightarrow (2y-1)(y-2) = 0 \Rightarrow y = \frac{1}{2}$ or 2 (1)

$$\frac{3x-4}{7} = \frac{1}{2}$$
 or $\frac{3x-4}{7} = 2$ (1)

$$\Rightarrow 6x - 8 = 7 \qquad \Rightarrow 3x = 18$$

$$\Rightarrow x = \frac{15}{6} (1) \qquad \Rightarrow x = 6 \tag{1}$$

15. Given that:

or

$$\frac{1}{x+1} + \frac{2}{x+2} = \frac{5}{x+4}; x \neq -1, -2, -4$$
$$x+2+2x+2 \qquad 5$$

$$\Rightarrow \frac{x+2+2x+2}{x^2+3x+2} = \frac{5}{x+4}$$
(1)
$$\Rightarrow (3x+4)(x+4) = 5(x^2+3x+2)$$
(1)

$$\Rightarrow (3x + 4)(x + 4) = 3(x + 3x + 2)$$
(1)
$$\Rightarrow 3x^{2} + 16x + 16 = 5x^{2} + 15x + 10$$
(1)

$$\Rightarrow 2x^2 - x - 6 = 0$$

$$\Rightarrow (2x + 3)(x - 2) = 0$$
(1)

$$\Rightarrow \qquad x = 2 \text{ or } x = \frac{-3}{2} \tag{1}$$

16. Case I. Let number of students = x24. and cost of food for each member = $\overline{\mathbf{x}} y$ Then $x \times y = 2,000$...(*i*)(1) **Case II.** New number of students = x - 5New cost of food for each member = $\overline{\mathbf{x}}(y+20)$ Then (x-5)(y+20) = 2,000xy + 20x - 5y - 100 = 2,000 \Rightarrow ...(ii)(1)Solving (i) and (ii), we get x = -20, 25(1)*.*.. x = -20 is rejected because number of students can't be negative. x = 25So, v = 80(1)*.*.. Number of students = 25Cost of food for each student = ₹80. (1). = **17.** 27 (5) **18.** 9 hrs. (5)19. 20 minutes, 25 minutes. *.*.. Hints: Solve same as Example 13. (5) **20.** Let P be the position of the pole. $\angle APB = 90^{\circ}$ (angle in a semicircle) P 90° В 17 m By Pythagoras Theorem, $AB^2 = AP^2 + PB^2$ $17^2 = AP^2 + PB^2$...(*i*)(1) \Rightarrow AP - PB = 7Now. ...(*ii*) **Rectangle:** $(AP - PB)^2 = 49$ \Rightarrow $\Rightarrow AP^2 + PB^2 - 2AP \cdot PB = 49$...(*iii*)(1) From (i) and (iii), we have So, $17^2 - 2AP \cdot PB = 49$ **Triangle:** $AP \cdot PB = 120$...(*iv*) \Rightarrow From (ii) and (iv), we have 120 = PB(7 + PB)(1)Let PB = x120 = x(7 + x) $x^2 + 7x - 120 = 0$ \Rightarrow (x-8)(x+15) = 0 \Rightarrow \Rightarrow x = 8x = -15(Rejected) or AT(PB = x = 8 m, *.*.. AP = 15 m(2) **21.** 6 km/h. (5) **22.** Nisha's age = 5 years, Asha's age = 27 years (5) **23.** Let the original average speed of train be x km/hr. $\frac{63}{x} + \frac{72}{x+6} = 3$ Therefore F (1) $x^2 - 39x - 126 = 0$ (1) \Rightarrow (x-42)(x+3) = 0 \Rightarrow (1) $x \neq -3$ *x* = 42 *.*.. (1)and (1) | **27.** 1 hr Original speed of train is 42 km/hr.

$$\frac{1}{-2} = 3$$

$$\frac{x-2-x}{x(x-2)} = \frac{5}{1}$$
 (1)

$$3x^2 - 6x = -2$$
 (1)

$$3x^2 - 6x + 2 = 0 \tag{1}$$

$$x = \frac{6 \pm \sqrt{12}}{6} \tag{1}$$

$$=\frac{3+\sqrt{3}}{3},\frac{3-\sqrt{3}}{3}$$
 (1)

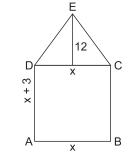
25. Let two consecutive positive integers be x and x + 1

$$\therefore \qquad x^2 + (x+1)^2 = 365 \tag{1}$$

$$\Rightarrow \quad x^2 + x - 182 = 0 \tag{1}$$

$$(x + 14)(x - 13) = 0$$
(1)
$$x = 13$$
(1)

26. Let ABCD is a rectangular park and CDE is a triangular park (isosceles triangle).



Let breadth =
$$x$$

Then its length = $x + 3$
b, area = $x(x + 3)$ (1)

Area of triangle =
$$\frac{1}{2} \times \text{Base} \times \text{Altitude}$$

= $\frac{1}{2} \times \text{CD} \times \text{Altitude}$ (1)

$$= - \times CD \times Altitude$$
(1)

 $=\frac{1}{2} \times x \times 12$ = 6x

Q,
$$x(x+3) = 4 + 6x$$
 (1)
 $x^2 + 3x = 4 + 6x$

$$x^{2} - 3x - 4 = 0$$

$$x^{2} - 4x + x - 4 = 0$$

$$x(x - 4) + 1(x - 4) = 0$$

$$(x - 4)(x + 1) = 0$$
Either
$$x - 4 = 0 \text{ or } x + 1 = 0$$

$$x = 4 \text{ or } x = -1$$
(1)
Since x cannot be negative.
So, x = 4 is the solution
Thus, Breadth = x = 4 m
we denote a set = x + 2 = 7 m
(1)

length = x + 3 = 4 + 3 = 7 m(1)(5)

Case Study Based Questions

I.	1. (<i>c</i>) $(20 - x)$ km/hr	2.	(a) speed = $\frac{\text{(dist)}}{\text{times}}$	ance)
	3. (c) $x^2 + 30x - 400 = 0$			lie

5. (*c*) 30 minutes

= Exercise 1.3 =

I. Very Short Answer Type Questions

I. Very Short Answer Type Q	uestions			[1 Mark]			
1. Multiple Choice Question	s (MCQs)						
Choose the correct answe							
(1) The discriminant of the	-	1 = 0 is					
(<i>a</i>) 0	(<i>b</i>) 1	(c) 2	(<i>d</i>) 3				
(2) If D is the discriminant	(2) If D is the discriminant of the equation $x^2 + 2x - 4$, then 2D is:						
(<i>a</i>) 20	(<i>b</i>) 40	(<i>c</i>) 60	(<i>d</i>) 80				
(3) The discriminant of the	e quadratic equation 4	$x^2 - 6x + 3 = 0$ is:					
(<i>a</i>) 12	(<i>b</i>) 84	(c) $2\sqrt{3}$	(d) -12				
(4) The roots of the quadra	atic equation $ax^2 + bx$	+c=0 are given by $-$	$\frac{-b \pm \sqrt{b^2 - 4ac}}{2ac} \text{ if } b^2 - 4ac$				
	$(b) \leq 0$	(c) > 0					
(a) < 0	$(b) \leq 0$	(c) > 0	$(d) \geq 0$				
(5) The quadratic formula	was given by an ancie	ent Indian mathematic					
(a) Sridharacharya	(b) Aryabhata	(c) Brahmagupt	ta (d) None of these				
2. Assertion-Reason Type Q	uestion						
	a statement of assert	tion (A) is followed b	oy a statement of reason (R).	Mark the correct			
choice as:		1 (D): (1		(A)			
			prrect explanation of assertion (e correct explanation of assertion				
(c) Assertion (A) is true by		ut reason (IC) is not the	e concer explanation of assertion	JII (A).			
(d) Assertion (A) is false b							
(1) Assertion (A): The val	(1) Assertion (A): The values of x are $-\frac{a}{2}$, a for a quadratic equation $2x^2 + ax - a^2 = 0$.						
	2, 410	er a quantane equation					
Reason (R): For quadr	ratio equation $ar^2 + b$	$r \pm c = 0$ $r = -b \pm \sqrt{-b}$	$b^2 - 4ac$				
Keason (K). For quadr		x + c = 0, x = -2	2a				
3. Answer the following:		·· · · · · · · · · · · · · · · · · · ·	•				
(1) Write the discriminant							
(2) Find the discriminant of	of the quadratic equati	ion: $4x^2 - \frac{2}{3}x - \frac{1}{16} =$	= 0.				
II. Short Answer Type Questi		5 10		[2 Marks]			
4. Find the roots of the equation	on $ax^2 + a = a^2x + x$.			[CBSE 2012]			
5. Solve the following quadra	tic equation for x: $4x^2$			[Delhi 2015]			
6. Solve the following quadration				[Delhi 2015]			
7. Solve the following quadra:				[AI 2015]			
8. Solve the following quadra		$-2ax - (4b^2 - a^2) = 0.$		[AI 2015]			
III. Short Answer Type Quest		11).		[3 Marks]			
Solve the following using quadr	<i>auc jormula</i> (Q. 9 to	11):					
9. $2\sqrt{3}x^2 - 5x + \sqrt{3} = 0$				[Imp.]			
10. $3x^2 + 2\sqrt{5}x - 5 = 0$			[For	eign 2011] [Imp.]			
11. $\frac{1}{x+4} - \frac{1}{x-7} = \frac{11}{30}, x \neq -4$	r, 7		[CBSE Stand	dard 2020] [Imp.]			
x+4 $x-7$ 30 12. Find the roots of quadratic		10 = 0		[All India 2017]			

- **13.** Find the roots of quadratic equation: $5\sqrt{5}x^2 + 30x + 8\sqrt{5}$
- 14. Solve for x: $4x^2 4ax + (a^2 b^2) = 0$.
- 15. Two water taps together can fill a tank in 9 hours 36 minutes. The tap of large diameter takes 8 hours less than the smaller one to fill the tank separately. Find the time in which each tap can separately fill the tank. [Foreign 2016]

[1 Mark]

[Delhi 2012]

IV. Long Answer Type Questions

- 16. A rectangular field is 20 m long and 14 m wide. There is a path of equal width all around it, having an area of 111 sq m. Find the width of the path. [CBSE 2013, 2012] [Imp.]
- 17. At 't' minutes past 2 pm, the time needed by the minute hand of a clock to show 3 pm was found to be 3 minutes less than $\frac{t^2}{4}$ minutes. Find t. [NCERT Exemplar]
- **18.** Find a natural number whose square diminished by 84 is equal to thrice of 8 more than the given number.
- 19. Solve for x: $\frac{x-3}{x-4} + \frac{x-5}{x-6} = \frac{10}{6}$; $x \neq 4, 6$ [AI 2014]
- **20.** Solve for x: $\frac{x-2}{x-3} + \frac{x-4}{x-5} = \frac{10}{3}$; $x \neq 3, 5$ [AI 2014]
- **21.** Solve for x: $3\left(\frac{3x-1}{2x+3}\right) 2\left(\frac{2x+3}{3x-1}\right) = 5; x \neq \frac{1}{3}, -\frac{3}{2}$
- 22. The difference of squares of two numbers is 88. If the larger number is 5 less than twice the smaller number, then find the two numbers. [Delhi 2010]
- 23. Sum of the areas of two squares is 544 m^2 . If the difference of their perimeters is 32 m, find the sides of the two squares.

Case Study Based Questions

I. Water Distribution System: Delhi Jal Board (DJB) is the main body of the Delhi Government which supplies drinking water in the National Capital Territory of Delhi. Distribution system is well knit and properly planned. Maintenance of underground pipe and hose system is also performed at regular interval of time. Many rivers and canals are inter-connected in order to ensure un-interrupted water supply. It has been meeting the needs of potable water for more than 16 million people. It ensures availability of 50 gallons per capita per day of pure and filtered water with the help of efficient network of water treatment plants and pumping stations.

In our locality, DJB constructed two big reservoir labelled as Reservoir–A and Reservoir–B.

Reservoir–A: In order to fill it, department uses two pipes of different diameter.

Reservoir–B: Department uses two taps to store water in this reservoir.

Refer to Reservoir-A

1. Two pipes running together can fill the reservoir in $11\frac{1}{9}$ minutes. If one pipe takes 5 minutes more than the other to fill the reservoir, the time in which each pipe alone would fill the reservoir is

(a) 10 min, 12 min (b) 25 min, 20 min (c) 15 min, 18 min (d) 22 min, 28 min

2. Two pipes running together can fill a reservoir in 6 minutes. If one pipe takes 5 minutes more than the other to fill the reservoir, the time in which each pipe would fill the reservoir separately is

(a) 8 min, 6 min (b) 10 min, 15 min (c) 12 min, 16 min (d) 16 min, 18 min **Refer to Reservoir-B**

- 3. Two water taps together can fill a reservoir in $9\frac{3}{8}$ hours. The tap of larger diameter takes 10 hours less than the smaller one to fill the reservoir separately. The time in which each tap can separately fill the reservoir will be
 - (a) 15 hrs, 25 hrs (b) 20 hrs, 22 hrs (c) 14 hrs, 18 hrs (d) 18 hrs, 16 hrs
- 4. Two taps running together can fill the reservoir in $3\frac{1}{13}$ minutes. If one tap takes 3 minutes more than the other to fill it, how many minutes each tap would take to fill the reservoir?
 - (d) 5 min, 8 min (a) $12 \min_{a} 15 \min_{b}$ (b) 6 min, 9 min (c) 18 min, 14 min
- 5. If two tapes function simultaneously, reservoir will be filled in 12 hours. One tap fills the reservoir 10 hours faster than the other. The time that the second tap takes to fill the reservoir is given by
 - (a) 25 hrs (b) 28 hrs (c) 30 hrs (*d*) 32 hrs
- **II.** A Hill Station: In the last summer, I enjoyed a tour to a hill station at Shimla. I was accompanied by my five friends and enjoyed the natural beauties of mountains, rivers, streams, forests etc. The beginning of the tour was the most adventurous

[5 Marks]

[NCERT Exemplar]

[Foreign 2014]

itself! How amazingly my group win the bet! Actually, the story is that my two friends along with me prefered train to go to Shimla, but other three were forcing for a car or a bus. At last the consensus was reached and we were divided ourselves in two groups of 3 each and started for Shimla at the same time. It was decided that the group who reach the destination first, would be declared as the winner, and runner up the group have to bear the expanses of the tour. I named my group, 'Group A' while the second group was named as 'Group B'. Luckily we reached Shimla 1 hour before the Group-B and enjoyed the trip for absolutely FREE!! How thrilling it was the tour!							
Refer to Group-A 1. An express train takes 1 hour less than a passenger train to travel 132 km between Delhi and Shimla (without taking into							
consideration the time they stop at intermediate stations).	consideration the time they stop at intermediate stations). If the average speed of the express train is 11 km/hr more than						
that of the passenger train, the average speeds of the two (1) 221 μ 4.44 μ (1) 40							
	40 km/h, 45 km/h 42 km/h, 62 km/h						
	Another train whose speed is 12 km/hr less takes an hour longer						
to make the same trip. The speed of the express train will							
(a) 60 km/h (b) 50 km/h (c) 65							
 3. A journey of 192 km from Delhi to Shimla takes 2 hours less by a super fast train than that by an ordinary passenger train. If the average speed of the slower train is 16 km/hr less than that of the faster train, average speed of super fast train is (a) 50 km/h (b) 48 km/h (c) 55 km/h (d) 60 km/h 							
Refer to Group-B							
-	journey of 600 km. If the speed of the ordinary bus is 10 km/hr						
less than that of the deluxe bus, the speeds of the two bus (a) 35 km/h, 42 km/h (b) 42	km/h, 52 km/h						
	km/h, 58 km/h						
	the speed of the bus is increased by 5 km an hour, the journey						
would have taken two hours less. The original speed of the							
(a) 20 km/h (b) 15 km/h (c) 22	km/h (<i>d</i>) 25 km/h						
Answers a	nd Hints						
1. (1) (<i>a</i>) 0 (1) (2) (<i>b</i>) 40 (1)	$\Rightarrow x = \frac{a^2 + b^2}{2} \text{ or } \frac{a^2 - b^2}{2} \tag{1}$						
$(3) (d) - 12 (1) (4) (d) \ge (1) $							
(5) (a) Sridharacharya (1)	$6. \ 9x^2 - 6b^2x - (a^4 - b^4) = 0$						
2. (1) (d) Assertion (A) is false but reason (R) is true. (1) 3. (1) $(x+5)^2 = 2(5x-3)$	$\Rightarrow x = \frac{6b^2 \pm \sqrt{36b^4 + 4 \times 9 \times (a^4 - b^4)}}{2 \times 9}$						
$\Rightarrow x^2 + 25 + 10x = 10x - 6$	$\Rightarrow x - \frac{2 \times 9}{2 \times 9}$						
$\Rightarrow \qquad x^2 + 31 = 0$	$\therefore x = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$						
$\Rightarrow x^2 + 0x + 31 = 0$	$\therefore x = \frac{2A}{2A}$						
$\therefore \qquad D = (0)^2 - 4 \times 1 \times 31$	$\Rightarrow x = \frac{6b^2 \pm \sqrt{36b^4 + 36a^4 - 36b^4}}{2 \times 9} \tag{1}$						
$= 0 - 124 = -124 \tag{1}$	$\rightarrow x$ 2×9 (1)						
(2) 3328 (1)	$\Rightarrow x = \frac{6b^2 \pm \sqrt{36a^4}}{2 \times 9} \Rightarrow x = \frac{6b^2 \pm 6a^2}{2 \times 3 \times 3}$						
4. $a, \frac{1}{a}$ (2)	$\Rightarrow x = \frac{1}{2 \times 9} \Rightarrow x = \frac{1}{2 \times 3 \times 3}$						
5. $4x^2 - 4a^2x + (a^4 - b^4) = 0$	$\Rightarrow x = \frac{b^2 \pm a^2}{3} \Rightarrow x = \frac{b^2 + a^2}{3} \text{ or } \frac{b^2 - a^2}{3} $ (1)						
$4a^2 \pm \sqrt{16a^4 - 4 \times 4 \times (a^4 - b^4)}$	7. $4x^2 + 4bx - (a^2 - b^2) = 0$						
$\Rightarrow x = \frac{4a^2 \pm \sqrt{16a^4 - 4 \times 4 \times (a^4 - b^4)}}{2 \times 4}$							
$\therefore x = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$							
$4a^2 \pm \sqrt{16b^4}$	$\Rightarrow x = \frac{-b+a}{2}, \frac{-b-a}{2} $ (1) 8. $x^2 - 2ax - (4b^2 - a^2) = 0$ $\therefore x = \frac{-(-2a) \pm \sqrt{16b^2}}{2 \times 1} = \frac{2a \pm 4b}{2} = a \pm 2b$ (1)						
$\Rightarrow x = \frac{4a^2 \pm \sqrt{16b^4}}{2 \times 4} \tag{1}$	$\sum_{n=1}^{2} \frac{2}{a^2} = 0$						
$\Rightarrow x = \frac{4a^2 \pm 4b^2}{2 \times 4} = \frac{a^2 \pm b^2}{2}$	$(2x) + \sqrt{16k^2} + 2x + 4k$						
$\Rightarrow x = \frac{1}{2 \times 4} = \frac{1}{2}$	$\therefore x = \frac{-(-2a) \pm \sqrt{16b^2}}{2 \times 1} = \frac{2a \pm 4b}{2} = a \pm 2b \tag{1}$						

$$\Rightarrow x = a + 2b \text{ or } a - 2b. \tag{1}$$

9.
$$\frac{\sqrt{3}}{2}, \frac{1}{\sqrt{3}}$$
 (3) 10. $\frac{\sqrt{5}}{3}, -\sqrt{5}$ (3)

11. 2, 1

12.
$$x = \frac{-b \pm \sqrt{D}}{2a} = \frac{3\sqrt{5} \pm \sqrt{5}}{2 \times 1}$$
 (1)

$$\Rightarrow x = \frac{3\sqrt{5} + \sqrt{5}}{2} \text{ or } \frac{3\sqrt{5} - \sqrt{5}}{2}$$
 (1)

(3)

$$\Rightarrow x = \frac{4\sqrt{5}}{2} \text{ or } \frac{2\sqrt{5}}{2}$$
$$\Rightarrow x = 2\sqrt{5} \text{ or } x = \sqrt{5}$$
(1)

13.
$$5\sqrt{5}x^2 + 30x + 8\sqrt{5} =$$

$$\Rightarrow 5\sqrt{5}x^{2} + 20x + 10x + 8\sqrt{5} = 0$$
(1)
$$\Rightarrow 5x(\sqrt{5}x + 4) + 2\sqrt{5}(\sqrt{5}x + 4) = 0$$

$$\Rightarrow \qquad (\sqrt{5}x+4)(5x+2\sqrt{5}) = 0 \qquad (1)$$

$$x = \frac{-4\sqrt{5}}{5} \text{ or } \frac{-2\sqrt{5}}{5}$$
 (1)

0

14. Roots are =
$$\frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$$

$$= \frac{-(-4a)\pm\sqrt{(-4a)^2-4\times4(a^2-b^2)}}{2\times4}$$
(1)

$$=\frac{4a\pm\sqrt{16a^2-16a^2+16b^2}}{8}$$
 (1)

$$=\frac{4a\pm4b}{8}=\frac{a\pm b}{2}\tag{1}$$

15. Let *x* be the time taken by larger diameter tap. $\therefore x + 8$ be the time taken by smaller diameter tap.

ATQ,
$$\frac{1}{x} + \frac{1}{x+8} = \frac{10}{96}$$

 $\left(\because 9 \text{ hrs } 36 \min = \frac{96}{10} \text{ hrs}\right)(1)$
 $\Rightarrow 10x^2 - 112x - 768 = 0$
 $\Rightarrow 5x^2 - 56x - 384 = 0$
 $\Rightarrow x = \frac{56 \pm \sqrt{(56)^2 - 4 \times 5 \times (-384)}}{2 \times 5}$ (1)

$$\Rightarrow x = \frac{56+104}{10}$$
 or $\frac{56-104}{10}$

 \Rightarrow x = 16 or x = -4.8 (Rejected) Hence, time taken by larger and smaller taps are 16 hrs and 24 hrs respectively. (1)**16.** 1.5 m (5) **17.** 14 minutes (5) **18.** 12 (5) **19.** $2 \pm \sqrt{10}$ (5) **20.** $\frac{7}{2}$, 6 (5) **21.** 0, -7 (5) **22.** 9 and 13 (5) 23. Let the sides of two squares in metres be x and yrespectively (where x > y). Given: Sum of areas of two squares = 544 m^2 $x^2 + y^2 = 544$ \Rightarrow ...(i)(1)Also, difference of their perimeters = 32 m4x - 4y = 32 \Rightarrow x - y = 8 \Rightarrow \Rightarrow y = x - 8...(*ii*) (1) Substituting the value of y for equation (ii) in equation (i), va aat

we get

$$x^{2} + (x - 8)^{2} = 544$$

$$\Rightarrow x^{2} + x^{2} - 16x + 64 - 544 = 0$$

$$\Rightarrow 2x^{2} - 16x - 480 = 0$$

$$\Rightarrow x^{2} - 8x - 240 = 0$$
(1)

$$\Rightarrow x = \frac{-(-8) \pm \sqrt{(-8)^{2} - 4 \times 1 \times (-240)}}{2 \times 1}$$

$$= \frac{8 \pm \sqrt{64 + 960}}{2}$$

$$= \frac{8 \pm \sqrt{1024}}{2}$$
(1)

$$= \frac{2}{2}$$

$$= \frac{8 \pm 32}{2} = 4 \pm 16$$

$$= 4 \pm 16 = 20$$
(1)

 $\Rightarrow \qquad x = 4 + 16 = 20$

or x = 4 - 16 = -12 (rejected)

From (*ii*), y = 20 - 8 = 12

Thus, the sides of two squares are 20 m and 12 m. (1)

Case Study Based Questions

- I. 1. (b) 25 min, 20 min 2. (b) 10 min, 15 min
 - **3.** (*a*) 15 hrs, 25 hrs **4.** (*d*) 5 min, 8 min

- **II.** (*a*) 33 km/h, 44 km/hr
 - **2.** (*a*) 60 km/h **3.** (*b*) 48 km/h
 - **4.** (*c*) 40 km/h, 50 km/h
 - 5. (*d*) 25 km/h

Exercise 1.4

I. Very Short Answer Type Questions

1. Multiple Choice Questions (MCQs)

- Choose the correct answer from the given options:
- (1) For what value of k, the equation $9x^2 24x + k = 0$ has equal roots?
 - (a) 12 (b) 16 (c) 18 (d) 20
- (2) The values of k for which the quadratic equation $(k + 1)x^2 + 2(k 1)x + (k 2) = 0$ has equal roots, is: (a) k = 2 (b) k = 3 (c) k = 0 (d) None of these
- (3) The value(s) of k for which the quadratic equation $2x^2 + kx + 2 = 0$ has equal roots, is (a) 4 (b) ± 4 (c) -4 (d) 0
- (4) The value(s) of k, for which the roots of the equation $3x^2 + 2k + 27 = 0$ are real and equal are (a) k=9 (b) $k=\pm 9$ (c) k=-9 (d) k=0
- (5) The value of k, for which the equation $2x^2 10x + k = 0$ has real roots is

(a)
$$k \le \frac{25}{2}$$
 (b) $k \ge \frac{25}{2}$ (c) $k = \frac{25}{2}$ (d) $k > \frac{25}{2}$

- (6) If one root of the equation (k 1)x² 10x + 3 = 0 is the reciprocal of the other, then the value of k is
 (a) 1
 (b) 2
 (c) 3
 (d) 4
 (7) If the quadratic equation x² 2x + k = 0 has equal roots, then value of k is
- (7) If the quadratic equation $x^2 2x + k = 0$ has equal roots, then value of k is (a) 1 (b) 2 (c) 3 (d) 0
- (8) If quadratic equation $3x^2 4x + k = 0$ has equal roots, then the value of k

(a)
$$\frac{1}{3}$$
 (b) $\frac{2}{3}$ (c) 3 (d)

2. Assertion-Reason Type Questions

In the following questions, a statement of assertion (A) is followed by a statement of reason (R). Mark the correct choice as:

- (a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).
- (b) Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A).
- (c) Assertion (A) is true but reason (R) is false.
- (d) Assertion (A) is false but reason (R) is true.
- (1) Assertion (A): The equation $8x^2 + 3kx + 2 = 0$ has equal roots, then the value of k is $\pm \frac{8}{3}$. Reason (R): The equation $ax^2 + bx + c = 0$ has equal roots if $D = b^2 - 4ac = 0$.
- (2) Assertion (A): The roots of the quadratic equation $x^2 + 2x + 2 = 0$ are imaginary. Reason (R): If discriminant $D = b^2 - 4ac < 0$, then the roots of quadratic equation $ax^2 + bx + c = 0$ are imaginary.

3. Answer the following.

- (1) Find the value of p, so that the quadratic equation px(x-3) + 9 = 0 has equal roots. [CBSE 2014]
- (2) For what values of k, the roots of the equation $x^2 + 4x + k = 0$ are real? [Delhi 2019]
- (3) Find the value of k for which the roots of the equation $3x^2 10x + k = 0$ are reciprocal of each other. [Delhi 2019]
- (4) Find the discriminant of the quadratic equation $2x^2 4x + 3 = 0$, hence find the nature of its roots. [NCERT]
- (5) If x = 3 is one root of the quadratic equation $x^2 2kx 6 = 0$, then find the value of k. [CBSE 2018] (6) For what values of k, the equation $9x^2 + 6kx + 4 = 0$ has equal roots? [CBSE Standard SP 2020-21]
- (6) For what values of k, the equation $9x^2 + 6kx + 4 = 0$ has equal roots? [CBSE Standard SP 2020-21] (7) For what value(s) of 'a' quadratic equation $3ax^2 - 6x + 1 = 0$ has no real roots? [CBSE Standard SP 2020-21]

II. Short Answer Type Questions - I

4. State whether the quadratic equation $4x^2 - 5x + \frac{25}{16} = 0$ has two distinct real roots or not. Justify your answer.

[NCERT Exemplar]

[2 Marks]

[1 Mark]

- 5. Find the value of k so that the quadratic equation kx(3x 10) + 25 = 0, has two equal roots.
- 6. For what value of k does the quadratic equation $(k-5)x^2 + 2(k-5)x + 2 = 0$ have equal roots? [Foreign 2011]
- 7. Find the value(s) of k so that the quadratic equation $2x^2 + kx + 3 = 0$ has equal roots.
- 8. Find the value(s) of k so that the quadratic equation $x^2 4kx + k = 0$ has equal roots.
- 9. Find the value(s) of k so that the quadratic equation $3x^2 2kx + 12 = 0$ has equal roots.
- 10. Find the values of k for which the quadratic equation $9x^2 3kx + k = 0$ has equal roots.

III. Short Answer Type Questions - II

- 11. Find the nature of the roots of the following quadratic equations. If the real roots exist, then also find them. (a) $4x^2 + 12x + 9 = 0$ (b) $3x^2 + 5x - 7 = 0$ (c) $7y^2 - 4y + 5 = 0$
- 12. If 2 is a root of the quadratic equation $3x^2 + px 8 = 0$ and the quadratic equation $4x^2 2px + k = 0$ has equal roots, find the value of k. [CBSE (F) 2014]
- 13. Find the value of p for which the quadratic equation $(p + 1)x^2 6(p + 1)x + 3(p + 9) = 0$, $p \neq -1$ has equal roots. Hence, find the roots of the equation. [Delhi 2015]
- 14. Find that non-zero value of k, for which the quadratic equation $kx^2 + 1 2(k-1)x + x^2 = 0$ has equal roots. Hence, find [Delhi 2015] the roots of the equation.
- **15.** The roots α and β of the quadratic equation $x^2 5x + 3(k-1) = 0$ are such that $\alpha \beta = 1$. Find the value k.

[CBSE Standard SP 2020-21]

[Delhi 2011]

[Delhi 2012]

[Delhi 2012]

[Delhi 2012]

[AI 2014]

[3 Marks]

[5 Marks]

[Imp.]

16. Find the values of k for which the quadratic equation $(3k + 1)x^2 + 2(k + 1)x + 1 = 0$ has equal roots. Also find these roots. [Delhi 2014]

IV. Long Answer Type Questions

17. Find whether the equation $\frac{1}{2x-3} + \frac{1}{x-5} = 1$, $x \neq \frac{3}{2}$, 5 has real roots. If real roots exist, find them.[NCERT Exemplar]

18. Check whether the equation $5x^2 - 6x - 2 = 0$ has real roots and if it has, find them by the method of completing the square. Also verify that roots obtained satisfy the given equation. [CBSE SP 2018]

Answers and Hints

0]

- **1.** (1) (*b*) 16 (1) (2) (b) k = 3(1)(1) (4) (b) $k = \pm 9$ (3) $(b) \pm 4$ (1)
 - (5) (a) $k \le \frac{25}{2}$ (1) (6) (d) 4 (1)

(7) (a) 1 (1) (8) (d)
$$\frac{1}{3}$$
 (1)

- 2. (1) (a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A). (1)
 - (2) (a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A). (1)

px(x-3)+9=0**3.** (1)

 \Rightarrow

 \Rightarrow

$$\Rightarrow px^2 - 3px + 9 = 0$$

When roots are equal,

$$D = b^{2} - 4ac = 0$$

$$9p^{2} - 36p = 0$$

$$9p(p - 4) = 0$$

$$p = 0, p = 4$$

But
$$p \neq 0$$

 \therefore $p = 4$ (1)
(2) For real roots, $D \ge 0$

 $b^2 - 4ac \ge 0$ \Rightarrow

 $\Rightarrow (4)^2 - 4 \times 1 \times k \ge 0$ $16 - 4k \ge 0$ \Rightarrow $16 \ge 4k, k \le 4$ \Rightarrow (1)(3) Let the roots of the given equation be α and $\frac{1}{\alpha}$ 1 c k(1)

$$\begin{array}{l} \alpha. \frac{\alpha}{\alpha} = \frac{1}{a} = \frac{1}{3} \Rightarrow k = 5 \\ (1) \\ (4) \quad -8, \text{ no real roots} \\ (1) \end{array}$$

(5)
$$x = 3$$
 is one root of the equation

0 - 6 - 6 - 0

$$\Rightarrow \qquad k = \frac{1}{2}$$
(1)
(6)
$$9x^2 + 6kx + 4 = 0$$

$$(6k)^2 - 4 \times 9 \times 4 = 0 \tag{1/2}$$

$$36k^2 = 144$$

$$k^2 = 4$$

$$k = \pm 2$$

$$(1/2)$$

(7)
$$3ax^2 - 6x + 1 = 0$$
 (1/2)
(-6)² - 4(3a)(1) < 0

$$a > 3$$
 (¹/₂)

4. No,
$$D = 0$$
 (2)
5. $kx(3x - 10) + 25 = 0$

$$kx(3x - 10) + 23 = 0$$

 $\Rightarrow 3kx^2 - 10kx + 25 = 0$

 \Rightarrow

 \Rightarrow

	$\mathbf{D} = (-10k)^2 - 4 \times 3k \times $	25		
	$= 100k^2 - 300k$			
	For equal roots, $D = 0$	(1)		
	$\Rightarrow 100k^2 - 300k = 0$			
	$\Rightarrow \qquad 100k(k-3) = 0$			
	$\Rightarrow \qquad k=0 \text{ or } k=3$			
	But $k \neq 0$,			
	So, $k = 0$ (Rejected)			
		quation, $a \neq 0$]		
	Hence, $k = 3$	(1)		
	<i>k</i> = 7	(2)		
7.	$2x^2 + kx + 3 = 0$			
	For equal roots, $D = 0$	(1)		
	$\Rightarrow \qquad b^2 - 4ac = 0$ $\Rightarrow \qquad k^2 - 24 = 0$			
	,			
	$\Rightarrow \qquad k = \pm 2\sqrt{6}$	(1)		
8.	$x^2 - 4kx + k = 0$			
	Since given equation has equal roots,			
	\therefore D = 0	(1)		
	$16k^2 - 4k = 0$			
	$\Rightarrow \qquad 4k(4k-1) = 0$			
	\Rightarrow $k = 0$ and $k = \frac{1}{4}$	(1)		
9.	$4x^{2} - 2kx + 12 = 0$			
Since given equation has equal roots, so				
	D = 0	(1)		
	$\Rightarrow 4k^2 - 144 = 0$	(-)		
	$\Rightarrow \qquad 4(k^2 - 36) = 0$			
	\Rightarrow $k = \pm 6$			
	\Rightarrow $k = 6$ and $k = -6$	(1)		
10.	For equal roots, $D = 0$	()		
	$\Rightarrow \qquad 9k^2 - 36k = 0$			
	$\Rightarrow \qquad 9k(k-4) = 0$	(1)		
	$\Rightarrow \qquad k=0 \text{ or } k=4$	(1)		
11.	(a) Real and equal roots: $\frac{-3}{2}, \frac{-3}{2}$	(1)		
	(b) Real and distinct roots:			
	$\frac{-5+\sqrt{109}}{6}, \frac{-5-\sqrt{109}}{6}$	(1)		
	6, 6	(1)		
	(c) No real roots	(1)		
12.	$3(2)^2 + p(2) - 8 = 0$			
	$\Rightarrow 12 + 2p - 8 = 0$ $\Rightarrow p = -2$	(z)(1)		
	$\Rightarrow \qquad p = -2$ So, equation becomes	(<i>i</i>)(1)		
	$4x^2 + 4x + k = 0$	[using (<i>i</i>)](1)		
		[

For equal roots, D = 0 $\Rightarrow \quad (4)^2 - 4 \times 4 \times k = 0$ 16 = 16k \Rightarrow k = 1(1) \Rightarrow **13.** 3, 3. (3) $kx^2 + 1 - 2(k-1)x + x^2 = 0$ 14. $(k+1)x^2 - 2(k-1)x + 1 = 0$ \Rightarrow : Above equation has equal roots, (1) So, discriminant, D = 0 $\Rightarrow \left\{-2(k-1)\right\}^2 - 4 \times (k+1) \times 1 = 0$ (1) $4(k^2 - 2k + 1) - 4(k + 1) = 0$ \Rightarrow $4k^2 - 12k = 0$ \Rightarrow 4k(k-3) = 0 \Rightarrow k = 3 (as $k \neq 0$) \Rightarrow (1) **15.** k = 3(3) **16.** For equal roots, D = 0 $\{2(k+1)\}^2 - 4(3k+1) \cdot 1 = 0$ (1) $4(k^2 + 2k + 1) - 12k - 4 = 0$ \Rightarrow $4k^2 + 8k + 4 - 12k - 4 = 0$ \Rightarrow (1) $4k^2 - 4k = 0$ \Rightarrow 4k(k-1) = 0 \Rightarrow k = 0, 1 \Rightarrow (1) $8 \pm 3\sqrt{2}$ (5) 17. Yes, -2 Discriminant = $b^2 - 4ac$ 18. $= 36 - 4 \times 5 \times (-2)$ = 76 > 0So, the given equation has two distinct real roots $5x^2 - 6x - 2 = 0$ (1) Multiplying both sides by 5, we get

$$(5x)^{2} - 2 \times (5x) \times 3 = 10$$

$$\Rightarrow (5x)^{2} - 2 \times (5x) \times 3 + 3^{2} = 10 + 3^{2}$$

$$\Rightarrow (5x - 3)^{2} = 19$$
(1)

$$5x - 3 = \pm \sqrt{19}$$

 \Rightarrow

$$\Rightarrow \qquad \qquad x = \frac{3 \pm \sqrt{19}}{5} \tag{1}$$

Verification:
$$5\left(\frac{3+\sqrt{19}}{5}\right)^2 - 6\left(\frac{3+\sqrt{19}}{5}\right) - 2$$

= $\frac{9+6\sqrt{19}+19}{5} - \frac{18+6\sqrt{19}}{5} - \frac{10}{5} = 0$ (1)
Similarly, $5\left(\frac{3-\sqrt{19}}{5}\right)^2 - 6\left(\frac{3-\sqrt{19}}{5}\right) - 2 = 0$ (1)