# PROBABILITY

To define probability in a clear, concise mathematical language, we require explanation of certain terms. They are:

- **RANDOM EXPERIMENT OR TRIAL (R.E):** An experiment which can be conducted any number of times under essentially identical conditions and the experiment whose possible outcomes or results are known before hand and yet we cannot say which one of the results materialises in a given situation is called a random experiment or trial. For example:
  - Tossing of a coin
  - Rolling of a die

• Drawing a specified number of cards from a well shuffled pack of 52 playing cards etc.,

**EVENT:** An outcome or the result of a random experiment is called an event. For example while tossing of a coin we may get head upwards, or tail upwards. Now getting head upwards is an event or getting tail upwards is also an event.

The event can be either an elementary event or a composite event.

• ELEMENTARY EVENT OR INDECOMPOSABLE EVENT: The possible outcome or the result of a random experiment that can not be split further is called an elementary or simple event. For example:

• The event of getting head upwards is an elementary event.

• The event of obtaining a face with 4 points upwards in rolling of a die is an elementary event.

• **COMPOSITE EVENT:** The possible outcome or the result of a random experiment that can be further split into more than one elementary event is called a composite event. For example:

• Getting a face with odd number of points upwards in rolling of a die is a composite event, since it can be divided further into three elementary events namely:

- Event of getting a face with one point upwards.
- Event of getting a face with three points upwards.
- Event of getting a face with five points upwards.

• Getting a face with even number of points upwards in rolling of a die is also a composite event, since it can be divided further into three elementary events namely:

• Event of getting a face with two points upwards.

• Event of getting a face with four points upwards.

• Event of getting a face with six points upwards. Briefly speaking a combination of two or more number of elementary events is called a composite event. The events whether elementary or composite are denoted by the latin letters A, B, C, D, E, .....

MUTUALLY EXCLUSIVE EVENTS (M.E.E.): The events of a R.E. are said to be M.E. events, if the occurence of any one of them precludes i.e, prevents or eliminates the occurence of all the other events of that R.E.

Two events A and B are said to be M.E. or disjoint when both cannot happen simultaneously in a sin-

gle trial or experiment. i.e.,  $A \cap B = \phi$ .

For example:

• In tossing of a coin head turning upwards eliminates tail turning upwards in that particular R.E. So head & tail are M.E. events.

• In rolling of a die the event of getting a face with one point turning upwards eliminates all the other faces turning upwards in that particular R.E. So all the six faces of the die are M.E.

The events  $A_1, A_2, A_3, \dots, A_n$  of a R.E. are said to be

M.E. or disjoint events if,  $A_i \cap A_j = \phi$ , for  $i \neq j$  &

 $1 \leq i, \ j \leq n$  .

•

**NOTE:** When ever it is possible for two or more number of events to happen simultaneously, then those events are said to be compatible.

**EQUALLY LIKELY EVENTS (E.L.E.):** The events of a R.E. are said to be E.L. When one does not occur more number of times than any one of the other events i.e., if all the events occur same number of times.

The events of a R.E. are said to be equally likely when there is no reason to expect a particular event in preference to any other event. For example:

• If an unbiased coin is tossed a large number of times, each face i.e., head and tail can be expected to appear same number of times.

• If a perfect or symmetrical or uniform die is rolled a large number of times, all the six faces can be expected to appear same number of times.

 EXHAUSTIVE EVENTS (E.E.): The events of a random experiment are said to be exhaustive, if the occurence of any one of them is a certainty.
 A set of events is said to be exhaustive if the conduct of the experiment always result in the occurence

of at least one of them. A set of events is said to be exhaustive, if these

include all possible outcomes of the R.E. For example:

• In tossing of a coin it is certain that either the head will turn upwards or the tail will turn upwards. So head & tail put together are called as exhaustive events.

• In rolling of a die it is certain that any one of the six faces will turn upwards. So all the six faces of a die put together are called as exhaustive events.

**SAMPLE SAPCE (S):** The list of all possible outcomes or results of a random experiment is called as sample for that experiment and it is denoted by S. (or)

The set of all possible elementary events in a R.E. or trial is called a sample space for that trial and is denoted by S. For example:

• In tossing of a coin, the sample space S is  $S=\{H, T\}$ .

• In rolling of a die, the sample space S is S={1, 2, 3, 4, 5, 6}.

Now consider:

A =  $\{1, 3, 5\}$ , the event of getting odd number of points upwards.

 $B = \{2, 4, 6\}$ , the event of getting even number of points upwards.

C =  $\{1, 2\}$ , the event of getting a face with 1 or 2 points upwards.

D =  $\{6\}$ , the event of getting a face with 6 points upwards.

Now A, B, C & D are subsets of S.

From these we can conclude that any subset of a sample space is called an event.

#### NOTE:

• The empty set  $\phi$ , which is a subset of every set also represents an event and is said to be an impossible event.

• The set S itself is a subset of S and it represents sure or certain event.

• An elementary or simple event of a R.E. is considered as one sample point. So a sample space can also be defined as collection of all possible sample points, each sample point being an elementary event of a R.E.

• **FAVOURABLE CASES:** The possible outcomes or results of a R.E. which entail the occurence of the event A are called as favourable cases for the event A to happen.

The possible outcomes or results of a R.E. which are helpful or responsible for the event A to happen are called as favourable cases for the event A. For example:

• In rolling of a symmetrical die 1, 3 & 5 are helpful or responsible for the event A, the event of getting odd number of points upwards. So they are called as favourable cases for the event A.

• In rolling of a symmetrical die 2, 4 & 6 are helpful or responsible for the event of occurence of even number of points upwards B. So they are called as favourable cases for the event B.

## CLASSICAL DEFINITION OF PROBABILITY (OR)

## MATHEMATICAL DEFINITION OF PROBABILITY (OR)

## APRIORI PROBABILITY

The probability of the event A, denoted by P(A) is

defined as 
$$P(A) = \frac{m}{n} = \frac{n(A)}{n(S)}$$

## Where

n = The total number of possible outcomes in a R.E. which are M.E., E.L. & collectively exhaustive.

m = The number of possible outcomes favourable to A in that R.E.

n(S) = The total number of sample points in a sample space S.

n(A) = The number of sample points favourable to A in that sample space S.

$$p(A) = \frac{m}{n}$$
 can also be expressed as

"The odds in favour of the event A are m to n - m or

$$\frac{m}{n-m}$$

"The odds against the event A are n-m to m or

$$\frac{n-m}{m}$$
 "

But in both the cases  $P(A) = \frac{favourable \ cases}{total \ no. \ of \ cases}$ 

$$=\frac{m}{m+n-m}=\frac{m}{n}$$

Now consider  $P(A) = \frac{m}{n}$ 

If m = 0, P(A) = 0, then A is said to be an impossible event.

If m=n,  $P(A) = \frac{n}{n} = 1$ , then A is said to be a sure or

certain event.

 $\therefore$  The limits of P(A) are [0, 1]

i.e.,  $0 \le P(A) \le 1 \Longrightarrow 0 \le P(\overline{A}) \le 1$ 

From these we can conclude that the probability of any event is a non-negative rational number which lies between 0 & 1, both inclusive.

## LIMITATIONS:

- If n is very very large say  $\infty$  we can not determine the probability of the event A with the help of this definition.
- The probability can not be found when the outcomes are not equally likely.
- When the outcomes are not M.E., our logic may go wrong.
- One of the serious draw backs of this definition is that in defining probability we use the term equally likely i.e., equally probable i.e., probability itself.

## VON MISES'S

#### STATISTICAL DEFINITION OF PROBABILITY EMPIRICAL DEFINITION OF PROBABILITY FREQUENCY INTERPRETATION OF PROBABILITY OR

## **APOSTERIORI PROBABILITY**

Let a trial be repeated independently any number of times under essentially identical conditions and let A be an event of it. Suppose the event A occurs m times out of n trials. Then  $\frac{m}{n}$  is called the relative frequency of the event A, denoted by R(A) i.e.,

 $R(A) = \frac{m}{n}$ . Now the probability of the event A i.e.,

P(A) is the limit approached by R(A) as the number of trials n increases indefinitely, provided a unique limit exists.

Symbolically

$$P(A) = \lim_{n \to \alpha} R(A)$$
$$= \lim_{n \to \alpha} \frac{m}{n}$$

# LIMITATIONS:

- It is practically impossible to repeat the experiment infinite number of times. So we have to be satisfied in practice by giving a large value for n as far as possible.
- As  $\frac{m}{n}$  is not a real variable we cannot determine the

value of P(A) with the help of known mathematical

methods. To determine  $P(A) = \lim_{n \to \alpha} \frac{m}{n}$ , we have

to make use of the concept of probability.

• All the identical trials are to be conducted independently. Again to define the concept of independence, we require the concept of probability.

# AXIOMATIC APPROACH TO PROBABILITY

Let S be a finite sample space associated with a random experiment. Then a real valued function P from the power set of S i.e., P(S) into the real line R is called a probability function on S, if P satisfies the following three axioms.

# • AXIOM OF POSITIVITY:

For every subset A of S,  $P(A) \ge 0$ 

i.e.,  $P(A) \ge 0, \forall A \in S$ 

- AXIOM OF CERTAINTY: P(S) = 1
- AXIOM OF UNION OR AXIOM OF ADDITIVITY:

If  $A_1, A_2$  are two disjoint subsets of S, then

 $P(A_1 \cup A_2) = P(A_1) + P(A_2)$ . Now the image P(A) of A is called the probability of the event A.

# NOTE:

• In general if  $A_1, A_2, A_3, \dots, A_n$  are n disjoint subsets of

S, then 
$$P\{A_1 \cup A_2 \cup A_3 \cup \dots \cup A_n\}$$
$$= P(A_1) + P(A_2) + P(A_3) + \dots + P(A_n)$$
i.e., 
$$P\left(\bigcup_{i=1}^n A_i\right) = \sum_{i=1}^n P(A_i)$$

If S consists of n equally likely elementary events and  $A_i$  is one such elementary event of S, then

$$P(A_i) = \frac{1}{n}; i = 1, 2, 3, \dots, n$$

- **NOTATIONS:** Let A and B be two events in a sample space S, then
- $\overline{A}$  or  $A^c$  or A' stands for the non-occurence or negation of A.
- $A \cup B$  stands for the occurence of at least one of A & B. i.e., for either the occurence of the event A or B or for the simultaneous occurence of both A & B i.e.,  $A \cap B$ .
- A ∩ B stands for the simultaneous occurence of A & B.
- $\overline{A} \cap \overline{B}$  or  $A' \cap B'$  or  $A^c \cap B^c$  stands for the non-occurence of both A and B.
- $A \subseteq B$  stands for "the occurence of A implies occurence of B".

**ADDITION THEOREM:** If A and B are any two compatible events in a sample space S, then the probability of occurence of either the event A or B or both the events A & B i.e., the event of  $A \cap B$  is given by

If A and B are M.E. events,  $P(A \cap B) = 0$ , then

 $P(A \cup B) = P(A) + P(B) \quad \dots \dots (2)$   $P(A \cup B) = P(A) + P(B) - P(A)P(B) \dots (3)$ (or)

 $P(A \cup B) = 1 - P(A^c)P(B^c)$ 

• From equation numbers (1) & (2) we can conclude that  $P(A \cup B) \le P(A) + P(B)$ Further  $A \& B \subseteq A \cup B$ 

$$P(A) \text{ or } P(B) \leq P(A \cup B) \leq P(A) + P(B)$$

P(exactly one of A, B occurs)

$$= P(A \cup B) - P(A \cap B)$$

$$= P(\overline{A} \cup \overline{B}) - P(\overline{A} \cap \overline{B})$$

If A & B are two events  $P(\overline{A} \cup \overline{B}) = 1 - P(A \cap B)$  &

$$P\left(\overline{A} \cap \overline{B}\right) = 1 - P\left(A \cup B\right)$$

•  $(A \cap \overline{B}) \cup B = A \cup B \& (\overline{A} \cap B) \cup A = (A \cup B)$ 

• For three events A, B & C  

$$P(A \cup B \cup C) = P(A) + P(B) + P(C) - P(A \cap B)$$

$$-P(A \cap C) - P(B \cap C) + P(A \cap B \cap C)$$

If A, B & C are M.E. events, the probabilities of com- $= P(A).P(B/A).P(C/A \cap B).P(D/A \cap B \cap C)$ events pound will be zero, then If A, B, C and D are independent, then  $P(A \cup B \cup C) = P(A) + P(B) + P(C)$  $P(A \cap B \cap C \cap D) = P(A).P(B).P(C).P(D)$ If A, B & C are three events then NOTE: P(exactly one of A, B, C occurs) = If A and B are M.E. events,  $P(A \cap B) = 0$ .  $P(A) + P(B) + P(C) - 2P(A \cap B)$ If A and B are independent  $-2P(A \cap C) - 2P(B \cap C) + 3P(A \cap B \cap C)$  $P(A \cap B) = P(A) \cdot P(B) \neq 0$ P(exactly two of A, B, C occur) =  $P(A \cap B)$ From these we can conclude that mutually exclu- $+P(A \cap C) + P(B \cap C) - 3P(A \cap B \cap C)$ sive events cannot be independent & independent events cannot be mutually exclusive. P(at least two of A, B, C occurs) =  $P(A \cap B)$ If A & B are independent,  $P(A \cap B) = P(A)P(B)$  $+P(A \cap C) + P(B \cap C) - 2P(A \cap B \cap C)$ then  $P(A \cup B) = P(A) + P(B) - P(A) \cdot P(B)$ . or CONDITIONAL PROBABILITY: If A & B are two events in a sample space S such that  $P(A) \neq 0$ , then the  $P(A \cup B) = 1 - P(\overline{A}) \cdot P(\overline{B})$ . probability of occurence of B, after the occurence of If A, B & C are three independent events, then the event A is called the conditional probability of B  $P(A \cup B \cup C) = 1 - P(\overline{A}) \cdot P(\overline{B}) \cdot P(\overline{C})$ given A, denoted by either P(B/A) or  $P\left(\frac{B}{A}\right)$  or If two events A & B are independent P(B;A)and is defined as A &  $\overline{B}$  are independent.  $P(B/A) = \frac{P(A \cap B)}{P(A)} = \frac{n(A \cap B)}{n(A)}.$  $\overline{A} \& B$  are independent.  $\overline{A} \& \overline{B}$  are independent. Similarly if  $P(B) \neq 0$ , then Three events A, B & C are said to be mutually inde- $P(A/B) = \frac{P(A \cap B)}{P(B)} = \frac{n(A \cap B)}{n(B)}$ pendent if If A & B are independent, then  $P(A \cap B) = P(A).P(B)$ P(B/A) = P(B) & P(A/B) = P(A) $P(A \cap C) = P(A).P(C)$ If A and B are M.E. events  $P(B \cap C) = P(B).P(C)$ P(B/A) = 0 & P(A/B) = 0 $P(A \cap B \cap C) = P(A).P(B).P(C)$ In general  $P(B/A) \neq P(A/B)$ Suppose the 1st three conditions (i), (ii) & (iii) are MULTIPLICATION THEOREM satisfied and the last i.e., (iv) condition is not satis-OR fied, then the three events A, B & C are said to be PRODUCT THEOREM pair-wise independent. OR **COMPLEMENTARY EVENTS:** If  $A \And \overline{A}$  are two events in THEOREM OF COMPOUND PROBABILITY a sample space S such that  $A \cup \overline{A} = S \& A \cap \overline{A} = \phi$ If A and B are two events in a sample space S such then  $A \& \overline{A}$  are said to be complementary events. that  $P(A) \neq 0 \& P(B) \neq 0$ , then the probability of For example: simultaneous occurence of the two events A & B is given by In rolling of a die  $S = \{1, 2, 3, 4, 5, 6\}$  $P(A \cap B) = P(A) \cdot P(B/A) = P(B) \cdot P(A/B) \cdot P(A/B)$ Let  $A = \{1, 3, 5\}$ , then  $\overline{A} = \{2, 4, 6\}$ If A & B are independent P(B/A) = P(B) & Now  $A \cup \overline{A} = \{1, 2, 3, 4, 5, 6\} = S$ P(A | B) = P(A), then  $P(A \cap B) = P(A) \cdot P(B)$ .  $A \cap \overline{A} = \phi$ For four events A, B, C & D The two events namely (1) The event of getting odd  $P(A \cap B \cap C \cap D)$ number of points upwards & (2) The event of getting

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even number of points upwards are complementary events.

**NOTE:** Complementary events are always mutually exclusive events.

Now consider  $A \cup \overline{A} = S$ , then

$$P(A \cup \overline{A}) = P(S)$$
$$P(A) + P(\overline{A}) = 1$$
$$\therefore P(A) = 1 - P(\overline{A}); \text{ where}$$
$$(\overline{A})$$

$$P\left(\overline{A}\right) = \frac{n(A)}{n(S)}.$$

#### BAYES THEOREM :

Suppose  $E_1, E_2, E_3, \dots, E_n$  are 'n' mutually exclusive and

exhaustive events with  $P(E_i) > 0$  for

 $i = 1, 2, 3, \dots, n$  in a random experiment. Then for any event A of the random experiment

$$P\left(\frac{E_{k}}{A}\right) = \frac{P(E_{k}).P\left(\frac{A}{E_{k}}\right)}{\sum_{i=1}^{n} P(E_{i}) P\left(\frac{A}{E_{i}}\right)} \text{ for } i=1,2,3...n$$

#### **GEOMETRIC PROBABILITY**

Classical definition of probability fails if the total number of outcomes of an experiment is infinite. Then the probability that a point selected in a given region will be in a specified part of it is called geometrical probability or probability in continuous.

Thus the probability P is given by

 $P = \frac{Measure of specified part of the region}{Measure of the whole region}$ 

Where measure refers to the length, area volume of the region of we are dealing with one, two or three dimensional space respectively.

#### NOTE:

1. When 'n' fair coins are tossed the probability of

getting exactly 'r' ( $\leq n$ ) heads (tails) =  $\frac{{}^{n}C_{r}}{2^{n}}$ 

2. When 'n' fair coins are tossed the probability of

getting atleast one head (tail) =  $1 - \frac{1}{2^n}$ 

$$s \ \frac{n+2}{2^{m+1}}$$

A coin is tossed (m+n) times (m>n), then the probability of getting exactly 'm' consecutive heads is

$$\frac{n+2}{2^{m+2}}$$

4.

6.

5. The probability of getting a sum of 'S' points when 'n' symmetrical dice are rolled is

$$P(X=S) = \sum_{k=0}^{\frac{S-n}{6}} \frac{(-1)^k \cdot {}^n c_k \cdot {}^{(s-6k-1)} c_{n-1}}{6^n} \quad \text{where}$$

$$k=0,1,2....\left[\frac{s-n}{6}\right]$$

If 'p' and 'q' are the probability of success, failure of a game in which  $A_1, A_2, A_3, \dots, A_n$  play then

i )probability of 
$$A_1$$
 's winning is  $\frac{p}{1-q^n}$ 

ii)probability of 
$$A_2$$
's winning is  $\frac{qp}{1-q^n}$ 

iii)probability of  $A_k$ 's  $(1 \le k \le n)$  winning is  $\frac{q^{k-1} \cdot p}{1-q^n}$ 

7. If 'n' letters are put at random in the 'n' addressed envelopes, the probability that

i) All the letters are in right envelopes is  $\frac{1}{n!}$ 

ii) Exactly one letter in wrong envelope is 0iii) At least one letter may be in wrongly addressed

envelope is 
$$1 - \frac{1}{n!}$$

iv) Exactly 'r'  $(r \neq 1)$  letters are in wrong envelopes

is 
$$\frac{{}^{n}p_{r}}{n!} \left(1 - \frac{1}{1!} + \frac{1}{2!} - \frac{1}{3!} + \dots + \frac{(-1)^{r}}{r!}\right)$$

v) all the letters may be in wrong envelopes

is 
$$\frac{{}^{n}p_{n}}{n!} \left( 1 - \frac{1}{1!} + \frac{1}{2!} - \frac{1}{3!} + \dots + \frac{(-1)^{n}}{n!} \right)$$
  
LEVEL-1

The probability of an impossible event is

1.  $\frac{1}{2}$ 2. 13. 04.  $\frac{1}{4}$ The probability of a certain event is1. 02.  $\frac{1}{2}$ 3. 14.  $\frac{1}{4}$ The probability of an event lies in

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1.

2.

3.

2. [0, 1) 3. [0, 1] 4. (0, 1) 1. (0, 1] If A and B are two events in a sample space S such that  $P(A) \neq 0$ , then  $P\left(\frac{B}{A}\right) =$ 2.  $\frac{P(A \cap B)}{P(B)}$ 14. 1. P(A).P(B) 3.  $\frac{P(A \cap B)}{P(A)}$ 4. P(B) 5. If A and B are any two events in a sample space S then  $P(A \cup B)$  is 1.  $\geq P(A) + P(B)$ 2. P(A) + P(B) 3.  $\leq P(A) + P(B)$ 4.  $P(A \cap B)$ 6. If A and B are two mutually exclusive events then  $P(A \cap B) =$ 1. P(A). P(B) 2. P(A) 3.0 4 1 7. If A and B are two mutually exclusive events then 16.  $P(A \cup B) =$ 1.  $P(A) + P(B) - P(A \cap B)$ 2.  $P(A) - 2P(A \cap B)$ 3. P(A) + P(B)4. P(A).P(B) 17. If A and B are independent events then  $P\left(\frac{A}{P}\right) =$ 8. 1. P(A) 2.  $\frac{P(B)}{P(A)}$  3. P(B) 4. P(A).P(B) 18. If A and B are independent events then  $P\left(\frac{B}{A}\right) =$ 9. 2.  $\frac{P(B)}{P(A)}$ 1.  $\frac{1}{2}$ 3. P(B) 4. P(A).P(B) 1. P(A) 19. 10. If A and B are two events in a sample space S such that  $P(A) \neq 0$  and  $P(B) \neq 0$ , then  $P(A \cap B) =$ 2.  $P(A).P\left(\frac{B}{A}\right)$ 1. P(A).P(B) 20. 4. P(A) 3. P(B) 11. If A and B are two independent events in a sample space S then  $P(A \cap B) =$ 1.  $P(A).P\left(\frac{A}{B}\right)$  2.  $P(B).P\left(\frac{B}{A}\right)$ 3. P(A).P(B) 4. P(A)+P(B) If  $A \subset B$ , then  $P(A \cap B^{C}) =$ 12. 1.1 2.0 3. P(A) 4. P(B) 21. 13. If A, B and C are any three events in a sample space S then  $P\{A \cap (B \cup C)\} =$ 1.  $P(A) + P(B) + P(C) - P(A \cap B) - P(A \cap C)$ 

2. P(A) + P(B) + P(C) - P(B)P(C)3.  $P(A \cap B) + P(A \cap C) - P(A \cap B \cap C)$ 4.  $P(B \cap C) + P(A \cap B) - P(A \cap B \cap C)$ P (at least one of the events A or B) = 1.  $1 - P(A \cap B)$ 2.  $1 - P(\overline{A} \cap \overline{B})$ **3.**  $1 - P(A \cup B)$  **4.**  $1 - P(A) \cdot P(B)$ 15. If  $P\left(\frac{B}{A}\right) < P(B)$ , the relationship between  $P\left(\frac{A}{B}\right)$ and P(A) is 1.  $P\left(\frac{A}{B}\right) < \frac{1}{2}P(A)$  2.  $P\left(\frac{A}{B}\right) > P(A)$ 3.  $P\left(\frac{A}{B}\right) < P(A)$  4.  $P\left(\frac{A}{B}\right) < 2P(A)$ If  $P\left(\frac{A}{C}\right) > P\left(\frac{B}{C}\right)$  and  $P\left(\frac{A}{\overline{C}}\right) > P\left(\frac{B}{\overline{C}}\right)$ , then the relationship between P(A) and P(B) is 2.  $P(A) \leq P(B)$ 1. P(A)=P(B) **3**. P(A) > P(B)4.  $P(A) \ge P(B)$ If E and  $\overline{E}$  denote the happening and not happening of an event and  $P(\overline{E}) = \frac{1}{5}, P(E) =$ 1.  $\frac{1}{5}$  2.  $\frac{2}{5}$  3.  $\frac{3}{5}$  4.  $\frac{4}{5}$ If A and B are two Mutually Exclusive events in a sample space S such that P(B) = 2P(A) and  $A \cup B = S$ , then P(A)= 2.  $\frac{1}{2}$  3.  $\frac{1}{4}$ 4.  $\frac{1}{2}$ An experiment yields 3 Mutually Exclusive and exhaustive events A, B and C. If P(A) = 2P(B) = 3P(C), then P(A)=1.  $\frac{1}{6}$  2.  $\frac{5}{6}$  3.  $\frac{6}{11}$  4.  $\frac{5}{11}$ If A and B are two events such that P(A) > 0 and  $P(B) \neq 1$ , then  $P(\overline{A}/\overline{B}) =$ 1.  $1 - \frac{P(A \cup B)}{P(\overline{B})}$  2.  $1 - \frac{P(A \cup B)}{P(B)}$ 3.  $\frac{1 - P(A \cup B)}{1 - P(B)}$  4.  $\frac{P(A \cup B)}{P(B)}$ If A & B are 2 events then  $P\{(A \cap \overline{B}) \cup (\overline{A} \cap B)\}=$ 1.  $P(A \cup B) - P(A \cap B)$  2.  $P(A \cup B) + P(A \cap B)$ **3.** P(A) + P(B) **4.**  $P(A) + P(B) + P(A \cap B)$ 

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If A and B are two events such that  $P(A) = \frac{1}{4}$ ; 22. 30.  $P(A \cup B) = \frac{1}{3}$  and P(B)=P, the value of P if A and B are mutually exclusive is 1.  $\frac{1}{3}$  2.  $\frac{1}{6}$  3.  $\frac{1}{12}$  4.  $\frac{1}{5}$ 31. If A and B are two events such that  $P(A) = \frac{1}{4}$  and 23.  $P(A \cup B) = \frac{1}{3}$  and P(B)=P, the value of P if A and B are independent 1.  $\frac{1}{0}$ 2.  $\frac{2}{9}$  3.  $\frac{4}{9}$  4.  $\frac{5}{9}$ 32. 24. If the probability of two events  $E_1$  and  $E_2$  in a random experiment are  $P(E_1) = 0.4, P(E_2) = P$ ,  $P(E_1 \cup E_2) = 0.7$ , the value of P, if  $E_1$  and  $E_2$  are is mutually exclusive is 3.0.3 1.0.1 2.0.2 4.0.5 25. If the probability of two events  $E_1$  and  $E_2$  in a ran-33. dom experiment are  $P(E_1) = 0.4, P(E_2) = P$ , is a square is  $P(E_1 \cup E_2) = 0.7$ , the value of P, if  $E_1$  and  $E_2$  are independent is 2.0.4 3.0.5 4.0.2 1.0.3 34. If A and B are two events such that  $P(A) = \frac{1}{A}$ , 26. by 3 or 5 is  $P(A \cup B) = \frac{1}{3}$  and P(B) = P, the value of P if  $A \subset B$ 35. 1.  $\frac{1}{12}$  2.  $\frac{3}{4}$  3.  $\frac{2}{3}$  4.  $\frac{1}{3}$ If A and B are two events such that  $P(A) = \frac{3}{8}$ , 27. 1 36.  $P(B) = \frac{5}{8}$  and  $P(A \cup B) = \frac{3}{4}$ , then  $P\left(\frac{B}{\overline{4}}\right) =$ is 1.  $\frac{2}{5}$  2.  $\frac{3}{5}$  3.  $\frac{4}{5}$  4.  $\frac{1}{5}$ 1. 28. One of the two events must happen. Given that the 37. chance of one is two-thirds that of the other, find the odds in favour of the other 3. 3 to 2 4.5 to 2 1. 2 to 3 2. 2 to 5 For two independent events  $P(A) = \frac{3}{4}$  and 29. 38.  $P(B) = \frac{5}{8}$ , then  $P(A \cup B) =$ 1. 1.  $\frac{3}{32}$  2.  $\frac{29}{32}$  3.  $\frac{15}{32}$  4.  $\frac{5}{32}$ 39.

If A and B are two events such that  $P(A) = \frac{3}{\circ}$ ,

$$P(B) = \frac{5}{8}$$
 and  $P(A \cup B) = \frac{3}{4}$ , then  $P\left(\frac{A}{\overline{B}}\right) =$   
1.  $\frac{2}{3}$  2.  $\frac{2}{5}$  3.  $\frac{1}{3}$  4.  $\frac{1}{5}$ 

31. The results of students of a college revealed the following facts. 25% of students failed in Mathematics, 15% of students failed in Chemistry, 10% of students failed in both. If a student is selected at random. The probability that he has failed in Mathematics, given that he failed in Chemistry is

1. 
$$\frac{1}{5}$$
 2.  $\frac{2}{3}$  3.  $\frac{3}{5}$  4.  $\frac{1}{3}$ 

- 32. In a class 40% of students read History, 25% Civics and 15% both History and Civics. If a student is selected at random from that class, the probability that he reads History, if it is known that he reads Civics is
  - 1.  $\frac{1}{5}$  2.  $\frac{2}{5}$  3.  $\frac{3}{5}$  4.  $\frac{3}{8}$
- A card is drawn from a pack of 100 cards numbered 1 to 100. The probability of drawing a number which is a square is

1. 
$$\frac{3}{10}$$
 2.  $\frac{1}{5}$  3.  $\frac{1}{10}$  4.  $\frac{3}{5}$ 

34. From a set of 17 cards numbered 1 to 17 one is drawn at random. The probability that it is divisible by 3 or 5 is

1. 
$$\frac{4}{17}$$
 2.  $\frac{5}{17}$  3.  $\frac{6}{17}$  4.  $\frac{7}{17}$ 

35. An integer is chosen from the 1st 200 positive integers. The probability that the integer selected is divisible by 6 or 8 is

$$\frac{2}{5}$$
 2.  $\frac{3}{8}$  3.  $\frac{1}{4}$  4.

6. The probability that a randomly chosen number from the set of first 100 natural numbers is divisible by 4 is

$$\frac{5}{24}$$
 2.  $\frac{3}{4}$  3.  $\frac{1}{2}$  4.  $\frac{3}{4}$ 

37. The probability that a randomly chosen number from the 1st 100 natural numbers is divisible by 4 or 6 is

1. 
$$\frac{11}{100}$$
 2.  $\frac{22}{100}$  3.  $\frac{33}{100}$  4.  $\frac{44}{100}$ 

38. From 25 tickets marked with the 1st 25 numerals, one is drawn at random, the probability that it is a multiple of 5 or 7 is

$$\frac{7}{25}$$
 2.  $\frac{10}{25}$  3.  $\frac{8}{25}$  4,  $\frac{9}{25}$ 

9. From the set of numbers {1, 2, 3, 4, 5, 6, 7, 8} two numbers are selected at random without replace-

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1

ment. The probability that their sum is more than 13 is

- 1.  $\frac{1}{14}$  2.  $\frac{2}{7}$  3.  $\frac{3}{7}$  4.  $\frac{4}{7}$
- 40. From a box containing 10 cards numbered 1 to 10, four cards are drawn together. The probability that their sum is even is

$$\frac{11}{21}$$
 2.  $\frac{5}{21}$  3.  $\frac{6}{21}$  4.  $\frac{1}{21}$ 

 An urn contains 25 balls numbered 1 through 25. Two balls drawn one at a time with replacement. The probability that both the numbers on the balls are odd is

1. 
$$\frac{{}^{13}c_2}{625}$$
 2.  $\frac{169}{625}$  3.  $\frac{{}^{25}c_2}{625}$  4.  $\frac{139}{625}$ 

42. There are 25 stamps numbered from 1 to 25 in a box. If a stamp is drawn at random from the box, the probability that the number on the stamp will be a prime number is

1. 
$$\frac{7}{25}$$
 2.  $\frac{8}{25}$  3.  $\frac{9}{25}$  4.  $\frac{6}{25}$ 

- 43. If the probabilities of two dogs A and B dying within 10 years are respectively p and q, then the probability that at least one of them will be alive at the end of 10 years is
- 1. p+q
  2. 1-pq
  3. p+q-pq
  4. pq
  44. If the probabilities of two dogs A and B dying within 10 years are respectively p and q, then the probability that exactly one of them will be alive at the end of 10 years is

  p+q-2pq
  p+q

3. 
$$1-pq$$
 4. pq  
5. The probability that the dog of Krishna will be

4

46.

10 years hence is  $\frac{7}{15}$  and that of Hari will be alive is

 $\frac{7}{10}$ . The probability that both the dogs will be dead within 10 years is

1. 
$$\frac{21}{150}$$
 2.  $\frac{24}{150}$  3.  $\frac{49}{150}$  4.  $\frac{5}{25}$ 

The probability that a man A will be alive for 20 more years is  $\frac{3}{5}$  and the probability that his wife will be

alive for 20 more years is  $\frac{2}{3}$ . The probability that

$$\frac{1}{2}$$
  $\frac{1}{2}$   $\frac{1}$ 

1. 
$$\frac{4}{15}$$
 2.  $\frac{2}{15}$  3.  $\frac{7}{15}$  4.  $\frac{3}{15}$ 

1. 
$$\frac{27}{80}$$
 2.  $\frac{53}{80}$  3.  $\frac{23}{80}$  4.  $\frac{51}{80}$ 

48. A husband and wife appear in an interview for two vacancies in the same post. The probability of husbands selection is  $\frac{1}{7}$  and that of wife is  $\frac{1}{5}$ . The probability that both of them will be selected is 1.  $\frac{24}{35}$  2.  $\frac{2}{7}$  3.  $\frac{1}{35}$  4.  $\frac{2}{35}$ 49. A husband and wife appear in an interview for two vacancies in the same post. The probability of husbands selection is  $\frac{1}{7}$  and that of wife is  $\frac{1}{5}$ . The probability that none of them will be selected is 1.  $\frac{1}{35}$  2.  $\frac{2}{7}$  3.  $\frac{24}{35}$  4.  $\frac{2}{35}$ 50. A husband and wife appear in an interview for two vacancies in the same post. The probability of husbands selection is  $\frac{1}{7}$  and that of wife is  $\frac{1}{5}$ . The probability that only one of them will be selected is 1.  $\frac{1}{35}$  2.  $\frac{24}{35}$  3.  $\frac{2}{7}$  4.  $\frac{2}{35}$ 51. From each of the three married couples one partner is selected at random. The probability that all the three are males is 1.  $\frac{1}{2}$  2.  $\frac{1}{4}$  3.  $\frac{1}{8}$  4.  $\frac{3}{8}$ 52. From each of the three married couples one partner is selected at random. The probability that all the three are females is 1.  $\frac{1}{2}$  2.  $\frac{1}{4}$  3.  $\frac{1}{8}$  4.  $\frac{3}{8}$ 53. From each of the three married couples one partner is selected at random. The probability that all the three belong to the same sex is 1.  $\frac{1}{2}$  2.  $\frac{1}{4}$  3.  $\frac{1}{8}$  4.  $\frac{3}{8}$ From each of the three married couples one partner 54. is selected at random. The probability that 2 are males and one is a female is 1.  $\frac{1}{8}$  2.  $\frac{1}{4}$  3.  $\frac{3}{8}$  4.  $\frac{1}{2}$ 55. A and B are two candidates seeking admission in I.I.T. The probability that both A and B are selected is at the most 0.3. If the probability of A's selection is 0.5, then the probability of B's selection if A and B are independent is 1.0.6 2. < 0.6 4. >0.6 3.  $\leq 0.6$ 56. In a room there are 6 couples. Out of them if 4 are selected at random, the probability that they may be couples is 1.  $\frac{4}{33}$  2.  $\frac{2}{33}$  3.  $\frac{1}{33}$  4.  $\frac{3}{33}$ 

57. In a race three horses A, B and C are taking part. The probability of A's winning is twice the probability of B's winning and the probability of B's winning is thrice the probability of C's winning. The probability

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alive

of C's winning. If the dead heat is not possible is  
1. 
$$\frac{6}{10}$$
 2.  $\frac{3}{10}$  3.  $\frac{1}{10}$  4.  $\frac{2}{10}$   
58. Three students A, B and C are to take part in a swimming zero his 3 lines the probability of C's winning of these is not hose is interesting a conservative of the same that all the three are while is  
1.  $\frac{4}{7}$  2.  $\frac{2}{7}$  3.  $\frac{2}{7}$  4.  $\frac{1}{7}$   
59. Three squares of a chess board having 8×8 squares being chosen at random, the chance that all the three are block is  
1.  $\frac{3}{4c_c}$  2.  $\frac{4}{4c_c}$  3.  $\frac{4}{4c_c}$  4.  $\frac{4}{4c_c}$   
60. Three squares of a chess board having 8×8 squares being chosen at random, the chance that all the three are block is  
1.  $\frac{3}{4c_c}$  2.  $\frac{2}{4c_c}$  3.  $\frac{4}{4c_c}$  4.  $\frac{4}{4c_c}$   
61. Three squares of a chess board having 8×8 squares being chosen at random, the chance that all the three of the same colour is  
1.  $\frac{3}{4c_c}$  2.  $\frac{2}{4c_c}$  3. 1. 4.  $\frac{4c_c}{4c_c}$   
62. Three squares of a chess board having 8×8 squares being chosen at random, the chance that all the three of the same colour is  
1.  $\frac{3}{4c_c}$  2.  $\frac{2}{4c_c}$  3. 1. 4.  $\frac{4c_c}{4c_c}$   
63. A speaks truth in 75% of the cases and B in 80% of the cases. The percentage of cases stared B in 80% of the cases. The percentage of cases stare and B in 80% of the cases. The percentage of cases stare and B in 80% of the cases. The percentage of cases they are likely to concur with each other in making the same statement is a 25%. A bage contains 17 Counters marked with numbers 1 to 17 on chils. A counter is drawn and replaced. A second draw is the manace. The chance that the result and the stare contains is 0 diverse and the second and is od dimense. The percentage of cases stare and bin 80% of the cases. The percentage of cases they are likely to concur with each other in making the same statement is a findary is 2. 35%. A source and the case stare dimense that the number on the counter stare wand replaced. A farge and the case stare dimense that mean the farge and finde. The chance that the recoming of

	problem are 7 to 5. If both of them try independently,		the papers A and B is
	the probability that the problem will be solved is $1 \frac{11}{2} 2 \frac{13}{3} 3 \frac{16}{4} 4 \frac{8}{3}$		1. $\frac{4}{20}$ 2. $\frac{3}{20}$ 3. $\frac{17}{20}$ 4. $\frac{15}{20}$
80	The odds against a certain event are 5 to 2 and the	88.	The probability that a student passes in Mathemat-
00.	odds in favour of an other event independent of the former are 6 to 5. The probability that none of the events will happen is		ics is $\frac{2}{3}$ and the probability that he passes in Eng-
	1. $\frac{52}{77}$ 2. $\frac{12}{77}$ 3. $\frac{25}{77}$ 4. $\frac{5}{77}$		lish is $\frac{4}{9}$ . The probability that he passes in any one
81.	A person is known to hit the target in 3 out of 4 shots, where as an other person is known to hit twice in every three attempts. If both of them try independ- ently the probability that the target being hit is		of the courses is $\frac{4}{5}$ . The probability that he passes in both is
	1. $\frac{1}{12}$ 2. $\frac{11}{12}$ 3. $\frac{5}{12}$ 4. $\frac{3}{12}$		1. $\frac{11}{45}$ 2. $\frac{14}{45}$ 3. $\frac{17}{45}$ 4. $\frac{15}{45}$
82.	A, B and C can solve a problem independently with	89.	In a group of 25 people everybody is proficient either
	respective probabilities $\frac{1}{3}$ , $\frac{1}{4}$ and $\frac{1}{5}$ . If all of them		them 19 people are proficient in Mathematics and 16 are proficient in Statistics. If a person is selected
	try independently the probability that the problem will be solved is		at random, the probability that he is proficient both in Mathematics & Statistics is
	1. $\frac{1}{60}$ 2. $\frac{3}{5}$ 3. $\frac{48}{60}$ 4. $\frac{57}{60}$		1. $\frac{1}{5}$ 2. $\frac{2}{5}$ 3. $\frac{3}{5}$ 4. $\frac{4}{5}$
83.	The probability that A can solve a problem in Math-	90.	Two cards are drawn at random from 10 cards num-
	ematics is $\frac{2}{5}$ and B can solve it is $\frac{3}{8}$ and for C it is		if the two cards are drawn together is
	$\frac{4}{2}$ When all of them try independently the prob-		1. $\frac{2}{9}$ 2. $\frac{4}{9}$ 3. $\frac{5}{9}$ 4. $\frac{3}{9}$
	10 ability that the problem will not be solved is	91.	The probability that A will fail in an examination is
	31 $9$ $11$ $3$		0.2 and that of B failing is 0.3. The probability that exactly one of them will fail is
	1. $\frac{1}{40}$ 2. $\frac{1}{40}$ 3. $\frac{1}{40}$ 4. $\frac{1}{40}$	02	1. 0.38 2. 0.35 3. 0.42 4. 0.62
84.	A can hit a target 3 times in 6 shots; B, 2 times in 4 shots and C, 4 times in 4 shots. All of them fire at a target independently. The probability that the target	92.	only one can happen. The odds are 7 to 3 against A and 6 to 4 against B. The odds against C are 1.3 to $4.2$ 4 to $33$ 7 to $34$ 3 to 7
	will be hit is 1. 1 2. 0.5 3. 0.25 4. 0.125	93.	The probability that A and B pass in an examination
85.	Two cards are selected at random from 10 cards numbered 1 to 10. The probaility that their sum is		is $\frac{2}{10}$ and $\frac{3}{10}$ respectively. The probability that only
	odd, if the 2 cards are drawn one after an other with- out replacement is		one of them will pass the examination is
	1. $\frac{5}{2}$ 2. $\frac{4}{2}$ 3. $\frac{2}{2}$ 4. $\frac{3}{2}$		1. $\frac{35}{100}$ 2. $\frac{38}{100}$ 3. $\frac{41}{100}$ 4. $\frac{45}{100}$
86.	9 9 9 9 9 The results of an examination in two papers A and B	94.	A single letter is selected at random from the word ARTICLE, the probability that it is a vowel is
	in paper A, 7 passed in paper B, 8 failed in both the papers A and B. If one is selected at random, the		1. $\frac{2}{7}$ 2. $\frac{3}{7}$ 3. $\frac{4}{7}$ 4. $\frac{5}{7}$
	probability that the candidate has failed in A or B is $15$ 16 $17$ 18	95.	The probability that at least one of the events A and B occur is 0.6. If A and B occur simultaneously with
	1. $\frac{10}{20}$ 2. $\frac{10}{20}$ 3. $\frac{17}{20}$ 4. $\frac{10}{20}$		probability 0.2, then $P(\overline{A}) + P(\overline{B}) =$
87.	The results of an examination in two papers A and B for 20 candidates were recorded as follows. 8 passed in paper A, 7 passed in paper B, 8 failed in both the papers A and B. If one is selected at random, the probability that the candidate has passed in both	96.	1. 0.4 2. 0.8 3. 1.2 4. 1.6 In a book of 100 pages, if a page is opened at ran- dom, the probability that the number on it is a prime is

$$1, \frac{1}{2}$$
 $2, \frac{1}{3}$  $3, \frac{1}{4}$  $4, \frac{1}{8}$ 97. A letter is taken out at random from the English alphabet. The probability that it is a vowel is $1, \frac{3}{26}$  $2, \frac{4}{26}$  $3, \frac{5}{26}$  $4, \frac{2}{26}$ 108. Let A and B be two events such that P(A)=0.3 and P(A \cup \overline{B}) = 0.8. If A and B are independent events P(B) = $1, \frac{3}{11}$  $2, \frac{4}{11}$  $3, \frac{2}{11}$  $4, \frac{5}{11}$ 99. A single letter is selected at random from the word PROBABILITY. The probability that it is not a vowel is $1, \frac{4}{11}$  $2, \frac{2}{11}$  $3, \frac{7}{11}$  $4, \frac{5}{11}$ 100. Two letters are taken at random from the word PROBABILITY. The probability that it is not a vowel is $1, \frac{4}{11}$  $2, \frac{2}{11}$  $3, \frac{7}{11}$  $4, \frac{5}{11}$ 100. Two letters are taken at random from the word PROBABILITY. The probability that it heast one of the norther of the probability that it least one is a vowel is $1, \frac{1}{4}$  $2, \frac{1}{2}$  $3, 1$  $4, \frac{4}{5}$ 100. Two letters are taken at random from the word PROBABILITY. The probability that the number on this a draw of the probability that it least one is a vowel is $1, \frac{1}{2}$  $2, \frac{2}{3}$  $3, \frac{5}{4}$  $4, \frac{1}{4}$ 101. There are 100 pages is two digit number made up with the same digit is $1, \frac{1}{5}$  $2, \frac{4}{5}$  $3, \frac{1}{5}$  $4, \frac{3}{10}$ 102. In a book of 100 pages, if a page is boyne and letel only is $1, \frac{1}{5}$  $2, \frac{4}{5}$  $3, \frac{1}{2}$  $4, \frac{1}{22}$ 103. The probability of getting a number between 1 and to ne its bay one and field roly is $1, \frac{1}{5}$  $2, \frac{4}{5}$  $3, \frac{1}{2}$  $4, \frac{1}{2}$ 104. Counters n

PROBABILITY

 $\frac{4}{5}$ 4.

4.  $\frac{4}{7}$ 

 $\frac{1}{8}$ 4.

5 of them "N" is

4.  $\frac{3}{36}$ 

 $\frac{19}{24}$ 4.

4. 2

4. 2

4. 2

 $4. \ \frac{{}^n c_r}{3^n}$ 

 $4. \ \frac{{}^{n}c_{r}}{2^{n}}$ 

4.  $\frac{1}{4}$ 

118.	The probability of getting a head and 6 tails when an unbiased coin is tossed 7 times is		1. $\frac{1}{4}$ 2. $\frac{1}{2}$ 3. $\frac{2}{3}$ 4. $\frac{3}{4}$
119.	1. $\frac{1}{128}$ 2. $\frac{5}{128}$ 3. $\frac{7}{128}$ 4. $\frac{3}{128}$ If two coins are tossed 5 times, the chance that there will be 5 heads and 5 tails is	131.	If a coin is tossed 3 times the probability of obtaining 2 heads or 2 tails is $1 \qquad 1 \qquad 2 \qquad 3$
120.	1. $\frac{45}{256}$ 2. $\frac{120}{256}$ 3. $\frac{63}{256}$ 4. $\frac{30}{256}$ The probability of getting at least one head when we	132.	1. $\frac{1}{4}$ 2. $\frac{1}{2}$ 3. $\frac{2}{3}$ 4. $\frac{3}{4}$ When a perfect die is rolled, the probability of getting a face with 4 points upward is
121.	1. $\frac{3}{8}$ 2. $\frac{5}{8}$ 3. $\frac{7}{8}$ 4. $\frac{1}{8}$ The probability of getting at least one head when we toss 5 unbiased coins is	133.	1. $\frac{4}{6}$ 2. $\frac{3}{6}$ 3. $\frac{2}{6}$ 4. $\frac{1}{6}$ When a perfect die is rolled, the probability of getting a face with 4 or 5 points upward is
122.	1. $\frac{5}{32}$ 2. $\frac{1}{32}$ 3. $\frac{31}{32}$ 4. $\frac{4}{32}$ A coin is weighted so that head is twice as likely to appear as tail. When such a coin is tossed once the probability of getting tail is	134.	1. $\frac{1}{3}$ 2. $\frac{2}{3}$ 3. $\frac{1}{2}$ 4. $\frac{1}{4}$ When a perfect die is rolled, the probability of getting a face with even number of points upward is
123	1. $\frac{1}{2}$ 2. $\frac{1}{3}$ 3. $\frac{2}{3}$ 4. $\frac{1}{4}$	135.	1. $\frac{1}{4}$ 2. $\frac{1}{3}$ 3. $\frac{1}{2}$ 4. $\frac{1}{8}$ When a perfect die is rolled the probability of getting a face with odd number of points upward is
123.	appear as tail, then the probability of head is 1. $\frac{1}{4}$ 2. $\frac{1}{2}$ 3. $\frac{3}{4}$ 4. $\frac{1}{8}$	136.	1. $\frac{1}{4}$ 2. $\frac{1}{3}$ 3. $\frac{1}{2}$ 4. $\frac{1}{8}$ When a perfect die is rolled the probability of getting
124.	Two persons A and B have respectively (n+1) and n coins which they toss simultaneously. The probabil- ity that A will have more number of heads is	407	1. $\frac{1}{6}$ 2. $\frac{1}{2}$ 3. 1 4. 2
125.	1. $\frac{1}{4}$ 2. $\frac{1}{3}$ 3. $\frac{1}{2}$ 4. $\frac{1}{8}$ A tosses 2 coins while B tosses 3. The probability	137.	In a single throw of a symmetrical die the probability that a number less than 4 is obtained, given that the throw resulted is an odd number is
	that B obtains more number of heads is 1. $\frac{1}{4}$ 2. $\frac{1}{3}$ 3. $\frac{1}{2}$ 4. $\frac{3}{4}$	138.	1. $\frac{1}{2}$ 2. $\frac{1}{3}$ 3. $\frac{2}{3}$ 4. $\frac{1}{4}$ A symmetrical die is rolled. If an odd number comes
126.	The probability of getting at least 2 heads, when an unbiased coin is tossed 6 times is $63    57    7    37$		greater than 3 on it is 1. $\frac{1}{2}$ 2. $\frac{1}{2}$ 3. $\frac{2}{3}$ 4. $\frac{1}{4}$
127.	1. $\frac{65}{64}$ 2. $\frac{57}{64}$ 3. $\frac{7}{64}$ 4. $\frac{57}{64}$ When a fair coin is tossed thrice, the probability of obtaining head at most twice is	139.	A perfect die is rolled. If the outcome is an odd number, the probability that it is a prime is $1 \qquad 2 \qquad 1 \qquad 1$
128.	1. $\frac{1}{8}$ 2. $\frac{5}{8}$ 3. $\frac{7}{8}$ 4. $\frac{3}{8}$ A fair coin is tossed 4 times. The probability that heads exceed tails in number is	140.	1. $\frac{1}{3}$ 2. $\frac{2}{3}$ 3. $\frac{1}{2}$ 4. $\frac{1}{8}$ Three faces of a fair die are yellow, two faces red and one blue. The die is tossed 3 times. The prob- ability that the colours yellow, red and blue appear in the 1st 2nd and 3rd tosses respectively is
129.	1. $\frac{3}{16}$ 2. $\frac{1}{4}$ 3. $\frac{5}{16}$ 4. $\frac{7}{16}$ A and B toss a coin alternately till one of them gets a head and wins the game. The probability of A's	141.	1. $\frac{1}{6}$ 2. $\frac{1}{36}$ 3. $\frac{35}{36}$ 4. $\frac{1}{3}$ Three faces of a fair die are yellow, two faces red and one blue. The die is tossed 3 times. The probability that all the three times we get yellow colour.
130.	Winning if A starts the game is 1. $\frac{1}{2}$ 2. $\frac{1}{3}$ 3. $\frac{2}{3}$ 4. $\frac{1}{4}$ If a coin is tossed 3 times the probability of getting one head or one tail is	142.	is 1. $\frac{3}{8}$ 2. $\frac{5}{8}$ 3. $\frac{1}{8}$ 4. $\frac{7}{8}$ Three faces of a fair die are yellow, two faces red

	and one blue. The die is tossed 3 times. The prob- ability that it will show yellow colour in the 1st 2 throws and red in the 3rd throw is	154	1. $\frac{5}{9}$ 2. $\frac{2}{9}$ 3. $\frac{11}{36}$ 4. $\frac{5}{36}$
	1. $\frac{1}{36}$ 2. $\frac{1}{18}$ 3. $\frac{1}{12}$ 4. $\frac{1}{6}$	104.	The probability that the sum is neither 7 nor 11 is $\frac{2}{3}$
143.	Three faces of a fair die are yellow, two faces red and one blue. The die is tossed 3 times. The prob- ability that it will show red colour in the 1st two throws and blue in the 3rd throw is	155.	1. $\frac{2}{9}$ 2. $\frac{3}{9}$ 3. $\frac{7}{9}$ 4. $\frac{4}{9}$ Two uniform dice marked 1 to 6 are thrown together. The probability that the sum is a prime number is
144.	1. $\frac{1}{18}$ 2. $\frac{1}{36}$ 3. $\frac{1}{54}$ 4. $\frac{1}{27}$ The probability of getting a number greater than 2 or an even number in a single throw of a fair die is	156.	1. $\frac{1}{12}$ 2. $\frac{1}{4}$ 3. $\frac{5}{12}$ 4. $\frac{4}{12}$ Two uniform dice marked 1 to 6 are thrown together. The probability that the sum is not a prime number
445	1. $\frac{1}{2}$ 2. $\frac{1}{3}$ 3. $\frac{5}{6}$ 4. $\frac{1}{4}$		1. $\frac{1}{4}$ 2. $\frac{5}{12}$ 3. $\frac{7}{12}$ 4. $\frac{9}{12}$
145.	I wo persons A and B alternately throw a die and the person who 1st throws 5 wins. If A starts the game the probability of his winning is	157.	Two uniform dice marked 1 to 6 are thrown together. The probability that the sum is even is
	1. $\frac{1}{6}$ 2. $\frac{5}{11}$ 3. $\frac{6}{11}$ 4. $\frac{3}{11}$		1. $\frac{1}{4}$ 2. $\frac{1}{3}$ 3. $\frac{1}{2}$ 4. $\frac{1}{12}$
146.	Two persons A and B alternately throw a die. The person who 1st throw 4 or 5 wins. If A starts the	158.	Two uniform dice marked 1 to 6 are thrown together. The probability that the sum is odd is
	game, the probability of his winning is $1$		1. $\frac{1}{4}$ 2. $\frac{1}{3}$ 3. $\frac{1}{2}$ 4. $\frac{1}{12}$
147.	1. $\frac{1}{5}$ 2. $\frac{1}{5}$ 3. $\frac{1}{5}$ 4. $\frac{1}{5}$ Two symmetrical dice are thrown. The probability of	159.	In a throw with a pair of symmetrical dice the prob- ability of obtaining a doublet is
	getting a sum of 6 points is		1. $\frac{1}{6}$ 2. $\frac{2}{3}$ 3. $\frac{1}{4}$ 4. $\frac{1}{2}$
1/18	1. $\frac{1}{36}$ 2. $\frac{3}{36}$ 3. $\frac{3}{36}$ 4. $\frac{1}{36}$	160.	When two symmetrical dice are rolled simultane- ously, the probability that both the dice show even
140.	getting a sum of 7 points is		numbers is
	1. $\frac{4}{36}$ 2. $\frac{5}{36}$ 3. $\frac{6}{36}$ 4. $\frac{1}{36}$	161	1. $\frac{-}{2}$ 2. $\frac{-}{3}$ 3. $\frac{-}{4}$ 4. $\frac{-}{8}$
149.	Two symmetrical dice are thrown. The probability of getting a sum of 8 points is		ously, the probability that both the dice show odd numbers is
150	1. $\frac{4}{36}$ 2. $\frac{5}{36}$ 3. $\frac{6}{36}$ 4. $\frac{1}{36}$		1. $\frac{1}{2}$ 2. $\frac{1}{3}$ 3. $\frac{1}{4}$ 4. $\frac{1}{8}$
150.	Two uniform dice marked 1 to 6 are thrown together. The probability that the total score on them is either minimum or maximum.	162.	A fair die is tossed twice. The probability of getting a 4, 5 or 6 on the 1st toss and a 1, 2, 3 or 4 on the 2nd toss is
	1. $\frac{4}{36}$ 2. $\frac{5}{36}$ 3. $\frac{2}{36}$ 4. $\frac{1}{36}$		$1\frac{1}{2}$ $2\frac{1}{2}$ $3\frac{1}{2}$ $4\frac{1}{2}$
151.	Two uniform dice marked 1 to 6 are thrown together. The probability that the score on the two dice is at least seven is	163.	Two dice are thrown. The probability that the absolute difference of points on them is 4 is
	1. $\frac{5}{12}$ 2. $\frac{7}{12}$ 3. $\frac{3}{4}$ 4. $\frac{1}{2}$	164.	1. $\frac{1}{7}$ 2. $\frac{1}{8}$ 3. $\frac{1}{9}$ 4. $\frac{1}{6}$
152.	The probability that the score on the two dice is at the most 7 is		The probability of getting at least an ace when two dice are rolled is
	1. $\frac{5}{12}$ 2. $\frac{7}{12}$ 3. $\frac{3}{4}$ 4. $\frac{1}{2}$		1. $\frac{11}{36}$ 2. $\frac{25}{36}$ 3. $\frac{1}{6}$ 4. $\frac{1}{8}$
153.	Two uniform dice marked 1 to 6 are thrown together. The probability that the score on the two dice is ei- ther 7 or 11 is	165.	If two symmetrical dice are thrown, the probability that at least one of the dice shows a number greater than 3 is

1.
$$\frac{1}{2}$$
 $2$ . $\frac{1}{4}$  $3$ . $\frac{3}{4}$  $4$ . $\frac{1}{8}$ 166.Two dice are thrown. The probability of sooring a  
sum greater than 9 or a doublet lity of sooring a  
sum greater than 9 or a doublet lity of sooring a  
sum greater than 9 or a doublet lity of sooring a  
sum greater than 9 or a doublet lity of sooring a  
two successive throws with an ordinary of the soning different points on them is  
1.167.The chance of throwing an ace in the 1st only of the  
two successive throws with an ordinary of the soning different points on them is  
of a soning a multiple of 2 on 1st throw and a multiple  
of 3 on the 2nd throw is  
1. $\frac{1}{3}$  $\frac{3}{5}$  $\frac{4}{3}$  $3$ . $\frac{5}{6}$  $4$ . $\frac{1}{18}$ 169.A and B alternately throw usits 1st will be the  
ever gate as sum of 7 points first will be the  
ordered at swinner. If A starts the game, the probability of his winning is $1$ . $\frac{1}{12}$  $2$ . $\frac{1}{3}$  $3$ . $\frac{1}{4}$  $\frac{1}{18}$ 170.A and B alternately throw a pair of symmetrical dice.  
Who ever throws a sum of 9 points first will be the  
clared a swinner. If A starts the game, the probability  
of obtaining a sum of 16 points is $1$ . $\frac{1}{12}$  $2$ . $\frac{1}{3}$  $3$ . $\frac{1}{14}$  $\frac{1}{16}$ 171.A and B alternately throw a pair of symmetrical dice.  
who ever throws 8. $3$ . $\frac{3}{14}$  $\frac{4}{5}$ 172.A pair of dice is rolled together thil a sum of eithers  
of soltaning a sum of 16 points is $1$ . $\frac{1}{12}$  $2$ . $\frac{1}{3}$  $\frac{1}{216}$  $\frac{1}{216}$ 173.A pair of dice is rolled together thil a sum of eithers<

189. A symmetrical die is thrown 4 times. The probability  
that 3 and 6 will turn up exactly 2 times each is1.
$$\frac{1}{6'}$$
 $2$ . $\frac{1}{6}$  $\frac{1}{6}$ 100. A cubical die is thrown 6 times. The probability that  
2 and 4 will turn up exactly 2 times each is $1$ . $\frac{25}{16}$  $2$ . $\frac{1}{8}$  $3$ . $\frac{7}{72}$  $4$ . $\frac{5}{72}$ 101. A cubical die is thrown 6 times. The probability of abulants a sum of 12 points is. $1$ . $\frac{25}{216}$  $2$ . $\frac{1}{8}$  $3$ . $\frac{7}{72}$  $4$ . $\frac{5}{72}$ 102. Two dice are thrown and the sum of points on tame  
is function to be 6. The probability of getting a lace  
with 2 points on any of the dica is $1$ . $\frac{1}{8}$  $2$ . $\frac{5}{22}$  $3$ . $\frac{7}{72}$  $4$ . $\frac{25}{216}$ 103. Two dice are thrown (the cubic time of points on them is even or less than 5 points  
in a is points on them is even or less than 5 points  
in the sum of points on them is 7, the chance that one of  
thrown y a sum of 12 points and 3 second  
throw a sum of 12 points in 5. $1$ . $\frac{3}{16}$  $2$ . $\frac{4}{6}$  $3$ . $\frac{4}{6}$ 103. Two clice are thrown with 2 points in  
throw a sum of 12 points in 5. $1$ . $\frac{3}{16}$  $\frac{3}{16}$  $\frac{4}{16}$ 104. Two symmetrical dice are thrown The probability of  
throwing a double such that their sum is less than 9  
is $1$ . $\frac{3}{16}$  $\frac{4}{16}$ 105. The probability of points in 5. $1$ . $\frac{1}{16}$  $2$ . $\frac{1}{16}$  $\frac{1}{16}$ 11. $\frac{1}{4}$  $2$ . $\frac{1}{3}$  $\frac{3}{4}$  $\frac{1}{2}$ 12. $\frac{1}{16}$ 

well shuffled playing cards. The probability that the cards drawn are aces is

1. 
$$\frac{5}{221}$$
 2.  $\frac{3}{221}$  3.  $\frac{1}{221}$  4.  $\frac{4}{22}$ 

214. When a card is drawn at random from a well shuffled pack of 52 playing cards, the probability that it may be either king or queen is

1. 
$$\frac{8}{13}$$
 2.  $\frac{5}{13}$  3.  $\frac{2}{13}$  4.  $\frac{1}{13}$ 

215. A card is drawn at random from a well shuffled pack of 52 playing cards. The probability that the card is either a face card or a six is

1. 
$$\frac{4}{13}$$
 2.  $\frac{3}{13}$  3.  $\frac{2}{13}$  4.  $\frac{6}{13}$ 

216. From a well shuffled pack of 52 playing cards two cards are drawn at random, one after an other without replacement. The probability that 1st one is a king and second one is gueen is

1. 
$$\frac{5}{663}$$
 2.  $\frac{4}{663}$  3.  $\frac{1}{221}$  4.  $\frac{3}{22}$ 

217. The chance of drawing a king, a queen and a knave in that order from a pack of cards in three consecutive draws, when the cards are not being replaced is

1. 
$$\frac{4}{52} \times \frac{4}{51} \times \frac{4}{50}$$
4.  $\frac{4}{52} \times \frac{3}{51} \times \frac{2}{50}$ 3.  $\frac{4}{52} \times \frac{4}{52} \times \frac{4}{52}$ 4.  $\frac{4}{52} \times \frac{3}{52} \times \frac{2}{52}$ 

218. From a well shuffled pack of 52 playing cards 4 cards are drawn, one at a time without replacement at random. The probability that they are aces is

1. 
$$\frac{4}{13^3}$$
  
3.  $\frac{4}{52} \times \frac{3}{51} \times \frac{2}{50} \times \frac{1}{49}$   
4.  $\frac{12}{13^3}$ 

219. A card is drawn from a well shuffled pack of 52 playing cards. It is replaced in the pack after noting its colour. Again a card is drawn at random. The probability that the 1st card drawn may be a heart and the second card drawn may not be a queen is

1. 
$$\frac{5}{13}$$
 2.  $\frac{4}{13}$  3.  $\frac{3}{13}$  4.  $\frac{2}{13}$ 

220. A card is drawn from a well shuffled pack of 52 playing cards. It is replaced in the pack after noting its colour. Again a card is drawn at random. The probability that both the cards drawn may be hearts is

1. 
$$\frac{1}{14}$$
 2.  $\frac{1}{15}$  3.  $\frac{1}{16}$  4.  $\frac{1}{12}$ 

221. A card is drawn from a well shuffled pack of 52 playing cards. It is replaced in the pack after noting its colour. Again a card is drawn at random. The probability that both cards drawn are red is

1. 
$$\frac{1}{16}$$
 2.  $\frac{1}{8}$  3.  $\frac{1}{4}$  4.  $\frac{1}{2}$   
222. A pack of cards is distributed among four hands equally. The probability that 5 spades, 3 clubs, 3 hearts and the rest diamonds may be in a particular hand is

**1** 

1. 
$$\frac{{}^{4}c_{1} \times {}^{13}c_{5} \times {}^{13}c_{3} \times {}^{13}c_{2}}{{}^{52}c_{13}}$$
2. 
$$\frac{{}^{13}c_{5} \times {}^{26}c_{6} \times {}^{13}c_{2}}{{}^{52}c_{13}}$$
3. 
$$\frac{{}^{13}c_{5} \times {}^{13}c_{3} \times {}^{13}c_{3} \times {}^{13}c_{2}}{{}^{52}c_{13}}$$
4. 
$$\frac{{}^{4}c_{1} \times {}^{13}c_{3} \times {}^{13}c_{3} \times {}^{13}c_{2}}{{}^{52}c_{13}}$$

223. If two cards are drawn from a well shuffled pack of 52 playing cards, the probability that there will be at least one club card is

1. 
$$\frac{{}^{39}c_2}{{}^{52}c_2}$$
  
2.  $1 - \frac{{}^{39}c_2}{{}^{52}c_2}$   
3.  $\frac{39}{52} \times \frac{39}{52} = \frac{9}{16}$   
4.  $\frac{{}^{30}c_2}{{}^{52}c_2}$ 

224. The probability of drawing a card which is a spade or a king from a well shuffled pack of playing cards is

$$\frac{2}{13}$$
 2.  $\frac{3}{13}$  3.  $\frac{4}{13}$  4.  $\frac{5}{13}$ 

225. A card is drawn from an ordinary pack of 52 playing cards and a gambler bets it as a spade or an ace. The probability that he wins the bet is

1. 
$$\frac{2}{13}$$
 2.  $\frac{3}{13}$  3.  $\frac{4}{13}$  4.  $\frac{1}{13}$ 

226. From a well shuffled pack of 52 playing cards two cards are drawn at random. The probability that either both are red or both are kings is

1. 
$$\frac{\binom{2^{6}c_{2}+4^{4}c_{2}}{5^{2}c_{2}}}{3. \frac{3^{0}c_{2}}{5^{2}c_{2}}}$$
  
2.  $\frac{\binom{2^{6}c_{2}+4^{4}c_{2}-2^{2}c_{2}}{5^{2}c_{2}}}{4. \frac{3^{9}c_{2}}{5^{2}c_{2}}}$ 

In shuffling a pack of cards, four cards are acciden-227. tally dropped. The probability that the cards dropped are one from each suit is

1. 
$$\frac{{}^{13}c_4}{{}^{52}c_4}$$
 2.  $\frac{13^4}{{}^{52}c_4}$  3.  $\frac{{}^{13}c_4}{13^4}$  4.  $\frac{13!}{{}^{52}c_4}$ 

Four persons draw a card each from a well shuffled 228. pack of 52 cards without replacement at random. The probability that they are a card from each suit is

1. 
$$\frac{13 \times 12 \times 11 \times 10}{52^4}$$
 2.  $\frac{13^4}{5^2 c_4}$   
3.  $\frac{^{13}c_4}{^{52}c_6}$  4.  $\frac{^{13}c_4}{12^4}$ 

229. Four cards are drawn at random from a well shuffled pack of 52 playing cards. The probability that all the 4 are hearts, but one is a queen is

1. 
$$\frac{{}^{4}c_{1} \times {}^{12}c_{3}}{{}^{52}c_{4}}$$
 2.  $\frac{{}^{12}c_{3}}{{}^{52}c_{4}}$  3.  $\frac{{}^{12}c_{4}}{{}^{52}c_{4}}$  4.  $\frac{{}^{13^{4}}}{{}^{52}c_{4}}$ 

230. From a well shuffled pack of 52 playing cards, four are drawn at random. The probability that all are spades, but one is a king is

$$\overset{39}{_{52}}C_4 \qquad 2. \ \overset{^{12}}{_{52}}C_4 \qquad 3. \ 1 - \frac{^{39}C_4}{_{52}}C_4 \qquad 4. \ \overset{^{12}C_4}{_{52}}C_4$$

231. If a card is drawn at random from a well shuffled pack of 52 playing cards, the probability that it is a court card is (Jack, Queen & King are court cards)

1.

1. 
$$\frac{5}{13}$$
 2.  $\frac{3}{13}$  3.  $\frac{1}{13}$  4.  $\frac{7}{13}$ 

232. Two cards are drawn from a well shuffled pack of 52 playing cards. The probability that they belong to different colours is

1. 
$$\frac{2 \times {}^{13}c_2}{{}^{52}c_2}$$
  
2.  $\frac{{}^{4}c_2 \times 13 \times 13}{{}^{52}c_2}$   
3.  $\frac{{}^{26}c_1 \times {}^{26}c_1}{{}^{52}c_2}$   
4.  $\frac{{}^{13}c_2}{{}^{52}c_2}$ 

233. Five cards are drawn at random from a well shuffled pack of 52 cards. The probability that out of these 5 there will be just one ace is

1. 
$$\frac{{}^{48}c_5}{{}^{52}c_5}$$
 2.  $\frac{{}^{4}c_1}{{}^{52}c_5}$  3.  $\frac{{}^{4}c_1 \times {}^{48}c_4}{{}^{52}c_5}$  4.  $\frac{{}^{48}c_4}{{}^{52}c_5}$ 

234. A pack of cards is distributed to four players as in the game of bridge. The probability that a particular player will not get an ace in three consecutive games is

1. 
$$\frac{3 \times {}^{48}c_{13}}{{}^{52}c_{13}}$$
 2.  $\left(\frac{{}^{48}c_{13}}{{}^{52}c_{13}}\right)^3$  3.  $\frac{{}^{48}c_{13}}{{}^{52}c_{13}}$  4.  $\left(\frac{3 \times {}^{48}c_{13}}{{}^{52}c_{13}}\right)^3$ 

- 235. Three cards are drawn successively with replacement. The probability of obtaining 2 aces and 1 king is
  - 1.  $\frac{1}{13^3}$  2.  $\frac{2}{13^3}$  3

3. 
$$\frac{3}{13^3}$$
 3.

 $13^{3}$ 

13

13

A card is drawn at random from a well shuffled pack 236. of 52 playing cards. The card is replaced after noting its colour. If this experiment is repeated six times, then the probability that the cards drawn consists of 2 hearts, 2 diamonds and 2 black cards is

1. 
$$\frac{1}{4^5}$$
 2.  $\frac{90}{4^5}$  3.  $\frac{72}{4^5}$  4.  $\frac{36}{4^5}$ 

237. In selecting 2 cards one at a time with replacement from a deck, the probability that the second is a face card, given that the 1st card was a red card is

1. 
$$\frac{2}{13}$$
 2.  $\frac{3}{13}$  3.  $\frac{4}{13}$  4

 In selecting 2 cards one at a time with replacement from a deck, the probability that the second card is an ace, given that the 1st card was a face card is

$$\frac{1}{13}$$
 2.  $\frac{2}{13}$  3.  $\frac{3}{13}$  4.

239. In selecting 2 cards one at a time with replacement from a deck, the probability that the second card is a black card, given that the 1st card was a red card is

1. 
$$\frac{1}{13}$$
 2.  $\frac{1}{2}$  3.  $\frac{1}{39}$ 

240. The face cards are removed from a well shuffled pack of 52 cards. Out of the remaining cards 4 are drawn at random. The probability that they belong to different suits is

1. 
$$\frac{13^4}{{}^{52}c_4}$$
 2.  $\frac{{}^{13}c_4}{{}^{40}c_4}$  3.  $\frac{10^4}{{}^{40}c_4}$  4.  $\frac{13^4}{{}^{40}c_4}$ 

The face cards are removed from a well shuffled pack 241. of 52 cards. Out of the remaining cards 4 are drawn at random. The probability that they belong to differ-

#### ent suits and different denominations is

1.

1

$$\frac{13^4}{{}^{52}c_4} \qquad 2. \ \frac{{}^{13}c_4}{{}^{40}c_4} \qquad 3. \ \frac{{}^{10}p_4}{{}^{40}c_4} \qquad 4. \ \frac{13}{{}^{40}c_4}$$

242. A and B alternately cut a card each from a pack of cards with replacement and pack is shuffled after each cut. If A starts the game and the game is continued till one cuts a spade, the respective probabilities of A and B cutting a spade are

1. 
$$\frac{1}{3}, \frac{2}{3}$$
 2.  $\frac{3}{4}, \frac{1}{4}$  3.  $\frac{4}{7}, \frac{3}{7}$  4.  $\frac{3}{7}, \frac{4}{7}, \frac{3}{7}$ 

243. A and B alternately cut a card each from a well shuffled pack of 52 cards with replacement and the pack is shuffled after each cut. If A starts the game and the game is continued till one cuts a spade or club, the respective probabilities of A and B cutting a spade or club card is

1. 
$$\frac{1}{3}, \frac{2}{3}$$
 2.  $\frac{2}{3}, \frac{1}{3}$  3.  $\frac{4}{7}, \frac{3}{7}$  4.  $\frac{3}{7}, \frac{4}{7}$ 

244. The probability of drawing an honour card from a well shuffled pack of 52 playing cards is (K,Q,J,A are honour cards)

$$\frac{2}{13}$$
 2.  $\frac{3}{13}$  3.  $\frac{4}{13}$  4.  $\frac{5}{13}$ 

245. Two cards are drawn simultaneously from a well shuffled pack of 52 playing cards. The probability that one of them is an ace of hearts is

1. 
$$\frac{1}{13}$$
 2.  $\frac{1}{26}$  3.  $\frac{1}{39}$  4.  $\frac{1}{52}$ 

246. A card is drawn from a well shuffled pack of 52 cards numbered 2 to 53. The probability that the number on the card is a prime less than 10 is

1. 
$$\frac{4}{13}$$
 2.  $\frac{3}{13}$  3.  $\frac{2}{13}$  4.  $\frac{1}{13}$ 

247. A card is drawn from a well shuffled pack of 52 cards numbered 2 to 53. The probability that the number on the card is a prime less than 20 is

1. 
$$\frac{4}{13}$$
 2.  $\frac{3}{13}$  3.  $\frac{2}{13}$  4.  $\frac{1}{13}$ 

248. A card is drawn from a well shuffled pack of 52 cards numbered 2 to 53. The probability that the number on the card is a prime less than 30 is

2. 
$$\frac{3}{26}$$
 3.  $\frac{5}{26}$ 

1.  $\frac{1}{26}$ 

- In a game of bridge, the probability of a particular 249. player having all the 13 cards of red colour is

1. 
$$\frac{13^4}{{}^{52}c_{13}}$$
 2.  $\frac{{}^{26}c_{13}}{{}^{52}c_{13}}$  3.  $\frac{13 \times 4}{{}^{52}c_{13}}$  4.  $\frac{13^2}{{}^{52}c_{13}}$ 

250. In a bridge game, the probability that a specified player has at least one ace is

1. 
$$\frac{{}^{48}c_{13}}{{}^{52}c_{13}}$$
 2.  $\frac{{}^{4}c_{1}}{{}^{52}c_{13}}$  3.  $1 - \frac{{}^{48}c_{13}}{{}^{52}c_{13}}$  4.  $1 - \frac{{}^{4}c_{1}}{{}^{52}c_{13}}$ 

251. Two cards are drawn from a well shuffled pack of 52 playing cards. The probability that one is a heart card and the other is not a heart card is

1. 
$$\frac{7}{34}$$
 2.  $\frac{9}{34}$  3.  $\frac{13}{34}$  4.  $\frac{15}{34}$   
From a well shuffled pack of 52 cards. 2 cards at

SR. MATHEMATICS

252.

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4.  $\frac{'}{26}$ 

drawn, one at a time with replacement at random. The probability that both the cards are not queens is

1. 
$$\frac{1}{16}$$
 2.  $\frac{1}{69}$  3.  $\frac{144}{169}$  4.  $\frac{1}{8}$ 

253. A card is drawn at random from a well shuffled pack of 52 cards. Again a card is drawn at random from the remaining cards. The probability that one is a king and the other is a queen is

$$\frac{4}{663}$$
 2.  $\frac{8}{663}$  3.  $\frac{1}{221}$  4.  $\frac{2}{663}$ 

254. A box contains 40 balls of the same shape and weight. Among the balls 10 are white, 16 are red and the rest are black, the probability that a ball drawn from the box is not a black is

1. 
$$\frac{1}{4}$$
 2.  $\frac{2}{5}$  3.  $\frac{13}{20}$  4.  $\frac{1}{20}$ 

255. A box contains 40 balls of the same shape and weight. Among the balls 10 are white, 16 are red and the rest are black, if two balls are drawn, the probability that one is red and one is black is

1. 
$$\frac{3}{4}$$
 2.  $\frac{56}{195}$  3. 1 4.  $\frac{1}{4}$ 

- 256. The probability that a teacher will give a surprise test during any class meeting is 3/5. If a student is absent on two days, then the probability that he will miss at least one test is
- 1.9/25 2.4/25 3.21/25 4.13/25 257. There are 4 red, 3 black and 5 white balls in a bag. If a ball is drawn at random, the probability that it may be either red or black ball is

1. 
$$\frac{1}{4}$$
 2.  $\frac{5}{12}$  3.  $\frac{7}{12}$  4.  $\frac{9}{12}$ 

258. There are 4 red, 3 black and 5 white balls in a bag. The probability of drawing 3 balls of different colour is

1. 
$$\frac{5}{11}$$
 2.  $\frac{3}{11}$  3.  $\frac{1}{11}$  4.  $\frac{7}{11}$ 

There are 4 red, 3 black and 5 white balls in a bag. 259. The probability of drawing 2 balls of the same colour and one is of different colour is

1. 
$$\frac{5}{44}$$
 2.  $\frac{15}{44}$  3.  $\frac{29}{44}$  4.  $\frac{131}{195}$ 

- 260. A bag contains 3 red, 4 white and 7 black balls. Two balls are drawn at random. The probability that they are of different colours is
  - 1.  $\frac{30}{91}$ 2.  $\frac{61}{91}$  3.  $\frac{31}{91}$  4.  $\frac{60}{91}$
- There are 5 green, 6 black and 7 white balls in a 261. bag. A ball is drawn at random from the bag. The probability that it may be either green or black is

1. 
$$\frac{5}{18}$$
 2.  $\frac{6}{18}$  3.  $\frac{11}{18}$  4.  $\frac{13}{18}$ 

262. A bag contains 2 white, 3 black and 4 green balls. One ballis drawn at random from the bag. The second ball is drawn at random from the remaining balls. The probability that 1st one is white and the 2nd is black is

1. 
$$\frac{2}{7}$$
 2.  $\frac{3}{7}$  3.  $\frac{1}{12}$  4.  $\frac{4}{7}$ 

263. A bag contains 3 white, 2 black and 4 red balls. The probability of drawing a white, a black and a red ball in succession in that order without replacement is

1. 
$$\frac{8}{243}$$
 2.  $\frac{1}{21}$  3.  $\frac{5}{21}$  4.  $\frac{3}{21}$ 

264. There are 6 red and 5 black balls in a bag. A ball is drawn from the bag at random and without replacing it another ball is drawn at random. The probability that both the balls drawn may be black is

1. 
$$\frac{2}{11}$$
 2.  $\frac{3}{11}$  3.  $\frac{6}{11}$  4.  $\frac{5}{11}$ 

265. There are 6 red and 5 black balls in a bag. A ball is drawn from the bag at random and without replacing it an other ball is drawn at random. The probability that both the balls drawn may be red is

1. 
$$\frac{2}{11}$$
 2.  $\frac{3}{11}$  3.  $\frac{6}{11}$  4.  $\frac{5}{11}$ 

266. There are 6 red and 5 black balls in a bag. A ball is drawn from the bag at random and without replacing it an other ball is drawn at random. The probability that one is red and one is black is

1. 
$$\frac{2}{11}$$
 2.  $\frac{3}{11}$  3.  $\frac{6}{11}$  4.  $\frac{5}{11}$ 

267. There are 6 red and 5 black balls in a bag. A ball is drawn from the bag at random and without replacing it an other ball is drawn at random. The probability that 1st one is red and the second is black is

$$\frac{2}{11}$$
 2.  $\frac{3}{11}$  3.  $\frac{6}{11}$  4.  $\frac{5}{11}$ 

268. A bag contains 2 white, 3 black and 4 green balls. Two balls are drawn one after another with replacement. The probability that 1st one is white and second one is black is

1. 
$$\frac{5}{27}$$
 2.  $\frac{1}{9}$  3.  $\frac{2}{27}$  4.  $\frac{4}{27}$ 

269. A bag contains 2 white, 3 black and 4 green balls. Two balls are drawn one after another with replacement. The probability that one is white and one is black is

1. 
$$\frac{5}{27}$$
 2.  $\frac{1}{9}$  3.  $\frac{2}{27}$  4.  $\frac{4}{27}$ 

270. A bag contains 3 white, 2 black and 4 red balls. Three balls are drawn one after another with replacement at random. The probability of drawing a white, a black and a red ball in succession in that order is

$$\frac{1}{1}$$
 2.  $\frac{5}{21}$ 

1.

1.  $\frac{1}{2}$ 3.  $\frac{1}{243}$ 4. 243 271. There are 6 red and 5 black balls in a bag. Two balls are drawn at random one after another with replacement. The probability that both the balls drawn may be red is

1. 
$$\frac{30}{121}$$
 2.  $\frac{25}{121}$  3.  $\frac{18}{121}$  4.  $\frac{36}{121}$   
272. There are 6 red and 5 black balls in a bag. Two balls

are drawn at random one after another with replacement. The probability that both the balls drawn may be black is

- 1.  $\frac{30}{121}$  2.  $\frac{25}{121}$  3.  $\frac{36}{121}$  4.  $\frac{36}{221}$ 273. There are 6 red and 5 black balls in a bag. Two balls are drawn at random one after another with replacement. The probability that 1st one is red and the second one is black is
  - 1.  $\frac{30}{121}$  2.  $\frac{60}{121}$  3.  $\frac{36}{221}$  4.  $\frac{36}{121}$
- 274. There are 6 red and 5 black balls in a bag. Two balls are drawn at random one after another with replacement. The probability that one is red and one is black is
  - 1.  $\frac{30}{121}$  2.  $\frac{60}{121}$  3.  $\frac{36}{121}$  4.  $\frac{36}{221}$
- 275. The probability of drawing 4 white and 2 black balls in two drawings in succession from a bag containing 1 red, 4 black and 6 white balls, if the drawing is without replacement is

1. 
$$\frac{{}^{6}c_{4}}{{}^{11}c_{4}} \times \frac{{}^{4}c_{2}}{{}^{11}c_{2}}$$
  
2.  $\frac{{}^{6}c_{4}}{{}^{11}c_{4}} \times \frac{{}^{4}c_{2}}{{}^{7}c_{2}}$   
3.  $\frac{{}^{10}c_{6}}{{}^{11}c_{6}}$   
4.  $\frac{{}^{10}c_{2}}{{}^{11}c_{2}}$ 

276. The probability of drawing 4 white and 2 black balls in two drawings in succession from a bag containing 1 red, 4 black and 6 white balls, if the drawing is with replacement is

1. 
$$\frac{{}^{6}c_{4}}{{}^{11}c_{4}} \times \frac{{}^{4}c_{2}}{{}^{11}c_{2}}$$
  
2.  $\frac{{}^{6}c_{4}}{{}^{11}c_{4}} \times \frac{{}^{4}c_{2}}{{}^{7}c_{2}}$   
3.  $\frac{{}^{10}c_{6}}{{}^{11}c_{6}}$   
4.  $\frac{{}^{10}c_{2}}{{}^{11}c_{2}}$ 

277. A bag contains 10 white and 8 black balls. Two successive drawings of 2 balls are made. The probability that the 1st draw will give 2 white and the 2nd draw will give 2 black if the drawing is without replacement is

1. 
$$\frac{{}^{10}c_2 + {}^8c_2}{{}^{18}c_2}$$
  
2.  $\frac{{}^{10}c_2}{{}^{18}c_2} \times \frac{{}^8c_2}{{}^{16}c_2}$   
3.  $\frac{{}^{10}c_2}{{}^{18}c_2} \times \frac{{}^8c_2}{{}^{18}c_2}$   
4.  $\frac{{}^{12}c_2}{{}^{18}c_2} \times \frac{{}^6c_2}{{}^{18}c_2}$ 

278. A bag contains 10 white and 8 black balls. Two successive drawings of 2 balls are made. The probability that the 1st draw will give 2 white and the 2nd draw will give 2 black if the drawing is with replacement is



279. A bag contains 8 red and 5 white balls. Two successive drawings of 3 balls are made. The probability that the 1st draw will give 3 white and the 2nd draw will give 3 red balls is if the drawing is with replacement is

1. 
$$\frac{{}^{5}C_{3}}{{}^{13}C_{3}} \times \frac{{}^{8}C_{3}}{{}^{10}C_{3}}$$
  
2.  $\frac{{}^{5}C_{3}}{{}^{13}C_{3}} \times \frac{{}^{8}C_{3}}{{}^{13}C_{3}}$   
3.  $\frac{{}^{5}C_{3} + {}^{8}C_{3}}{{}^{13}C_{3}}$   
4.  $\frac{{}^{5}C_{3} \times {}^{8}C_{3}}{{}^{13}C_{3}}$ 

280. A bag contains 8 red and 5 white balls. Two successive drawings of 3 balls are made. The probability that the 1st draw will give 3 white and the 2nd draw will give 3 red balls is if the drawing is without replacement is

1. 
$$\frac{{}^{8}c_{3}}{{}^{13}c_{3}} \times \frac{{}^{5}c_{3}}{{}^{10}c_{3}}$$
  
2.  $\frac{{}^{5}c_{3}}{{}^{13}c_{3}} \times \frac{{}^{8}c_{3}}{{}^{13}c_{3}}$   
3.  $\frac{{}^{5}c_{3} + {}^{8}c_{3}}{{}^{13}c_{3}}$   
4.  $\frac{{}^{5}c_{3} \times {}^{8}c_{3}}{{}^{13}c_{3}}$ 

281. Out of 10 balls in a bag 3 are red. The probability that there will be at least one red ball in a draw of 2 balls is

1. 
$$\frac{7}{15}$$
 2.  $\frac{8}{15}$  3.  $\frac{6}{15}$  4.  $\frac{9}{15}$ 

282. A bag contains 4 white and 2 black balls. Another contains 3 white and 5 black balls. If one ball is drawn from each, the probability that both are white is

$$\frac{13}{24}$$
 2.  $\frac{5}{24}$  3.  $\frac{1}{4}$  4.  $\frac{2}{14}$ 

- 283. A bag contains 4 white and 2 black balls. Another contains 3 white and 5 black balls. If one ball is drawn from each, the probability that both are black is
  - 1.  $\frac{13}{24}$  2.  $\frac{5}{24}$  3.  $\frac{1}{14}$  4.  $\frac{2}{14}$
- 284. A bag contains 4 white and 2 black balls. Another contains 3 white and 5 black balls. If one ball is drawn from each, the probability that one is white and one is black is

1. 
$$\frac{13}{24}$$
 2.  $\frac{5}{24}$  3.  $\frac{1}{14}$  4.  $\frac{2}{14}$ 

1.

1.

285. A bag contains 5 white and 3 black balls, 4 balls are successively drawn out and not replaced. The chance that they are alternately of different colours is

1. 
$$\frac{1}{7}$$
 2.  $\frac{1}{14}$  3.  $\frac{1}{21}$  4.  $\frac{1}{28}$   
A bag contains 3 white, 3 black and 2 red balls. One

286. A bag contains 3 white, 3 black and 2 red balls. One by one 3 balls are drawn without replacing them. For only the 3rd ball to be red the probability is

$$\frac{1}{28}$$
 2.  $\frac{3}{28}$  3.  $\frac{5}{28}$  4.  $\frac{7}{28}$ 

287. The probability of drawing two red balls in succession from a bag containing 4 red and 5 black balls, when the ball that is drawn 1st is not replaced is

1.1.1.2.4.3.1.286.From a bag containing 4 white and 6 black balls 3  
are drawn at random time bag, the probability  
that balls are drawn at random time bag, the probability  
that balls are drawn at random time bag, the probability  
that balls are drawn at random time bag, the probability  
that balls are drawn at random time bag. A 142 to 5  
to 2002.280.1.1.
$$\frac{e_c}{e_c}$$
  
 $z_c$  $\frac{e_c}{e_c}$   
 $z_c$  $\frac{e_c}{e_c}$   
 $z_c$  $\frac{e_c}{e_c}$   
 $z_c$  $\frac{e_c}{e_c}$ 2. $\frac{e_c}{e_c}$  $\frac{e_c}{e_c}$ 2. $\frac{e_c}{e_c}$  $\frac{e_c}{e_c}$ 2. $\frac{e_c}{e_c}$ 2.2.2. $\frac{e_c}{e_c}$ 2. $\frac{e_c}{e_c}$ 2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.

$$\frac{5}{21}$$
 2.  $\frac{6}{21}$  3.  $\frac{10}{21}$ 

1.

307. Five men in a company of 20 are graduates. If 3 men are picked out at random. The probability that at least one is a graduate is

1. 
$$\frac{{}^{15}c_3}{{}^{20}c_3}$$
 2.  $\frac{{}^{5}c_3}{{}^{20}c_3}$  3.  $1 - \frac{{}^{15}c_3}{{}^{20}c_3}$  4.  $1 - \frac{{}^{5}c_3}{{}^{20}c_3}$ 

308. From 7 gentlemen and 4 ladies, a committee of 5 is to be formed. The probability that this can be done so as to include at least one lady is

1. 
$$\frac{{}^{7}c_{5}}{{}^{11}c_{5}}$$
 2.  $\frac{{}^{4}c_{1}}{{}^{11}c_{5}}$  3.  $1 - \frac{{}^{7}c_{5}}{{}^{11}c_{5}}$  4.  $1 - \frac{{}^{4}c_{1}}{{}^{11}c_{5}}$ 

309. A cricket 11 is to be selected at random out of 15 players of whom 4 are bowlers. The probability that at least 3 bowlers will be there

1. 
$$\frac{\binom{4}{c_{3}} + \binom{4}{c_{4}}}{\frac{15}{c_{11}}}$$
  
2.  $\frac{\binom{4}{15} \frac{c_{4}}{c_{11}}}{\frac{15}{c_{11}}}$   
3.  $\frac{\binom{4}{c_{3}} \times \frac{11}{c_{8}} + \binom{4}{c_{4}} \times \frac{11}{c_{7}}}{\frac{15}{c_{11}}}$   
4.  $\frac{\frac{4}{15} \frac{c_{3}}{c_{11}}}{\frac{15}{c_{11}}}$ 

310. Six boys and six girls are to sit in a row at random. The probability that all the 6 girls sit together is

1. 
$$\frac{\angle 6 \angle 6}{\angle 12}$$
 2.  $\frac{\angle 6 \angle 7}{\angle 12}$  3.  $\frac{2\angle 6 \angle 6}{\angle 12}$  4.  $\frac{2\angle 6 \angle 7}{\angle 12}$ 

311. Six boys and six girls are to sit in a row at random. The probability that all the six girls and all the six boys sit together is

1. 
$$\frac{\angle 6 \angle 6}{\angle 12}$$
 2.  $\frac{\angle 6 \angle 7}{\angle 12}$  3.  $\frac{2\angle 6 \angle 6}{\angle 12}$  4.  $\frac{2\angle 6 \angle 7}{\angle 12}$ 

312. The probability that all the vowels of the word EAMCET come together, when the letters are arranged at random is

1.  $\frac{1}{5}$  2.  $\frac{1}{6}$  3.  $\frac{1}{7}$  4.  $\frac{1}{8}$ 

313. If the letters of the word MISSISSIPPI are arranged at random, the probability that all the 4 S's appear consecutively is

1. 
$$\frac{\angle 8}{\angle 11}$$
 2.  $\frac{\angle 4}{\angle 11}$  3.  $\frac{\angle 8 \angle 4}{\angle 11}$  4.  $\frac{\angle 6}{\angle 11}$ 

314. If n students are to be seated around a round table at random, the probability that two particular students will be together is

1. 
$$\frac{1}{n-1}$$
 2.  $\frac{2}{n-1}$  3.  $\frac{3}{n-1}$  4.  $\frac{4}{n-1}$ 

315. If 10 persons are to sit around a round table, the odds against two specified persons sitting together is

$$\frac{1}{9}$$
 2.  $\frac{2}{9}$  3. 7 to 2 4. 2 to 7

316. 4 boys and 7 girls are to sit in a row at random. The probability that no two boys will sit together is

1. 
$$\frac{\angle 7 \times \angle 4}{\angle 11}$$
 2.  $\frac{\angle 7 \times {}^8 p_4}{\angle 11}$ 

3. 
$$\frac{\angle 7 \times {}^{8}c_{4}}{\angle 11}$$
 4. 
$$\frac{\angle 7 \times \angle 8}{\angle 11}$$

317. If the letters of the word ASSASSIN are written in a row at random, the probability that no two S's come together is

1. 
$$\frac{1}{7}$$
 2.  $\frac{2}{7}$  3.  $\frac{1}{14}$  4.  $\frac{3}{14}$ 

318. 10 gentlemen and 6 ladies are to sit for a dinner at a round table. The probability that no two ladies sit together is

1. 
$$\frac{\angle 9 \times \angle 5}{\angle 15}$$
  
3.  $\frac{\angle 9 \times {}^{10}c_6}{\angle 15}$   
4.  $\frac{\angle 9 \times {}^{10}c_5}{\angle 15}$ 

319. Six boys and six girls are to sit in a row at random. The probability that boys and girls sit alternately is

1. 
$$\frac{\angle 6 \times p_{6}}{\angle 12}$$
2. 
$$\frac{\angle 6 \angle 6}{\angle 12}$$
3. 
$$\frac{2\angle 6 \angle 6}{\angle 12}$$
4. 
$$\frac{2\angle 6}{\angle 12}$$

320. Six boys and six girls are to sit around a round table. The probability that boys and girls sit alternately is

1. 
$$\frac{\angle 5 \angle 5}{\angle 11}$$
 2.  $\frac{\angle 5 \angle 6}{\angle 11}$  3.  $\frac{\angle 6 \angle 6}{\angle 12}$  4.  $\frac{\angle 5 \angle 6}{\angle 12}$ 

321. 100 tickets are numbered as 00, 01, 02 ..... 09, 10, 11, 12, ..... 99 out of them one ticket is drawn at random. The probability that the sum of the digits of the number on the ticket is 9 is

$$\frac{7}{100}$$
 2.  $\frac{9}{100}$  3.  $\frac{1}{10}$  4.  $\frac{1}{100}$ 

322. 100 tickets are numbered as 00, 01, 02, ..... 09, 10, 11, 12, ...... 99 out of them one ticket is drawn at random. The probability that the product of the digits of the number on the ticket is 0 is

1. 
$$\frac{1}{10}$$
 2.  $\frac{19}{100}$  3.  $\frac{1}{5}$  4.  $\frac{1}{15}$ 

323. n biscuits of different shape and size are to be distributed to N beggars at random. The probability that

a particular beggar receives r (r < n) biscuits is

$$\cdot \frac{{}^{n}c_{r}}{N^{n}} \qquad 2. \frac{{}^{n}c_{r} \times {}^{n-1}c_{n}}{{}^{n}c_{n}}$$

$$3. \ \frac{{}^{n}c_{r} \times (N-1)^{n-r}}{N^{n}} \qquad 4.$$

1.

1

324. 10 pens of different shape and size are to be distributed to 6 students at random. The probability that a particular student receives 4 pens is

1. 
$$\frac{{}^{10}c_4}{{}^{10}c_6}$$
 2.  $\frac{{}^{10}c_4}{10^6}$  3.  $\frac{{}^{10}c_4 \times 5^6}{6^{10}}$  4.  $\frac{{}^{10}c_4 \times 5^6}{3^{10}}$ 

325. If n letters are placed into n addressed envelopes at random, the probability that atleast one letter will go into wrongly addressed envelope is

1. 
$$\frac{1}{n}$$
 2.  $\frac{n-1}{n}$  3.  $1-\frac{1}{\Delta n}$  4.  $\frac{1}{\Delta n}$ 

326.From a set of 17 cards numbered 1 to 17, one cards is drawn at random. The probability that the number on the cards is drawn at random. The probability that the number is dold is both the cards are drawn tandom from 10 cards numbered 1 to 10. The probability that the sum is dold in both the cards are drawn tandom from 10 cards numbered 1 to 10. The probability that the sum is dold in both the cards are drawn tandom from 10 cards numbered 1 to 10. The probability that the sum is even in a set of 100 natural numbers is dolkies by 4 or 6 is 1.337.328. The chance that Doctor A with degonies discall the probability that he infravous of seven probe is 160%. The traven diagonalies discall the probability that he birthdys of 5 seven probability that he birthdys of 5 seven probability for the days, the probability that he birthdys of 5 seven probability for the days. It probability for the days, the probability that he birthdys of 5 seven probability for the days. It probability for the days, the probability that a group of n people (n ± 356) have all different days of the week is332. Assuming equal probability for the days, the probability that a group of n people (n ± 356) have all different birthdays is332. Assuming that a year consito 36 366 days, the probability that a group of n people (n ± 356) have all different birthdays is333. The probability that birt days of the week is333. The probability that a group of n people (n ± 356) have all different calendar months of a year is334. The chashing that a year consito 36 366 days, the probability that a group of n people (n ± 356) have all different calendar months of a year is335. The arc days of the week is1. 
$$\frac{1}{22}$$
 $\frac{2}{363}$  $\frac{n}{365}$  $\frac{n}{365}$ 335. The probability that the number of the stam p drawn is a prime numbers is $\frac{n}{365}$  $\frac{n}{12}$ 1.