# **Chapter 5. Factorisation**

## Ex 5.1

## **Answer 1A.**

$$4x^2v^3 - 6x^3v^2 - 12xv^2$$

Here, the common factor is  $2xy^2$ .

Dividing throughout by 2xy2, we get

$$\frac{4x^2y^3}{2xy^2} - \frac{6x^3y^2}{2xy^2} - \frac{12xy^2}{2xy^2}$$

$$= 2xy - 3x^2 - 6$$

$$4x^2y^3 - 6x^3y^2 - 12xy^2 = 2xy^2(2xy - 3x^2 - 6)$$

## **Answer 1B.**

$$5a(x^2 - y^2) + 35b(x^2 - y^2)$$

Here, the common factor is  $5(x^2 - y^2)$ .

Dividing throughout by  $5(x^2 - y^2)$ , we get

$$\frac{5a(x^2-y^2)}{5(x^2-y^2)} + \frac{35b(x^2-y^2)}{5(x^2-y^2)}$$

$$= a + 7b$$

$$5a(x^2 - y^2) + 35b(x^2 - y^2) = 5(x^2 - y^2)(a + 7b)$$

#### **Answer 1C.**

$$2x^5y + 8x^3y^2 - 12x^2y^3$$

Here, the common factor is  $2x^2y$ .

Dividing throughout by 2x²y, we get

$$\frac{2x^5y}{2x^2y} + \frac{8x^3y^2}{2x^2y} - \frac{12x^2y^3}{2x^2y}$$

$$= x^3 + 4xy - 6y^2$$

$$2x^{5}y + 8x^{3}y^{2} - 12x^{2}y^{3} = 2x^{2}y(x^{3} + 4xy - 6y^{2})$$

#### **Answer 1D.**

 $12a^{3} + 15a^{2}b - 21ab^{2}$ Here, the common factor is 3a. Dividing throughout by 3a, we get  $\frac{12a^{3}}{3a} + \frac{15a^{2}b}{3a} - \frac{21ab^{2}}{3a}$   $= 4a^{2} + 5ab - 7b^{2}$   $\therefore 12a^{3} + 15a^{2}b - 21ab^{2} = 3a(4a^{2} + 5ab - 7b^{2})$ 

# **Answer 1E.**

 $24m^4n^6 + 56m^6n^4 - 72m^2n^2$ Here, the common factor is  $8m^2n^2$ . Dividing throughout by 3a, we get  $\frac{24m^4n^6}{8m^2n^2} + \frac{56m^6n^4}{8m^2n^2} - \frac{72m^2n^2}{8m^2n^2}$   $= 3m^2n^4 + 7m^4n^2 - 9$   $\therefore 24m^4n^6 + 56m^6n^4 - 72m^2n^2 = 8m^2n^2(3m^2n^4 + 7m^4n^2 - 9)$ 

# **Answer 1F.**

 $(a-b)^2 - 2(a-b)$ Here, the common factor is (a-b). Dividing throughout by (a-b), we get  $\frac{(a-b)^2}{(a-b)} - \frac{2(a-b)}{(a-b)}$  = a-b-2  $\therefore (a-b)^2 - 2(a-b) = (a-b)(a-b-2)$ 

## **Answer 1G.**

 $2a(p^2 + q^2) + 4b(p^2 + q^2)$ Here, the common factor is  $2(p^2 + q^2)$ Dividing throughout by  $2(p^2 + q^2)$ , we get  $\frac{2a(p^2 + q^2)}{2(p^2 + q^2)} + \frac{4b(p^2 + q^2)}{2(p^2 + q^2)}$ = a + 2b $\therefore 2a(p^2 + q^2) + 4b(p^2 + q^2) = 2(p^2 + q^2)(a + 2b)$ 

#### **Answer 1H.**

$$81(p + q)^2 - 9p - 9q$$
  
=  $81(p + q)^2 - 9(p + q)$ 

Here, the common factor is 9(p+q)

Dividing throughout by 9(p+q), we get

$$\frac{81(p+q)^2}{9(p+q)} - \frac{9(p+q)}{9(p+q)}$$

$$= 9(p+q)-1$$

$$3.81(p+q)^2 - 9p - 9q = 9(p+q)[9(p+q) - 1]$$

## **Answer 1I.**

$$(mx + ny)^2 + (nx - my)^2$$

$$= m^2x^2 + n^2y^2 + 2mnxy + n^2x^2 + m^2y^2 - 2mnxy$$

$$= m^2x^2 + n^2y^2 + n^2x^2 + m^2y^2$$

$$= m^2 \times^2 + n^2 \times^2 + m^2 V^2 + n^2 V^2$$

$$= \times^2 (m^2 + n^2) + v^2 (m^2 + n^2)$$

Here, the common factor is  $(m^2 + n^2)$ .

Dividing throughout by  $(m^2 + n^2)$ , we get

$$\frac{x^2(m^2+n^2)}{(m^2+n^2)} + \frac{y^2(m^2+n^2)}{(m^2+n^2)}$$

$$= x^2 + y^2$$

$$(mx + ny)^2 + (nx - my)^2 = (m^2 + n^2)(x^2 + y^2)$$

## **Answer 1J.**

$$36(x+y)^3 - 54(x+y)^2$$

Here, the common factor is  $18(x + y)^2$ .

Dividing throughout by  $18(x + y)^2$ , we get

$$\frac{36(x+y)^3}{18(x+y)^2} - \frac{54(x+y)^2}{18(x+y)^2}$$

$$= 2(x + y) - 3$$

$$36(x+y)^3 - 54(x+y)^2 = 18(x+y)^2[2(x+y) - 3]$$

#### **Answer 1K.**

$$\begin{split} &p(p^2+q^2-r^2)+q(r^2-q^2-p^2)-r(p^2+q^2-r^2)\\ &=p(p^2+q^2-r^2)-q(-r^2+q^2+p^2)-r(p^2+q^2-r^2)\\ &=p(p^2+q^2-r^2)-q(p^2+q^2-r^2)-r(p^2+q^2-r^2)\\ &=p(p^2+q^2-r^2)-q(p^2+q^2-r^2)-r(p^2+q^2-r^2).\\ &\text{Here, the common factor is } (p^2+q^2-r^2), \text{ we get}\\ &\frac{p(p^2+q^2-r^2)}{(p^2+q^2-r^2)}-\frac{q(p^2+q^2-r^2)}{(p^2+q^2-r^2)}-\frac{r(p^2+q^2-r^2)}{(p^2+q^2-r^2)}\\ &=p-q-r\\ &\therefore p(p^2+q^2-r^2)+q(r^2-q^2-p^2)-r(p^2+q^2-r^2)=(p^2+q^2-r^2)(p-q-r) \end{split}$$

#### **Answer 2A.**

$$15xy - 9x - 25y + 15$$

$$= (15xy - 9x) - (25y + 15)$$

$$= 3x(5y - 3) - 5(5y - 3)$$

$$= (5y - 3)(3x - 5)$$

# Answer 2B.

$$15x^{2} + 7y - 3x - 35xy$$

$$= 15x^{2} - 3x - 35xy + 7y$$

$$= (15x^{2} - 3x) - (35xy - 7y)$$

$$= 3x(5x - 1) - 7y(5x - 1)$$

$$= (5x - 1)(3x - 7y)$$

#### **Answer 2C.**

$$9 + 3xy + x^{2}y + 3x$$

$$= 9 + 3xy + 3x + x^{2}y$$

$$= (9 + 3xy) + (3x + x^{2}y)$$

$$= 3(3 + xy) + y(3 + xy)$$

$$= (3 + xy)(3 + x)$$

#### Answer 2D.

$$8(2a + b)^{2} - 8a - 4b$$

$$= 8(2a + b)^{2} - (8a + 4b)$$

$$= 8(2a + b)^{2} - 4(2a + b)$$

$$= 4(2a + b)[2(2a + b) - 1]$$

$$= 4(2a + b)[4a + 2b - 1]$$

## **Answer 2E.**

$$x(x-4)-x+4$$
  
=  $x(x-4)-1(x-4)$   
=  $(x-4)(x-1)$ 

# Answer 2F.

$$2m^{3} - 5n^{2} - 5m^{2}n + 2mn$$

$$= 2m^{3} + 2mn - 5m^{2}n - 5n^{2}$$

$$= (2m^{3} + 2mn) - (5m^{2}n + 5n^{2})$$

$$= 2m(m^{2} + n) - 5n(m^{2} + n)$$

$$= (m^{2} + n)(2m - 5n)$$

## **Answer 2H.**

$$9x^{3} + 6x^{2}y^{2} - 4y^{3} - 6xy$$

$$= 9x^{3} + 6x^{2}y^{2} - 6xy - 4y^{3}$$

$$= (9x^{3} + 6x^{2}y^{2}) - (6xy + 4y^{3})$$

$$= 3x^{2}(3x + 2y^{2}) - 2y(3x + 2y^{2})$$

$$= (3x + 2y^{2})(3x^{2} - 2y)$$

## Answer 2I.

$$3ax^{2} - 5bx^{2} + 9az^{2} + 6ay^{2} - 10by^{2} - 15bz^{2}$$

$$= 3ax^{2} + 6ay^{2} + 9az^{2} - 5bx^{2} - 10by^{2} - 15bz^{2}$$

$$= (3ax^{2} + 6ay^{2} + 9az^{2}) - (5bx^{2} + 10by^{2} + 15bz^{2})$$

$$= 3a(x^{2} + 2y^{2} + 3z^{2}) - 5b(x^{2} + 2y^{2} + 3z^{2})$$

$$= (x^{2} + 2y^{2} + 3z^{2})(3a - 5b)$$

#### Answer 2J.

$$8x^{3} - 24x^{2}y + 54xy^{2} - 162y^{3}$$

$$= (8x^{3} - 24x^{2}y) + (54xy^{2} - 162y^{3})$$

$$= 8x^{2}(x - 3y) + 54y^{2}(x - 3y)$$

$$= (x - 3y)(8x^{2} + 54y^{2})$$

#### **Answer 2K.**

$$2a + b + 3c - d + (2a + b)^{3} + (2a + b)^{2}(3c - d)$$

$$= (2a + b + 3c - d) + [(2a + b)^{3} + (2a + b)^{2}(3c - d)]$$

$$= 1(2a + b + 3c - d) + (2a + b)^{2}(2a + b + 3c - d)$$

$$= (2a + b + 3c - d)[1 + (2a + b)^{2}]$$

# **Answer 2L.**

$$xy(a^{2} + 1) + a(x^{2} + y^{2})$$

$$= a^{2}xy + xy + ax^{2} + ay^{2}$$

$$= (a^{2}xy + ax^{2}) + (ay^{2} + xy)$$

$$= ax(ay + x) + y(ay + x)$$

$$= (ay + x)(ax + y)$$

## **Answer 2M.**

$$p^{2}x^{2} + (px^{2} + 1)x + p$$

$$= p^{2}x^{2} + px^{3} + x + p$$

$$= (p^{2}x^{2} + px^{3}) + (p + x)$$

$$= px^{2}(p + x) + 1(p + x)$$

$$= (p + x)(px^{2} + 1)$$

# Answer 2N.

$$x^{2} - (p + q)x + pq$$
  
=  $x^{2} - px - qx + pq$   
=  $(x^{2} - px) - (qx + pq)$   
=  $x(x - p) - q(x - p)$   
=  $(x - p)(x - q)$ 

#### Answer 20.

$$p^{2} + \frac{1}{p^{2}} - 2 - 5p + \frac{5}{p}$$

$$= \left(p^{2} + \frac{1}{p^{2}} - 2\right) - \left(5p - \frac{5}{p}\right)$$

$$= \left((p)^{2} + \left(\frac{1}{p}\right)^{2} - 2 \times p \times \frac{1}{p}\right) - \left(5p - \frac{5}{p}\right)$$

$$= \left(p - \frac{1}{p}\right)^{2} - 5\left(p - \frac{1}{p}\right)$$

$$= \left(p - \frac{1}{p}\right)\left(p - \frac{1}{p} - 5\right)$$

## Answer 2P.

$$x + y + m(x + y)$$
  
=  $(x + y) + m(x + y)$   
=  $(x + y)(1 + m)$ 

# Answer 20.

$$\frac{1}{25x^{2}} + 16x^{2} + \frac{8}{5} - 12x - \frac{3}{5x}$$

$$= \left(\frac{1}{25x^{2}} + 16x^{2} + \frac{8}{5}\right) - \left(12x + \frac{3}{5x}\right)$$

$$= \left(\left(\frac{1}{5x}\right)^{2} + (4x)^{2} + 2x + \frac{1}{5x}x + 4x\right) - \left(12x + \frac{3}{5x}\right)$$

$$= \left(\frac{1}{5x} + 4x\right)^{2} - 3\left(4x + \frac{1}{5x}\right)$$

$$= \left(\frac{1}{5x} + 4x\right)^{2} - 3\left(\frac{1}{5x} + 4x\right)$$

$$= \left(\frac{1}{5x} + 4x\right)\left(\frac{1}{5x} + 4x - 3\right)$$

#### **Answer 2R.**

$$2p(a^{2}-2b^{2})-14p+(a^{2}-2b^{2})^{2}-7(a^{2}-2b^{2})$$

$$=2p(a^{2}-2b^{2})+(a^{2}-2b^{2})^{2}-14p-7(a^{2}-2b^{2})$$

$$=[2p(a^{2}-2b^{2})+(a^{2}-2b^{2})^{2}]-[14p+7(a^{2}-2b^{2})]$$

$$=(a^{2}-2b^{2})(2p+a^{2}-2b^{2})-7(2p+a^{2}-2b^{2})$$

$$=(2p+a^{2}-2b^{2})(a^{2}-2b^{2}-7)$$

# Ex 5.2

# Answer 1Q.

$$x^2 + 6x + 8$$

$$= x^2 + 4x + 2x + 8$$

$$= x(x + 4) + 2(x + 4)$$

$$=(x+4)(x+2)$$

# **Answer 1B.**

$$x^2 - 11x + 24$$

$$= x^2 - 8x - 3x + 24$$

$$= x(x - 8) - 3(x - 8)$$

$$=(x-8)(x-3)$$

# **Answer 1C.**

$$x^2 + 5x - 6$$

$$= x^2 + 6x - x - 6$$

$$= x(x + 6) - 1(x + 6)$$

$$=(x+6)(x-1)$$

# **Answer 1D.**

$$p^2 - 12p - 64$$

$$= p^2 - 16p + 4p - 64$$

$$= p(p - 16) + 4(p - 16)$$

$$= (p - 16)(p + 4)$$

# **Answer 1E.**

$$= y^2 - 6y + 4y - 24$$

$$= y(y-6) + 4(y-6)$$

$$=(y-6)(y+4)$$

# **Answer 1F.**

$$3x^2 + 19x - 14$$

$$=3x^2+21x-2x-14$$

$$=3x(x+7)-2(x+7)$$

$$=(x+7)(3x-2)$$

# **Answer 1G.**

$$= (5a - 8)(3a + 2)$$

## **Answer 1H.**

$$12 + x - 6x^2$$

$$= 12 + 9x - 8x - 6x^2$$

$$=3(4+3x)-2x(4+3x)$$

$$=(4+3x)(3-2x)$$

## **Answer 1I.**

$$7x^2 + 40x - 12$$

$$=7x^2+42x-2x-12$$

$$= 7x(x+6) - 2(x+6)$$

$$=(x+6)(7x-2)$$

#### **Answer 2A.**

$$5x^2 - 17xy + 6y^2$$

$$=5x^2 - 15xy - 2xy + 6y^2$$

$$= 5x(x - 3y) - 2y(x - 3y)$$

$$= (x - 3y)(5x - 2y)$$

#### Answer 2B.

$$9x^2 - 22xy + 8y^2$$

$$= 9x^2 - 18xy - 4xy + 8y^2$$

$$= 9x(x - 2y) - 4y(x - 2y)$$

$$= (x - 2y)(9x - 4y)$$

## **Answer 2C.**

$$2x^{3} + 5x^{2}y - 12xy^{2}$$

$$= 2x^{3} + 8x^{2}y - 3x^{2}y - 12xy^{2}$$

$$= 2x^{2}(x + 4y) - 3xy(x + 4y)$$

$$= (x + 4y)(2x^{2} - 3xy)$$

$$= (x + 4y)x(2x - 3y)$$

$$= x(x + 4y)(2x - 3y)$$

#### Answer 2D.

$$x^{2}y^{2} + 15xy - 16$$

$$= x^{2}y^{2} + 16xy - xy - 16$$

$$= xy(xy + 16) - 1(xy + 16)$$

$$= (xy + 16)(xy - 1)$$

#### **Answer 2E.**

$$(2p+q)^2 - 10p - 5q - 6$$

$$= (2p+q)^2 - (10p - 5q) - 6$$

$$= (2p+q)^2 - 5(2p+q) - 6$$

$$= (2p+q)^2 - 6(2p+q) + (2p+q) - 6$$

$$= (2p+q)(2p+q-6) + 1(2p+q-6)$$

$$= (2p+q-6)(2p+q+1)$$

#### **Answer 2F.**

$$y^{2} + 3y + 2 + by + 2b$$

$$= y^{2} + y + 2y + 2 + by + 2b$$

$$= y^{2} + y + by + 2y + 2 + 2b$$

$$= y(y + 1 + b) + 2(y + 1 + b)$$

$$= (y + 1 + b)(y + 2)$$

## **Answer 2G.**

$$x^{3}y^{3} - 8x^{2}y^{2} + 15xy$$

$$= x^{3}y^{3} - 3x^{2}y^{2} - 5x^{2}y^{2} + 15xy$$

$$= x^{2}y^{2}(xy - 3) - 5xy(xy - 3)$$

$$= (xy - 3)(x^{2}y^{2} - 5xy)$$

$$= (xy - 3)xy(xy - 5)$$

$$= xy(xy - 3)(xy - 5)$$

# Answer 2H.

$$6\sqrt{3}x^{2} - 19x + 5\sqrt{3}$$

$$= 6\sqrt{3}x^{2} - 10x - 9x + 5\sqrt{3}$$

$$= 2x(3\sqrt{3}x - 5) - \sqrt{3}(3\sqrt{3}x - 5)$$

$$= (3\sqrt{3}x - 5)(2x - \sqrt{3})$$

#### **Answer 2I.**

$$2\sqrt{5}x^{2} - 7x - 3\sqrt{5}$$

$$= 2\sqrt{5}x^{2} - 10x + 3x - 3\sqrt{5}$$

$$= 2\sqrt{5}x(x - \sqrt{5}) + 3(x - \sqrt{5})$$

$$= (x - \sqrt{5})(2\sqrt{5}x + 3)$$

#### **Answer 3A.**

$$5(3x + y)^{2} + 6(3x + y) - 8$$

$$= 5(3x + y)^{2} + 10(3x + y) - 4(3x + y) - 8$$

$$= 5(3x + y)(3x + y + 2) - 4(3x + y + 2)$$

$$= (3x + y + 2)[5(3x + y) - 4]$$

#### **Answer 3B.**

$$5 - 4(a - b) - 12(a - b)^{2}$$

$$= 5 - 10(a - b) + 6(a - b) - 12(a - b)^{2}$$

$$= 5[1 - 2(a - b)] + 6(a - b)[1 - 2(a - b)]$$

$$= [5 + 6(a - b)][1 - 2(a - b)]$$

$$= (5 + 6a - 6b)(1 - 2a + 2b)$$

#### **Answer 3C.**

$$(3a-2b)^2 + 3(3a-2b) - 10$$
  
=  $(3a-2b)^2 + 5(3a-2b) - 2(3a-2b) - 10$   
=  $(3a-2b)(3a-2b+5) - 2(3a-2b+5)$   
=  $(3a-2b+5)((3a-2b-2)$ 

#### Answer 3D.

$$(a^{2}-2a)^{2}-23(a^{2}-2a)+120$$

$$=(a^{2}-2a)^{2}-15(a^{2}-2a)-8(a^{2}-2a)+120$$

$$=(a^{2}-2a)(a^{2}-2a-15)-8(a^{2}-2a-15)$$

$$=(a^{2}-2a-15)(a^{2}-2a-8)$$

$$=(a^{2}-5a+3a-15)(a^{2}-4a+2a-8)$$

$$=[a(a-5)+3(a-5)][a(a-4)+2(a-4)]$$

$$=[(a-5)(a+3)][(a-4)(a+2)]$$

$$=(a+2)(a+3)(a-4)(a-5)$$

## **Answer 3E.**

$$(x + 4)^{2} - 5xy - 20y - 6y^{2}$$

$$= (x + 4)^{2} - 5y(x + 4) - 6y^{2}$$

$$= (x + 4)^{2} - 6y(x + 4) + y(x + 4) - 6y^{2}$$

$$= (x + 4)(x + 4 - 6y) + y(x + 4 - 6y)$$

$$= (x + 4 - 6y)(x + 4 + y)$$

$$= (x - 6y + 4)(x + y + 4)$$

#### **Answer 3F.**

$$7(x-2)^{2}-13(x-2)-2$$

$$=7(x-2)^{2}-14(x-2)+(x-2)-2$$

$$=7(x-2)(x-2-2)+1(x-2-2)$$

$$=7(x-2)(x-4)+1(x-4)$$

$$=(x-4)[7(x-2)+1]$$

$$=(x-4)(7x-14+1)$$

$$=(x-4)(7x-13)$$

#### **Answer 3G.**

$$12 - (y + y^{2})(8 - y - y^{2})$$

$$= 12 - a(8 - a) [Taking y + y^{2} = a]$$

$$= 12 - 8a + a^{2}$$

$$= 12 - 6a - 2a + a^{2}$$

$$= 6(2 - a) - a(2 - a)$$

$$= (2 - a)(6 - a)$$

$$= [2 - (y + y^{2})][6 - (y + y^{2})]$$

$$= (2 - y - y^{2})(6 - y - y^{2})$$

$$= (2 - 2y + y - y^{2})(6 - 3y + 2y - y^{2})$$

$$= [2(1 - y) + y(1 - y)][3(2 - y) + y(2 - y)]$$

$$= [(1 - y)(2 + y)][(2 - y)(3 + y)]$$

$$= (y - 1)(y + 2)(y - 2)(y + 3)$$

#### Answer 3H.

$$(p^{2} + p)^{2} - 8(p^{2} + p) + 12$$

$$= (p^{2} + p)^{2} - 6(p^{2} + p) - 2(p^{2} + p) + 12$$

$$= (p^{2} + p)(p^{2} + p - 6) - 2(p^{2} + p - 6)$$

$$= (p^{2} + p - 6)(p^{2} + p - 2)$$

$$= (p^{2} + 3p - 2p - 6)(p^{2} + 2p - p - 2)$$

$$= [p(p + 3) - 2(p + 3)][p(p + 2) - 1(p + 2)]$$

$$= [(p + 3)(p - 2)][(p + 2)(p - 1)]$$

$$= (p + 3)(p - 2)(p + 2)(p - 1)$$

# Answer 4A.

$$(y^{2}-3y)(y^{2}-3y+7)+10$$

$$= a(a+7)+10 [taking (y^{2}-3y) = a]$$

$$= a^{2}+7a+10$$

$$= a^{2}+5a+2a+10$$

$$= a(a+5)+2(a+5)$$

$$= (a+5)(a+2)$$

$$= (y^{2}-3y+5)(y^{2}-3y+2)$$

$$= (y^{2}-3y+5)(y^{2}-2y-y+2)$$

$$= (y^{2}-3y+5)[y(y-2)-1(y-2)]$$

$$= (y^{2}-3y+5)[(y-2)(y-1)]$$

$$= (y-1)(y-2)(y^{2}-3y+5)$$

#### Answer 4B.

$$(t^{2}-t)(4t^{2}-4t-5)-6$$

$$= (t^{2}-t)[4(t^{2}-t)-5]-6$$

$$= a[4a-5]-6[Taking (t^{2}-t)=a]$$

$$= 4a^{2}-5a-6$$

$$= 4a^{2}-8a+3a-6$$

$$= 4a(a-2)+3(a-2)$$

$$= (a-2)(4a+3)$$

$$= (t^{2}-t-2)[4(t^{2}-t)+3]$$

$$= (t^{2}-2t+t-2)(4t^{2}-4t+3)$$

$$= [t(t-2)+1(t-2)](4t^{2}-4t+3)$$

$$= [(t-2)(t+1)](4t^{2}-4t+3)$$

$$= (t+1)(t-2)(4t^{2}-4t+3)$$

#### **Answer 4C.**

$$12(2x-3y)^{2}-1(2x-3y)-1$$

$$= 12a^{2}-a-1[Taking (2x-3y) = a]$$

$$= 12a^{2}-4a+3a-1$$

$$= 4a(3a-1)+1(3a-1)$$

$$= (3a-1)(4a+1)$$

$$= [3(2x-3y)-1][4(2x-3y)+1]$$

$$= (6x-9y-1)(8x-12y+1)$$

#### Answer 4D.

$$6-5x+5y+(x-y)^{2}$$

$$=6-5(x-y)+(x-y)^{2}$$

$$=6-3(x-y)-2(x-y)+(x-y)^{2}$$

$$=3[2-(x-y)]-(x-y)[2-(x-y)]$$

$$=3(2-x+y)-(x-y)(2-x+y)$$

$$=(2-x+y)(3-x+y)$$

# **Answer 4E.**

$$2x^{2} + \frac{x}{6} - 1$$

$$= \frac{1}{6} (12x^{2} + x - 6)$$

$$= \frac{1}{6} (12x^{2} + 9x - 8x - 6)$$

$$= \frac{1}{6} [3x (4x + 3) - 2(4x + 3)]$$

$$= \frac{1}{6} [(4x + 3)(3x - 2)]$$

$$= \frac{1}{6} (4x + 3)(3x - 2)$$

# **Answer 4F.**

$$\begin{aligned} &P^4 + 23p^2q^2 + 90q^4 \\ &= p^4 + 18p^2q^2 + 5p^2q^2 + 90q^4 \\ &= p^2(p^2 + 18q^2) + 5q^2(p^2 + 18q^2) \\ &= (p^2 + 18q^2)(p^2 + 5q^2) \end{aligned}$$

## Answer 4G.

$$2a^{3} + 5a^{2}b - 12ab^{2}$$

$$= 2a^{3} + 8a^{2}b - 3a^{2}b - 12ab^{2}$$

$$= 2a^{2}(a + 4b) - 3ab(a + 4b)$$

$$= (a + 4b)(2a^{2} - 3ab)$$

$$= (a + 4b)a(2a - 3b)$$

$$= a(a + 4b)(2a - 3b)$$

# Ex 5.3

# **Answer 1A.**

$$x^2 - 16$$

$$= x^2 - 4^2$$

$$=(x-4)(x+4)$$

# **Answer 1B.**

$$=(8x)^2-(11y)^2$$

$$= (8x - 11y)(8x + 11y)$$

# **Answer 1C.**

$$=(21)^2-(9y)^2$$

$$=(21-9y)(21+9y)$$

$$=3(7-3y)3(7+3y)$$

$$= 9(7 - 3y)(7 + 3y)$$

# **Answer 1D.**

$$=(x^3)^2-(14)^2$$

$$=(x^3-14)(x^3+14)$$

# **Answer 1E.**

$$=(25)^2-(b)^2$$

$$= (25 - b)(25 + b)$$

# **Answer 1F.**

$$m^{2} - \frac{1}{9}n^{2}$$

$$= m^{2} - \left(\frac{1}{3}n\right)^{2}$$

$$= \left(m - \frac{1}{3}n\right)\left(m + \frac{1}{3}n\right)$$

## **Answer 1G.**

$$= 2x(4y^2 - 9x^2)$$

$$= 2x[(2y)^2 - (3x)^2]$$

$$= 2x[(2y - 3x)(2y + 3x)]$$

$$= 2x(2y - 3x)(2y + 3x)$$

# **Answer 1H.**

$$=(4a^2)^2-(9b^2)^2$$

$$=(4a^2-9b^2)(4a^2+9b^2)$$

$$=[(2a)^2-(3b)^2](4a^2+9b^2)$$

$$=[(2a-3b)(2a+3b)](4a^2+9b^2)$$

$$= (2a - 3b)(2a + 3b)(4a^2 + 9b^2)$$

# Answer 1I.

$$= a^2 - a - b^2 + b$$

$$= a^2 - b^2 - a + b$$

$$= (a^2 - b^2) - (a - b)$$

# **Answer 1J.**

$$(x + y)^2 - 1$$

$$=(x+y)^2-(1)^2$$

$$= (x + y + 1)(x + y - 1)$$

## **Answer 1K.**

$$x^{2} + y^{2} - z^{2} - 2xy$$

$$= x^{2} + y^{2} - 2xy - z^{2}$$

$$= (x^{2} + y^{2} - 2xy) - z^{2}$$

$$=(x-y)^2-(z)^2$$

$$= (x - y - z)(x - y + z)$$

## **Answer 1L.**

$$(x-2y)^2 - z^2$$
=  $(x-2y)^2 - (z)^2$   
=  $(x-2y-z)(x-2y+z)$ 

#### **Answer 2A.**

$$9(a - b)^{2} - (a + b)^{2}$$

$$= [3(a - b)]^{2} - (a + b)^{2}$$

$$= [3(a - b) - (a + b)][3(a - b) + (a + b)]$$

$$= (3a - 3b - a - b)(3a - 3b + a + b)$$

$$= (2a - 4b)(4a - 2b)$$

$$= 2(a - 2b)2(2a - b)$$

# Answer 2B.

= 4(a - 2b)(2a - b)

$$25(x-y)^{2}-49(c-d)^{2}$$
=  $[5(x-y)]^{2}-[7(c-d)]^{2}$   
=  $[5(x-y)-7(c-d)][5(x-y)+7(c-d)]$   
=  $(5x-5y-7c+7d)(5x-5y+7c-7d)$ 

# **Answer 2C.**

$$(2a - b)^{2} - 9(3c - d)^{2}$$

$$= (2a - b)^{2} - [3(3c - d)]^{2}$$

$$= [(2a - b) - 3(3c - d)][(2a - b) + 3(3c - d)]$$

$$= (2a - b - 9c + 3d)(2a - b + 9c - 3d)$$

## Answer 2D.

$$b^{2} - 2bc + c^{2} - a^{2}$$
  
=  $(b^{2} - 2bc + c^{2}) - a^{2}$   
=  $(b - c)^{2} - (a)^{2}$   
=  $(b - c - a)(b - c + a)$ 

# **Answer 2E.**

$$x^{2} + \frac{1}{x^{2}} - 2$$

$$= x^{2} + \frac{1}{x^{2}} - 2x \times x + \frac{1}{x}$$

$$= \left(x - \frac{1}{x}\right)^{2}$$

$$= \left(x - \frac{1}{x}\right)\left(x - \frac{1}{x}\right)$$

## **Answer 2F.**

$$(x^{2} + y^{2} - z^{2})^{2} - 4x^{2}y^{2}$$

$$= (x^{2} + y^{2} - z^{2})^{2} - (2xy)^{2}$$

$$= (x^{2} + y^{2} - z^{2} - 2xy)(x^{2} + y^{2} - z^{2} + 2xy)$$

$$= [(x^{2} + y^{2} - 2xy) - z^{2}][(x^{2} + y^{2} + 2xy) - z^{2}]$$

$$= [(x - y)^{2} - z^{2}][(x + y)^{2} - z^{2}]$$

$$= [(x - y - z)(x - y + z)][(x + y - z)(x + y + z)]$$

$$= (x - y - z)(x - y + z)(x + y - z)(x + y + z)$$

## **Answer 2G.**

$$a^{2} + b^{2} - c^{2} - d^{2} + 2ab - 2cd$$
  
=  $(a^{2} + b^{2} + 2ab) - (c^{2} + d^{2} + 2cd)$   
=  $(a + b)^{2} - (c + d)^{2}$   
=  $(a + b + c + d)(a + b - c - d)$ 

#### **Answer 2H.**

$$4xy - x^{2} - 4y^{2} + z^{2}$$

$$= z^{2} - x^{2} - 4y^{2} + 4xy$$

$$= z^{2} - (x^{2} + 4y^{2} - 4xy)$$

$$= z^{2} - (x - 2y)^{2}$$

$$= [z - (x - 2y)][z + (x - 2y)]$$

$$= (z - x + 2y)(z + x - 2y)$$

## **Answer 2I.**

$$4x^{2} - 12ax - y^{2} - z^{2} - 2yz + 9a^{2}$$

$$= (4x^{2} - 12ax + 9a^{2}) - (y^{2} + z^{2} + 2yz)$$

$$= (2x - 3a)^{2} - (y + z)^{2}$$

$$= [(2x - 3a) + (y + z)][(2x - 3a) - (y + z)]$$

$$= (2x - 3a + y + z)(2x - 3a - y - z)$$

## Answer 2J.

$$(x+y)^3 - x - y$$

$$= (x+y)(x+y)^2 - (x+y)$$

$$= (x+y)[(x+y)^2 - 1]$$

$$= (x+y)[(x+y+1)(x+y-1)]$$

$$= (x+y)(x+y+1)(x+y-1)$$

## **Answer 2K.**

$$y^{4} + y^{2} + 1$$

$$= y^{4} + 2y^{2} + 1 - y^{2}$$

$$= (y^{2} + 1)^{2} - y^{2}$$

$$= (y^{2} + 1 + y)(y^{2} + 1 - y)$$

#### **Answer 2L.**

$$(a^{2} - b^{2})(c^{2} - d^{2}) - 4abcd$$

$$= a^{2}c^{2} - a^{2}d^{2} - b^{2}c^{2} + b^{2}d^{2} - 4abcd$$

$$= a^{2}c^{2} + b^{2}d^{2} - 2abcd - a^{2}d^{2} - b^{2}c^{2} - 2abcd$$

$$= (a^{2}c^{2} + b^{2}d^{2} - 2abcd) - (a^{2}d^{2} + b^{2}c^{2} + 2abcd)$$

$$= (ac - bd)^{2} - (ad + bc)^{2}$$

$$= [(ac - bd) + (ad + bc)][(ac - bd) - (ad + bc)]$$

$$= (ac - bd + ad + bc)(ac - bd - ad - bc)$$

#### **Answer 3A.**

$$(x^{2} - 2x + 3)(x^{2} + 2x + 3)$$

$$= [x^{2} + 3 - 2x][x^{2} + 3 + 2x]$$

$$= [(x^{2} + 3) - 2x][(x^{2} + 3) + 2x]$$

$$= (x^{2} + 3)^{2} - (2x)^{2}$$

$$= (x^{2} + 3)^{2} - 4x^{2}$$

# Answer 3B.

$$(x^{2} - 2x + 3)(x^{2} - 2x - 3)$$

$$= [(x^{2} - 2x) + 3][(x^{2} - 2x) + 3]$$

$$= (x^{2} - 2x)^{2} - (3)^{2}$$

$$= (x^{2} - 2x)^{2} - 9$$

# **Answer 3C.**

$$(x^{2} + 2x - 3)(x^{2} - 2x + 3)$$

$$= [x^{2} + (2x - 3)][x^{2} - (2x - 3)]$$

$$= x^{2} - (2x - 3)^{2}$$

$$= x^{4} - (2x - 3)^{2}$$

# **Answer 4A.**

$$y^{2} + \frac{1}{4y^{2}} + 1 - 6y - \frac{3}{y}$$

$$= \left(y^{2} + \frac{1}{4y^{2}} + 1\right) - \left(6y + \frac{3}{y}\right)$$

$$= \left(y + \frac{1}{2y}\right)^{2} - 6\left(y + \frac{1}{2y}\right)$$

$$= \left(y + \frac{1}{2y}\right)\left(y + \frac{1}{2y} - 6\right)$$

#### Answer 4B.

$$4a^{2} + \frac{1}{4a^{2}} - 2 - 6a + \frac{3}{2a}$$

$$= \left(4a^{2} + \frac{1}{4a^{2}} - 2\right) - \left(6a - \frac{3}{2a}\right)$$

$$= \left(2a - \frac{1}{2a}\right)^{2} - 3\left(2a - \frac{1}{2a}\right)$$

$$= \left(2a - \frac{1}{2a}\right)\left(2a - \frac{1}{2a} - 3\right)$$

#### **Answer 4C.**

$$x^{4} + y^{4} - 6x^{2}y^{2}$$

$$= (x^{2})^{2} + (y^{2})^{2} - 2x^{2}y^{2} - 4x^{2}y^{2}$$

$$= [(x^{2})^{2} + (y^{2})^{2} - 2x^{2}y^{2}] - (4x^{2}y^{2})$$

$$= (x^{2} - y^{2})^{2} - (2xy)^{2}$$

$$= (x^{2} - y^{2} - 2xy)(x^{2} - y^{2} + 2xy)$$

#### **Answer 4D.**

$$4x^{4} + 25y^{4} + 19x^{2}y^{2}$$

$$= 4x^{4} + 25y^{4} + 20x^{2}y^{2} - x^{2}y^{2}$$

$$= (2x^{2})^{2} + (5y^{2})^{2} + 2x(2x^{2})x(5y^{2}) - x^{2}y^{2}$$

$$= [(2x^{2})^{2} + (5y^{2})^{2} + 2x(2x^{2})x(5y^{2})] - x^{2}y^{2}$$

$$= [2x^{2} + 5y^{2}] - (xy)^{2}$$

$$= (2x^{2} + 5y^{2} - xy)(2x^{2} - 5y + xy)$$

## **Answer 4E.**

$$p^{2} + \frac{1}{p^{2}} - 3$$

$$= p^{2} + \frac{1}{p^{2}} - 2 - 1$$

$$= \left(p^{2} + \frac{1}{p^{2}} - 2 \times p \times \frac{1}{p}\right) - 1$$

$$= \left(p - \frac{1}{p}\right)^{2} - 1^{2}$$

$$= \left(p - \frac{1}{p} + 1\right) \left(p - \frac{1}{p} - 1\right)$$

# **Answer 4F.**

$$5x^{2} - y^{2} - 4xy + 3x - 3y$$

$$= x^{2} + 4x^{2} - y^{2} - 4xy + 3x - 3y$$

$$= (x^{2} - y^{2}) + (4x^{2} - 4xy) + (3x - 3y)$$

$$= (x - y)(x + y) + 4x(x - y) + 3(x - y)$$

$$= (x - y)[(x + y) + 4x + 3]$$

$$= (x - y)(x + y + 4x + 3)$$

$$= (x - y)(5x + y + 3)$$