

DPP No. 72

Total Marks : 25

Max. Time : 26 min.

(3 marks, 3 min.)

(3 marks, 3 min.)

(5 marks, 4 min.)

(4 marks, 5 min.)

M.M., Min.

9]

3]

4]

10]

[9,

[3,

[5,

[8,

## **Topics : Permutation & Combination, Binomial Theorem**

Туре	of	Questions
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Comprehension (no negative marking) Q.1 to Q.3 Single choice Objective (no negative marking) Q.4 Multiple choice objective (no negative marking) Q.5 Subjective Questions (no negative marking) Q.6,7

## COMPREHENSION #1 (1 to 3)

Consider, sum of the series  $\sum_{0 \leq i < j \leq n} \ f(i) \ f(j)$ 

In the given summation, i and j are not independent.

In the sum of series  $\sum_{i=1}^{n} \sum_{j=1}^{n} f(i) f(j) = \sum_{i=1}^{n} \left( f(i) \left( \sum_{j=1}^{n} f(j) \right) \right)$  i and j are independent. In this summation, three

types of terms occur, those when i < j, i > j and i = j.

Also, sum of terms when i < j is equal to the sum of the terms when i > j if f(i) and f(j) are symmetrical. So, in that case

$$\begin{split} &\sum_{i=1}^{n}\sum_{j=1}^{n}f(i)f(j) = \sum_{0\leq i< j\leq n}f(i)f(j) \\ &+ \sum_{0\leq i< j\leq n}f(i)f(j) + \sum_{i=j}f(i)f(j) \\ &= 2\sum_{0\leq i< j\leq n}f(i)f(j) + \sum_{i=j}f(i)f(j) \\ &\Rightarrow \sum_{0\leq i< j\leq n}f(i)f(j) = \frac{\sum_{i=1}^{n}\sum_{j=1}^{n}f(i)f(j) - \sum_{i=j}f(i)f(j)}{2} \end{split}$$

When f(i) and f(j) are not symmetrical, we find the sum by listing all the terms.

1. 
$$\sum_{0 \le i < j \le n} \sum_{n=0}^{n} C_{i}^{n} C_{j}^{n} \text{ is equal to } -$$
(A)  $\frac{2^{2n} - {}^{2n}C_{n}}{2}$  (B)  $\frac{2^{2n} + {}^{2n}C_{n}}{2}$  (C)  $\frac{2^{2n} - {}^{n}C_{n}}{2}$  (D)  $\frac{2^{2n} + {}^{n}C_{n}}{2}$ 

2. 
$$\sum_{m=0}^{n} \sum_{p=0}^{m} {}^{n}C_{m} \cdot {}^{m}C_{p}$$
 is equal to -  
(A) 2<sup>n</sup>-1 (B) 3<sup>n</sup> (C) 3<sup>n</sup>-1 (D) 2<sup>n</sup>

- 3.  $\sum_{0 \le i \le j \le n} {\binom{n}{C_i} + {^nC_j}}_{is equal to -}$ (A) n2<sup>n</sup> (B) (n + 1)2<sup>n</sup> (C) (n 1)2<sup>n</sup> (D) (n + 1)2<sup>n</sup>-1
- Find the three digit numbers in which the middle one is a perfect square are formed using the digits 1 to 9 is (repeatition of digits is allowed)
   (A) 243
   (B) 242
   (C) 244
   (D) 246
- 5. The no. of ways in which 5 different books to be distributed among 3 persons to that each person gets at least one book, is equal to the number of ways in which
  - (A) 5 persons are alloted 3 different residential flats such that each person is alloted at most one flat and no two persons are alloted the some flat.
  - (B) No. of parallelograms formed by one set of 6 parallel lines and other set of 5 parallel lines that goes in other direction.
  - (C) 5 different toys are to be distributed among 3 children, so that each child gets at least one toy.
- 6. In how many ways can 5 colours be selected out of 8 different colours including red, blue and green
  - (1) if blue and green are always to be included
  - (2) if red is always excluded
  - (3) if red & blue are always included but green excluded ?
- 7. How many numbers between 400 and 1000 (both exclusive) can be made with the digits 2,3,4,5,6,0 if
  - (1) repetition of digits not allowed
  - (2) repetition of digits is allowed

## **Answers Key**

- **1.** (A)
- **2.** (B)
- **3.** (A)
- **4.** (A)
- **5.** (B)(C)
- **6.** (1) 20 (2) 21 (3) 10
- **7.** (1) 60 (2) 107