

Topics : Quadratic Equation, Fundamentals of Mathematics, Circle, Complex Number

Type of Questions

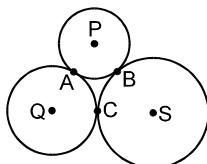
M.M., Min.

Comprehension (no negative marking) Q.1 to Q.3	(3 marks, 3 min.)	[9, 9]
Single choice Objective (no negative marking) Q.4, 5, 6	(3 marks, 3 min.)	[9, 9]
Fill in the Blanks (no negative marking) Q.7, 8	(4 marks, 4 min.)	[8, 8]
Subjective Questions (no negative marking) Q.9, 10	(4 marks, 5 min.)	[8, 10]

COMPREHENSION (For Q.No. 1 to 3)

A polynomial $P(x)$ of third degree vanish when $x = 1$ & $x = -2$. This polynomial have the values 4 & 28 when $x = -1$ and $x = 2$ respectively.

- One of the factor of $P(x)$ is
(A) $x + 1$ (B) $x - 2$ (C) $3x + 1$ (D) none of these
- If the polynomial $P(x)$ is divided by $(x + 3)$, the remainder is
(A) -32 (B) 100 (C) 32 (D) 0
- $P(i)$, where $i = \sqrt{-1}$ is
(A) purely real (B) purely imaginary (C) imaginary (D) none of these
- The value of x satisfying the equation $\frac{6x + 2a + 3b + c}{6x + 2a - 3b - c} = \frac{2x + 6a + b + 3c}{2x + 6a - b - 3c}$ is
(A) ab/c (B) $2ab/c$ (C) $ab/3c$ (D) $ab/2c$
- If $x = 3 - \sqrt{8}$, then $x^3 + \frac{1}{x^3}$ is equal to
(A) 6 (B) 198 (C) $6\sqrt{2}$ (D) 102
- Which of these five numbers $\sqrt{\pi^2}$, $\sqrt[3]{0.8}$, $\sqrt[4]{0.00016}$, $\sqrt[3]{-1}$, $\sqrt{(0.09)^{-1}}$, is (are) rational :
(A) none (B) all (C) the first and fourth (D) only fourth and fifth
- Circles with centres P, Q & S are touching each other externally as shown in the figure at points A, B & C. If the radii of circles with centres P, Q & S are 1, 2 and 3 respectively then the length of chord AB is _____



- In a circle, chords AB and CD intersect at a point R inside the circle. If $AR : RB = 1 : 4$ and $CR : RD = 4 : 9$, then the ratio AB: CD is _____.
- (i) Find the smallest positive integer 'n' for which $\left(\frac{1+i}{1-i}\right)^n = 1$
(ii) If $g(x) = x^4 - x^3 + x^2 + 3x - 5$, find $g(2 + 3i)$
(iii) Given that $x, y \in \mathbb{R}$, solve
(a) $x^2 - y^2 - i(2x + y) = 2i$ (b) $(x + 2y) + i(2x - 3y) = 5 - 4i$
- Find the real values of x & y for which $z_1 = 9y^2 - 4 - 10ix$ and $z_2 = 8y^2 - 20i$ are conjugate complex of each other.

Answers Key

1. (C) 2. (A) 3. (C) 4. (A)
5. (B) 6. (D) 7. $\sqrt{2}$ 8. 15: 13
9. (i) 4 (ii) $-(77 + 108i)$
(iii) (a) $x = -2, -\frac{2}{3}, y = 2, -\frac{2}{3}$ (b) $x = 1, y = 2$
10. $(-2, 2); (-2, -2)$