

## **Question 1**

**A certain screw gauge has a pitch of 0.5 mm. If there are 50 divisions on the head scale, the dimension of the object can then be determined to an accuracy of**

**Options:**

- A. 0.05 cm
- B. 0.01 cm
- C. 0.001 cm
- D. 0.0001 cm

**Answer: C**

**Solution:**

**Solution:**

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## **Question 2**

**The refractive index of glass measured by a given method by four independent measurements is found to have values of 1.54, 1.58, 1.52 and 1.56 respectively. The mean value of refractive index with percentage error is**

**Options:**

- A.  $1.55 \pm 1.29\%$
- B.  $1.55 \pm 0\%$
- C.  $1.56 \pm 6\%$
- D.  $1.56 \pm 0\%$

**Answer: A**

**Solution:**

**Solution:**

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## Question 3

A particle moves for 20 seconds with velocity  $3\text{m / s}$  and then with velocity  $4\text{m / s}$  for another 20 seconds and finally moves with velocity  $5\text{m / s}$  for next 20 seconds. Then the average velocity of the particle is

Options:

A.  $3\text{m / s}$

B.  $4\text{m / s}$

C.  $5\text{m / s}$

D. Zero

**Answer: B**

**Solution:**

**Solution:**

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## Question 4

An athlete completes one round of a circular track of radius  $R$  in 40 s. What will be his displacement at the end of 2 min 40 seconds?

Options:

A.  $8R$

B.  $8\pi R$

C.  $2R$

D. Zero

**Answer: D**

**Solution:**

**Solution:**

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## Question 5

A wheel having 1m diameter makes 60 revolutions per minute. The linear speed of a point on its circumference is

Options:

A.  $\pi / 2\text{m / s}$

- B.  $\pi m / s$
- C.  $2\pi m / s$
- D.  $60\pi m / s$

**Answer: B**

**Solution:**

**Solution:**

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## Question 6

**A car starts from rest to cover a distance  $s$ . The coefficient of friction between the road and the tyres is  $\mu$ . The maximum time in which the car can cover the distance is proportional to**

**Options:**

- A.  $\mu$
- B.  $\sqrt{\mu}$
- C.  $1 / \mu$
- D.  $1 / \sqrt{\mu}$

**Answer: D**

**Solution:**

**Solution:**

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## Question 7

**A diesel engine pumps 40 kg of water in 1 second. The water comes out vertically upwards with a velocity of  $3m / s$ . What is the power of the engine in kilo Watt?**

**Options:**

- A. 12 kW
- B. 1.2 kW
- C. 120 kW
- D. 1200 kW

**Answer: B**

**Solution:**

**Solution:**

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## Question 8

**Which one of the following is the S.I. unit of electric field strength?**

**Options:**

A.  $\text{Am}^{-1}$

B.  $\text{Nm}^{-1}$

C.  $\text{Vm}^{-1}$

D. Coulomb s  $\text{cm}^{-1}$

**Answer: C**

**Solution:**

**Solution:**

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## Question 9

**If the distance between the two charged particles is reduced to half the original distance, then the force between them becomes**

**Options:**

A. doubled

B. one-fourth

C. one-half

D. four times

**Answer: D**

**Solution:**

**Solution:**

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## Question 10

**A metal sheet is placed between two charges separated by a distance. Then the force between them will**

**Options:**

- A. increase
- B. decrease
- C. remains the same
- D. be reduced to half the initial value

**Answer: A**

**Solution:**

**Solution:**

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## Question 11

**If the separation between carbon and oxygen in CO molecule is 0.12 nm, then the distance of the center of mass from the carbon atom is**

**Options:**

- A. 0.03 nm
- B. 0.068 nm
- C. 0.05 nm
- D. 0.06 nm

**Answer: B**

**Solution:**

**Solution:**

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## Question 12

**A hole is drilled along the earth's diameter and a stone is dropped into it. When the stone is at the center of the earth, it has**

**Options:**

- A. mass
- B. weight
- C. potential energy
- D. zero mass

**Answer: A**

**Solution:**

**Solution:**

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## Question 13

**Two wires of the same radius and material have lengths in the ratio 1 : 2. If these are stretched by the same force, the strain produced in the two cases will be in the ratio**

**Options:**

- A. 1 : 2
- B. 2 : 1
- C. 1 : 1
- D. 4 : 1

**Answer: C**

**Solution:**

**Solution:**

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## Question 14

**Two wires of the same radius and material have lengths in the ratio 1 : 2. If these are stretched by the same force, the strain produced in the two cases will be in the ratio**

**Options:**

- A. 1 : 2
- B. 2 : 1
- C. 1 : 1
- D. 4 : 1

**Answer: C**

**Solution:**

**Solution:**

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## Question 15

**Standing waves are produced in a 10m long stretched string. If the**

**string vibrates in 5 segments and the wave velocity is 20m / sec, the frequency is**

**Options:**

- A. 2 Hz
- B. 4 Hz
- C. 5 Hz
- D. 10 Hz

**Answer: C**

**Solution:**

**Solution:**

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## Question 16

**A parallel plate condenser is charged and isolated. When a sheet of glass is interposed between the plates**

**Options:**

- A. the charges on the plates will be reduced
- B. the potential difference between the plates will be reduced
- C. the potential difference between the plates will be increased
- D. the charges on the plates will be increased

**Answer: C**

**Solution:**

**Solution:**

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## Question 17

**If a capacitor of Capacitance 10 micro Farad ( $\mu\text{F}$ ) is charged to a potential difference of 100V, the energy stored in it is**

**Options:**

- A. 0.5J
- B. 0.05 ergs
- C. 10J

D. 0.05J

**Answer: D**

**Solution:**

**Solution:**

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## Question 18

**With increase in altitude, the conductivity of the atmosphere**

**Options:**

A. first increases and then decreases

B. increases

C. decreases

D. remains constant

**Answer: B**

**Solution:**

**Solution:**

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## Question 19

**An electric iron box has a heater coil of resistance  $50\Omega$ . If it is connected to 230V AC mains, the current flowing through the heater coil will be**

**Options:**

A. 4.6 mA

B. 5A

C. 4.6A

D. 15A

**Answer: C**

**Solution:**

**Solution:**

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## Question 20

**Glass has a resistivity of the order of**

**Options:**

A.  $10^{-8}\Omega\text{m}$

B.  $10^{-5}\Omega\text{m}$

C.  $10^8\Omega\text{m}$

D.  $10^{12}\Omega\text{m}$

**Answer: D**

**Solution:**

**Solution:**

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## Question 21

**A long solenoid of n turns has a self inductance L and area of cross section a. When a current flows through the solenoid, it produces a magnetic field B. The current flowing through the solenoid is**

**Options:**

A.  $Ban / L$

B.  $BanL$

C.  $Bn / aL$

D.  $B / anL$

**Answer: A**

**Solution:**

**Solution:**

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## Question 22

**A conductor of length r moves in a uniform magnetic field of induction B with a velocity  $\mathbf{v}$ . The emf induced across the conductor is**

**Options:**

A.  $(\mathbf{v} \times \mathbf{B}) \cdot \mathbf{r}$

B.  $\mathbf{v} \cdot (\mathbf{r} \times \mathbf{B})$

C.  $\mathbf{B. (r \times v)}$

D.  $\mathbf{r \times (v \times B)}$

**Answer: A**

**Solution:**

**Solution:**

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## Question 23

**The penetrating powers of  $\alpha$ ,  $\beta$  and  $\gamma$  radiation, in decreasing order are**

**Options:**

A.  $\alpha, \beta, \gamma$

B.  $\gamma, \alpha, \beta$

C.  $\beta, \gamma, \alpha$

D.  $\gamma, \beta, \alpha$

**Answer: D**

**Solution:**

**Solution:**

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## Question 24

**A half-wave rectifier is being used to rectify an alternating voltage of frequency 50 Hz. The number of pulses of rectified current obtained in one second is**

**Options:**

A. 50

B. 25

C. 100

D. 6

**Answer: B**

**Solution:**

**Solution:**

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## Question 25

The voltage  $V$  and the current  $I$  flowing through an A.C circuit are given by  $V = 2 \cos 100\pi t$  and  $I = 4 \sin 100\pi t$ , where  $t$  represents time. The power dissipated in the circuit is

**Options:**

- A. zero Watt
- B. 8 Watt
- C. 4 Watt
- D. 2 Watt

**Answer: A**

**Solution:**

**Solution:**

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## Question 26

An alternating e.m.f. is given by  $V = 100 \sin 314t$ . Its frequency is

**Options:**

- A. 100 Hz
- B. 50 Hz
- C. 314 Hz
- D. 60 Hz

**Answer: B**

**Solution:**

**Solution:**

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## Question 27

In a purely inductive circuit, the current

**Options:**

- A. is in phase with voltage
- B. is out of phase with voltage

C. leads the voltage by  $90^\circ$

D. lags behind the voltage by  $90^\circ$

**Answer: D**

**Solution:**

**Solution:**

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## Question 28

The current and voltage in an A.C. circuit are given by

$I = I_o \sin \left( \omega t - \frac{\pi}{2} \right)$  and  $E = E_o \sin \omega t$ . Then the average power consumption  $P$  in the circuit is

**Options:**

A.  $P = \frac{E_o I_o}{\sqrt{2}}$

B.  $P = \frac{E I}{\sqrt{2}}$

C.  $P = \frac{E_o I_o}{2}$

D. zero

**Answer: D**

**Solution:**

**Solution:**

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## Question 29

Two electric bulbs whose resistances are in the ratio 1 : 2, are connected in parallel to a constant voltage source. The power dissipated in them is in the ratio

**Options:**

A. 1 : 2

B. 2 : 1

C. 1:1

D. 1 : 4

**Answer: B**

**Solution:**

**Solution:**

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## Question 30

**The neutral temperature for a thermocouple is  $270^{\circ}\text{C}$ . If the temperature of the cold junction is  $15^{\circ}\text{C}$ , then the inversion temperature is**

**Options:**

A.  $255^{\circ}\text{C}$

B.  $285^{\circ}\text{C}$

C.  $570^{\circ}\text{C}$

D.  $525^{\circ}\text{C}$

**Answer: D**

**Solution:**

**Solution:**

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## Question 31

**A source emits a sound of frequency 400 Hz but the listener hears it to be 390 Hz. Then**

**Options:**

A. the listener is moving towards the source

B. the source is moving toward the listener

C. the listener is moving away from the source

D. the listener has a defective ear

**Answer: C**

**Solution:**

**Solution:**

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## Question 32

**The binding energy of the electron in a hydrogen atom is 13.6 eV, the energy required to remove the electron from the first excited state of  $\text{Li}^{++}$  is**

**Options:**

- A. 122.4 eV
- B. 30.6 eV
- C. 13.6 eV
- D. 3.4 eV

**Answer: B**

**Solution:**

**Solution:**

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## Question 33

**Which of the following nuclei has lowest value of the binding energy per nucleon?**

**Options:**

- A.  $2\text{He}^4$
- B.  $24\text{Cr}^{52}$
- C.  $62\text{Sm}^{152}$
- D.  $80\text{Hg}^{100}$

**Answer: A**

**Solution:**

**Solution:**

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## Question 34

**The average number of neutrons emitted during the fission of  $\text{U}^{235}$  is**

**Options:**

- A. 3
- B. 2
- C. 1.5

D. 2.5

**Answer: D**

**Solution:**

**Solution:**

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## Question 35

**The radioactive decay of uranium into thorium is represented by the equation  $92\text{U}^{238} \rightarrow 90\text{Th}^{234} + \text{X}$ , then X is**

**Options:**

- A. an electron
- B. a neutron
- C. a proton
- D. an alpha particle

**Answer: D**

**Solution:**

**Solution:**

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## Question 36

**The same radioactive nucleus may emit**

**Options:**

- A. all the three  $\alpha$ ,  $\beta$  and  $\gamma$  simultaneously
- B. either  $\alpha$  or  $\beta$  or  $\gamma$  at a time
- C. all the three  $\alpha$ ,  $\beta$  and  $\gamma$  at a time
- D. only  $\alpha$  and  $\beta$

**Answer: B**

**Solution:**

**Solution:**

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## Question 37

The radius of a nucleus of mass number A is proportional to

Options:

A. A

B.  $A^{1/2}$

C.  $A^{1/3}$

D.  $A^3$

**Answer: C**

**Solution:**

**Solution:**

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## Question 38

Which one of the statements about nuclear forces is INCORRECT?

Options:

A. Nuclear forces are short range forces

B. Nuclear forces are charge independent forces

C. Nuclear forces are exchange forces

D. Nuclear forces are central forces

**Answer: D**

**Solution:**

**Solution:**

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## Question 39

Which one of the statements about neutron is INCORRECT?

Options:

A. Neutron is a fundamental particle

B. Neutron has no charge

C. Nuclei of all elements in nature contain neutron

D. Neutron has a spin



**Answer: C**

**Solution:**

**Solution:**

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## Question 40

**The ground state energy of the hydrogen atom is**

**Options:**

- A. 13.6 eV
- B. 0 eV
- C.  $-3.4$  eV
- D.  $-13.6$  eV

**Answer: D**

**Solution:**

**Solution:**

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## Question 41

**Which one of the statements about matter waves is INCORRECT?**

**Options:**

- A. Matter waves are not electromagnetic waves
- B. Matter waves are also called probability waves
- C. de Broglie waves are pilot waves i.e., these waves guide the particle
- D. The phase velocity of the matter waves in vacuum is independent of wavelength

**Answer: D**

**Solution:**

**Solution:**

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## Question 42

**Kinetic energy of the cathode rays (electrons) depend on**

**Options:**

- A. voltage applied to the electrode
- B. depend on work function
- C. depend on both (A) and (B)
- D. does not depend on any physical quantity

**Answer: C**

**Solution:**

**Solution:**

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## Question 43

**A man cannot see objects clearly at a distance greater than 2m. He is then suffering from**

**Options:**

- A. short sight
- B. long sight
- C. astigmatism
- D. presbyopia

**Answer: A**

**Solution:**

**Solution:**

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## Question 44

**The magnifying power of a simple microscope can be increased by if we use eyepiece of**

**Options:**

- A. higher focal length
- B. smaller focal length
- C. higher diameter
- D. smaller diameter

**Answer: B**

**Solution:**

**Solution:**

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## Question 45

If the focal length of the objective and eyepiece lens of an astronomical telescope are  $f_o$  and  $f_e$  respectively, then its magnifying power is

**Options:**

A.  $\frac{f_o}{f_e}$

B.  $\frac{f_e}{f_o}$

C.  $\frac{2f_o}{f_e}$

D.  $2f_e$

**Answer: A**

**Solution:**

**Solution:**

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## Question 46

If  $f_r$  and  $f_v$  stand for focal length of the lens for red colour and violet colour respectively, then the longitudinal chromatic aberration of the lens for parallel rays is given by

**Options:**

A.  $f_r - f_v$

B.  $f_v - f_r$

C.  $f_r f_v$

D.  $f_v + f_r$

**Answer: A**

**Solution:**

**Solution:**

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## Question 47

The deviation produced by a flint glass prism for violet and red light rays are  $3.25^\circ$  and  $3.10^\circ$  respectively. Then the angular dispersion is

**Options:**

- A.  $6.35^\circ$
- B.  $3.175^\circ$
- C.  $0.15^\circ$
- D. 6.35 radians

**Answer: C**

**Solution:**

**Solution:**

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## Question 48

Total internal reflection is NOT possible in the case when light travels from

**Options:**

- A. glass to air
- B. glass to water
- C. water to glass
- D. water to air

**Answer: C**

**Solution:**

**Solution:**

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## Question 49

When the angle of incidence on a certain material is  $60^\circ$ , the reflected light is completely polarized. The angle of refraction is then

**Options:**

- A.  $60^\circ$

B.  $90^\circ$

C.  $30^\circ$

D.  $45^\circ$

**Answer: C**

**Solution:**

**Solution:**

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## Question 50

**A sugar solution of length 15 cm has specific rotation of  $65^\circ$  and produces a optical rotation of  $7^\circ$ . Then the concentration of the solution is**

**Options:**

A. 0.7g / cc

B. 13.9g / cc

C. 0.0717g / cc

D. 0.01g / cc

**Answer: C**

**Solution:**

**Solution:**

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## Question 51

**To observe diffraction, the size of an obstacle**

**Options:**

A. should be of the order of wavelength

B. should be much larger than the wavelength

C. has no relation to wavelength

D. should be exactly  $\lambda/2$ .

**Answer: A**

**Solution:**

**Solution:**

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## Question 52

**If the distance between the screen and the slit is doubled in Young's double slit experiment, the fringe width will become**

**Options:**

- A. four times
- B. two times
- C. one-half
- D. one-fourth

**Answer: B**

**Solution:**

**Solution:**

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## Question 53

**When light waves suffer reflection at the interface between air and glass, the change of phase of the reflected wave is**

**Options:**

- A. zero
- B.  $\pi$
- C.  $2\pi$
- D.  $\pi / 2$

**Answer: B**

**Solution:**

**Solution:**

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## Question 54

**If a string of string constant k is stretched by a length x under tension T, the energy stored is**

**Options:**

A.  $\frac{2k}{T^2}$

B.  $\frac{2T^2}{k^2}$

C.  $\frac{T^2}{2k}$

D.  $\frac{2T}{k^2}$

**Answer: C**

**Solution:**

**Solution:**

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## Question 55

**The Young's modulus of a perfectly rigid body is**

**Options:**

A. zero

B. unity

C. infinite

D. may be any finite non-zero value

**Answer: C**

**Solution:**

**Solution:**

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## Question 56

**A wire elongates by 1 mm when a load W is hanged at from it. If the wire goes over a pulley and the two weights W each are hung at the two ends, the elongation of the wire (in mm ) will be**

**Options:**

A. 1 / 2

B. 1

C. 2l

D. zero

**Answer: B**

**Solution:**

**Solution:**

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## Question 57

**If two liquids of same masses but densities  $\rho_1$  and  $\rho_2$  respectively are mixed, then the density of the mixture is**

**Options:**

A.  $\rho_1 + \rho_2$

B.  $\frac{\rho_1 + \rho_2}{2}$

C.  $\frac{\rho_1 \rho_2}{\rho_1 + \rho_2}$

D.  $\frac{2\rho_1 \rho_2}{\rho_1 + \rho_2}$

**Answer: D**

**Solution:**

**Solution:**

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## Question 58

**A boy carries on his head an airtight box containing a bird resting on the floor of the box. When the bird starts flying inside the box, he will feel that the box is now**

**Options:**

A. lighter

B. heavier

C. same in weight as before

D. lighter in the beginning and heavier later

**Answer: C**

**Solution:**

**Solution:**



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## Question 59

**A cork ball is floating on the surface of water in a beaker. The beaker is covered with a bell jar and the air is evacuated. What will happen to the ball?**

**Options:**

- A. Sink a little
- B. Rise a little
- C. Remain unchanged
- D. Sink completely

**Answer: A**

**Solution:**

**Solution:**

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## Question 60

**The thermometer used as a reference standard is**

**Options:**

- A. mercury thermometer
- B. platinum resistance thermometer
- C. gas thermometer
- D. thermocouple thermometer

**Answer: C**

**Solution:**

**Solution:**

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## Question 61

**If  $\alpha$  is coefficient of linear expansion,  $\beta$  is coefficient of superficial expansion and  $\gamma$  is the coefficient of cubical expansion, then for the same rise in temperature, the percentage changes in  $\alpha$ ,  $\beta$  and  $\gamma$  are in the ratio**

**Options:**

A. 1 : 2 : 3

B. 3 : 2 : 1

C. 1 : 1 : 1

D. 1 : 2 : 4

**Answer: A**

**Solution:**

**Solution:**

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## Question 62

**If  $K$  and  $\sigma$  respectively are the thermal and electrical conductivities of a metal at absolute temperature  $T$ , then**

**Options:**

A.  $\frac{K}{\sigma T} = \text{constant}$

B.  $\frac{K}{\sigma} = \text{constant}$

C.  $\frac{K}{T} = \text{constant}$

D.  $\frac{\sigma}{KT} = \text{constant}$

**Answer: A**

**Solution:**

**Solution:**

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## Question 63

**The velocity  $V$  of thermal radiation is (  $C$  = velocity of light in vacuum)**

**Options:**

A.  $V < C$

B.  $V > C$

C.  $V = C$

D. dependent on the medium

**Answer: C**

**Solution:**

**Solution:**

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## Question 64

**Which one of the following statements about electromagnetic waves is INCORRECT?**

**Options:**

- A. They do not require material medium for propagation
- B. They are not deflected in electric and magnetic fields
- C. The waves are transverse in nature
- D. They cannot be diffracted

**Answer: D**

**Solution:**

**Solution:**

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## Question 65

**If  $\vec{E}$  and  $\vec{B}$  represent electric and magnetic field vectors of the electromagnetic waves, then the direction of propagation of the waves will be along**

**Options:**

- A.  $\vec{B} \times \vec{E}$
- B.  $\vec{E}$
- C.  $\vec{B}$
- D.  $\vec{E} \times \vec{B}$

**Answer: D**

**Solution:**

**Solution:**

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## Question 66

**The area of B – H hysteresis loop in a ferromagnetic material is a measure of the**

**Options:**

- A. net energy dissipated per unit volume per cycle of magnetization of the material
- B. permeability of the material
- C. susceptibility of the material
- D. retentivity of the material

**Answer: A**

**Solution:**

**Solution:**

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## Question 67

**The unit cubic cell of Al has an edge length equal to  $4.5 \times 10^{-10}$  m. The number of unit cells in an aluminium foil of volume  $91 \times 10^{-6}$  m<sup>3</sup> is**

**Options:**

- A.  $10^{24}$
- B.  $10^{-24}$
- C.  $10^8$
- D.  $10^{23}$

**Answer: A**

**Solution:**

**Solution:**

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## Question 68

**The gate with the Boolean expression  $Y = \overline{A \cdot B}$  for its output is**

**Options:**

- A. AND
- B. NAND

C. XOR

D. XNOR

**Answer: B**

**Solution:**

**Solution:**

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## Question 69

**The Boolean expression for NOR gate is**

**Options:**

A.  $Y = A + \overline{B}$

B.  $Y = \overline{A + B}$

C.  $Y = \overline{A} + B$

D.  $Y = \overline{A} + \overline{B}$

**Answer: B**

**Solution:**

**Solution:**

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## Question 70

**What gate has the truth table given below?**

A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

**Options:**

A. NOT

B. AND

C. NAND

D. NOR

**Answer: B**

**Solution:**

**Solution:**

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## Question 71

**A transistor amplifier is operated in common emitter configuration at constant collector voltage of  $V_C = 1.5V$ , such that the change in the base current from  $100\mu A$  to  $150\mu A$  produces a change in the collector current from  $5\text{ mA}$  to  $10\text{ mA}$ . The current gain  $\beta$  of the circuit is then**

**Options:**

- A. 50
- B. 67
- C. 75
- D. 100

**Answer: D**

**Solution:**

**Solution:**

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## Question 72

**A two stage transistor amplifier has a gain of 10 for the first stage and a gain of 20 for the second stage. The overall gain of the cascade amplifier will be**

**Options:**

- A. 30
- B. 10
- C. 200
- D. 2

**Answer: C**

**Solution:**

**Solution:**

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## Question 73

**Long range radio transmission is possible when the radio waves are reflected from the ionosphere. For this to happen, the frequency of the radio waves must be in the range**

**Options:**

- A. 80 – 150 MHz
- B. 8 – 25 MHz
- C. 1 – 3 MHz
- D. 150 – 1500 kHz

**Answer: B**

**Solution:**

**Solution:**

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## Question 74

**The colour of a star is dependent on its**

**Options:**

- A. radius
- B. distance from the earth
- C. temperature
- D. structure

**Answer: C**

**Solution:**

**Solution:**

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## Question 75

**Hubble constant  $H$  has the dimensions of**

**Options:**

- A. mass
- B. length

C. ( time )<sup>-1</sup>

D. temperature

**Answer: C**

**Solution:**

**Solution:**

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## Question 76

**mole of water converted to steam at 373K is**

**Options:**

A. 109.1JK<sup>-1</sup>mol<sup>-1</sup>

B. 40.7 kJ mol<sup>-1</sup>

C. 81.4 kJ mol<sup>-1</sup>

D. 218.2JK<sup>-1</sup>mol<sup>-1</sup>

**Answer: A**

**Solution:**

**Solution:**

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## Question 77

**For a non-linear triatomic gas the value of the ratio of C<sub>p</sub> and C<sub>v</sub> at laboratory temperature is (assuming no vibrational contribution)**

**Options:**

A. 7 / 5

B. 9 / 7

C. 8 / 3

D. 4 / 3

**Answer: D**

**Solution:**

**Solution:**



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## Question 78

6 moles of  $\text{SO}_2$  and 6 moles of  $\text{O}_2$  are allowed to form  $\text{SO}_3$  in a closed vessel. At the equilibrium stage, 60% of  $\text{SO}_2$  is used up. The total number moles of the mixture at equilibrium is

**Options:**

- A. 10.2
- B. 9.8
- C. 7.2
- D. 11.2

**Answer: A**

**Solution:**

**Solution:**

---

## Question 79

pH of a solution obtained by mixing equal volumes of the solutions with pH 3 and pH 5 is

**Options:**

- A. 4.0
- B. 3.5
- C. 3.3
- D. 2.0

**Answer: C**

**Solution:**

**Solution:**

---

## Question 80

The  $K_{\text{sp}}$  of  $\text{AgCl}$  is  $1 \times 10^{-10}$ , its solubility in pure water in 0.01M  $\text{NaCl}$  is

**Options:**

- A.  $2 \times 10^{-10}$

B.  $1 \times 10^{-8}$

C.  $2 \times 10^{-8}$

D.  $1 \times 10^{-10}$

**Answer: B**

**Solution:**

**Solution:**

---

## Question 81

**The edge length of fcc unit cell is 508 pm. The radius of the atom is pm.**

**Options:**

A. 180

B. 200

C. 618

D. 288

**Answer: A**

**Solution:**

**Solution:**

---

## Question 82

**Crystalline solids having the least enthalpy of fusion is**

**Options:**

A. Molecular solid

B. Metallic solid

C. Ionic solid

D. Covalent solid

**Answer: A**

**Solution:**

**Solution:**

---

## Question 83

**Vapour pressure of water at 298K is 19.8 mm of Hg. 0.1 mole of glucose is dissolved in 172.8g of water. The vapour pressure of the solution is**

**Options:**

A. 19.6 mm

B. 16.9 mm

C. 19.0 mm

D. 18.9 mm

**Answer: A**

**Solution:**

**Solution:**

---

## Question 84

**Osmotic pressure of blood is 8.21 atm at 37°C. Amount of glucose that should be used per litre of intravenous injection that is at the same osmotic pressure of blood is**

**Options:**

A. 58.4g

B. 29.2g

C. 5.84g

D. 2.92g

**Answer: A**

**Solution:**

**Solution:**

---

## Question 85

**The equitant conductance of 1M benzoic acid is  $12.8 \text{ Scm}^2 \text{eq}^{-1}$  and if the limiting equivalent conductance of benzoate ion and  $\text{H}^+$  ion are 42 and  $288.42 \text{ Scm}^2 \text{eq}^{-1}$ , respectively, its degree of dissociation is**

**Options:**

- A. 39%
- B. 3.9%
- C. 0.35%
- D. 0.039%

**Answer: B**

**Solution:**

**Solution:**

---

## Question 86

Two half-cells of electrode potentials of  $E_1$  and  $E_2$  are combined to form a cell of potential  $E_3$ , ( $n_1$ ,  $n_2$  and  $n_3$  are number of electrons involved in first electrode, second electrode and the cell)  $E_3$  is

**Options:**

- A.  $E_3 = E_2 - E_1$
- B.  $E_3 = (E_1 n_1 + E_2 n_2) / n_3$
- C.  $E_3 = (E_1 n_1 - E_2 n_2) / n_3^2$
- D.  $E_3 = E_1 + E_2$

**Answer: A**

**Solution:**

**Solution:**

---

## Question 87

The potential of half-cell consisting of zinc electrode in 0.01M  $ZnSO_4$  solution at 25°C is ( $E^\circ = -0.763V$ )

**Options:**

- A.  $-0.8221V$
- B.  $-0.704V$
- C.  $-0.881V$
- D.  $-0.645V$

**Answer: A**

**Solution:**

**Solution:**

---

## Question 88

**A dilute aqueous solution of  $\text{CuSO}_4$  is electrolyzed using Pt electrodes. The products at the anode and cathode are**

**Options:**

A.  $\text{O}_2$ ,  $\text{H}_2$

B.  $\text{H}_2$ ,  $\text{O}_2$

C.  $\text{O}_2$ , Cu

D.  $\text{S}_2\text{O}_8^{2-}$ ,  $\text{H}_2$

**Answer: C**

**Solution:**

**Solution:**

---

## Question 89

**The half-life for radioactive decay of  $\text{C}^{14}$  is 5730 years. An archaeological artefact containing wood had only 80% of the  $\text{C}^{14}$  found in living tree. The age of the sample is**

**Options:**

A. 1845 years

B. 2865 years

C. 4584 years

D. 1146 years

**Answer: A**

**Solution:**

**Solution:**

---

## Question 90

If the volume of the reaction vessel is halved, for the reaction,  $2\text{SO}_2(\text{g}) + \text{O}_2(\text{g}) \rightarrow 2\text{SO}_3(\text{g})$ , then the rate is

Options:

- A.  $1 / 6^{\text{th}}$  of its initial value
- B.  $1 / 4^{\text{th}}$  of its initial value
- C. 8 times of its initial value
- D. 4 times of its initial value

**Answer: C**

**Solution:**

**Solution:**

-----

## Question 91

The rate equation for a reaction:  $\text{A} \rightarrow \text{B}$  is  $r = k[\text{A}]^0$ . If the initial concentration of the reactant is 'a'  $\text{mol dm}^{-3}$ , then half-life period of reaction is

Options:

- A.  $a / k$
- B.  $2a / k$
- C.  $a / 2k$
- D.  $k / a$

**Answer: C**

**Solution:**

**Solution:**

-----

## Question 92

The number of unit cells present in 39g of potassium that crystallizes as body centered cubic structure is  $N_A =$  Avogadro number)

Options:

- A.  $N_A$

B.  $0.25N_A$

C.  $0.5N_A$

D.  $0.75N_A$

**Answer: C**

**Solution:**

**Solution:**

---

## Question 93

**Which one of the following is not correctly matched?**

**Options:**

A.  $[\text{Ni}(\text{CN})_4]^{2-}$  –  $\text{dsp}^2$  hybridization, dia-magnetic

B.  $[\text{Cu}(\text{NH}_3)_4]^{2+}$  –  $\text{sp}^3$  hybridization, para-magnetic

C.  $[\text{NiCl}_4]^{2-}$  –  $\text{sp}^3$  hybridization, tetrahedral

D.  $[\text{CuCl}_4]^{2-}$  –  $\text{sp}^3$  hybridization, para-magnetic

**Answer: B**

**Solution:**

**Solution:**

---

## Question 94

**Which one of the following statements is not true according to Werner's theory of coordination compounds?**

**Options:**

A. Both primary and secondary valencies can be satisfied by anions

B. Secondary valency is non-directional

C. Primary valency is ionic valency

D. Metal ions exhibit two types of valencies

**Answer: B**

**Solution:**

**Solution:**

---

## Question 95

**Which one of the following is true regarding the energies of d-orbitals of tetragonally distorted octahedral geometry?**

**Options:**

A.  $d_{yz} > d_{xz} > d_{xy}$

B.  $d_{x^2-y^2} = d_{z^2}$

C.  $d_{xz} > d_{yz}$

D.  $d_{z^2} > d_{x^2-y^2}$

**Answer: D**

**Solution:**

**Solution:**

---

## Question 96

**In the estimation of Ca (II) ions, in the presence of ammonia-ammonium chloride buffer solution, EDTA acts as a ligand.**

**Options:**

A. flexidentate

B. pi-donor

C. hexadentate

D. tetradentate

**Answer: C**

**Solution:**

**Solution:**

---

## Question 97

**How much amount of oxalic acid dihydrate crystals are required to prepare 1L of a decinormal solution of it?**



**Options:**

- A. 6.3g
- B. 12.6g
- C. 3.15g
- D. 9g

**Answer: A**

**Solution:**

**Solution:**

-----

## Question 98

**What is correct order of increasing acidic strength of oxides of nitrogen?**

**Options:**

- A.  $\text{NO} < \text{N}_2\text{O}_3 < \text{N}_2\text{O}_4 < \text{N}_2\text{O}_5$
- B.  $\text{NO} = \text{N}_2\text{O}_3 < \text{N}_2\text{O}_4 = \text{N}_2\text{O}_5$
- C.  $\text{NO} > \text{N}_2\text{O}_3 < \text{N}_2\text{O}_4 > \text{N}_2\text{O}_5$
- D.  $\text{NO} > \text{N}_2\text{O}_3 > \text{N}_2\text{O}_4 > \text{N}_2\text{O}_5$

**Answer: A**

**Solution:**

**Solution:**

-----

## Question 99

**Regarding compounds of sulfur, which one of the following statements in not true?**

**Options:**

- A.  $\text{SF}_6$  does not undergo hydrolysis
- B.  $\text{SF}_4$  undergoes hydrolysis
- C.  $\text{SF}_6$  is thermally stable and chemically inert
- D.  $\text{SF}_4$  acts as Lewis acid

**Answer: D**

**Solution:**

**Solution:**

---

## Question 100

**Fluorine does not act as the central atom in interhalogen compounds, because**

**Options:**

- A. it is highly electronegative
- B. of absence of d-orbitals
- C. of its small size
- D. of its gaseous nature

**Answer: B**

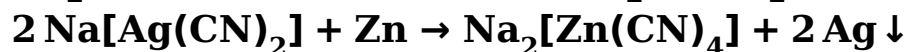
**Solution:**

**Solution:**

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## Question 101

**A hydrometallurgical process involves the following steps.**



**Which one of the following statements is true?**

**Options:**

- A. In the second step Zn (II) is reduced to Zn(0)
- B. Dicyanoargentum(I) complex is insoluble in water
- C. In the first step Ag(I) is reduced to Ag(0)
- D. Tetracyanozinc(II) complex is soluble in water

**Answer: D**

**Solution:**

**Solution:**

---

## Question 102

**Transition metals exhibit variable oxidation states. This is because**

**Options:**

- A. the outermost shell is empty
- B. they are all metals
- C. the energies of  $(n - 1)d$  and  $ns$  orbitals are almost equal
- D. the ionization energy to remove electron from  $ns$  orbital is very low

**Answer: C**

**Solution:**

**Solution:**

---

## Question 103

**The general electronic configuration of inner-transition elements is**

**Options:**

- A.  $(n - 2)f^{1 - 14}(n - 1)d^{0, 1}$
- B.  $(n - 2)f^{1 - 14}(n - 1)d^{0 - 1}n s^2$
- C.  $(n - 1)f^{1 - 14}(n - 1)d^{0 - 1}n s^2$
- D.  $(n - 2)f^{1 - 14}n s^2$

**Answer: B**

**Solution:**

**Solution:**

---

## Question 104

**Which of the following species would be diamagnetic?**

**Options:**

- A.  $\text{Cr}^{3+}$
- B.  $\text{Co}^{3+}$
- C. Br
- D.  $\text{Zn}^{2+}$

**Answer: D**

**Solution:**

**Solution:**

---

## Question 105

**Which orbital is designated by the quantum numbers:  
 $n = 5, l = 1, m_l = 0$  ?**

**Options:**

A. 5 s

B. 5p

C. 5d

D. 5f

**Answer: B**

**Solution:**

**Solution:**

---

## Question 106

**If travelling at equal speeds, which of the following matter waves have the longest wavelength?**

**Options:**

A. Electron

B. Proton

C. Neutron

D.  $\alpha$  particle

**Answer: A**

**Solution:**

**Solution:**

---

## Question 107

**Number of angular nodes for 4d orbital is**

**Options:**

- A. 4
- B. 3
- C. 2
- D. 1

**Answer: C**

**Solution:**

**Solution:**

-----

## Question 108

**Which of the following will not show deflection from the path on passing through electric field?**

**Options:**

- A. Electron
- B. Neutron
- C. Cathode rays
- D. Proton

**Answer: B**

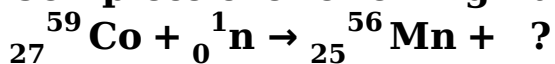
**Solution:**

**Solution:**

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## Question 109

**Complete the following nuclear equation:**



**Options:**

- A.  ${}_1^1\text{H}$
- B.  ${}_1^1\text{n}$
- C.  ${}_2^4\text{He}$

D.  $2_1^1\text{H}$

**Answer: C**

**Solution:**

**Solution:**

---

## Question 110

**Which among the following sequence is best suited for selective transformation on 2-methylbutane to 2-methylbutan-2-ol?**

**Options:**

A. Treatment with  $\text{Cl}_2$  in the presence of UV light followed by hydrolysis with potassium hydroxide in water

B. Treatment with  $\text{Cl}_2$  in the presence of UV light followed by hydrolysis with potassium hydroxide in ethanol

C. Treatment with  $\text{Br}_2$  in the presence of UV light followed by hydrolysis with potassium hydroxide in water

D. Treatment with  $\text{I}_2$  in the presence of UV light followed by hydrolysis with potassium hydroxide in a 1:1 mixture of water and ethanol

**Answer: D**

**Solution:**

**Solution:**

---

## Question 111

**Ozone depletion in Antartica is due to**

**Options:**

A. sulphur containing gases

B. peroxy acetyl nitrate

C. chlorine nitrate

D. fluorine

**Answer: C**

**Solution:**

**Solution:**

---

## Question 112

**When an organic compound ' A ' was treated sequentially with ammonia and  $\text{Br}_2$  / KOH, methanamine was obtained. Then ' A ' is an**

**Options:**

- A. ethanol
- B. ethyl acetate
- C. acetonitrile
- D. acetic acid

**Answer: B**

**Solution:**

**Solution:**

---

## Question 113

**How many structural isomers are possible for  $\text{C}_3\text{H}_9\text{N}$  ?**

**Options:**

- A. 3
- B. 4
- C. 5
- D. 6

**Answer: B**

**Solution:**

**Solution:**

---

## Question 114

**Which is a non-reducing sugar?**

**Options:**

- A. Glucose

- B. Sucrose
- C. Maltose
- D. Fructose

**Answer: B**

**Solution:**

**Solution:**

---

## Question 115

**0.200g of an organic compound contains 71% carbon. What is the mass of CO<sub>2</sub> produced when it is subjected to complete combustion?**

**Options:**

- A. 0.142
- B. 0.039
- C. 0.521
- D. 0.733

**Answer: C**

**Solution:**

**Solution:**

---

## Question 116

**Consider the following compounds:**

- (i) hydrazine**
- (ii) paracetamol**
- (iii) chlorophyll**
- (iv) saccharin**

**How many among them will test negative for nitrogen in Lassaigne's test ?**

**Options:**

- A. 1
- B. 2
- C. 3
- D. 4



**Answer: A**

**Solution:**

**Solution:**

---

## Question 117

**Which among the following is more reactive towards nitration using nitrating mixture?**

**Options:**

- A. tertiary-Butylbenzene
- B. Toluene
- C. Benzene
- D. Chlorobenzene

**Answer: B**

**Solution:**

**Solution:**

---

## Question 118

**Which among the following is antiaromatic?**

**Options:**

A.



B.



C.



D.



**Answer: A**

**Solution:**

**Solution:**

---

## Question 119

**Hydrogenation of acetyl chloride in the presence of Pd – BaSO<sub>4</sub> as catalyst to obtain ethanal is**

**Options:**

- A. Clemmensen reduction
- B. Rosenmund reduction
- C. Schmidt reaction
- D. Dakin reaction

**Answer: B**

**Solution:**

**Solution:**

---

## Question 120

**Which among the following compounds will selectively give the same addition product with HBr under both Markonikkoff's and anti-Markonikkoff's addition conditions?**

**Options:**

- A.  $\text{CH}_3 - \text{CH} = \text{CH} - \text{CH}_2 - \text{CH}_3$
- B.  $\text{CH}_3 - \text{CH} = \text{CH} - \text{C}(\text{CH}_3)_2$
- C.  $\text{CH}_3 - \text{CH} = \text{CH} - \text{CH}(\text{CH}_3)_2$
- D.  $\text{C}_6\text{H}_5 - \text{CH} = \text{CH}_2$

**Answer: C**

**Solution:**

**Solution:**

---

## Question 121

Among the following, the organic compound that gives propyne on treatment with sodamide with minimal side products is

Options:

- A.  $\text{CH}_3\text{CH}_2\text{CHCl}_2$
- B.  $\text{CH}_3\text{CCl}=\text{CH}_2$
- C.  $\text{CH}_3\text{CCl}=\text{CH}_2\text{Cl}$
- D.  $\text{CH}_3\text{CCl}_2-\text{CH}_3$

Answer: A

Solution:

Solution:

---

## Question 122

Which among the following tests is useful to differentiate between styrene and phenol?

Options:

- A. Lucas test
- B. Test with bromine water
- C. Test with bromine in dry chloroform
- D. Test with  $\text{KMnO}_4$

Answer: C

Solution:

Solution:

---

## Question 123

Identify the incorrect statement about natural rubber.

Options:

- A. Double bonds are located between  $\text{C}_2$  and  $\text{C}_3$  of each isoprene unit
- B. Has mostly trans double bonds

C. Intermolecular forces are quite weak

D. Has a randomly coiled structure

**Answer: B**

**Solution:**

**Solution:**

---

## Question 124

**The monomer unit/units in cellulose is/are**

**Options:**

A.  $\alpha$ -D-glucose

B.  $\beta$ -D-glucose

C. Alternating  $\alpha$ -D-glucose and D-fructose units

D. Alternating  $\beta$ -D-fructose and D-fructose units

**Answer: B**

**Solution:**

**Solution:**

---

## Question 125

**Which among the following vitamins is the most efficient antioxidant?**

**Options:**

A. Vitamin D

B. Vitamin C

C. Vitamin B

D. Vitamin A

**Answer: B**

**Solution:**

**Solution:**

---

## Question 126

Suppose  $\sqrt{\frac{1 + \cos A}{1 - \cos A}} = 2$ . Then  $\tan A =$

Options:

- A.  $\tan A < 1$
- B.  $\tan A > 2$
- C.  $\tan A > 1$
- D.  $\tan A = \infty$

Answer: C

Solution:

Solution:

---

## Question 127

Let  $a$  and  $b$  be non zero real numbers such that  $a^2 + b^2 = 1$ . Then

Options:

- A.  $a + b = 1$
- B.  $a + b \leq \sqrt{2}$
- C.  $a + b \geq \sqrt{2}$
- D.  $a + b = 2$

Answer: B

Solution:

Solution:

---

## Question 128

Let  $\tan^2 x = 2 \tan^2 y + 1$ . Then  $\sin^2 y =$

Options:

- A.  $\sin 2x$
- B.  $-\cos 2x$
- C.  $\cos 2x$

D.  $-\sin 2x$

**Answer: B**

**Solution:**

**Solution:**

---

## Question 129

Let  $\tan \alpha = \frac{x}{x+1}$  and  $\tan \beta = \frac{x+1}{x}$ . Then  $\alpha + \beta =$

**Options:**

A.  $\frac{\pi}{3}$

B.  $\frac{\pi}{6}$

C.  $\frac{\pi}{2}$

D.  $\frac{\pi}{4}$

**Answer: C**

**Solution:**

**Solution:**

---

## Question 130

Let  $a = \sin x$ ,  $b = \operatorname{cosec} x$  and  $a + b = 3$ . Then  $a^2 + b^2 =$

**Options:**

A. 3

B. 5

C. 7

D. 9

**Answer: C**

**Solution:**

**Solution:**

---

## Question 131

Suppose  $\frac{1 + \sin 2\theta}{1 - \sin 2\theta} = \cot^2(x + \theta)$ , then  $x$  is equal to

Options:

- A.  $\frac{\pi}{4}$
- B.  $\frac{\pi}{3}$
- C.  $\frac{2\pi}{3}$
- D.  $\frac{3\pi}{4}$

**Answer: D**

**Solution:**

**Solution:**

-----

## Question 132

The maximum value of  $5\sin^2 x + 4\cos^2 x + \sin \frac{x}{2} + \cos \frac{x}{2}$  is

Options:

- A.  $5 + 2\sqrt{2}$
- B.  $5 - 2\sqrt{2}$
- C.  $5 + \sqrt{2}$
- D.  $5 - \sqrt{2}$

**Answer: C**

**Solution:**

**Solution:**

-----

## Question 133

The chances to fail in Mathematics is 20% and the chances to fail in Chemistry is 25%. The chance to fail in at least one subject is

Options:

- A.  $\frac{11}{13}$

B.  $\frac{14}{15}$

C.  $\frac{2}{5}$

D.  $\frac{11}{12}$

**Answer: C**

**Solution:**

**Solution:**

---

## Question 134

**An urn contains 4 red and 6 blue balls. The probability that two balls are drawn in which second ball drawn is blue without replacements, is**

**Options:**

A.  $\frac{3}{5}$

B.  $\frac{4}{5}$

C.  $\frac{2}{5}$

D.  $\frac{7}{15}$

**Answer: A**

**Solution:**

**Solution:**

---

## Question 135

**The third moment about the mean for normal distribution is**

**Options:**

A.  $5\sigma$

B.  $3\sigma^2$

C.  $7\sigma^2$

D. 0

**Answer: D**



**Solution:**

**Solution:**

---

## Question 136

A box contains 24 identical balls of which 12 are white and remaining black. The balls are drawn at random from the box one at a time with replacement. The probability that a white ball is drawn for the 4<sup>th</sup> time on the 7<sup>th</sup> draw is

**Options:**

- A.  $\frac{6}{32}$
- B.  $\frac{5}{32}$
- C.  $\frac{7}{32}$
- D.  $\frac{1}{2}$

**Answer: B**

**Solution:**

**Solution:**

---

## Question 137

5 gentlemen and 5 ladies take seats at random round a table. The probability that they are sitting alternatively is

**Options:**

- A.  $\frac{3}{126}$
- B.  $\frac{1}{252}$
- C.  $\frac{1}{126}$
- D.  $\frac{3}{252}$

**Answer: C**

**Solution:**

**Solution:**

---

## Question 138

**Let A and B be two non-empty subsets of a set X such that A is not a subset of B. Then**

**Options:**

- A. A and B are disjoint
- B.  $B \subseteq A$
- C. A is the complement of B
- D. A and B may be disjoint

**Answer: D**

**Solution:**

**Solution:**

---

## Question 139

**Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be defined by  $f(x) = \cos 2x$ . Then f is**

**Options:**

- A. a one-to-one function
- B. an onto function
- C. both one-to-one and onto function
- D. neither one-to-one nor onto function

**Answer: D**

**Solution:**

**Solution:**

---

## Question 140

**Let  $f\left(z + \frac{1}{z}\right) = z^2 + \frac{1}{z^2}$  for all real  $z \in \mathbb{R} \backslash \{0\}$ . Then  $f(z) =$**

**Options:**

- A.  $z^2$

B.  $z^2 - 1$

C.  $z^2 - 2$  for all  $|z| \geq 2$

D.  $z^2 + 2$  for all  $|z| \geq 2$

**Answer: C**

**Solution:**

**Solution:**

---

## Question 141

**Define  $f(x) = |x - 1|$  for all real numbers  $x$ . Then**

**Options:**

A.  $f(x^2) = (f(x))^2$  for all  $x$

B.  $f(x + y) = f(x) + f(y)$  for all  $x, y$

C.  $f(|x|) = |f(x)|$  for all  $x$

D. All (A) to (C) above are not true

**Answer: D**

**Solution:**

**Solution:**

---

## Question 142

**The sum  $\sum_{i=1}^{\infty} \frac{1}{i!} \left( \sum_{k=1}^{i-1} \frac{1}{2^k} \right)$  is equal to**

**Options:**

A.  $e^2 - e$

B.  $e^2 + e$

C.  $e^2 + 1 / e$

D.  $e + 1 / e$

**Answer: A**

**Solution:**

**Solution:**

---

## Question 143

If  $S = \sum_{n=0}^{\infty} \frac{(\log x)^{2n}}{(2n)!}$ , then  $S =$

**Options:**

A.  $x + x^{-1}$

B.  $x - x^{-1}$

C.  $\frac{x + x^{-1}}{2}$

D. 0

**Answer: C**

**Solution:**

**Solution:**

---

## Question 144

The sum of the series  $\frac{2^2}{2!} + \frac{3^2}{3!} + \dots + \infty$  is

**Options:**

A.  $2e$

B.  $2e^2$

C.  $e / 2$

D.  $-e / 2$

**Answer: A**

**Solution:**

**Solution:**

---

## Question 145

If  $y = - \left( x^3 + \frac{x^6}{2} + \frac{x^9}{3} + \dots + \infty \right)$

**Options:**

A.  $x = 1 - e^y$

B.  $x = 1 + e^y$

C.  $x^3 = 1 - e^y$

D.  $x^3 = 1 + e^{-y}$

**Answer: C**

**Solution:**

**Solution:**

## Question 146

**Sum of the series**  $\frac{2}{1!} + \frac{4}{3!} + \frac{6}{5!} + \dots + \infty$

**Options:**

A.  $e$

B.  $e^2$

C.  $-e$

D.  $-e^2$

**Answer: A**

**Solution:**

**Solution:**

## Question 147

**The value of  $f(\theta) =$**   $\begin{vmatrix} \cos^2\theta & \cos\theta\sin\theta & \sin\theta \\ \cos\theta\sin\theta & \sin^2\theta & -\cos\theta \\ \sin\theta & -\cos\theta & 0 \end{vmatrix}$

**Options:**

A.  $0$

B.  $1$

C.  $-1$

D.  $2$

**Answer: C**

**Solution:**

**Solution:**

---

## Question 148

**If A is a skew-symmetric matrix of order n, then the trace of A is**

**Options:**

- A.  $n^2$
- B. n
- C. 0
- D. 1

**Answer: C**

**Solution:**

**Solution:**

---

## Question 149

**Suppose  $A = \begin{vmatrix} y-1 & 0 & 7 \\ y^2-1 & y-1 & 8 \\ 2y & 3y & 0 \end{vmatrix} = ay^3 + by^2 + cy + d$ . Then**

**Options:**

- A.  $c = -17, d = 0$
- B.  $b = 38, d = 0$
- C.  $a = -21, b = 38$
- D.  $a = 21, d = 0$

**Answer: D**

**Solution:**

**Solution:**

---

## Question 150

**Let  $A = \begin{bmatrix} 4x-7 & 2 & 2 \\ 2 & 4x-7 & 2 \\ 2 & 2 & 4x-7 \end{bmatrix}$ . One of the root of the equation  $|A| = 0$  is**

**Options:**

- A.  $3/4$
- B.  $-3/4$
- C.  $4/3$
- D.  $-4/3$

**Answer: A**

**Solution:**

**Solution:**

---

## Question 151

**Let A be the matrix  $\begin{bmatrix} -2 & 0 & 0 \\ 0 & -2 & 0 \\ 0 & 0 & -2 \end{bmatrix}$ . Then the value of  $|\text{adj } A|$  is equal to**

**Options:**

- A. 8
- B. 64
- C. 16
- D. 32

**Answer: B**

**Solution:**

**Solution:**

---

## Question 152

**Given that the matrix  $\begin{bmatrix} 1/36 & 0 \\ x & 1/36 \end{bmatrix} = \begin{bmatrix} 6 & 0 \\ -a & 6 \end{bmatrix}^{-2}$ . Then the value of x is**

**Options:**

A.  $\frac{a}{108}$

B.  $\frac{5a}{108}$

C.  $\frac{3a}{118}$

D.  $\frac{a}{118}$

**Answer: A**

**Solution:**

**Solution:**

-----

## Question 153

**For a positive integer n, the third term in the expansion of  $\left( \sqrt[4]{a} + \frac{a}{\sqrt{a^{-1}}} \right)^n$  is  $15a^4$ . Then the value of n is**

**Options:**

A. 6

B. -5

C. 3

D. 15

**Answer: A**

**Solution:**

**Solution:**

-----

## Question 154

**$\sum_{i=0}^k \frac{{}^iC_i}{{}^kC_{i-1}}$  is equal to**

**Options:**

A.  $\frac{k(2k+1)}{2}$

B.  $\frac{k(k+1)}{2}$



C.  $\frac{k(2k-1)}{2}$

D.  $\frac{k(k^2+1)}{2}$

**Answer: B**

**Solution:**

**Solution:**

-----

## Question 155

**The coefficient of  $x^8$  in the expansion of  $[(1+x)^7 + (1+x)^8 + \dots + (1+x)^{14}]$**

**Options:**

A.  $^{15}C_8$

B.  $^{15}C_6$

C.  $^{15}C_4$

D.  $^{15}C_5$

**Answer: B**

**Solution:**

**Solution:**

-----

## Question 156

**Given that the coefficient of  $x^7$  and  $x^8$  in the expansion of  $\left(2 + \frac{x}{4}\right)^n$  are equal. Then  $n =$**

**Options:**

A. 91

B. 8.7!

C. 71

D. 7.8!

**Answer: C**

**Solution:**

**Solution:**

---

## Question 157

**Number of terms in the expansion of  $(y^2 + \sqrt{y^2 - 1})^4 + (y^2 - \sqrt{y^2 - 1})^4$  is**

**Options:**

A. 10

B. 8

C. 6

D. 5

**Answer: D**

**Solution:**

**Solution:**

---

## Question 158

**There are 5 letters and 5 different envelopes. The number of ways in which all the letters can be put in wrong envelope is**

**Options:**

A. 119

B. 44

C. 59

D. 40

**Answer: B**

**Solution:**

**Solution:**

---

## Question 159

**The number of diagonals in an octagon will be**

**Options:**

- A. 12
- B. 16
- C. 18
- D. 20

**Answer: D**

**Solution:**

**Solution:**

---

## Question 160

**The number of divisors of the form  $4n + 2$  ( $n \geq 0$ ) of the integer 240 is equal to**

**Options:**

- A. 3
- B. 4
- C. 12
- D. 15

**Answer: B**

**Solution:**

**Solution:**

---

## Question 161

**There are three coplanar parallel lines. If any  $p$  points are taken on each of the lines, the maximum number of triangles with vertices at these points is**

**Options:**

- A.  $p^2(p + 3)$
- B.  $p^2(p - 3)$
- C.  $p^2(4p + 3)$
- D.  $p^2(4p - 3)$

**Answer: D**

**Solution:**

**Solution:**

---

## Question 162

**In class of 18 students, every student has to hand shake with every other student. The total number of handshakes was**

**Options:**

- A. 17
- B. 18
- C. 153
- D. 306

**Answer: C**

**Solution:**

**Solution:**

---

## Question 163

**Total number of numbers that are less than  $4 \cdot 10^6$  and can be formed using the digits 1, 2, 3 is equal to**

**Options:**

- A.  $\frac{9 \cdot 3^8 + 3}{2}$
- B.  $\frac{9 \cdot 3^8 - 2}{3}$
- C.  $\frac{9 \cdot 3^8 + 3}{3}$
- D.  $\frac{9 \cdot 3^8 - 3}{2}$

**Answer: D**

**Solution:**

**Solution:**

---

## Question 164

A variable name in certain computer language must be either an alphabet or an alphabet followed by a decimal digit. Total number of different variable names that can exist in that language is equal to

Options:

- A. 280
- B. 286
- C. 290
- D. 296

**Answer: B**

**Solution:**

**Solution:**

---

## Question 165

Let  $X = \{ a \mid a \text{ is a prime number and } a < 30 \}$ . The number of different rational numbers whose numerator and denominator belong to  $X$  is

Options:

- A. 90
- B. 91
- C. 180
- D. 181

**Answer: B**

**Solution:**

**Solution:**

---

## Question 166

Let  $z^2 - z + 1 = 0$  and  $z$  be a complex number. Then the value of  $z^n - z^{-n}$ , where  $n$  is a multiple of 3 is

Options:

A.  $2(-1)^n$

B.  $2^n$

C.  $(-1)^{n+1}$

D. 0

**Answer: D**

**Solution:**

**Solution:**

---

## Question 167

Assume that  $(1 + i)(1 + 2i)(1 + 3i) \dots (1 + xi) = \alpha + i\beta$ . Then  $2.5.10 \dots (1 + x^2)$  is equal to

**Options:**

A.  $\alpha^2 - \beta^2$

B.  $\alpha^2 + \beta^2$

C.  $\alpha - i\beta$

D.  $\alpha \cdot \beta$

**Answer: B**

**Solution:**

**Solution:**

---

## Question 168

If  $\omega$  is a cube root of unity, then  $(3 + 5\omega + 3\omega^2)^2 + (3 + 3\omega + 5\omega^2)^2$  is equal to

**Options:**

A. -2

B. 2

C. 4

D. -4

**Answer: D**

**Solution:**

**Solution:**

---

## Question 169

$\cos \left( i \log \left( \frac{x - iy}{x + iy} \right) \right)$  is equal to

**Options:**

A.  $\frac{x^2 - y^2}{x^2 + y^2}$

B.  $\frac{xy}{x^2 + y^2}$

C.  $\frac{x^2 - y^2}{2xy}$

D.  $\frac{2xy}{x^2 + y^2}$

**Answer: A**

**Solution:**

**Solution:**

---

## Question 170

Let  $z$  be a complex number satisfying the relation  $|z - 36|^2 = 36z - 1|^2$ . Then  $|z|$  is equal to

**Options:**

A. 5

B. 6

C. 7

D. 8

**Answer: B**

**Solution:**

**Solution:**

---

## Question 171

**If  $z$  is a complex number such that  $\left| \frac{z-1}{z+1} \right| = 0$  is purely real. Then**

**Options:**

- A.  $z$  is purely imaginary
- B.  $z$  is purely real
- C.  $|z| = 1$
- D.  $\operatorname{Re}(z) \neq 0$  and  $\operatorname{Im}(z) \neq 0$

**Answer: B**

**Solution:**

**Solution:**

---

## Question 172

**The product of all values of  $(\cos x + i \sin x)^{\frac{3}{4}}$  is**

**Options:**

- A.  $(\cos 4x + i \sin 4x)$
- B.  $(\cos 4x - i \sin 4x)$
- C.  $(\cos 3x - i \sin 3x)$
- D.  $(\cos 3x + i \sin 3x)$

**Answer: D**

**Solution:**

**Solution:**

---

## Question 173

**Let  $z$  be a complex number such that  $|z + 4| \leq 3$ . Then**

**Options:**

- A.  $|z + 1| = 6$
- B.  $0 \leq |z + 1| \leq 6$
- C.  $|z + 1| = 0$
- D.  $3 \leq |z + 1| \leq 6$



**Answer: B**

**Solution:**

**Solution:**

---

## Question 174

**Let  $a, b, c > 0$ . Then  $a(1 - b) > \frac{1}{4}$ ,  $b(1 - c) > \frac{1}{4}$ ,  $c(1 - a) > \frac{1}{4}$**

**Options:**

- A. are never possible
- B. are always possible
- C. are sometimes possible
- D. cannot be discussed

**Answer: A**

**Solution:**

**Solution:**

---

## Question 175

**The inequality  $\frac{2}{x} < 3$  is true, when  $x$  belongs to**

**Options:**

- A.  $[2 / 3, \infty)$
- B.  $(-\infty, 2 / 3]$
- C.  $(2 / 3, \infty) \cup (-\infty, 0)$
- D.  $(-\infty, 0)$

**Answer: C**

**Solution:**

**Solution:**

---

## Question 176

Let  $\alpha \in \left(0, \frac{\pi}{2}\right)$ . The value of the expression  $\sqrt{x^2 + x} + \frac{\sin^2 \alpha}{\sqrt{x^2 + x}}$  is always greater than or equal to

Options:

- A. 1
- B. 2
- C.  $2\sin \alpha$
- D.  $2 \operatorname{cosec} \alpha$

**Answer: C**

**Solution:**

**Solution:**

---

## Question 177

Solutions of  $2y - 3 = |y + 6|$  are

Options:

- A.  $-1, -1$
- B.  $1, -1$
- C.  $-1, 9$
- D. 9

**Answer: D**

**Solution:**

**Solution:**

---

## Question 178

If  $a \in \mathbb{R}$  and  $m = \frac{a^2}{1 + a^4}$  is real, then

Options:

- A.  $0 \leq m \leq \frac{1}{2}$
- B.  $0 \leq m \leq 1$
- C.  $0 \leq m \leq 2$

D.  $0 \leq m \leq \infty$

**Answer: A**

**Solution:**

**Solution:**

---

## Question 179

**Let a, b, c be three distinct numbers which are in a Geometric Progression. Also the numbers a, 2b, 3c are in an Arithmetic Progression. Then the common ratio of the Geometric Progression is**

**Options:**

A. 3

B. 1

C.  $\frac{2}{3}$

D.  $\frac{1}{3}$

**Answer: D**

**Solution:**

**Solution:**

---

## Question 180

**Three positive real numbers x, y, z are in Arithmetic Progression and  $xyz = 4$ . The the minimum value of y is**

**Options:**

A.  $\sqrt{2}$

B.  $\sqrt[3]{2}$

C.  $2^{1/3}$

D.  $2^{2/3}$

**Answer: D**

**Solution:**

**Solution:**

---

## Question 181

The maximum possible integer value of sum  $15 + 14\frac{1}{7} + 13\frac{2}{7} + \dots$  is

Options:

- A. 134
- B. 136
- C. 138
- D. 140

**Answer: C**

**Solution:**

**Solution:**

---

## Question 182

Let  $S_n$  denotes the sum of  $n$  terms of an Arithmetic Progression. Then the value of  $S_{n+3} - 5S_{n+2} + 7S_{n+1} - 3S_n$  is

Options:

- A. 0
- B. 3
- C. 6
- D. 9

**Answer: A**

**Solution:**

**Solution:**

---

## Question 183

The sum of 10 terms of the series  $\sqrt{3} + \sqrt{12} + \sqrt{48} + \dots$

Options:

- A.  $S = 1023\sqrt{3}$

B.  $S = 1023\sqrt{2}$

C.  $S = 1025\sqrt{2}$

D.  $S = 1025\sqrt{3}$

**Answer: A**

**Solution:**

**Solution:**

---

## Question 184

The harmonic mean of two numbers is 8 . Also their arithmetic mean is A and geometric mean is G. If G satisfies  $2A + G^2 = 90$ , then the numbers are

**Options:**

A. 2, -2

B. 6, -12

C. 2,12

D. 6,12

**Answer: D**

**Solution:**

**Solution:**

---

## Question 185

The harmonic mean of two numbers is 8 . Also their arithmetic mean is A and geometric mean is G. If G satisfies  $2A + G^2 = 90$ , then the numbers are

**Options:**

A. 2, -2

B. 6, -12

C. 2,12

D. 6,12

**Answer: B**

**Solution:**

**Solution:**

---

## Question 186

The equation  $\sqrt{y+2-4\sqrt{y-2}} + \sqrt{y+7-6\sqrt{y-2}} = 1$  has

**Options:**

- A. no solution
- B. one solution
- C. two solutions
- D. more than two solutions

**Answer: D**

**Solution:**

**Solution:**

---

## Question 187

Let  $\alpha$  and  $\beta$  be the roots of the equation  $my^2 - ny - p = 0$ . Then the root of the equation  $(m + px)^2 = n^2x$  are

**Options:**

- A.  $\alpha + \beta, \alpha - \beta$
- B.  $\frac{1}{\alpha^2}, \frac{1}{\beta^2}$
- C.  $\frac{1}{\alpha^2}, -\frac{1}{\beta^2}$
- D.  $\alpha^2, \beta^2$

**Answer: B**

**Solution:**

**Solution:**

---

## Question 188

If the roots of the equation  $y^2 - 2my + m^2 + m - 3 = 0$  are real and less than 3 , then

Options:

- A.  $m = 1$
- B.  $m < -1$
- C.  $m = 2$
- D.  $m < 2$

Answer: D

Solution:

Solution:

-----

## Question 189

Let  $\beta, \beta^2$  be the roots of the equation  $y^2 + 4y + 1 = 0$ . Then  $\beta^{46}, \beta^{62}$  are roots of the equation

Options:

- A.  $y^2 + 4y + 1 = 0$
- B.  $y^2 - 4y + 1 = 0$
- C.  $y^2 - 4y - 1 = 0$
- D.  $y^2 + 4y - 1 = 0$

Answer: A

Solution:

Solution:

-----

## Question 190

The number of real solutions of the equation  $\left(\frac{7}{13}\right)^x = -13 + x - x^2$  is

Options:

- A. 3
- B. 2
- C. 1

D. 0

**Answer: D**

**Solution:**

**Solution:**

---

## Question 191

**Given that the sum of the squares of the roots of the equation  $y^2 - (k - 3)y - k - 2 = 0$  is 13 . Then number of values of k lying in the interval  $[1, 4]$  is**

**Options:**

A. 0

B. 1

C. 2

D. 3

**Answer: B**

**Solution:**

**Solution:**

---

## Question 192

**Let  $8^{\sin^2 x} + 8^{\cos^2 x} = 6$ . Then**

**Options:**

A.  $\sin^2 x = \frac{2}{3}$

B.  $\sin x = -\frac{1}{3}$

C.  $\cos^2 x = \frac{1}{2}$

D.  $\cos x = -\frac{1}{2}$

**Answer: A**

**Solution:**

**Solution:**



---

## Question 193

The equation  $|\sin x| = 2 \cos x$  has

Options:

- A. infinitely many solutions
- B. finitely many solutions
- C. has no solutions in integers
- D. has no solutions

**Answer: D**

**Solution:**

**Solution:**

---

## Question 194

The value of  $x$  satisfying  $1 + \cos x + \cos^2 x + \dots = 4 + 2\sqrt{3}$  in the interval  $\left[ \frac{\pi}{2}, \pi \right]$  is

Options:

- A.  $\frac{2\pi}{3}$
- B.  $\frac{\pi}{2}$
- C.  $\frac{4\pi}{5}$
- D.  $\frac{3\pi}{4}$

**Answer: A**

**Solution:**

**Solution:**

---

## Question 195

In a triangle ABC, let  $\frac{2 \cos A}{a} + \frac{\cos B}{b} + \frac{2 \cos C}{c} = \frac{a}{bc} + \frac{b}{ac}$ . Then  $b^2 + c^2$  is equal to

**Options:**

- A.  $a^2$
- B.  $ac$
- C.  $bc$
- D.  $a + b$

**Answer: A**

**Solution:**

**Solution:**

-----

## Question 196

**In a triangle ABC, let  $\frac{2 \cos A}{a} + \frac{\cos B}{b} + \frac{2 \cos C}{c} = \frac{a}{bc} + \frac{b}{ac}$ . Then  $b^2 + c^2$  is equal to**

**Options:**

- A.  $a^2$
- B.  $ac$
- C.  $bc$
- D.  $a + b$

**Answer: B**

**Solution:**

**Solution:**

-----

## Question 197

**If the sides of a triangle are proportional to the cosines of the opposite angles, then**

**Options:**

- A. the triangle is right angled
- B. the triangle is isosceles
- C. the triangle is equilateral
- D. one of the angle is obtuse

**Answer: C**

**Solution:**

**Solution:**

---

## Question 198

Let  $a = 7$ ,  $b = 4$ ,  $c = 9a$  in a  $\triangle ABC$ . Then the values of  $\sin \frac{A}{2}$  and  $\cos A$  are equal to respectively

**Options:**

A.  $\sqrt{\frac{4}{13}}$  and  $\frac{9}{13}$

B.  $\sqrt{\frac{5}{13}}$  and  $\frac{8}{13}$

C.  $\sqrt{\frac{7}{13}}$  and  $\frac{6}{13}$

D.  $\sqrt{\frac{6}{13}}$  and  $\frac{7}{13}$

**Answer: D**

**Solution:**

**Solution:**

---

## Question 199

Given that the lengths of the sides  $p$ ,  $q$ ,  $r$  of a  $\triangle PQR$  are in an Arithmetic Progression. Then the ration  $\frac{q}{r}$  lies in the interval

**Options:**

A.  $\left( \frac{1}{3}, \frac{2}{3} \right)$

B.  $\left( \frac{2}{3}, 2 \right)$

C.  $\left( \frac{2}{3}, 1 \right)$

D.  $\left( \frac{1}{3}, \frac{4}{3} \right)$

**Answer: B**

**Solution:**

**Solution:**

---

## Question 200

The two adjacent sides AB and BC of a cyclic quadrilateral ABCD are 2 and 5 units respectively and the angle between them is  $60^\circ$ . Then the area of circle circumscribing the quadrilateral ABCD is

**Options:**

A.  $\frac{9\pi}{2}$

B.  $\frac{19\pi}{2}$

C.  $\frac{9\pi}{3}$

D.  $\frac{19\pi}{3}$

**Answer: D**

**Solution:**

**Solution:**

---

## Question 201

In a  $\triangle ABC$ ,  $2a^2 + 9b^2 + c^2 = 6ab + 2ac$ , then  $\cos C$  is equal to

**Options:**

A.  $1/2$

B.  $1/3$

C.  $1/4$

D.  $1/6$

**Answer: D**

**Solution:**

**Solution:**

---

## Question 202

**In the  $\triangle ABC$ ,  $(a + b + c) \left( \tan \frac{A}{2} + \tan \frac{B}{2} \right)$  is equal to**

**Options:**

A.  $2c \cot \frac{C}{2}$

B.  $2a \cot \frac{A}{2}$

C.  $2b \cot \frac{B}{2}$

D.  $\tan \frac{C}{2}$

**Answer: A**

**Solution:**

**Solution:**

---

## Question 203

**$\sin \left[ \frac{\pi}{6} - \sin^{-1} \left( -\frac{1}{2} \right) \right]$  is equal to**

**Options:**

A. 0

B.  $\infty$

C. 1

D. -1

**Answer: C**

**Solution:**

**Solution:**

---

## Question 204

**If  $\sin A + \cos B = a$  and  $\sin B + \cos A = b$ ,  $\sin (A + B)$  is equal to**

**Options:**

A.  $\frac{a^2 + b^2 - 2}{2}$

B.  $\frac{a^2 + b^2 + 2}{2}$

C.  $\frac{a^2 - b^2 + 2}{2}$

D.  $\frac{a^2 - b^2 - 2}{2}$

**Answer: A**

**Solution:**

**Solution:**

---

## Question 205

**The first and last terms of an Arithmetic Progression are 1 and 56. If the sum of its terms is 290 , then the number of terms will be**

**Options:**

A. 4

B. 6

C. 8

D. 10

**Answer: D**

**Solution:**

**Solution:**

---

## Question 206

**Suppose A is a point which is at equidistant from X (1, 3), Y (−3, 5) and Z (5, −1). Then the point A is**

**Options:**

A. (−8, −10)

B. (8, −10)

C. (−8, 10)

D. (8, 10)

**Answer: A**

**Solution:**

**Solution:**

---

## Question 207

The midpoint of the line joining  $(-6, 4)$  and  $(8, -6)$  divides the line joining  $(3, 6)$  and  $(-6, -3)$  in the ratio

**Options:**

- A. 2:7 externally
- B. 2:7 internally
- C. 3:7 internally
- D. 3:7 externally

**Answer: B**

**Solution:**

**Solution:**

---

## Question 208

The sum of the distances from a point to the two perpendicular lines is 2 . The locus of the point is

**Options:**

- A. a square
- B. a pair of straight lines
- C. an ellipse
- D. a parabola

**Answer: A**

**Solution:**

**Solution:**

---

## Question 209

If a point  $P(2, 1)$  is shifted by a distance  $\sqrt{2}$  units parallel to the line  $x + y = 0$ , then the new position of P is

**Options:**

- A.  $(-1, 2)$

B.  $(-1, -2)$

C.  $(1, -2)$

D.  $(1, 2)$

**Answer: D**

**Solution:**

**Solution:**

-----

## Question 210

The length of the common chord of intersection of the circles  $x^2 + y^2 - 2x + 4y - 4 = 0$  and  $x^2 + y^2 - 2x - 6y + 6 = 0$  is

**Options:**

A. 0

B. 1

C. 2

D. 3

**Answer: A**

**Solution:**

**Solution:**

-----

## Question 211

The equation of the tangents to the circle  $x^2 + y^2 = 25$  with 3 as x coordinate are

**Options:**

A.  $3x \pm 5y = 25$

B.  $3x \pm 4y = 5$

C.  $3x \pm 4y = 25$

D.  $3x \pm 5y = 5$

**Answer: C**

**Solution:**



**Solution:**

---

## Question 212

**The equation of the circumcircle of the triangle formed by the lines  $x = 2$ ,  $y = 0$  and  $x + y - 6 = 0$  is**

**Options:**

A.  $x^2 + y^2 + 8x - 4y - 12 = 0$

B.  $x^2 + y^2 - 8x - 4y - 12 = 0$

C.  $x^2 + y^2 - 8x - 4y + 12 = 0$

D.  $x^2 + y^2 + 8x - 4y + 12 = 0$

**Answer: C**

**Solution:**

**Solution:**

---

## Question 213

**The equation of a parabola is  $y^2 = 4x$ .  $P(1, 3)$  and  $Q(1, 1)$  are two points in the  $xy$ -plane. Then, for the parabola**

**Options:**

A.  $P$  and  $Q$  are exterior points

B.  $P$  is an interior point while  $Q$  is an exterior point

C.  $P$  and  $Q$  are interior points

D.  $P$  is an exterior point while  $Q$  is an interior point

**Answer: D**

**Solution:**

**Solution:**

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## Question 214

**A circle having its center at  $(2, 3)$  is cut orthogonally by the parabola  $y^2 = 4x$ . The possible intersection point of these curves can be**

**Options:**

- A. (1, 2) or (3,  $3\sqrt{3}$ )
- B. (9, 6) or (2,  $2\sqrt{2}$ )
- C. (1, 2) or (4, 4)
- D. (1, 3) or (2,  $2\sqrt{2}$ )

**Answer: C**

**Solution:**

**Solution:**

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## Question 215

If the polar of  $y^2 = 4ax$  is always touching the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ , then the locus of the pole is

**Options:**

- A.  $4a^2x^2 + b^2y^2 = 4a^4$
- B.  $4a^2x^2 - b^2y^2 = 4a^4$
- C.  $4a^2x^2 - b^2y^2 = 4b^4$
- D.  $4a^2x^2 - b^2y^2 = 4b^4$

**Answer: B**

**Solution:**

**Solution:**

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## Question 216

The radius of the circle passing through the foci of the ellipse  $\frac{x^2}{16} + \frac{y^2}{9} = 1$  and having its center (0, 3) is

**Options:**

- A. 4
- B. 3
- C.  $\sqrt{12}$
- D.  $\frac{7}{2}$

**Answer: A**

**Solution:**

**Solution:**

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## Question 217

**The equation to the hyperbola having its eccentricity 2 and the distance between foci as 8 , is**

**Options:**

A.  $\frac{x^2}{4} - \frac{y^2}{12} = 1$

B.  $\frac{x^2}{12} - \frac{y^2}{4} = 1$

C.  $\frac{x^2}{2} - \frac{y^2}{4} = 1$

D.  $\frac{x^2}{4} - \frac{y^2}{2} = 1$

**Answer: A**

**Solution:**

**Solution:**

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## Question 218

**The equation of the hyperbola whose vertices are at (5, 0) and (−5, 0) and  $x = \frac{25}{7}$  as one of its directrices, is**

**Options:**

A.  $\frac{x^2}{25} - \frac{y^2}{24} = 1$

B.  $\frac{x^2}{24} - \frac{y^2}{25} = 1$

C.  $\frac{x^2}{16} - \frac{y^2}{25} = 1$

D.  $\frac{x^2}{25} - \frac{y^2}{16} = 1$

**Answer: A**

**Solution:**

**Solution:**

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## Question 219

$\frac{d}{dx} \left\{ \tan^{-1} \left( \frac{3x - x^3}{1 - 3x^2} \right) \right\}$  is equal to

**Options:**

A.  $\frac{3}{1 + 9x^2} \forall |x| < \frac{1}{\sqrt{3}}$

B.  $\frac{9}{1 + x^2} \forall |x| < \frac{1}{\sqrt{3}}$

C.  $\frac{3}{1 + x^2} \forall |x| < \frac{1}{\sqrt{3}}$

D.  $\frac{1}{9 + x^2} \forall |x| < \frac{1}{\sqrt{3}}$

**Answer: C**

**Solution:**

**Solution:**

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## Question 220

Let  $x = \sec\theta - \cos\theta$  and  $y = \sec^2\theta - \cos^2\theta$ . Then  $\left( \frac{dy}{dx} \right)^2 =$

**Options:**

A.  $\frac{4(y^2 - 4)}{x^2 + 4}$

B.  $\frac{4(y^2 + 4)}{x^2 + 4}$

C.  $\frac{4(y^2 - 4)}{x^2 - 4}$

D.  $\frac{4(y^2 + 4)}{x^2 - 4}$

**Answer: B**

**Solution:**

**Solution:**

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## Question 221

**Given that the line  $y = 3x + c$  touches the curve  $\frac{x^2}{4} + \frac{y^2}{9} = 1$ . The value of  $c$  is**

**Options:**

- A. an integer
- B. always a rational number
- C. always an irrational number
- D. sometimes a rational number

**Answer: C**

**Solution:**

**Solution:**

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## Question 222

**Let  $f(x) = |\cos x| + |\sin x|$ . Then  $f'(2\pi/3) =$**

**Options:**

- A.  $\frac{1 - \sqrt{3}}{2}$
- B.  $\frac{\sqrt{3} - 1}{2}$
- C. 0
- D.  $\frac{\sqrt{3} + 1}{2}$

**Answer: B**

**Solution:**

**Solution:**

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## Question 223

**If  $x = a \left\{ \cos \theta + \log \tan \left( \frac{\theta}{2} \right) \right\}$  and  $y = a \sin \theta$ , then  $\frac{dy}{dx}$  is**

**Options:**

- A.  $\cot \theta$
- B.  $\tan \theta$
- C.  $\sin \theta$

D.  $\cos \theta$

**Answer: B**

**Solution:**

**Solution:**

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## Question 224

If  $f(x) = |x - 1|$  &  $g(x) = f(f(x))$ , then, for all  $x \geq 2$ ,  $g'(x) =$

**Options:**

A. 1

B. 2

C. -1

D. 0

**Answer: A**

**Solution:**

**Solution:**

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## Question 225

If  $y = \sin[\cos^{-1}\{\sin(\cos^{-1}x)\}]$ , then  $\frac{dy}{dx}$  at  $x = \frac{1}{2}$  is equal to

**Options:**

A. 0

B. 1

C.  $2/\sqrt{3}$

D. -1

**Answer: B**

**Solution:**

**Solution:**

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## Question 226

The function  $f(x) = \sqrt{\log_{10}\left(\frac{5x - x^2}{4}\right)}$  exists for

Options:

A.  $[1, 4]$

B.  $[1, 0]$

C.  $[0, 5]$

D.  $[5, 0]$

Answer: A

Solution:

Solution:

---

## Question 227

The range of the function  $f(x) = \frac{x+3}{|x+3|}$ ,  $x \neq -3$  is

Options:

A.  $\{0\}$

B.  $\{0, 1\}$

C.  $\{-3, 3\}$

D.  $\{-1, 1\}$

Answer: D

Solution:

Solution:

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## Question 228

The period of the function  $f(x) = \cos \frac{2x}{7} + \sin \frac{x}{2}$  is

Options:

A.  $7\pi$

B.  $4\pi$

C.  $14\pi$

D.  $28\pi$

**Answer: D**

**Solution:**

**Solution:**

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## Question 229

Let  $f: R \rightarrow R$  be defined as  $f(x) = \begin{cases} 0, & x \text{ is irrational} \\ \sin |x|, & x \text{ is rational} \end{cases}$ .

Then which of the following is true?

**Options:**

- (A)  $f$  is discontinuous for all  $x$
- (B)  $f$  is continuous for all  $x$
- (C)  $f$  is discontinuous at  $x = k\pi$ , where  $k$  is an integer
- (D)  $f$  is continuous at  $x = k\pi$ , where  $k$  is an integer

**Answer: D**

**Solution:**

**Solution:**

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## Question 230

The period of the function  $f(x) = \operatorname{cosec}^3 3x + \cot 4x$  is

**Options:**

- A.  $\frac{\pi}{3}$
- B.  $\frac{\pi}{4}$
- C.  $\frac{\pi}{6}$
- D.  $\pi$

**Answer: D**

**Solution:**

**Solution:**

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## Question 231



$\lim_{x \rightarrow \infty} \left( \frac{x+7}{x+3} \right)^{x+2}$  is equal to

**Options:**

- A.  $e^2$
- B.  $e^4$
- C.  $e^{-4}$
- D.  $e^{-2}$

**Answer: B**

**Solution:**

**Solution:**

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## Question 232

Let  $m, n$  be natural numbers with  $n > m$  .  $\lim_{x \rightarrow 0} \frac{\sin x^n}{(\sin x)^m}$  is equal to

**Options:**

- A. 2
- B. -2
- C. -1
- D. 0

**Answer: D**

**Solution:**

**Solution:**

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## Question 233

$\lim_{x \rightarrow \frac{\pi}{2}} \frac{\sin x - (\sin x)^{\sin x}}{1 - \sin x + \log \sin x}$

**Options:**

- A. 1
- B. 2
- C. 3

D. 4

**Answer: B**

**Solution:**

**Solution:**

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## Question 234

If the curve  $y = x^2 + bx + c$  touches the line  $y = x$  at the point (1, 1), then the values of  $x$  for which the curve has a negative gradient are

**Options:**

A.  $x > \frac{3}{2}$

B.  $x < \frac{3}{2}$

C.  $x > \frac{1}{2}$

D.  $x < \frac{1}{2}$

**Answer: D**

**Solution:**

**Solution:**

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## Question 235

The sub tangent, ordinate and sub normal to the parabola  $y^2 = 4ax$  at a point (different from the origin) are

**Options:**

A. in Harmonic Progression

B. in Geometric Progression

C. in Arithmetic Progression

D. equal

**Answer: B**

**Solution:**

**Solution:**

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## Question 236

If  $0 < x < \frac{\pi}{2}$ , then

Options:

A.  $\cos(\sin x) < \sin(\cos x)$

B.  $\sin(\cos x) > \cos x$

C.  $\cos(\sin x) > \sin(\cos x)$

D.  $\cos(\sin x) \leq \cos x$

**Answer: C**

**Solution:**

**Solution:**

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## Question 237

The minimum value of  $e^{(2x^2 + 2x + 1)\sin^2 x}$  is

Options:

A. 0

B. 1

C. 2

D. 3

**Answer: B**

**Solution:**

**Solution:**

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## Question 238

$\int \frac{dx}{x^2 + 4x + 5}$  is equal to

Options:

A.  $\frac{1}{2} \left\{ \tan^{-1}(x + 2) + \frac{x + 2}{x^2 + 4x + 5} \right\} + c$

B.  $\frac{1}{2} \left\{ \tan^{-1}(x + 2) + \frac{x}{x^2 + 4x + 5} \right\} + c$

C.  $\frac{1}{2} \left\{ \tan^{-1}(x + 2) + \frac{x - 2}{x^2 + 4x + 5} \right\} + c$

D.  $\frac{1}{2} \left\{ \tan^{-1}(x - 2) + \frac{x}{x^2 + 4x + 5} \right\} + c$

**Answer: A**

**Solution:**

**Solution:**

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## Question 239

$\int \left( \frac{x+2}{x+4} \right)^2 e^x dx$  is equal to

**Options:**

A.  $e^x \left( \frac{x}{x+4} \right) + c$

B.  $e^x \left( \frac{x+2}{x+4} \right) + c$

C.  $e^x \left( \frac{x-2}{x+4} \right) + c$

D.  $e^x \left( \frac{2xe^x}{x+4} \right) + c$

**Answer: A**

**Solution:**

**Solution:**

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## Question 240

The value of  $I = \int_0^1 x \left| x - \frac{1}{2} \right| dx$  is equal to

**Options:**

A.  $\frac{1}{2}$

B.  $\frac{1}{3}$

C.  $\frac{1}{4}$

D.  $\frac{1}{8}$

**Answer: D**

**Solution:**

**Solution:**

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## Question 241

Consider the group  $\left( \mathbb{R} \setminus \left\{ \frac{1}{2} \right\}, * \right)$  where  $a * b = a + b - 2ab$  for all  $a, b \in \mathbb{R} \setminus \left\{ \frac{1}{2} \right\}$ . Then the inverse of arbitrary element  $a$  is

**Options:**

A.  $\frac{a}{a-1}$

B.  $\frac{a}{2a+1}$

C.  $\frac{a}{2a-1}$

D.  $\frac{a}{a+1}$

**Answer: C**

**Solution:**

**Solution:**

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## Question 242

The area bounded by  $y = 2x - x^2$  and y-axis is

**Options:**

A. 3 sq. units

B. 2 sq. units

C. 1 sq. units

D. 0 sq. units

**Answer: D**

**Solution:**

**Solution:**

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## Question 243

**If the position vector of three points are**

**$\vec{a} - 2\vec{b} + 3\vec{c}$ ,  $3\vec{a} + 4\vec{b} - 5\vec{c}$ ,  $-\vec{a} - 8\vec{b} + 11\vec{c}$ , then the three points are**

**Options:**

A. non-coplanar

B. non-collinear

C. collinear

D. unit vectors

**Answer: C**

**Solution:**

**Solution:**

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## Question 244

**The sides of a parallelogram are  $\vec{a} = \vec{i} + 2\vec{j} - 3\vec{k}$ ,  $\vec{b} = \vec{i} + \vec{j} + 2\vec{k}$ . Then the unit vector parallel to one of the diagonals is**

**Options:**

A.  $\frac{1}{\sqrt{14}}(2\vec{i} + 3\vec{j} + \vec{k})$

B.  $\frac{1}{\sqrt{14}}(2\vec{i} + 3\vec{j} - \vec{k})$

C.  $\frac{1}{\sqrt{26}}(\vec{j} + 5\vec{k})$

D.  $\frac{1}{26}(-\vec{j} - 5\vec{k})$

**Answer: B**

**Solution:**

**Solution:**

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## Question 245

In a three dimensional space, the equation  $8x + 7y = 0$  represents

**Options:**

- A. the z-axis
- B. the z-plane
- C. the x-axis
- D. the plane  $y = 0$

**Answer: A**

**Solution:**

**Solution:**

---

## Question 246

The plane  $x - 2y + z = 6$  and the line  $\frac{x}{1} = \frac{y}{2} = \frac{z}{3}$  are related as

**Options:**

- A. parallel to the plane
- B. at right angles to a plane
- C. lies in the plane
- D. meets the plane obliquely

**Answer: A**

**Solution:**

**Solution:**

---

## Question 247

If the position vectors of A, B and C are respectively  $\hat{i} + \hat{j} + \hat{k}$ ,  $\hat{i} - 2\hat{j} - 4\hat{k}$  and  $2\hat{i} - 3\hat{j} - 3\hat{k}$ , then  $\cos^2 B$  is equal to

**Options:**

- A.  $\frac{1}{63}$
- B.  $\frac{4}{63}$

C.  $\frac{6}{63}$

D.  $\frac{11}{63}$

**Answer: B**

**Solution:**

**Solution:**

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## Question 248

The number of solutions at  $x = 5$  for the equation  $\left| \frac{dy}{dx} \right| + |x| + 7 = 0$  is

**Options:**

A. 0

B. 1

C. 5

D.  $\infty$

**Answer: A**

**Solution:**

**Solution:**

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## Question 249

A solution of the differential equation  $(x + y)^2 \frac{dy}{dx} = 4$  is

**Options:**

A.  $y = 2 \tan^{-1} \left( \frac{x-y}{2} \right) + c$

B.  $y = 2 \tan^{-1} \left( \frac{x+y}{2} \right) + c$

C.  $y = \tan^{-1} \left( \frac{x-y}{2} \right) + c$

D.  $y = \tan^{-1} \left( \frac{x+y}{2} \right) + c$

**Answer: B**

**Solution:**



**Solution:**

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## Question 250

$$\mathbf{I} = \int\limits_{-3}^2 (|\mathbf{x} + 1| + |\mathbf{x} + 2|) \, \mathrm{d}\mathbf{x} =$$

**Options:**

A. 10

B. 12

C. 15

D. 18

**Answer: C**

**Solution:**

**Solution:**

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