

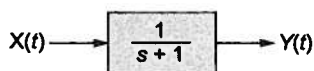
5

Frequency Response Analysis



Multiple Choice Questions

Q.1 For $X(t) = \sin t$. Find $Y(t)$.



(a) $\sqrt{2} \sin(t + 45^\circ)$ (b) $\frac{1}{\sqrt{2}} \sin(t - 45^\circ)$

(c) $\sqrt{2} \sin(t - 45^\circ)$ (d) $\frac{1}{\sqrt{2}} \sin(t + 45^\circ)$

Q.2 A u.f.b. system has forward path transfer function

$$G(s) = \frac{100}{s(s+10)}$$

The resonant frequency and B.W. are respectively

- (a) 7.07 r/s, 12.7 r/s
(b) 12.7 r/s, 7.70 r/s
(c) 7.70 r/s, 1.27 r/s
(d) 1.27 r/s, 7.07 r/s

Q.3 The transfer function of a system is

$$\frac{C(s)}{R(s)} = \frac{S}{S+P}$$

When $r(t) = P \sin(2t - 90^\circ)$

and $C(t) = \sin(2t - 60^\circ)$

The value of 'P' will be

- (a) $\frac{1}{\sqrt{3}}$ (b) $\frac{2}{\sqrt{3}}$
(c) $\sqrt{3}$ (d) 1

Q.4 The phase margin (in degrees) of a system having the loop transfer function

$$G(s)H(s) = \frac{2\sqrt{3}}{s(s+1)}$$
 is

- (a) 45° (b) -30°
(c) 60° (d) 30°

[GATE-1999]

Q.5 The system with the open loop transfer function

$$G(s)H(s) = \frac{1}{s(s^2 + s + 1)}$$
 has a gain margin of

- (a) -6 dB (b) 0 dB
(c) 3.5 dB (d) 6 dB

[GATE-2002]

Q.6 The open loop transfer function of a unity

feedback system is given by $G(s) = \frac{3e^{-2s}}{s(s+2)}$.

The gain and phase margins of the system will be

- (a) -7.09 and 87.5°
(b) 7.09 and 87.5°
(c) 7.09 dB and -87.5°
(d) -7.09 dB and -87.5°

[GATE-2005]

Q.7 A second order system has

$$M(j\omega) = \frac{100}{100 - \omega^2 + 10\sqrt{2}j\omega}$$

Its M_r (peak magnitude) is

- (a) 0.5 (b) 1
(c) $\sqrt{2}$ (d) 2

[GATE-2007]

Q.8 The phase angle of the system

$$G(s) = \frac{s+5}{s^2+4s+9}, \text{ varies between}$$

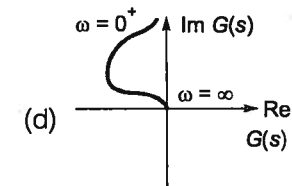
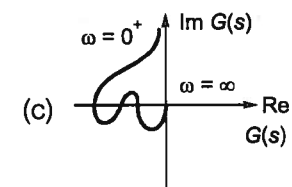
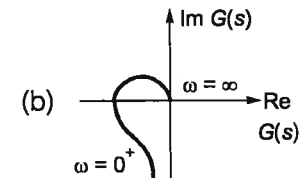
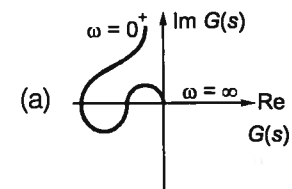
- (a) 0° and 90° (b) 0° and -90°
(c) 0° and -180° (d) -90° and -180°

[ESE-2001]

Q.9 The open-loop transfer function of a unity negative feed-back system is

$$G(s) = \frac{k(s+10)(s+20)}{s^3(s+100)(s+200)}$$

The polar plot of the system will be



[ESE-1999]

Q.10 The OLTF of unity feedback system is

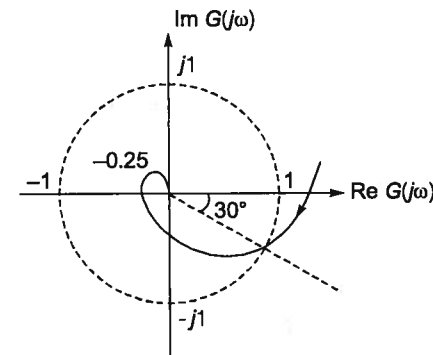
$$G(s) = \frac{as+1}{s^2}$$

The value of 'a' to give phase margin = 45° will be

- (a) $\sqrt{2}$ (b) $\frac{1}{\sqrt{2}}$

- (c) $\sqrt{\sqrt{2}}$ (d) $\frac{1}{\sqrt{\sqrt{2}}}$ [ESE-2004]

Q.11 The polar plot (for positive frequencies) for the open-loop transfer function of a unity feedback control system is shown in the given figure



The phase margin and the gain margin of the system are respectively

- (a) 150° and 4 (b) 150° and $3/4$
(c) 30° and 4 (d) 30° and $3/4$

[ESE-2000]

Q.12 The open-loop transfer function of a unity feedback control system is given as

$$G(s) = \frac{1}{s(1+sT_1)(1+sT_2)}$$

The phase crossover frequency and the gain margin are, respectively

(a) $\frac{1}{\sqrt{T_1T_2}}$ and $\frac{T_1+T_2}{T_1T_2}$

(b) $\sqrt{T_1T_2}$ and $\frac{T_1+T_2}{T_1T_2}$

(c) $\frac{1}{\sqrt{T_1T_2}}$ and $\frac{T_1T_2}{T_1+T_2}$

(d) $\sqrt{T_1T_2}$ and $\frac{T_1T_2}{T_1+T_2}$

[ESE-2001]

Q.13 The phase margin (PM) and the damping ratio (ξ) are related by

(a) $PM = 90^\circ - \tan^{-1} \left\{ \frac{\sqrt{-2\xi^2 + \sqrt{1+4\xi^4}}}{2\xi} \right\}$

(b) $PM = \tan^{-1} \left\{ \frac{2\xi}{-2\xi^2 + \sqrt{1+4\xi^4}} \right\}$

(c) $PM = 90^\circ + \tan^{-1} \left\{ \frac{\sqrt{2\xi + \sqrt{1+4\xi^4}}}{2\xi} \right\}$

(d) $PM = 180^\circ - \tan^{-1} \left\{ \frac{\sqrt{2\xi - \sqrt{1+4\xi^4}}}{2} \right\}$

[ESE-2003]

Q.14 List-I and List-II show the transfer function and polar plots respectively. Match List-I with List-II and select the correct answer:

List-I

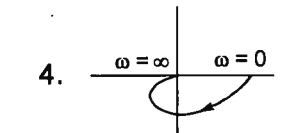
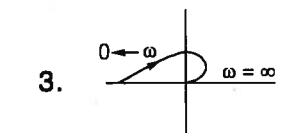
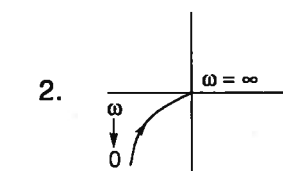
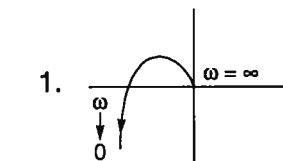
A. $\frac{1}{s(1+sT)}$

B. $\frac{1}{(1+sT_1)(1+sT_2)}$

C. $\frac{1}{s(1+sT_1)(1+sT_2)}$

D. $\frac{1}{s^2(1+sT_1)(1+sT_2)}$

List-II

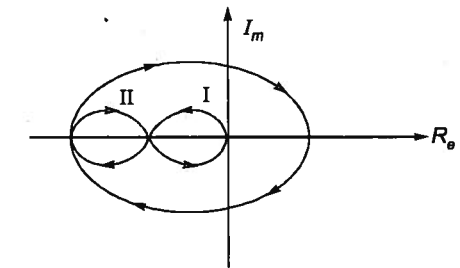


Codes:

	A	B	C	D
(a)	2	1	4	3
(b)	3	4	1	2
(c)	2	4	1	3
(d)	3	1	4	2

[ESE-2002]

Q.15 Consider the Nyquist diagram for given $KG(s)$ $H(s)$. The transfer function $KG(s)H(s)$ has no poles and zeros in the right half of s-plane. If the $(-1, j0)$ point is located first in region I and then in region II, the change in stability of the system will be from



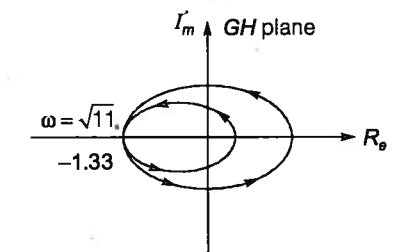
- (a) unstable to stable
(b) stable to stable
(c) unstable to unstable
(d) stable to unstable

[ESE-2002]

Q.16 The Nyquist plot of a unity feedback system having open loop transfer function

$$G(s) = \frac{k(s+3)(s+5)}{(s-2)(s-4)} \text{ for } K = 1 \text{ is as shown}$$

below. For the system to be stable, the range of values of K is



- (a) $0 < K < 1.33$ (b) $0 < K < 1/1.33$
(c) $K > 1.33$ (d) $K > 1/1.33$

[ESE-2003]

Q.17 A unity feedback control system has a forward

loop transfer function as $\frac{e^{-Ts}}{s(s+1)}$. Its phase

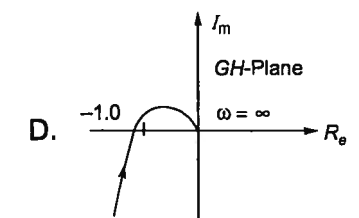
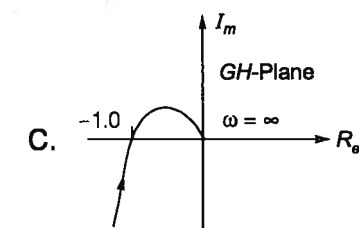
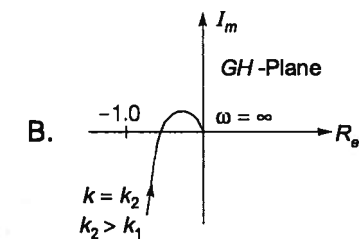
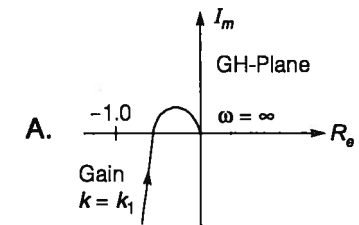
value will be zero at frequency ω_1 . Which one of the following equations should be satisfied by ω_1 ?

- (a) $\omega_1 = \cot(T\omega_1)$ (b) $\omega_1 = \tan(T\omega_1)$
(c) $T\omega_1 = \cot(\omega_1)$ (d) $T\omega_1 = \tan(\omega_1)$

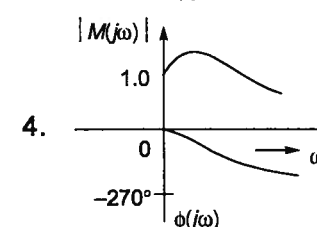
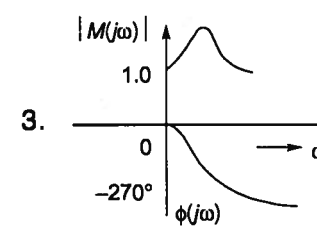
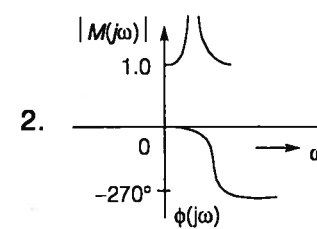
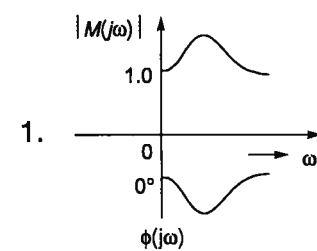
[ESE-2004]

Q.18 Match List-I (Nyquist Plot) with List-II (Frequency Response) and select the correct answer using the code given below the lists:

List-I



List-II

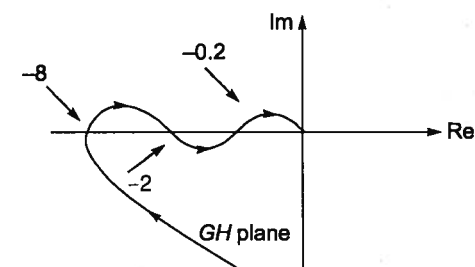


Codes:

- | | A | B | C | D |
|-----|---|---|---|---|
| (a) | 4 | 3 | 2 | 1 |
| (b) | 4 | 2 | 1 | 3 |
| (c) | 2 | 1 | 3 | 4 |
| (d) | 2 | 4 | 3 | 1 |

[ESE-2006]

Q.19 The polar diagram of a conditionally stable system for open loop gain $K = 1$ is shown in the figure. The open loop transfer function of the system is known to be stable. The closed loop system is stable for



(a) $K < 5$ or $\frac{1}{2} < K < \frac{1}{8}$

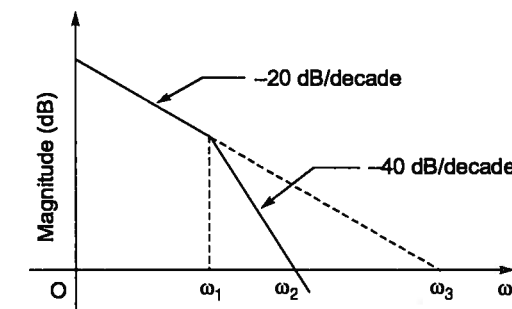
(b) $K < \frac{1}{8}$ or $\frac{1}{2} < K < 5$

(c) $K < \frac{1}{8}$ or $5 < K$

(d) $K < \frac{1}{8}$ or $K < 5$

[GATE-2005]

Q.20 Consider the following statements regarding the frequency response of a system as shown below:



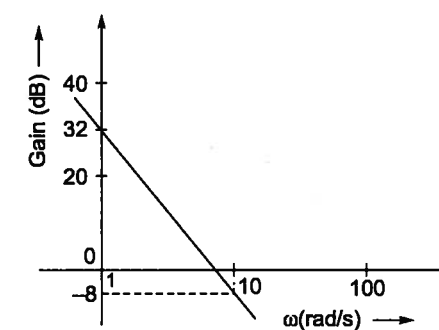
- The type of the system is one
- ω_3 = static error coefficient (numerically)
- $\omega_2 = \frac{\omega_1 + \omega_3}{2}$

Select the correct answer using the codes given below

- (a) 1, 2 and 3 (b) 1 and 2
(c) 2 and 3 (d) 1 and 3

[ESE-2003]

Q.21 The Bode plot of a transfer function $G(s)$ is shown in the figure below:

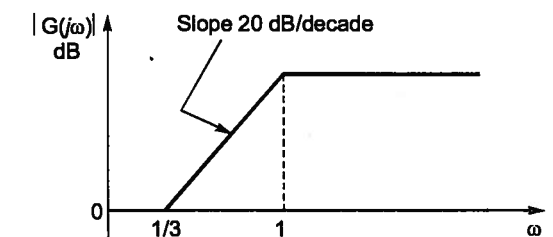


The gain ($20\log|G(s)|$) is 32 dB and -8 dB at 1 rad/s and 10 rad/s respectively. The phase is negative for all ω . Then $G(s)$ is

- (a) $\frac{39.8}{s}$ (b) $\frac{39.8}{s^2}$
(c) $\frac{32}{s}$ (d) $\frac{32}{s^2}$

[GATE-2013]

Q.22 The magnitude Bode plot of a network is shown in the figure



The maximum phase angle ϕ_m and the corresponding gain G_m respectively, are

- (a) -30° and 1.73 dB
(b) -30° and 4.77 dB
(c) $+30^\circ$ and 4.77 dB
(d) $+30^\circ$ and 1.73 dB

[GATE-2014]

Q.23 The polar plot of the open loop transfer function

$G(s) = \frac{10(s+1)}{s+10}$ for $0 \leq \omega < \infty$ will be in the

- (a) first quadrant (b) second quadrant
(c) third quadrant (d) fourth quadrant

[GATE-2015]

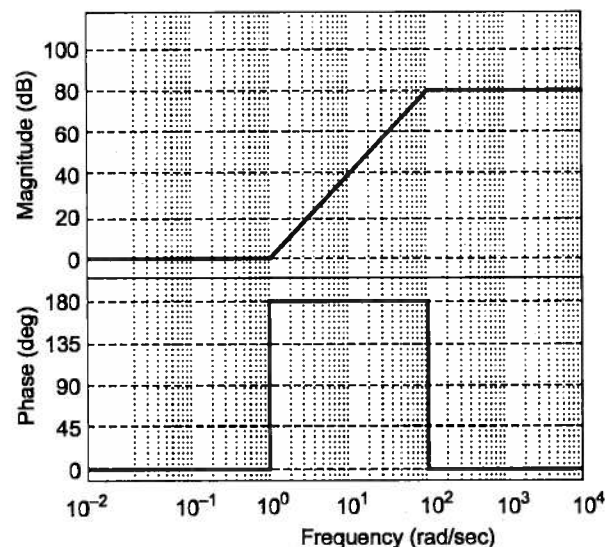
Q.24 The number and direction of encirclements around the point $-1 + j0$ in the complex plane

by the Nyquist plot of $G(s) = \frac{1-s}{4+2s}$ is

- (a) zero. (b) one, anti-clockwise.
(c) one, clockwise. (d) two, clockwise.

[GATE-2016]

Q.25 The transfer function $G(s)$ of a system which has the asymptotic Bode plot shown below is:

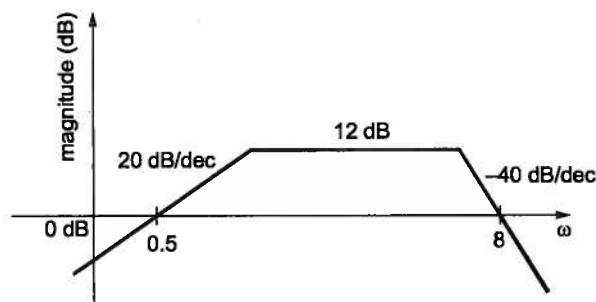


- (a) $10^4 \frac{(s-1)^2}{(s+100)^2}$ (b) $10^4 \frac{(s+1)^2}{(s+100)^2}$
 (c) $10^4 \frac{(s+1)}{(s+100)^2}$ (d) $10^4 \frac{(s-1)^2}{(s-100)^2}$

[IN: GATE-2016]

Q.26 Consider the following asymptotic Bode magnitude plot (ω is in rad/s).

Which one of the following transfer functions is best represented by the above Bode magnitude plot?



- (a) $\frac{2s}{(1+0.5s)(1+0.25s)^2}$
 (b) $\frac{4(1+0.25s)}{s(1+0.25s)}$
 (c) $\frac{2s}{(1+2s)(1+4s)}$
 (d) $\frac{4s}{(1+2s)(1+4s)^2}$

[EE: GATE-2016]

Q.27 Loop transfer function of a feedback system is

$$G(s)H(s) = \frac{s+3}{s^2(s-3)}$$

Take the Nyquist contour in the clockwise direction. Then, the Nyquist plot of $G(s)H(s)$ encircles $-1 + j0$

- (a) once in clockwise direction
 (b) twice in clockwise direction
 (c) once in anticlockwise direction
 (d) twice in anticlockwise direction



Numerical Data Type Questions

Q.28 _____ rad/sec is frequency at which the steady state sinusoidal response becomes zero.

$$G(s) = \frac{(s^2 + 9)(s+2)}{(s+3)(s+4)(s+5)}$$

Q.29 _____ is the value of damping ratio when resonant peak is unity?

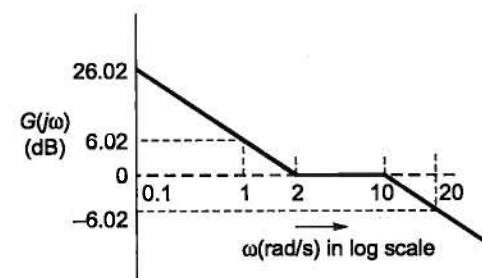
Q.30 The phase margin in degrees of

$$G(s) = \frac{10}{(s+0.1)(s+1)(s+10)}$$

calculated using the asymptotic Bode plot is _____.

[GATE-2014]

Q.31 The Bode asymptotic magnitude plot of a minimum phase system is shown in the figure.



If the system is connected in a unity negative feedback configuration, the steady state error of the closed loop system, to a unit ramp input, is _____.

[GATE-2014]

Q.32 The transfer function of a mass-spring-damper system is given by

$$G(s) = \frac{1}{Ms^2 + Bs + K}$$

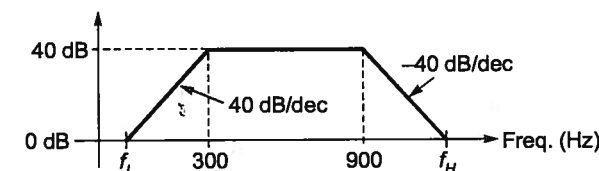
The frequency response data for the system are given in the following table.

ω in rad/s	$ G(j\omega) $ in dB	$\arg(G(j\omega))$ in deg
0.01	-18.5	-0.2
0.1	-18.5	-1.3
0.2	-18.4	-2.6
1	-16	-16.9
2	-11.4	-89.4
3	-21.5	-151
5	-32.8	-167
10	-45.3	-174.5

The unit step response of the system approaches a steady state value of _____.

[GATE-2015]

Q.33 Consider the Bode plot shown in figure. Assume that all the poles and zeroes are real valued.



The value of $f_H - f_L$ (in Hz) is _____.

[GATE-2015]

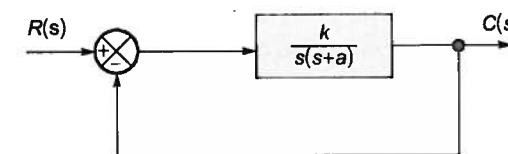
Q.34 The phase margin (in degrees) of the system having open loop transfer function

$$G(s) = \frac{10}{s(s+10)}$$

is _____.

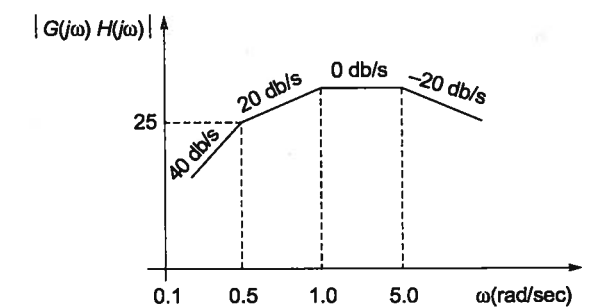
[GATE-2015]

Q.35 For the system shown in the figure, obtain the values of k and a , to satisfy, $M_r = 1.04$ and $\omega_r = 11.55$ rad/sec.



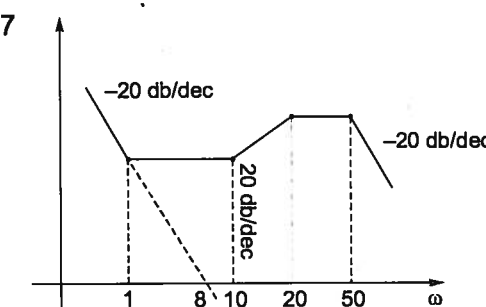
[ESE-2007]

Q.36 Determine the open loop transfer function, $G(s)$ $H(s)$, of a feedback control system whose Bode-Plot's magnitude characteristic is shown in the figure.



[ESE-2008]

Q.37



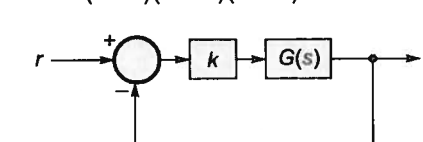
Find the transfer function?

Q.38 A minimum phase function has 3 finite poles and 1 finite zeroes. Its phase angle as $\omega \rightarrow \infty$ will be $-k \times \pi/2$ rad.

Then the value of k is _____.

Q.39 In the feedback system shown below

$$G(s) = \frac{1}{(s+1)(s+2)(s+3)}$$



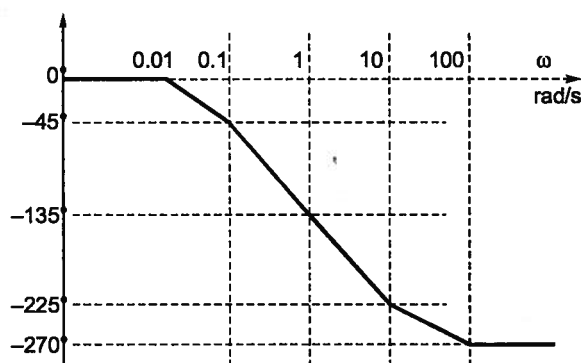
The positive value of k for which the gain margin of the loop is exactly 0 dB and the phase margin of the loop is exactly zero degree is _____.

[GATE-2016]

Q.40 The asymptotic Bode phase plot of

$$G(s) = \frac{k}{(s+0.1)(s+10)(s+p_1)}$$

with k and p_1 both positive, is shown below.



The value of p_1 is _____

[GATE-2016]

Q.41 The input $i(t) = 2 \sin(3t + \pi)$ is applied to a system whose transfer function

$G(s) = \frac{8}{(s+10)^2}$. The amplitude of the output of the system is _____.

[IN: GATE-2016]



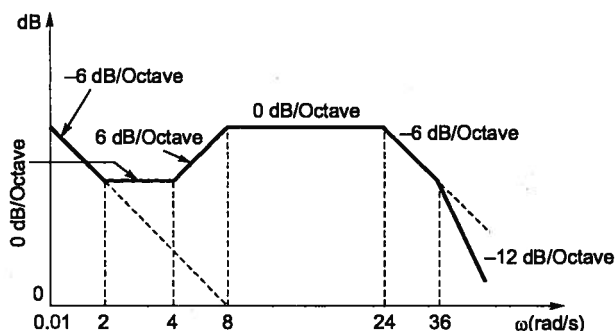
Try Yourself

T1. The Bode magnitude plot of the transfer function

$$G(s) = \frac{K(1+0.5s)(1+as)}{s\left(1+\frac{s}{8}\right)(1+bs)\left(1+\frac{s}{36}\right)}$$

is shown below.

Note that $-6 \text{ dB/octave} = -20 \text{ dB/decade}$. The value of a/bK is _____.



[Ans: 0.755 (0.7 to 0.8)]

T2. An open loop T.F. of a unity feedback system is given by

$$G(s) = \frac{1}{(s+2)^2}$$

The closed loop transfer function will have poles at _____.

[Ans: $-2 + j$; $-2 - j$]

T3. By adding a pole at the origin of s-plane, the Nyquist plot of a system will rotate by

- (a) 90° in anti-clockwise direction
- (b) 90° in clockwise direction
- (c) 180° in anti-clockwise direction
- (d) 180° in clockwise direction

[Ans. (b)]

T4. Using polar plot method, find the gain margin of a feedback system whose open-loop transfer function is given by

$$G(s)H(s) = \frac{0.75}{s(1+s)(1+0.5s)}$$

[Ans: gain margin in dB = $20 \log 4 = 12 \text{ dB}$]

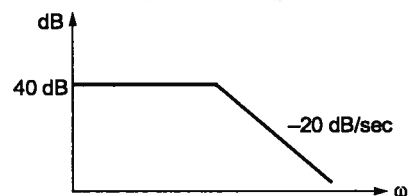
T5. The open-loop transfer function of a system is

$$G(s)H(s) = \frac{K}{s(1+2s)(1+3s)}$$

The phase crossover frequency is _____ rad/sec

[Ans: 0.41]

T6. The Bode plot for a transfer function is given below. The steady state error corresponding to a unit step input is _____



[Ans: 0.009]

