

Operational Amplifiers

10

Differential Amplifier

- Here,

$$V_{out} = A(V_1 - V_2)$$

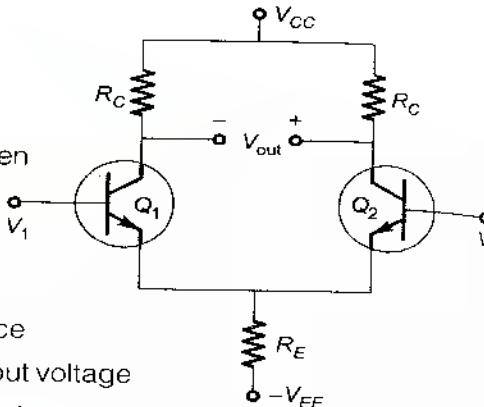
where, V_{out} = Voltage between collectors

$$A = \frac{R_C}{R_E}$$

where, R_E = Emitter resistance

V_1 = Noninverting input voltage

V_2 = Inverting input voltage



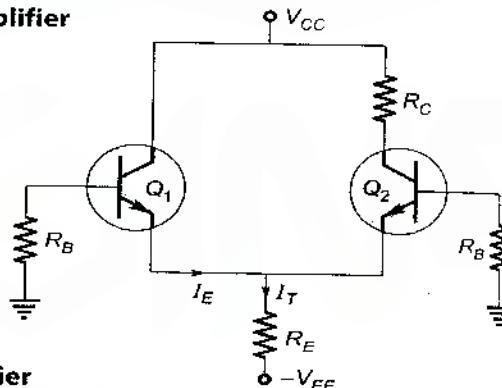
DC Analysis of a Differential Amplifier

- Emitter bias current

$$I_E = \frac{V_{EE} - V_{BE}}{2R_E}$$

- Tail current

$$I_T = \frac{V_{EE} - V_{BE}}{R_E}$$



AC Analysis of a Differential Amplifier

1. Non-inverting input

- AC emitter current

$$I_E = \frac{V_1}{2R_E}$$

where, R_E = emitter resistance

- AC output voltage is $V_{out} = I_C R_C = \frac{V_1}{2R_E} R_C$

- Voltage gain for noninverting input is $\frac{V_{out}}{V_1} = \frac{R_C}{2R_E}$

2. Inverting input

- AC emitter current is

$$I_E = \frac{V_2}{2R_E}$$

- AC output voltage is

$$V_{out} = -I_C R_C = -\frac{V_2}{2R_E} R_C$$

- Voltage gain for inverting input is

$$\frac{V_{out}}{V_2} = \frac{R_C}{2R_E}$$

- Differential Voltage gain

$$A = \frac{R_C}{2R_E}$$

- Input impedance $R_{in} = 2\beta R_E$

Common Mode Voltage Gain

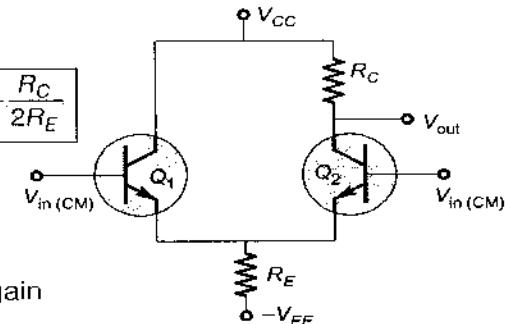
$$A_{CM} = \frac{V_{out}}{V_{in(CM)}} = -\frac{R_C}{r_e + 2R_E} \approx -\frac{R_C}{2R_E}$$

$$CMRR = \frac{A}{A_{CM}}$$

where, A_{CM} → common mode gain

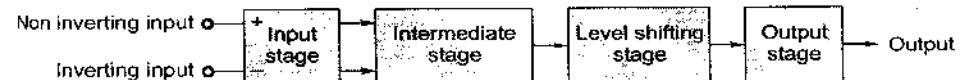
Note:

$$R_E \gg r_e$$



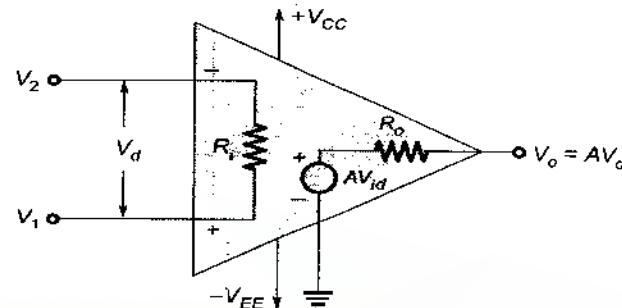
Operational Amplifier

An op-Amp is basically a very high gain, direct-coupled amplifier with high input impedance and low output impedance.



Equivalent circuit of an Op-Amp

Op-amp amplifies the difference between the two input signals applied at non inverting and inverting input terminals.



Equivalent circuit of op-amp

where,

$$\text{Difference input voltage } V_d = V_1 - V_2$$

A = Open loop gain of op-amp

Output voltage

$$V_o = A V_d$$

R_f = Differential input resistance

R_o = Output resistance

Properties of Op-Amp

Parameters	Ideal value	Practical value
Voltage gain	∞	10^6
Input resistance	∞	$10^6 \Omega$ or $1 M\Omega$
Output resistance	0	10Ω to 100Ω
B.W.	∞	10^6 Hz or 1 MHz
CMRR	∞	10^6 or 120 dB
Slew rate	∞	$80V/\mu sec.$

Slew rate

For input $V_m \sin \omega t$

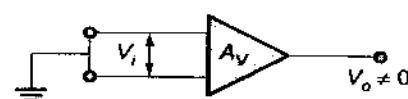
$$f_{max} = \frac{SR}{2\pi A_{CL} V_m}$$

where, SR = Slew rate

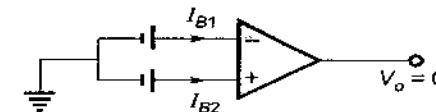
f_{max} = Maximum frequency of operation

A_{CL} = Closed loop gain of OP-AMP.

Bias Currents and Voltage



$V_o \neq 0 \rightarrow$ Called O/P offset voltage.



Balanced condition.

Input bias current (I_B)

$$I_B = \frac{I_{B1} + I_{B2}}{2}$$

Input offset current

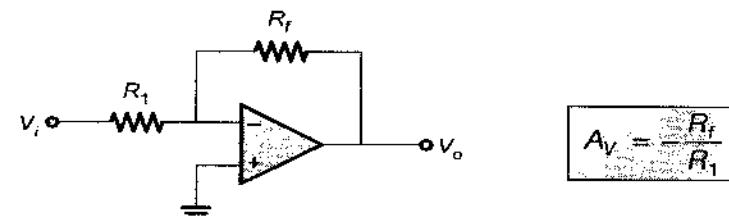
$$I_{io} = (I_{B1} - I_{B2})$$

Note:

Input offset voltage is the voltage which must be applied between input terminals to balance amplifier ($V_o = 0$).
.....

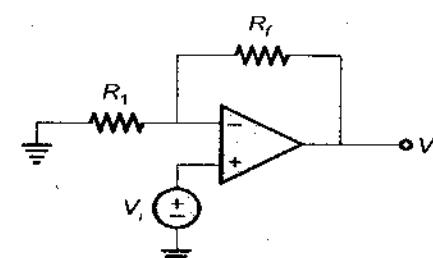
Linear Op-Amp Circuits

Inverting Amplifier



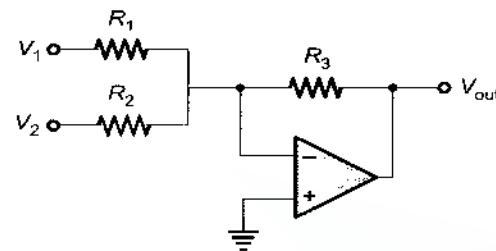
$$A_V = -\frac{R_f}{R_1}$$

Non-inverting Amplifier



$$A_V = \left(1 + \frac{R_f}{R_1}\right)$$

Summing Amplifier



Output voltage

$$V_{\text{out}} = \frac{R_3}{R_1} V_1 - \frac{R_3}{R_2} V_2$$

Differential Amplifier

$$V_0 = -\frac{R_2}{R_1} V_1 + \left(\frac{R_4}{R_3 + R_4} \right) \left(1 + \frac{R_2}{R_1} \right) V_2$$

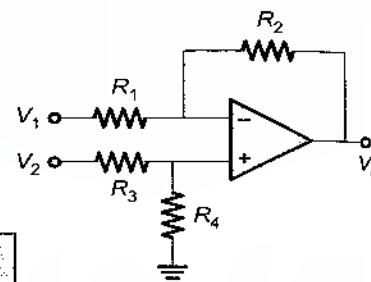
$$\text{if } \frac{R_2}{R_1} = \frac{R_4}{R_3}$$

$$\text{then, } V_0 = \frac{R_4}{R_3} [V_2 - V_1] = \frac{R_2}{R_1} (V_2 - V_1)$$

Note:

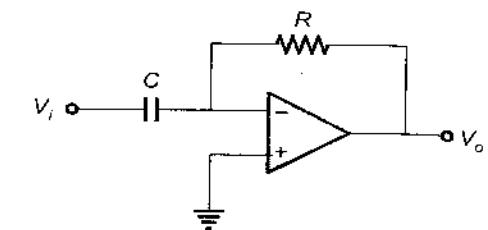
In this case when $\frac{R_2}{R_1} = \frac{R_4}{R_3}$,

$A_c = 0 \rightarrow \text{Common mode gain and CMRR} = \infty$



Differentiator

$$V_0 = -RC \frac{dV_i}{dt}$$



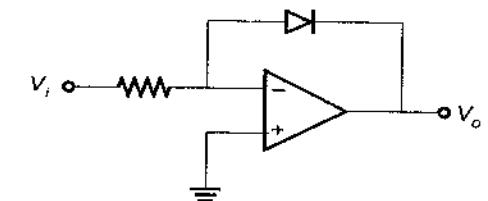
Logarithmic Amplifier

$$V_0 = -\eta V_T \ln \frac{V_i}{I_0 R}$$

where, η = Recombination factor

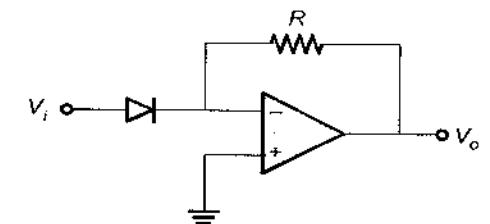
V_T = Thermal voltage

I_0 = Reverse saturation current of diode



Antilog Amplifier

$$V_0 = -I_0 R \text{ antilog} \frac{V_i}{\eta V_T}$$



where, I_0 = Reverse saturation current of diode

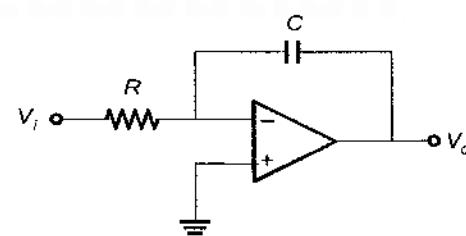
η = Recombination factor

V_T = Thermal voltage

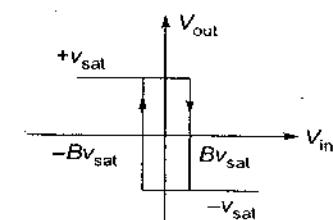
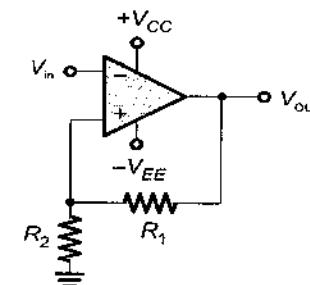
Nonlinear Op-Amp circuits

Integrator

$$V_0 = -\frac{1}{RC} \int V_i dt + V_c(0+)$$



Schmitt Trigger



$$V_{Th} = \frac{R_1}{(R_1 + R_2)} V_H$$

$$V_{Tl} = \frac{R_1}{(R_1 + R_2)} V_L \quad (\text{where } V_L \ll V_H)$$

Remember:

- The complete transfer characteristics of Schmitt trigger shows a hysteresis effect.
 - The width of hysteresis is the difference between the two cross-over voltages V_{Th} and V_{Tl} .
-

Op-Amp as a Multivibrator

Square Wave Generator or Astable Multivibrator

Time period of output waveform generated is

$$T = 2RC \ln 3 \quad (\text{For } R_1 = R_2)$$

$$T = 2RC \ln \left[\frac{1+B}{1-B} \right] \quad \left(\text{where } B = \frac{R_2}{R_1+R_2} \right)$$

Monostable Multivibrator

Width of pulse generated at output is

$$T = RC \ln \left(1 + \frac{R_2}{R_1} \right)$$

if $R_2 = R_1$,

then

$$T = RC \ln 2$$

Note:

- Astable multivibrator is a square wave generator.
 - Monostable multivibrator is used as pulse stretcher and missing pulse detector.
-

