Unit 13 (Playing With Numbers)

Multiple Choice Questions

Question. 1 Generalised form of a four-digit number abdc is

(a) 1000a + 100b + 10c + d (b) 1000a + 100c + 10b + d

(c) 1000a + 100b + 10d + c (d) a x b x c x d

Solution. (c) In generalised form, we express a number as the sum of the products of its digits with their respective place values.

abdc is written in generalised form as 1000a + 100b + 10d + c.

i.e. abdc = 1000a + 100b + 10d + c

Question. 2 Generalised form of a two-digit number xy is

(a)x + y (b)10x + y (c)10x-y (d)10y+x

Solution. (b) In generalised form, xy can be written as the sum of the products of its digits with their respective place values, i.e. xy = 10x + y

Question. 3 The usual form of 1000a + 10b + c is

(a) abc (b) abc0 (c) a0be (d) ab0c

Solution. (c) Given expanded (or generalised) form of a number is 1000a + 10b + c. Then, we have to find its usual form.

We can write it as $1000 \times a + 100 \times 0 + 10 \times b + c$

i.e. a0bc, which is the usual form.

Question. 4 Let abc be a three-digit number. Then, abc - cba is not divisible by

(a) 9 (b) 11 (c) 18 (d) 33

Solution. (c) Given, abc is a three-digit number.

Then, abc = 100a + 10b + c

and cba = 100c + 10b + a

abc - eba = (100a + 10b + c) - (100c + 10b + a)

= 100a - a + 10b - 10b + c - 100 =

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= 99a - 99c = 99 (a -c)
= abc-cba is divisible by 99.
=> abc - cba is divisible by 9,11,33, but it is not divisible by 18.
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Question. 5 The sum of all the numbers formed by the digits x, y and z of the number xyz is divisible by (a) 11 (b) 33 (c) 37 (d) 74

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Solution. (c) We have, xyz + yzx + zxy
= (100x + 10y + z) + (100y + 10z + x) + (100z + 10x + y) ...(i)
= 100x + 10x + x + 10y + 100y + y + z + 100z + 10Z
= 111x + 111y + 111z = 111(x + y + z)
= 3 \times 37 \times (x + y + z)
Hence, Eq. (i) is divisible by 37, but not divisible by 11,33 and 74.
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Question. 6 A four-digit number aabb is divisible by 55. Then, possible value(s) of b is/are (a) 0 and 2 (b) 2 and 5 (c) 0 and 5 (d) 7

Solution. (c) It is given that, aabb is divisible by 55. Then, it is also divisible by 5. Now, if a number is divisible by 5, then its unit digit is either 0 or 5. Hence, the possible values of b are 0 and 5.

Question. 7 Let abc be a three-digit number. Then, abc + bca + cab is not divisible by (a) a + b + c (b) 3 (c) 37 (d) 9

Solution. (d) We know that, the sum of three-digit numbers taken in cyclic order can be written as 111 (a + b + c).

i.e. $abc + pea + cab = 3 \times 37 \times (a + b + c)$

Hence, the sum is divisible by 3, 37 and (a + b + c) but not divisible by 9.

Question. 8 A four-digit number 4ob5 is divisible by 55. Then, the value of b-a is (a) 0 (b) 1 (0 4 (d) 5

Solution. (b) Given, a four-digit number 4ab5 is divisible by 55. Then, it is also divisible by 11. The difference of sum of its digits in odd places and sum of its digits in even places is either 0 or multiple of 11.

i.e. (4 + b) - (a + 5) is 0 or a multiple of 11, if $4 + b - a - 5 = 0 \Rightarrow b-a = 1$

Question. 9 If abc is a three-digit number, then number abc -a-b-c is divisible by (a) 9 (b) 90 (c)10 (d) 11

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Solution. (d) We have, abc= 100a + 10b+c
.-. abc -a - b-c = (100a + 10b + c)-a - b-c = 100a - a + 10b - b = <math>99a + 9b = 9(11a + b)
Hence, the given number abc -a - b-c is divisible by 9.
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Question. 10 A six-digit number is formed by repeating a three-digit number. For example, 256256, 678678 etc. Any number of this form is divisible by (a) 7 only (b) 11 only (c) 13 only (d) 1001

Solution.

(d) Let the six-digit number be abcabc, then

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= 100000 \times a + 10000b + 1000c + 100a + 10b + c

= a(100000 + 100) + b(10000 + 10) + c(1000 + 1)

= a(100100) + b(10010) + c(1001) = 1001(a \times 100 + b \times 10 + c)
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Hence, it is divisible by 1001.

Question. 11 If the sum of digits of a number is divisible by three, then the number is always divisible by (a) 2 (b) 3 (c) 6 (d) 9

Solution. (b) We know that, if sum of digits of a number is divisible by three, then the number must be divisible by 3, i.e. the remainder obtained by dividing the number by 3 is same as the

remainder obtained by dividing the sum of its digits by 3.

Question. 12 If x + y + z = 6 and z is an odd digit, then the three-digit number xyz is

- (a) an odd multiple of 3 (b) an odd multiple of 6
- (c) an even multiple of 3 (d) an even multiple of 9

Solution. (a) We have, x + y + z = 6 and z is an odd digit. Since, sum of the digits is divisible by 3, it will also be divisible by 2 and 3 but unit digit is odd, so it is divisible by 3 only. Hence, the number is an odd multiple of 3.

Question. 13 If 5A + 53 = 65, then the values of A and B is

Solution.

(c) We have,
$$\frac{5A+B3}{65}$$

Evidently, A + 3 is a number taking values from 3 to 12. So, either A + 3 is 5 or it is a two-digit number whose unit digit is 5. But, A + 3 is less than or equal to 12.

In the tens column, we have $5 + B = 6 \implies B = 1$

Hence, A=2 and B=1

Question. 14 If A3 + 8B = 150, then the value of A + B is

(a) 13 (b) 12 (c) 17 (d) 15

Solution. (a) We have, A3+ 8B = 150

Here, 3 + B = 0, so 3 + B is a two-digit number whose unit's digit is zero.

$$-.3+B = 10=>B = 7$$

: Now, considering ten's column, A+8+1=15

$$= A + 9 = 15$$

=> A = 6

Hence, A+B=6+7 = 13

Question. 15 If 5A x A = 399, then the value of A is

(a) 3 (b) 6 (c) 7 (d) 9

Solution. (c) We have, $5A \times A = 399$

Here, A x A= 9 i.e. A x A is the number 9 or a number whose unit's digit is 9. Thus, the number whose product with itself produces a two-digit number having its unit's digit as 9 is 7.

i.e. A x A = 49 => A=7

Now, $5 \times A + 4 = 39$

=> 5 x 7+4 = 39

So, A satisfies the product.

Hence, the value of A is 7.

Question. 16 If 6A x B = > 488, then the value of A-B is

(a)-2 (b) 2 (c) -3 (d) 3

Solution. (c) Given, 6A x B = A86

Let us assume, A = 1 and S = 3 Then, LHS = 61 x 3 = 183 and RHS = 183 Thus, our assumption is true.

A-6 = 1-3=-2

Question. 17 Which of the following numbers is divisible by 99?

(a) 913462 (b) 114345 (c) 135792 (d) 3572406

Solution. (b) Given a number is divisible by 99.

Now, going through the options, we observe that the number (b) is divisible by 9 and 11 both as the sum of digits of the number is divisible by 9 and sum of digits at odd places = sum of digits at even places.

Fill in the Blanks

In questions 18 to 33, fill in the blanks to make the statements true.

Question. 18 3134673 is divisible by 3 and -----

Solution. 9

3134673 is divisible by 3 and 9 as sum of the digits, 3+1+3+4+6+7+3=27 is divisible by both 3 and 9.

Question. 19 20 x 3 is a multiple of 3, if the digit x is---or--- or----

Solution. 1,4,7

We know that, if a number is a multiple of 3, then the sum of its digits is again a multiple of 3, i.e. 2+0+x+3 is a multiple of 3.

x + 5 = 0, 3, 6, 9, 12, 15 But, x is a digit of the number 20 x 3.

x can take values 0, 1,2, 3,......9.

=> x + 5 = 6 or 9 or 12

Hence, x = 1 or 4 or 7

Question. 20 3 x 5 is divisible by 9, if the digit x is———.

Solution. 1

Since, the number 3×5 is divisible by 9, then the sum of its digits is also divisible by 9. i.e. 3 + x + 5 is divisible by 9.

=>x + 8 can take values 9,18, 27,...

But x is a digit of the number 3×5 , so x = 1.

Question. 21 The sum of a two-digit number and the number obtained by reversing the digits is always divisible by———.

Solution. 11

Let ab be any two-digit number, then the number obtained by reversing its digits is ba.

Now, ab + ba = (10a + b) + (10b + a) = 11a + 11b = 11(a + b)

Hence, ab + ba is always divisible by 11 and (a + b).

Question. 22 The difference of two-digit number and the number obtained by reversing its digits is always divisible by ———-.

Solution. 9

Let ab be any two-digit number, then we have

$$ab - ba = (10a + b) - (10b + a)$$

$$= 9a - 9b = 9(a - b)$$

Hence, ab - ba is always divisible by 9 and (a - b).

Question. 23 The difference of three-digit number and the number obtained by putting the digits in reverse order is always divisible by 9 and——.

Solution. 11

Let abc be a three-digit number, then we have

$$abc - cba = (100a + 10b + c) - (100c + 10b + a); = (100a - a) + (c - 100c)$$

$$= 99a - 99c = 99(a - c)$$

$$= 9 \times 11 \times (a - c)$$

Hence, abc – cba is always divisible by 9,11 and (a - c).

Question. 24

If
$$\frac{+A}{8}\frac{B}{A}$$
, then $A = \underline{}$ and $B = \underline{}$.

Here, B can take values from 0 to 9.

For B=0, A=0, which does not fit in tens column

For B=1, A=2, which does not fit in tens column

For B=3, A=6, which satisfies the tens column.

Hence, A = 6 and B = 3

Question. 25

If
$$\frac{\times B}{9 6}$$
, then $A = \underline{\hspace{1cm}}$ and $B = \underline{\hspace{1cm}}$.

Solution.

2,4

We have, × B

Here $B \times B = 6$, therefore B can take values either 4 or 6.

For
$$B = 4$$
, $A \times B + 1 = 9$

$$\Rightarrow A \times 4 + 1 = 9 \Rightarrow A = 2$$

Hence.

$$A = 2, B = 4$$

Question. 26

If
$$\frac{\times B}{4 + 9B}$$
, then $B =$ ______.

Solution.

7

Here, B can take values from

B x B= 49 is not satisfied.

Hence,

Question. 27 1 x 35 is divisible by 9, if x = ---.

Solution.

0

If 1x35 is divisible by 9, then the sum of its digits is also divisible by 9.

i.e. 1 + x + 3 + 5 is divisible by 9.

⇒ 9 + x can take values 0, 9, 18, 27, ...

m 9 + x = 9 or 18

 $\Rightarrow x = 0 \text{ or } 9$

[::x is a digit]

Question. 28 A four-digit number abed is divisible by 11, if d + b = ----or-----

Solution.
$$a + c,12(a + c)$$

We know that, a number is divisible by 11, if the difference between the sum of digits at odd places and the sum of its digits at even places is either 0 or a multiple of 11.

Hence, abcd is divisible by 11, if (d + b)- (a + c) = 0,11,22,33,...

$$=> d + b = a + c \text{ or } d + b = 12(a + c)$$

Question. 29 A number is divisible by 11, if the differences between the sum of digits at its odd places and that of digits at the even places is either 0 or divisible by -----

Solution. 11

By test of divisibility by 1,1, we know that, a number is divisible by 11, if the sum of digits at odd places and even places are equal or differ by a number, which is divisible by 11.

11.

Solution. (a+c)-b

Since, abc is divisible by 11, the difference of sum of its digits at odd places and that of even places is either zero or multiple of 11, i.e. (a + c) - b is either zero or multiple of 11.

Question. 31 If A x 3 = IA then A = ----.

Solution.

5

Here, 3 x A is a two-digit number whose unit digit is A.

A can take any value between 0 to 9, but only A= 5 satisfies the product.

Hence, A = 5

Question. 32 If B x B = AB, then either A = 2, B = 5 or A =----- B =-----. Solution.

3, 6

Here, $B \times B$ is a two-digit number, whose unit digit is B, therefore the value of B is either 5

If B=5, then A=2 and if B=6, then A=3.

Question. 33 If the digit 1 is placed after a two-digit number whose ten's is t and one's digit is u, the new number is----.

Solution. tu1

Given, a two-digit number whose ones digit isu in and tens digit isu. If the digit 1 is placed after this number, then the next number will be tu1.

True/False

In questions 34 to 44, state whether the given statements are True or False.

Question. 34 A two-digit number ab is always divisible by 2, if b is an even number.

Solution. True

By the test of divisibility by 2, we know that a number is divisible by 2, if its unit's digit is even.

Question. 35 A three-digit number abc is divisible by 5, if c is an even number.

Solution. False

By the test of divisibility by 5, we know that if a number is divisible by 5, then its one's digit will be either 0 or 5, i.e. the numbers ending with the digits 0 or 5 are divisible by 5.

Question. 36 A four-digit mmbeFabcd is divisible by 4, if ab is divisible by 4.

As we know that, if a number is divisible by 4, then the number formed by its digits in unit's and ten's place is divisible by 4.

Question. 37 A three-digit number abc is divisible by 6, if c is an even number and a + b + c is a multiple of 3.

Solution. True

If a number is divisible by 6, then it is divisible by both 2 and 3. Since, abc is divisible by 6, it is also divisible by 2 and 3. Therefore, c is an even number and the sum of digits is divisible by 3, i.e. multiple of 3.

Question. 38 Number of the form 3N + 2 will leave remainder 2 when divided by 3.

Solution. True

Let x = 3N + 2. Then, it can be written as.

x = (a multiple of 3) + 2

i.e. x is a number which is 2 more than a multiple of 3

i.e. x is a number, which when divided by 3, leaves the remainder 2.

Question. 39 Number 7N+1 will leave remainder 1 when divided by 7.

Solution. True

Given, a number of the form 7N + 1 = x (say)

Here, we observe that * is a number which is one more than a multiple of 7. i.e. when x is divided by 7, it leaves the remainder 1.

Question. 40 If a number a is divisible by b, then it must be divisible by each factor of b.

Solution. True

Given, a is divisible by b.

Let $b = p1 \cdot p2$, where p1 and p2 are primes.

Since, a is divisible by b, a is a multiple of b

i.e. a = mb

=> a = m.p1.p2

or a=cp2=dp1, where c=mp1, d=mp2

=>a is a multiple of p1 as well as p2.

Hence, a is divisible by each factor b.

Question. 41 If AB x 4 = 192, then A + 6 = 7.

Solution.

False

AB

We have, × 4 192

Here, $B \times 4$ is a two-digit number whose unit's digit is 2.

Therefore, the value of B is either 3 or 8.

But $\theta = 3$ is not possible as $A \times 4 + 1 \neq 19$ for any value of A between 0 to 9

∴ B = 8 and then A = 4

Hence, A + B= 12

Question. 42 If AB + 7C = 102, where $B \neq 0$, $C \neq 0$, then A + B + C = 14. Solution.

True

A B We have, +7C

Here, B + C is either 2 or a two-digit number whose one's digit is 2.

If B = C = 1, If8 = 5, C = 7, A = 2 and A + B + C = 2 + 5 + 7 = 14

Question. 43 If 213 x 27 is divisible by 9, then the value of x is 0.

Solution. False

Given, 213 x 27 is divisible by 9, so sum of its digits is also divisible by 9.

i.e. 21 + 3 + x + 2 + 7 - 0, 9,18, 27, 36,...

=> x+ 15= 0,9,18,27,36,...

=> x + 15 = 18 [x is a digit of a number]

=> x = 3

Question. 44 In N + 5 leaves remainder 3 and $N \div 2$ leaves remainder 0, then $N \div 10$ leaves remainder 4.

Solution.

False

: N + 5 leaves remainder 3.

⇒ N = 5n + 3, where n = 0, 1, 2, 3, ...

Now, it is also given, N+2 leaves remainder 0.

So, N must be an even number.

But N = 5n + 3 i.e. sum of two terms whose second term is odd.

So, for N should be even it is necessary that 5n must be odd.

which is possible, when n = 1, 3, 5, ...

So, in this case value of N should be

N=8, 18, 28, 38, ...

i.e.

$$N = 10n + 8, n = 0.1, 2, 3, ...$$

When N + 10 leaves remainder 8 always.

Question. 45 Find the least value that must be given to number a, so that the number 91876a2 is divisible by 8.

Solution. Given, 91876a2 is divisible by 8.

Since, we know that, if a number is divisible by 8, then the number formed by last 3 digits is divisible by 8.

So, 6a2 is divisible by 8.

Here, a can take values from 0 to 9.

For a = 0, 602 is not divisible by 8.

For a = 1, 612, which is not divisible by 8.

For a = 3, 632 is divisible by 8.

Hence, the minimum value of a is 3 to make 91876a2 divisible by 8.

Question. 46

If
$$\frac{\times P}{Q - 6}$$
, where $Q - P = 3$, then find the values of P and Q .

Solution.

We have,
$$\frac{\times P}{Q - 6}$$
 and $Q - P = 3$

Here, $P \times P$ is 6, so the value of P is either 4 or 6.

But if P = 4, Q = 5, which does not satisfy the relation Q - P = 3.

Hence, P = 6 and then Q = 9.

Question. 47 If 1AB + CCA = 697 and there is no carry-over in addition, find the value of A + B + C.

Solution.

Since, there is no carry-over in addition,

Question. 48 A five-digit number AABAA is divisible by 33. Write all the numbers of this form.

Solution. Given, a number of the form AABAA is divisible by 33. Then, it is also divisible by 3 and

11, as if a number a is divisible by b, then it is also divisible by each factor of b.

Since, AABAA is divisible by 3, sum its digits is also divisible by 3. i.e. 4 + 4 + 8 + A + .4 = 0,3,6,9...

or
$$4/4 + 8 = 0, 3, 69, \dots$$
 (i)

From Eq. (i), we have

Further, the given number is also divisible by 11, therefore (2/4 + 8) - 2A = 0,11,22,...

B=Q 11,22,...

8 = 0 [v8 is a digit of the given number]

Hence, the required numbers are 33033, 66066 and 99099.

In questions 49 to 60, find the value of the letters in each of the following questions.

Question. 49

Solution.

Here A + A = Z, therefore A can take any value between 0 to 9.

Since the sum in second column is a two-digit number, the possible values of A are 5 to 9.

The values A= 5 to 8 are not fitted in second column.

Hence,
$$A = 9 \Rightarrow Z = 8$$
 and $X = 1$

Question. 50

Here, $5 + A = 3 \Rightarrow 5 + A$ can be a single-digit number.

So, 5 + A is a two-digit number whose one's digit is 3.

$$\Rightarrow$$
 $B=1, C=3$ [: $BC=8+4+1 \Rightarrow 10B+C=13=10 \times 1+3 \Rightarrow B=1, C=3$]

Question. 51

Solution.

Here, 6 + A = 2, therefore the possible value of A is 6.

Now,

$$CA = B + B + 1$$

 \Rightarrow

$$C6 = B + 9$$

i.e. B + 9 is a number whose one's digit is 6.

Therefore, B=7 and C=1

Question. 52

Solution.

Here, A + A is a number whose one's digit is 2, therefore A = 6.

Now,
$$B + B + 1 = B$$

So, the possible value of B is 9.

Again, in third column,

 \Rightarrow

$$A = 6$$
, which is true.

Hence, $A \approx 6$ and B = 9

Question. 53

In first column, A + A = 0

⇒ .

A = 0 or 5

For A = 0, the second and third column, sums are not satisfied.

So. A = 5

Now, in second column,

$$B + B + 1 = 3$$

For B = 1, third column sum is not satisfied.

So, B = 6

Again, in third column, C + C + 1 = 1 A

=>

$$C+C=15-1 \Rightarrow 2C=14$$

=

Hence, A = 5, B = 6 and C = 7

Question. 54

Solution.

Here, A + A = 8

[: rejecting A= 4 as A + A can not be a single digit number]

Now, in third column, we have B + B + 1 = 3

$$\Rightarrow$$
 2B = 2 \Rightarrow B = 1

Hence, A = 9 and B = 1

Question. 55

Solution.

In first column, B + B = B

[::B = 4 does not fit in fourth column]

In second column, we have

$$A + 1 + 1 = 0$$

So, A should be 8

Third column is true for these values.

Also, the fourth column is satisfied.

Hence, A= Band B = 9

Question. 56

Solution.

We have
$$\frac{A}{C} = \frac{B}{6}$$
 and $B - A = 1$

Hers, $6 \times B$ is a number, whose unit's digit is 8. Therefore, the possible values of B are 3 and 8.

If B = 3, then $A \times 6 + 1 = C6$ which is not possible for any value of A between 0 to 9.

 $\therefore B = B$ and then A = T

The values of A and B also satisfies the given condition i.e 8-7+1.

If A = 7, then $7 \times 6 + 4 = C6$

6 = C6

4

C = 4

Hence,

A=7, B=8 and C=4

Question. 57

A B

× A B

Solution.

A I

Given, × A B 6 A B

i.e.

 $AB \times AB = 6AB$

...(1)

Here, $B \times B$ is a number whose unit's digit is B. Therefore, B = 1 or 5

[::B ≠ 0, else AB × A + ≠ 6A]

Again.

⇒ The square of a two-digit number is a three-digit number.

So, A can take values 1, 2 and 3.

For A= 1,2, 3 and B= 1, Eq. (i) is not satisfied.

Now, for A = 1, B = 5, Eq. (i) is not satisfied.

We find that A = 2, B = 5 satisfies the Eq. (i).

Hence, A=2, B=5

Question. 58

$$\frac{A \quad A}{\times \quad A} \times \frac{A}{C \quad A \quad B} \quad \text{and} \quad B - A = 1$$

Solution.

Hence, A = 9 and then B = 1, C = 8.

Solution.

In the ones column.

$$B-7=5$$

Clearly. $12-7=5 \text{ so } B=2$

Question. 60

Solution.

In the ones column, C - 5 = 8

Obviously, 13 - 5 = 8, so C = 3

In the ten's column, B - (C + 1) = 8

$$B = 8 + C + 1$$

$$B = 8 + 3 + 1$$

In the hundred's column, A-(B+1)=4

$$A = 4 + B + 1$$

$$A = 4 + 2 + 1 = 7$$

In the thousand's column, B - A = D

Hence,
$$A = 7$$
, $B = 2$, $C = 3$ and $D = 1$

Question. 61 If $27 \div A$ = 33, then find the value of A

Solution. We observe that, 4×3 can never be a single digit number 2, so 4×3 must be a two-digit number, whose ten's digit is 2 and unit's digit is the number less than or equal to 4. Therefore, the value of 4 can be 9, as the values of 4 from 1 to 8 do not fit.

Question. 62 212 x 5 is a multiple of 3 and 11. Find the value of x.

Solution. Since, 212 x 5 is a multiple of 3,

$$2 + 1 + 2 + x + 5 = 0, 3, 6, 9, 12, 15, 18,$$

$$=> 10 + x = 0, 3, 6,...$$

Again, 212×5 is a multiple of 11, (2 + 2 + 5) - (1 + x) = 0,11,22,33

$$=> 8 - x = 0,11,22,...$$

From Eqs. (i) and (ii), we have '

x = 8

Question. 63 Find the value of k, where 31K2 is divisible by 6.

Solution. Given, 31k2 is divisible by 6. Then, it is also divisible by 2 and 3 both.

Now, 31K2 is divisible by 3, sum of its digits is a multiple of 3.

i.e.
$$3+1+k+2=0$$
, 3, 6, 9,12,...

$$=> k+6=0,3,6,9,12$$

$$=> k = 0 \text{ or } 3, 6, 9$$

Question. 64 1y3y6is divisible by 11. Find the value of y.

Solution. It is given that, 1y3y6 is divisible by 11.

Then, we have
$$(1 + 3 + 6) - (y + y) = 0,11,22,...$$

=> 10-2y = 0 [other values give a negative number]

$$=> 2y = 10$$

$$=> y= 5$$

Question. 65 756x is a multiple of 11, find the value of x.

Solution. We are given that, 756x is a multiple of 11. Then, we have to find the value of x.

Since, 756x is divisible by 11, then (7 + 6) - (5 + x) is a multiple of 11,

$$=> 8- x = 0$$

$$=> x = 8$$

Question. 66 A three-digits number 203 is added to the number 326 to give a three-digits number 5b9 Which is divisible by 9. Find the value of b - a.

Solution.

We see that.

In one's column, 3 + 6 = 9 (true)

In third column, 2 + 3 = 5 (true)

∴ a + 2 is a single digit number b as there is no carry-over in the addition.

$$a+2=b \Rightarrow b-a=2$$

Question. 67 Let E = 3, B = 7 and A = 4. Find the other digits in the sum

Given,
$$\frac{+ \ B \ A \ L \ L}{G \ A \ M \ E \ S}$$
, $E = 3$, $B = 7$ and $A = 4$

Now,
$$\frac{+}{G} \frac{7}{4} \frac{4}{L} \frac{L}{L}$$
In one's column, we have $3+L=S$ or $S-L=3$...(i)
In ten's column, we have $S+L=3$...(ii)
On solving Eqs. (i) and (ii), we get.
$$S=3 \text{ and } L=O$$
In hundred's column, we have
$$4+4=M$$

$$M=8$$
and in thousand's column, we have
$$7+7=G4$$

$$14=G4$$

$$G=1$$
Hence $L=O, S=3, M=8$ and $G=1$

Question. 68 Let D = 3, L = 7 and A = 8. Find the other digits in the sum

Solution. In the first column, we have

3 + S + 8, which is definitely a two digits number whose unit's digit is 7.

S must be 6.

Now, in second column, 2A + 1 = 16 + 1 = 7 [1 is carry forward]

In third column, M + 1 is a 2 digit number, therefore M must be 9.

Then, M + 1 = 9 + 1 = 106 = 1, U = 0

Hence, S = 6, M = 9, 6 = 1 and U = 0

Question. 69 If from a two-digit number, we subtract the number formed by reversing its digits then the result so obtained is a perfect cube. How many such numbers are possible? Write all of them.

Solution. Let ab be any two-digit number. Then, the digit formed by reversing it digits is ba.

Now, ab-ba = (10a+b)-(10b+a)

=(10a-a)+(b-10b)

$$= 9a - 9b = 9(a - b)$$

Further, since ab-ba is a perfect cube and is a multiple of 9.

.-. The possible value of a - b is 3.

i.e. a = b + 3

Here, b can take value from 0 to 6.

Hence, possible numbers are as follow.

For b = 0, a = 3, i.e. 30

For b = 1, a = 4, i.e. 41

For b = 2, a = 5, i.e. 52

For b = 3, a = 6, i.e. 63

For b = 4, a = 7, i.e. 74

For b = 5,a = 8, i.e. 85

For b = 6, a = 9, i.e. 96

Question. 70 Work out the following multiplication.

12345679

×	0
5.0	
	_

Use the result to answer the following questions.

- (a) What will be 12345679 x 45?
- (b) What will be 12345679 x 63?
- (c) By what number should 12345679 be multiplied to get 888888888?
- (d) By what number should 12345679 be multiplied to get 999999999? Solution.

12345679

We have, × 9

Here, we observe that in the product all the digits are same i.e. 1, which is actually the unit digit of the product 9×9 . Also, total of digits in the multiplier is 90° .

12345679

(a) We have to compute, × 45

Here, multiplier is 45 whose sum of digits is 9.

Thus, by conjecture we conclude that the product consists of digits 5 only as unit's digit of 9×5 is 5

12345679

× 45 555555555

(b) We have to compute the value of 12345679 x 63. Here, sum of the digits of the multiplier is 9 and unit's digit of the product is 9 and unit's digit of the products of 3 x 9 is 7.

12345679 × 63 = 777777777

- (c) We have to obtain the number 8 in the product, we should multiply the given number 12345679 by 72 as sum of its digits is 9 and 2 x 9 has only digit as 8.
- (d) To get the number 9 in the product we have to find out a two-digit number whose sum of digits is 9 and the product of its unit's digit with the unit's digit of the given number is 9, such number is 81.

Question. 71 Find the value of the letters in each of the following.

$$(i) \frac{\times 6}{0.00}$$

4

(f) We have,
$$\frac{\times}{Q} \frac{6}{Q}$$

Here, in first column, we see that $6 \times QP = Q$. Therefore, the possible values of Q are 2, 4, 6 and 8

For Q = 2, $6 \times P + 1$ can not be equal to 22 for any value of P.

So, Q = 2 is not possible.

Hence,
$$P=7$$
 and $Q=4$

(ii) We have,
$$+\frac{L}{M}\frac{M}{1}\frac{1}{8}$$

In first column,
$$M+1=8$$

Clearly, $M=7$
In second column, $L+M=1$
 $L+7=1$

:. The value of L can be 4.

In third column,
$$2+L+1=M$$

 \Rightarrow $-2+4+1=7$.

 \Rightarrow 7 = 7, so the third column is satisfied for L = 4, M = 7.

Hence, L = 4 and M = 7

Question. 72 If 148101B095 is divisible by 33, find the value of B.

Solution. Given that the number 148101S095 is divisible by 33, therefore it is also divisible by 3 and 11 both.

Now, the number is divisible by 3, its sum of digits is a multiple of 3. i.e. 1 + 4 + 8 + 1 + 0 + 1 + B + 0 + 9 + 5 is a multiple of 3.

Also, given number is divisible by 11, therefore

$$(1+8+0+B+9)-(4+1+1+0+5)=0$$
, 11,22, ...

$$B+7=0,11,22$$

From Eqs. (i) and (ii), we have B = 4

Question. 73 If 123123A4 is divisible by 11, find the value of A.

Solution. Given, 12312344 is divisible by 11, then we have (1 + 3 + 2 + 4) - (2 + 1 + 3 + 4) is a multiple of 11.

$$=> A-4 = 0,11,22,...$$

=> A-4 = 0 [A is a digit of the given number]

=> A = 4

Question. 74 If 56 x 32y is divisible by 18, find the least value of y.

Solution. It is given that, the number 56 x 32y is divisible by 18. Then, it is also divisible by each factor of 18.

Thus, it is divisible by 2 as well as 3.

Now, the number is divisible by-2, its unit's digit must be an even number that is 0, 2,4, 6,

Therefore, the least value of y is 0.

Again, the number is divisible by 3 also, sum of its digits is a multiple of 3. i.e. 5 + 6 + x + 3 + 2 + y is a multiple of 3

=> 16 + x + y = 0, 3, 6, 9,...

=> 16+ x = 18

=>x=2, which is the least value of x.