

Class -VII Mathematics (Ex. 13.1)

Answers

1. (i) $2^6 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 = 64$

(ii) $9^3 = 9 \times 9 \times 9 = 729$

(iii) $11^2 = 11 \times 11 = 121$

(iv) $5^4 = 5 \times 5 \times 5 \times 5 = 625$

2. (i) $6 \times 6 \times 6 \times 6 = 6^4$

(ii) $t \times t = t^2$

(iii) $b \times b \times b \times b = b^4$

(iv) $5 \times 5 \times 7 \times 7 \times 7 = 5^2 \times 7^3$

(v) $2 \times 2 \times a \times a = 2^2 \times a^2$

(vi) $a \times a \times a \times c \times c \times c \times d = a^3 \times c^4 \times d$

3. (i) 512

$$= 2 \times 2 = 2^9$$

2	512
2	256
2	128
2	64
2	32
2	16
2	8
2	4
2	2
	1

(ii) 343

$$= 7 \times 7 \times 7 = 7^3$$

7	343
7	49
7	7
	1

(iii) 729

$$= 3 \times 3 \times 3 \times 3 \times 3 \times 3 = 3^6$$

3	729
3	243
3	81
3	27
3	9
3	3
	1

(iv) 3125

5	3125
5	625
5	125
5	25
5	5
	1

4. (i) $4^3 = 4 \times 4 \times 4 = 64$
 $3^4 = 3 \times 3 \times 3 \times 3 = 81$
 Since $64 < 81$
 Thus, 3^4 is greater than 4^3 .
- (ii) $5^3 = 5 \times 5 \times 5 = 125$
 $3^5 = 3 \times 3 \times 3 \times 3 \times 3 = 243$
 Since, $125 < 243$
 Thus, 3^4 is greater than 5^3 .
- (iii) $2^8 = 2 \times 2 = 256$
 $8^2 = 8 \times 8 = 64$
 Since, $256 > 64$
 Thus, 2^8 is greater than 8^2 .
- (iv) $100^2 = 100 \times 100 = 10,000$
 $2^{100} = 2 \times 2 \times 2 \times 2 \times 2 \times \dots \text{14 times } \times \dots \times 2 = 16,384 \times \dots \times 2$
 Since, $10,000 < 16,384 \times \dots \times 2$
 Thus, 2^{100} is greater than 100^2 .

5. (i) $648 = 2^3 \times 3^4$

2	648
2	324
2	162
3	81
3	27
3	9
3	3
	1

(ii) $405 = 5 \times 3^4$

5	405
3	81
3	27
3	9
3	3
	1

(iii) $540 = 2^2 \times 3^3 \times 5$

2	540
2	270
3	135
3	45
3	15
5	5
	1

(iv) $3,600 = 2^4 \times 3^2 \times 5^2$

2	3600
2	1800
2	900
2	450
3	225
3	75
5	25
5	5
	1

6. (i) $2 \times 10^3 = 2 \times 10 \times 10 \times 10 = 2,000$

(ii) $7^2 \times 2^2 = 7 \times 7 \times 2 \times 2 = 196$

(iii) $2^3 \times 5 = 2 \times 2 \times 2 \times 5 = 40$

(iv) $3 \times 4^4 = 3 \times 4 \times 4 \times 4 \times 4 = 768$

(v) $0 \times 10^2 = 0 \times 10 \times 10 = 0$

(vi) $5^3 \times 3^3 = 5 \times 5 \times 3 \times 3 \times 3 = 675$

(vii) $2^4 \times 3^2 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 = 144$

(viii) $3^2 \times 10^4 = 3 \times 3 \times 10 \times 10 \times 10 \times 10 = 90,000$

7. (i) $(-4)^3 = (-4) \times (-4) \times (-4) = -64$

(ii) $(-3) \times (-2)^3 = (-3) \times (-2) \times (-2) \times (-2) = 24$

(iii) $(-3)^2 \times (-5)^2 = (-3) \times (-3) \times (-5) \times (-5) = 225$

(iv) $(-2)^3 \times (-10)^3 = (-2) \times (-2) \times (-2) \times (-10) \times (-10) \times (-10)$

8. (i) 2.7×10^{12} and 1.5×10^8

On comparing the exponents of base 10,

$$2.7 \times 10^{12} > 1.5 \times 10^8$$

(ii) 4×10^{14} and 3×10^{17}

On comparing the exponents of base 10,

$$4 \times 10^{14} < 3 \times 10^{17}$$

Class -VII Mathematics (Ex. 13.1)

Questions

Class -VII Mathematics (Ex. 13.2)
Answers

1. (i) $3^2 \times 3^4 \times 3^8 = 3^{(2+4+8)} = 3^{14}$ $\left[\because a^m \times a^n = a^{m+n} \right]$
(ii) $6^{15} \div 6^{10} = 6^{15-10} = 6^5$ $\left[\because a^m \div a^n = a^{m-n} \right]$
(iii) $a^3 \times a^2 = a^{3+2} = a^5$ $\left[\because a^m \times a^n = a^{m+n} \right]$
(iv) $7^x \times 7^2 = 7^{x+2}$ $\left[\because a^m \times a^n = a^{m+n} \right]$
(v) $(5^2)^3 \div 5^3 = 5^{2 \times 3} \div 5^3 = 5^6 \div 5^3$ $\left[\because (a^m)^n = a^{m \times n} \right]$
 $= 5^{6-3} = 5^3$ $\left[\because a^m \div a^n = a^{m-n} \right]$
(vi) $2^5 \times 5^5 = (2 \times 5)^5 = 10^5$ $\left[\because a^m \times b^m = (a \times b)^m \right]$
(vii) $a^4 \times b^4 = (a \times b)^4$ $\left[\because a^m \times b^m = (a \times b)^m \right]$
(viii) $(3^4)^3 = 3^{4 \times 3} = 3^{12}$ $\left[\because (a^m)^n = a^{m \times n} \right]$
(ix) $(2^{20} \div 2^{15}) \times 2^3 = (2^{20-15}) \times 2^3$ $\left[\because a^m \div a^n = a^{m-n} \right]$
 $= 2^5 \times 2^3 = 2^{5+3} = 2^8$ $\left[\because a^m \times a^n = a^{m+n} \right]$
(x) $8^t \div 8^2 = 8^{t-2}$ $\left[\because a^m \div a^n = a^{m-n} \right]$
2. (i) $\frac{2^3 \times 3^4 \times 4}{3 \times 32} = \frac{2^3 \times 3^4 \times 2^2}{3 \times 2^5} = \frac{2^{3+2} \times 3^4}{3 \times 2^5}$ $\left[\because a^m \times a^n = a^{m+n} \right]$
 $= \frac{2^5 \times 3^4}{3 \times 2^5} = 2^{5-5} \times 3^{4-3}$ $\left[\because a^m \div a^n = a^{m-n} \right]$
 $= 2^0 \times 3^3 = 1 \times 3^3 = 3^3$
(ii) $\left[(5^2)^3 \times 5^4 \right] \div 5^7 = \left[5^6 \times 5^4 \right] \div 5^7$ $\left[\because (a^m)^n = a^{m \times n} \right]$
 $= \left[5^{6+4} \right] \div 5^7 = 5^{10} \div 5^7$ $\left[\because a^m \times a^n = a^{m+n} \right]$
 $= 5^{10-7} = 5^3$ $\left[\because a^m \div a^n = a^{m-n} \right]$
(iii) $25^4 \div 5^3 = (5^2)^4 \div 5^3 = 5^8 \div 5^3$ $\left[\because a^m \div a^n = a^{m-n} \right]$
 $= 5^{8-3} = 5^5$ $\left[\because a^m \div a^n = a^{m-n} \right]$
(iv) $\frac{3 \times 7^2 \times 11^8}{21 \times 11^3} = \frac{3 \times 7^2 \times 11^8}{3 \times 7 \times 11^3} = 3^{1-1} \times 7^{2-1} \times 11^{8-3}$ $\left[\because a^m \div a^n = a^{m-n} \right]$
 $= 3^0 \times 7^1 \times 11^5 = 7 \times 11^5$
(v) $\frac{3^7}{3^4 \times 3^3} = \frac{3^7}{3^{4+3}} = \frac{3^7}{3^7}$ $\left[\because a^m \times a^n = a^{m+n} \right]$

	$= 3^{7-7} = 3^0 = 1$	$\left[\because a^m \div a^n = a^{m-n} \right]$
(vi)	$2^0 + 3^0 + 4^0 = 1 + 1 + 1 = 3$	$\left[\because a^0 = 1 \right]$
(vii)	$2^0 \times 3^0 \times 4^0 = 1 \times 1 \times 1 = 1$	$\left[\because a^0 = 1 \right]$
(viii)	$(3^0 + 2^0) \times 5^0 = (1+1) \times 1 = 2 \times 1 = 2$	$\left[\because a^0 = 1 \right]$
(ix)	$\frac{2^8 \times a^5}{4^3 \times a^3} = \frac{2^8 \times a^5}{(2^2)^3 \times a^3} = \frac{2^8 \times a^5}{2^6 \times a^3}$ $= 2^{8-6} \times a^{5-2} = 2^2 \times a^2$ $= (2a)^2$	$\left[\because (a^m)^n = a^{m \times n} \right]$ $\left[\because a^m \div a^n = a^{m-n} \right]$ $\left[\because a^m \times b^m = (a \times b)^m \right]$
(x)	$\left(\frac{a^5}{a^3} \right) \times a^8 = (a^{5-3}) \times a^8 = a^2 \times a^8$ $= a^{2+8} = a^{10}$	$\left[\because a^m \div a^n = a^{m-n} \right]$ $\left[\because a^m \times a^n = a^{m+n} \right]$
(xi)	$\frac{4^5 \times a^8 b^3}{4^5 \times a^5 b^2} = 4^{5-5} \times a^{8-5} \times b^{3-2} = 4^0 \times a^3 \times b$ $= 1 \times a^3 \times b = a^3 b$	$\left[\because a^m \div a^n = a^{m-n} \right]$ $\left[\because a^0 = 1 \right]$
(xii)	$(2^3 \times 2)^2 = (2^{3+1})^2 = (2^4)^2$ $= 2^{4 \times 2} = 2^8$	$\left[\because a^m \times a^n = a^{m+n} \right]$ $\left[\because (a^m)^n = a^{m \times n} \right]$

3. (i) $10 \times 10^{11} = 100^{11}$
L.H.S. $10^{1+11} = 10^{12}$ and R.H.S. $(10^2)^{11} = 10^{22}$

Since, L.H.S. \neq R.H.S.
Therefore, it is false.

(ii) $2^3 > 5^2$
L.H.S. $2^3 = 8$ and R.H.S. $5^2 = 25$

Since, L.H.S. is not greater than R.H.S.
Therefore, it is false.

(iii) $2^3 \times 3^2 = 6^5$
L.H.S. $2^3 \times 3^2 = 8 \times 9 = 72$ and R.H.S. $6^5 = 7,776$

Since, L.H.S. \neq R.H.S.
Therefore, it is false.

(iv) $3^0 = (1000)^0$
L.H.S. $3^0 = 1$ and R.H.S. $(1000)^0 = 1$

Since, L.H.S. = R.H.S.
Therefore, it is true.

4. (i) 108×192
 $= (2^2 \times 3^3) \times (2^6 \times 3)$
 $= 2^{2+6} \times 3^{3+1}$
 $= 2^8 \times 3^4$

2	192
2	96
2	48
2	24
2	12
2	6
3	3
	1

(ii) 270
 $= 2 \times 3^5 \times 5$

2	270
3	135
3	45
3	15
5	5
	1

(iii) 729×64
 $= 3^6 \times 2^6$

2	64
2	32
2	16
2	8
2	4
2	2
	1

(iv) 768
 $= 2^8 \times 3$

2	768
2	384
2	192
2	96
2	48
2	24
2	12
2	6
3	3
	1

$$\begin{aligned}
 5. \quad (i) \quad & \frac{(2^5)^2 \times 7^3}{8^3 \times 7} = \frac{2^{5 \times 2} \times 7^3}{(2^3)^3 \times 7} \\
 &= \frac{2^{10} \times 7^3}{2^9 \times 7} \\
 &= 2^{10-9} \times 7^{3-1} = 2 \times 7^2 \\
 &= 2 \times 49 \\
 &= 98
 \end{aligned}$$

$$\begin{aligned}
 (ii) \quad & \frac{25 \times 5^2 \times t^8}{10^3 \times t^4} = \frac{5^2 \times 5^2 \times t^8}{(5 \times 2)^3 \times t^4} \\
 &= \frac{5^{2+2} \times t^{8-4}}{2^3 \times 3^3} \\
 &= \frac{5^4 \times t^4}{2^3 \times 5^3} \\
 &= \frac{5^{4-3} \times t^4}{2^3} \\
 &= \frac{5t^4}{8}
 \end{aligned}$$

$$\begin{aligned}
 (iii) \quad & \frac{3^5 \times 10^5 \times 25}{5^7 \times 6^5} = \frac{3^5 \times (2 \times 5)^5 \times 5^2}{5^7 \times (2 \times 3)^5} \\
 &= \frac{3^5 \times 2^5 \times 5^5 \times 5^2}{5^7 \times 2^5 \times 3^5} \\
 &= \frac{3^5 \times 2^5 \times 5^{5+2}}{5^7 \times 2^5 \times 3^5} \\
 &= \frac{3^5 \times 2^5 \times 5^7}{5^7 \times 2^5 \times 3^5} \\
 &= 2^{5-5} \times 3^{5-5} \times 5^{5-5} \\
 &= 2^0 \times 3^0 \times 5^0 \\
 &= 1 \times 1 \times 1 \\
 &= 1
 \end{aligned}$$

Class -VII Mathematics (Ex. 13.2)
Questions

1. Using laws of exponents, simplify and write the answer in exponential form:

- | | |
|--|---------------------------|
| (i) $3^2 \times 3^4 \times 3^8$ | (ii) $6^{15} \div 6^{10}$ |
| (iii) $a^3 \times a^2$ | (iv) $7^x \times 7^2$ |
| (v) $(5^2)^2 \div 5^3$ | (vi) $2^5 \times 5^5$ |
| (vii) $a^4 \times b^4$ | (viii) $(3^4)^3$ |
| (ix) $(2^{20} \div 2^{15}) \times 2^3$ | (x) $8^t \div 8^2$ |

2. Simplify and express each of the following in exponential form:

- | | |
|--|--|
| (i) $\frac{2^3 \times 3^4 \times 4}{3 \times 32}$ | (ii) $\left[(5^2)^3 \times 5^4 \right] \div 5^7$ |
| (iii) $25^4 \div 5^3$ | (iv) $\frac{3 \times 7^2 \times 11^8}{21 \times 11}$ |
| (v) $\frac{3^7}{3^4 \times 3^3}$ | (vi) $2^0 + 3^0 + 4^0$ |
| (vii) $2^0 \times 3^0 \times 4^0$ | (viii) $(3^0 + 2^0) \times 5^0$ |
| (ix) $\frac{2^8 \times a^5}{4^3 \times a^3}$ | (x) $\left(\frac{a^5}{a^3} \right) \times a^8$ |
| (xi) $\frac{4^5 \times a^8 b^3}{4^5 \times a^5 b^2}$ | (xii) $(2^3 \times 2)^2$ |

3. Say true or false and justify your answer:

- | | |
|------------------------------------|-----------------------|
| (i) $10 \times 10^{11} = 100^{11}$ | (ii) $2^3 > 5^2$ |
| (iii) $2^3 \times 3^2 = 6^5$ | (iv) $3^0 = (1000)^0$ |

4. Express each of the following as a product of prime factors only in exponential form:

- | | |
|-----------------------|------------|
| (i) 108×192 | (ii) 270 |
| (iii) 729×64 | (iv) 768 |

5. Simplify:

- | |
|--|
| (i) $\frac{(2^5)^2 \times 7^3}{8^3 \times 7}$ |
| (ii) $\frac{25 \times 5^2 \times t^8}{10^3 \times t^4}$ |
| (iii) $\frac{3^5 \times 10^5 \times 25}{5^7 \times 6^5}$ |

Class -VII Mathematics (Ex. 13.3)

Answers

1. (i) 2,79,404 $= 2,00,000 + 70,000 + 9,000 + 400 + 00 + 4$
 $= 2 \times 100000 + 7 \times 10000 + 9 \times 1000 + 4 \times 100 + 0 \times 10 + 4 \times 1$
 $= 2 \times 10^5 + 7 \times 10^4 + 9 \times 10^3 + 4 \times 10^2 + 0 \times 10^1 + 4 \times 10^0$
 - (ii) 30,06,194 $= 30,00,000 + 0 + 0 + 6,000 + 100 + 90 + 4$
 $= 3 \times 1000000 + 0 \times 100000 + 0 \times 10000 + 6 \times 1000 + 1 \times 100 + 9 \times 10 + 4 \times 1$
 $= 3 \times 10^6 + 0 \times 10^5 + 0 \times 10^4 + 6 \times 10^3 + 1 \times 10^2 + 9 \times 10 + 4 \times 10^0$
 - (iii) 28,06,196 $= 20,00,000 + 8,00,000 + 0 + 6,000 + 100 + 90 + 6$
 $= 2 \times 1000000 + 8 \times 100000 + 0 \times 10000 + 6 \times 1000 + 1 \times 100 + 9 \times 10 + 6 \times 1$
 $= 2 \times 10^6 + 8 \times 10^5 + 0 \times 10^4 + 6 \times 10^3 + 1 \times 10^2 + 9 \times 10 + 6 \times 10^0$
 - (iv) 1,20,719 $= 1,00,000 + 20,000 + 0 + 700 + 10 + 9$
 $= 1 \times 100000 + 2 \times 10000 + 0 \times 1000 + 7 \times 100 + 1 \times 10 + 9 \times 1$
 $= 1 \times 10^5 + 2 \times 10^4 + 0 \times 10^3 + 7 \times 10^2 + 1 \times 10^1 + 9 \times 10^0$
 - (v) 20,068 $= 20,000 + 00 + 00 + 60 + 8$
 $= 2 \times 10000 + 0 \times 1000 + 0 \times 100 + 6 \times 10 + 8 \times 1$
 $= 2 \times 10^4 + 0 \times 10^3 + 0 \times 10^2 + 6 \times 10^1 + 8 \times 10^0$
2. (a) $8 \times 10^4 + 6 \times 10^3 + 0 \times 10^2 + 4 \times 10^1 + 5 \times 10^0$
 $= 8 \times 10000 + 6 \times 1000 + 0 \times 100 + 4 \times 10 + 5 \times 1$
 $= 80000 + 6000 + 0 + 40 + 5$
 $= 86,045$
 - (b) $4 \times 10^5 + 5 \times 10^3 + 3 \times 10^2 + 2 \times 10^0$
 $= 4 \times 100000 + 0 \times 10000 + 5 \times 1000 + 3 \times 100 + 0 \times 10 + 2 \times 1$
 $= 400000 + 0 + 5000 + 3000 + 0 + 2$
 $= 4,05,302$
 - (c) $3 \times 10^4 + 7 \times 10^2 + 5 \times 10^0$
 $= 3 \times 10000 + 0 \times 1000 + 7 \times 100 + 0 \times 10 + 5 \times 1$
 $= 30000 + 0 + 700 + 0 + 5$
 $= 30,705$
 - (d) $9 \times 10^5 + 2 \times 10^2 + 3 \times 10^1$
 $= 9 \times 100000 + 0 \times 10000 + 0 \times 1000 + 2 \times 100 + 3 \times 10 + 0 \times 1$
 $= 900000 + 0 + 0 + 200 + 30 + 0$
 $= 9,00,230$
3. (i) 5,00,00,000 $= 5 \times 1,00,00,000 = 5 \times 10^7$
 - (ii) 70,00,000 $= 7 \times 10,00,000 = 7 \times 10^6$
 - (iii) 3,18,65,00,000 $= 31865 \times 100000 = 3.1865 \times 10000 \times 100000 = 3.1865 \times 10^9$
 - (iv) 3,90,878 $= 3.90878 \times 100000 = 3.90878 \times 10^5$
 - (v) 39087.8 $= 3.90878 \times 10000 = 3.90878 \times 10^4$

	(vi)	3908.78	$= 3.90878 \times 1000 = 3.90878 \times 10^3$
4.	(a)	The distance between Earth and Moon	$= 384,000,000 \text{ m}$ $= 384 \times 1000000 \text{ m} = 3.84 \times 100 \times 1000000$ $= 3.84 \times 10^8 \text{ m}$
	(b)	Speed of light in vacuum	$= 300,000,000 \text{ m/s}$ $= 3 \times 100000000 \text{ m/s}$ $= 3 \times 10^8 \text{ m/s}$
	(c)	Diameter of the Earth	$= 1,27,56,000 \text{ m}$ $= 12756 \times 1000 \text{ m} = 1.2756 \times 10000 \times 1000 \text{ m}$ $= 1.2756 \times 10^7 \text{ m}$
	(d)	Diameter of the Sun	$= 1,400,000,000 \text{ m}$ $= 14 \times 100,000,000 \text{ m} = 1.4 \times 10 \times 100,000,000 \text{ m}$ $= 1.4 \times 10^9 \text{ m}$
	(e)	Average of Stars	$= 100,000,000,000$ $= 1 \times 100,000,000,000$ $= 1 \times 10^{11}$
	(f)	Years of Universe	$= 12,000,000,000 \text{ years}$ $= 12 \times 1000,000,000 \text{ years}$ $= 1.2 \times 10 \times 1000,000,000 \text{ years}$ $= 1.2 \times 10^{10} \text{ years}$
	(g)	Distance of the Sun from the centre of the Milky Way Galaxy	$= 300,000,000,000,000,000,000 \text{ m}$ $= 3 \times 100,000,000,000,000,000,000 \text{ m}$ $= 3 \times 10^{20} \text{ m}$
	(h)	Number of molecules in a drop of water weighing 1.8 gm	$= 60,230,000,000,000,000,000,000$ $= 6023 \times 10,000,000,000,000,000,000$ $= 6.023 \times 1000 \times 10,000,000,000,000,000,000$ $= 6.023 \times 10^{22}$
	(i)	The Earth has Sea water	$= 1,353,000,000 \text{ km}^3$ $= 1,353 \times 1000000 \text{ km}^3$ $= 1.353 \times 1000 \times 1000,000 \text{ km}^3$ $= 1.353 \times 10^9 \text{ km}^3$
	(j)	The population of India	$= 1,027,000,000$ $= 1027 \times 1000000$ $= 1.027 \times 1000 \times 1000000$ $= 1.027 \times 10^9$

Class -VII Mathematics (Ex. 13.3)
Questions

1. Write the following numbers in the expanded form:
279404, 3006194, 2806196, 120719, 20068
2. Find the number from each of the following expanded forms:
 - (a) $8 \times 10^4 + 6 \times 10^3 + 0 \times 10^2 + 4 \times 10^1 + 5 \times 10^0$
 - (b) $4 \times 10^5 + 5 \times 10^3 + 3 \times 10^2 + 2 \times 10^0$
 - (c) $3 \times 10^4 + 7 \times 10^2 + 5 \times 10^0$
 - (d) $9 \times 10^5 + 2 \times 10^2 + 3 \times 10^1$
3. Express the following numbers in standard form:

(i) 5,00,00,000	(ii) 70,00,000
(iii) 3,18,65,00,000	(iv) 3,90,878
(v) 39087.8	(vi) 3908.78
4. Express the number appearing in the following statements in standard form:
 - (a) The distance between Earth and Moon is 384,000,000 m.
 - (b) Speed of light in vacuum is 300,000,000 m/s.
 - (c) Diameter of Earth id 1,27,56,000 m.
 - (d) Diameter of the Sun is 1,400,000,000 m.
 - (e) In a galaxy there are on an average 100,000,000,000 stars.
 - (f) The universe is estimated to be about 12,000,000,000 years old.
 - (g) The distance of the Sun from the centre of the Milky Way Galaxy is estimated to be 300,000,000,000,000,000 m.
 - (h) 60,230,000,000,000,000,000 molecules are contained in a drop of water weighing 1.8 gm.
 - (i) The Earth has 1,353,000,000 cubic km of sea water.
 - (j) The population of India was about 1,027,000,000 in march, 2001.