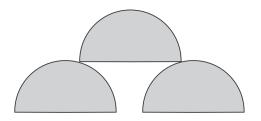
Surface Areas and Volumes

Case Study Based Questions

Case Study 1

Priyansh had three hemispherical shaped boxes. He thought of putting down his stationary in one of these boxes, so that it does not get lost. The radius of each hemispherical box is 7 cm.



On the basis of the above information, solve the following questions:

Q1. The capacity of a box is:

a. 730 cm ³	b. 1500 cm³	
$c 719.67 \text{ cm}^3$	d 1000 cm ³	

c. 718.67 cm ³	d. 1900 cm

Q2. If any two box is melted and recasted into a single sphere, then radius of sphere will be:

a. 3.5 cm l	b. 7 cm
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c. 14 cm d. 10.5 cm

Q3. The base area of a box is:

- a. 150 cm² b. 180 cm²
- c. 154 cm² d. 170 cm²

Q4. The total surface area of a box is:

- a. 340 cm² b. 308 cm²
- c. 380 cm² d. 830 cm²

Q5. If the cost of painting a box per cm^2 is \gtrless 2, then the total cost of painting a box is:

a. 740 b. 750

c. 730 d. 616

Solutions

(c) Given, radius, r = 7 cm
 ∴ The capacity of a box = Volume of hemispherical shaped box

$$= \frac{2}{3}\pi r^{3}$$
$$= \frac{2}{3} \times \frac{22}{7} \times (7)^{3} = \frac{2156}{3}$$
$$= 718.67 \text{ cm}^{3}$$

So, option (c) is correct.

2. (b) Given, 2× Volume of hemisphere = Volume of sphere

$$\Rightarrow 2 \times \frac{2}{3} \times \pi \times (7)^3 = \frac{4}{3} \pi R^3$$
$$\Rightarrow 7^3 = R^3$$
$$\Rightarrow R = 7 \text{ cm}$$

Hence, radius of required sphere is 7cm. So, option (b) is correct.

3. (c) The base area of a box = πr^2

$$=\frac{22}{7}\times(7)^2=154$$
 cm²

So, option (c) is correct.

4. (b) The total surface area of a box = $2\pi r^2$

$$= 308 \text{ cm}^2$$

So, option (b) is correct.

5. (d) Given, 1 cm² area is painted in ₹ 2.
 Therefore, 308 cm² area is painted in ₹ 2 × 308

So, option (d) is correct.

Case Study 2

During vacation, two friends decided to visit Shimla. Due to peak days in Shimla, they did not get any room to stay it. So, they thought to buy a tent and set up in a park. They made a tent in the shape of cone, whose diameter is 14 cm and height is 22 cm.



On the basis of the above information, solve the following questions:

Q1. How much volume of air is stored in a conical tent?

a. 1140 cm ³	b. 1132 cm³

c. 1129.33 cm³ d. 1134 cm³

Q2. The slant height of a cone is:

a. √521 cm	b. √533 cm

c. $2\sqrt{533}$ cm d. $\sqrt{537}$ cm

Q3. The base area covered by a conical tent is:

c. 154 cm² d. 159 cm²

Q4. The curved surface area of a conical tent is:

(Use
$$\sqrt{533} = 23.09$$
)

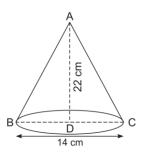
- a. 508 cm² b. 507.98 cm²
- c. 509 cm^2 d. 512 cm^2

Q5. If the cost of painting a tent is 50 paise per cm², then the cost of painting the tent is (approximate):

a. 260 b. 255

Solutions

1. (c) Given, diameter of cone, d = 14 cm and height of cone, h = 22 cm



Therefore, radius of a cone, $r = \frac{d}{2} = \frac{14}{2} = 7$ cm

... Volume of air stored in a conical tent

= Volume of cone

$$=\frac{1}{3}\pi r^{2}h=\frac{1}{3}\times\frac{22}{7}\times(7)^{2}\times22 \text{ cm}^{3}$$

= 1129.33 cm³

So, option (c) is correct.

2. (b)

 \therefore The slant height of a cone = $\sqrt{(7)^2 + (22)^2}$

$$=\sqrt{49+484} = \sqrt{533}$$
 cm

So, option (b) is correct.

3. (c) The base area covered by a conical tent is $A = Area \text{ of circle} = \pi r^2$

$$= \frac{22}{7} \times (7)^2 = 22 \times 7 = 154 \text{ cm}^2$$

So, option (c) is correct.

4. (b) The curved surface area of a conical tent = πrl

$$= \frac{22}{7} \times 7 \times \sqrt{533}$$
 [∵ *l* = $\sqrt{533}$ cm]
= 22 × 23.09 = 507.98 cm²
So, option (b) is correct.

5. (c) Given, 1 cm² is painted for 50 paise or ₹ 0.5.
∴ 507.98 cm² is painted for ₹ 507.98 × 0.5
= ₹ 253.99 ≈ ₹ 254
So, option (c) is correct.

Case Study 3

For decoration purpose, Sneha bought 100 orbeez balls and put it in a cylindrical shaped box. After filling it with water, the orbeez ball swell up and completely filled the cylindrical shaped box. Behind the orbeez ball packet, the change in volume of each orbeez ball was mentioned and which was 32% increase. Suppose the volume of all orbeez ball is 9900 cm³.



On the basis of the above information, solve the following questions:

Q1. The volume of each orbeez ball is:

a. 97 cm ³	b. 99 cm³
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c. 96 cm³ d. 94 cm³

Q2. Volume of orbeez ball before swelling is:

- a. 70 cm³ b. 78 cm³
- c. 75 cm³ d. 85 cm³

Q3. How many orbeez balls before swelling was needed to completely fill the cylindrical shaped box?

b. 138

c. 134 d. 140

Q4. What is the cubic radius of an orbeez ball before swelling up?

a. 17.30 cm³ b. 16.50 cm³

7.89 cm^3

Q5. If the change in volume of orbeez ball is increased to 48%, then the volume of orbeez ball after swell up will be:

c. 112 cm ³	d. 116 cm³
	u. 110 cm

Solutions

- 1. (b) Volume of 1 orbeez ball \times 100 = Volume of all orbeez ball
 - \therefore Volume of one orbeez ball $= \frac{9900}{100} = 99 \text{ cm}^3$

So, option (b) is correct.

2. (c) Let original volume of orbeez ball be *x*. Change in volume of orbeez ball

$$=\frac{99-x}{x}\times100$$

Given,

...

$$32 = \frac{(99 - x) \times 100}{x}$$

$$\Rightarrow \qquad 32x = 9900 - 100x$$

 \Rightarrow 132 x = 9900

$$\Rightarrow \qquad \qquad x = \frac{9900}{132}$$

$$x = 75 \text{ cm}^3$$

So, option (c) is correct.

3. (a) n x Volume of 1 orbeez ball before swell up

= Volume of container

 \Rightarrow n x 75 cm³ = 9900 cm³

 \Rightarrow n = $\frac{9900}{75}$

∴ n = 132 balls

So, option (a) is correct.

4. (d) Volume of an orbeez ball before swell up = 75 cm^3

$$\Rightarrow \qquad \frac{4}{3}\pi r^3 = 75$$
$$\Rightarrow \qquad \frac{4}{3} \times \frac{22}{7} \times r^3 = 75$$
$$\Rightarrow \qquad r^3 = \frac{75 \times 3 \times 7}{4 \times 22}$$
$$\therefore \qquad r^3 = 17.89 \text{ cm}^3$$

So, option (d) is correct.

5. (b) Let the volume of orbeez ball after swell up be x.

Then,	$48 = \frac{x - 75}{75} \times 100$
\Rightarrow	$48 = \frac{x - 75}{3} \times 4$
\Rightarrow	$48 \times 3 = 4x - 300$
\Rightarrow	$4x = 144 + 300 \Longrightarrow 4x = 444 \text{ cm}^3$
<i>.</i>	$x = 111 \text{ cm}^3$

So, option (b) is correct.

Case Study 4

Students of class IX were taken to an educational trip to Delhi. They were first shown Humayun's Tomb. It was the tomb of Mughal Emperor Humayun and is a great example of Mughal Architecture and it is an UNESCO approved World Heritage site. Since, it was a very old monument restoration and paint was going on. Maths teacher decided to ask some questions. He told them in the figure a dome can be seen, when radius of the dome is 15 m and, in the monument, there can be seen 2 pillars which resembles a cylinder whose radius and height is 28 m and 47 m.



On the basis of the above information, solve the following questions:

Q1. Find the curved surface area of the dome.

Q2. Find the volume of the dome.

Solutions

1. The dome resembles a hemispherical sphere

Given, radius = 15 m

Curved surface area of the hemispherical sphere

= 2πг²

$$= 2 \times \frac{22}{7} \times 15 \times 15 = \frac{9900}{7} \text{ m}^2$$

2. Volume of the dome = Volume of hemisphere

$$= \frac{2}{3}\pi r^{3}$$

= $\frac{2}{3} \times \frac{22}{7} \times 15 \times 15 \times 15 = \frac{49500}{7}$
= 7071.43 m³