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NDAY

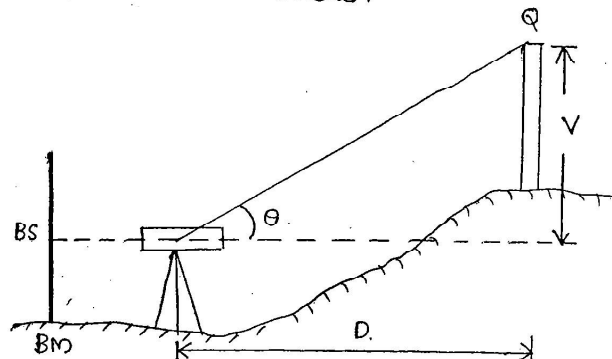
TRIGONOMETRICAL LEVELLING

It is an indirect levelling in which heights and distances can be calculated by measuring vertical angles.

Case 1: When the base of object is accessible.

$$V = D \tan \theta$$

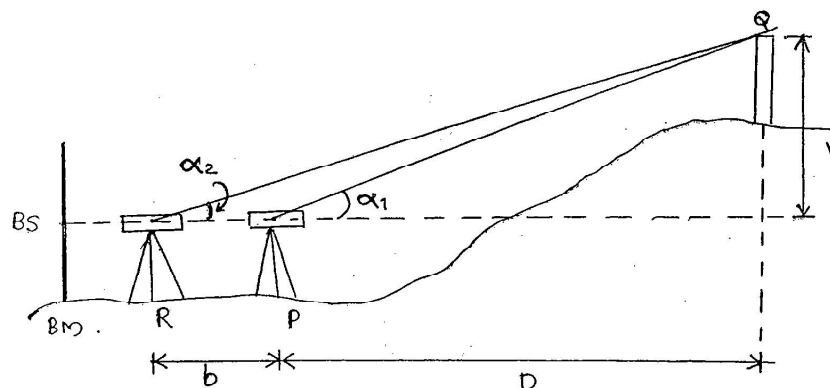
$$\text{RL of } Q = \text{RL of BM} + \text{BS} + v.$$



Case 2: Base of object is inaccessible.

Instrument stations & Object must be in same vertical plane

a) Instrument axes are at the same level.



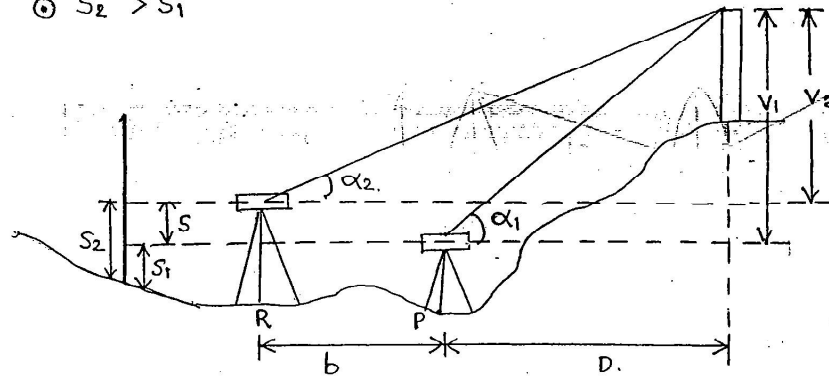
$$V = D \tan \alpha_1 = (D + b) \tan \alpha_2$$

$$D = \frac{b \tan \alpha_2}{(\tan \alpha_1 - \tan \alpha_2)}$$

$$RL \text{ of } Q = RL \text{ of BM} + BS + V_1$$

b) Instrument axes are at different levels

$$\odot S_2 > S_1$$



$$S_2 - S_1 = S = V_1 - V_2$$

$$= D \tan \alpha_1 - (D+b) \tan \alpha_2$$

$$D = \frac{S + b \tan \alpha_2}{\tan \alpha_1 - \tan \alpha_2}$$

$$RL \text{ of } Q = RL \text{ of BM} + S_1 + V_1 \quad (\text{or})$$

$$RL \text{ of BM} + S_2 + V_2$$

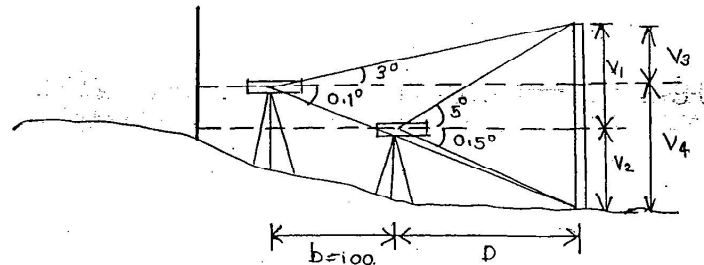
$$\odot S_2 < S_1$$

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$$D = \frac{S - b \tan \alpha_2}{\tan \alpha_2 - \tan \alpha_1}$$

Q Horizontal distance b/w 2 stations P & Q is 100 m. The vertical angles from P & Q to the top of a vertical tower, at T are 3° & 5° above horizontal resp. The vertical angle from the P & Q to the base of tower are 0.1° & 0.5° below horizontal resp. Stations P & Q and tower are in the same vertical plane, and also P & Q being on the same side of T.

Neglecting combined correction, height in m of tower is 9 (96)



$$h = V_1 + V_2 = V_3 + V_4$$

$$\Rightarrow D \tan 5^\circ + D \tan 0.5^\circ = (100 + D) \tan 3^\circ + (100 + D) \tan 0.1^\circ$$

$$0.0962 D = 5.415 + 0.054 D$$

$$0.042 D = 5.415$$

$$D = \underline{\underline{128.78 \text{ m}}}$$

$$\begin{aligned} \therefore \text{Height of object} &= D (\tan 5^\circ + \tan 0.5^\circ) \\ &= \underline{\underline{12.39 \text{ m}}} \end{aligned}$$