

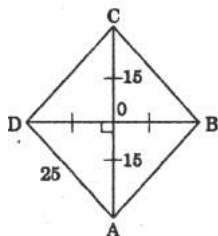
Surface Areas and Volumes

IIT Foundation Material

SECTION - I

Straight Objective Type

1.



Area of rhombus

$$= \frac{1}{2} d_1 d_2$$

$$= \frac{1}{2} \times 30 \times d_2$$

$$OD^2 = 25^2 - 15^2$$

$$= 625 - 225 \Rightarrow d_2 = 2 \times OD$$

$$= 400 \quad \quad \quad = 2 \times 20$$

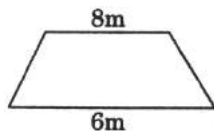
$$OD = 20 = 40$$

$$\Rightarrow \text{Area of rhombus} = \frac{1}{2} \times 30 \times 40$$

$$= 30 \times 20 = 600 \text{ sq.cm}$$

Hence (a) is the correct option.

2.



Area of the trapezium

$$= \frac{h}{2} (a + b)$$

$$644 = \frac{h}{2}(8+6)$$

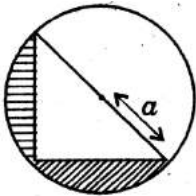
$$644 \times 2 = 14h$$

$$\Rightarrow h = \frac{644 \times 2}{14} = 46 \times 2 = 92m$$

The length of the canal = 92 m.

Hence (b) is the correct option.

3. Area of the shaded portion = $\frac{a^2}{2} \left(\frac{\pi}{2} - 1 \right)$



Hence (d) is the correct option.

4. Area of the triangle

$$\Delta_1 = \sqrt{s(s-a)(s-b)(s-c)}$$

$$\text{where } s = \frac{a+b+c}{2}$$

If the sides of a triangle are doubled

$$s^1 = \frac{2a+2b+2c}{2} = \frac{2(a+b+c)}{2} = 2s$$

$$\Delta^1 = \sqrt{s^1(s^1-2a)(s^1-2b)(s^1-2c)}$$

$$= \sqrt{2s(2s-2a)(2s-2b)(2s-2c)}$$

$$= \sqrt{16s(s-a)(s-b)(s-c)}$$

$$\Rightarrow = 4\sqrt{s(s-a)(s-b)(s-c)}$$

$$= 4\Delta$$

The area becomes four times

Hence (d) is the correct option

5.

$$b_1 = 15dm$$

$$h_1 = 12dm$$

$$A_1 = \frac{1}{2}b_1h_1$$

$$= \frac{1}{2} \times 15 \times 12$$

$$= 90dm^2$$

$$A_2 = 180dm^2$$

$$b_2 = 20dm$$

$$h_2 = ?$$

$$A_2 = \frac{1}{2}b_2h_2$$

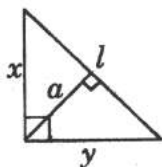
$$180 = \frac{1}{2} \times 20 \times h_2$$

$$\frac{180}{10} = h_2$$

$$\Rightarrow h_2 = 18dm$$

Hence (b) is the correct option.

6.



$$\text{Area of the triangle} = \frac{1}{2}al = \frac{1}{2}xy$$

$$\Rightarrow xy = al$$

$$l^2 = x^2 + y^2 \quad (\because \text{Pythagoras theorem})$$

$$\frac{1}{x^2} + \frac{1}{y^2} = \frac{x^2 + y^2}{(xy)^2} = \frac{l^2}{(al)^2}$$

$$= \frac{l^2}{a^2 l^2} = \frac{1}{a^2}$$

$$\Rightarrow \frac{1}{x^2} + \frac{1}{y^2} = \frac{1}{a^2}$$

Hence (d) is the correct option.

7. $D_1 = (x + y)$

$$A_1 = \frac{D_1^2}{2}$$

$$= \frac{(x + y)^2}{2}$$

$$D_2 = D_1$$

$$A_2 = 2A_1$$

$$= 2 \cdot \frac{(x + y)^2}{2}$$

i.e., $\frac{D_2^2}{2} = (x + y)^2$

$$\Rightarrow D_2^2 = 2(x + y)^2$$

$$\Rightarrow D_2 = \sqrt{2}(x + y)$$

The diagonal of a square B with twice the area of $A = \sqrt{2}(x + y)$

Hence (a) is the correct option.

8. A circle and square have the same polimeter then

$$2\pi r = 4a$$

$$\Rightarrow \pi r = 2a$$

$$\Rightarrow a = \frac{\pi r}{2}$$

Area of the square = a^2

Area of the circle $= \pi r^2$

$$a^2 = \left(\frac{\pi r}{2}\right)^2 = \frac{\pi^2 r^2}{4} = (\pi r^2) \cdot \frac{\pi}{4}$$

$$\frac{\pi}{4} = \frac{22}{28} < 1 \text{ i.e., } \frac{\pi}{4} < 1$$

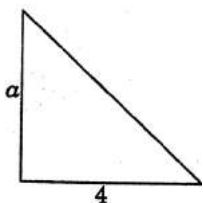
$$\Rightarrow (\pi r^2) \cdot \frac{\pi}{4} < \pi r^2$$

$$\Rightarrow a^2 < \pi r^2$$

Area of the square $<$ Area of the circle

Hence (b) is the correct option.

9.



Area of the right angles triangle $= 20$ sq. cm

$$\Rightarrow A = \frac{1}{2} ab$$

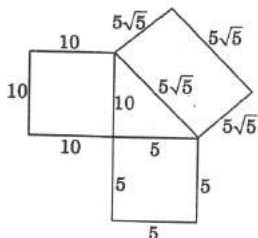
$$20 = \frac{1}{2} \times a \times 4$$

$$\Rightarrow 2a = 20$$

$$\Rightarrow a = 10 \text{ cm}$$

Hence (c) is the correct option.

10.



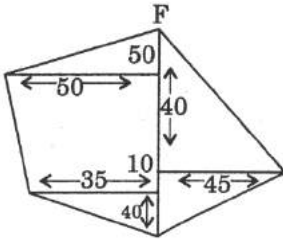
Total Area

$$= 10^2 + 25 + (5\sqrt{5})^2 + \frac{1}{2} \times 10 \times 5$$

$$= 100 + 25 + 125 + 25 = 275$$

Hence (d) is the correct option.

11.



Total Area

$$= \frac{1}{2} \times 35 \times 40 + \frac{1}{2} \times 90 \times 45 + \frac{1}{2} \times 40 \times 45$$

$$+ \frac{1}{2} \times 50 \times 50 + \frac{1}{2} \times 50(50 + 35)$$

$$= 700 + 2025 + 900 + 1250 + 2975$$

$$= 7225m^2$$

Hence (a) is the correct option.

12.

Total surface area of a cube = $216cm^2$

$$6a^2 = 216$$

$$\Rightarrow a^2 = 36$$

$$a = 6m$$

The length of the longest pole that can be inside the cube = $\sqrt{3}a$

$$= \sqrt{36}$$

$$= 6\sqrt{3}$$

Hence (a) is the correct option.

13.

Perimeter of square = perimeter of equilateral triangle

$$4a = 3b$$

Where a is the length of the side of the square and b is the length of the side of the equilateral triangle

Diagonal of the square = $6\sqrt{2}cm$

$$\sqrt{2}a = 6\sqrt{2}$$

\Rightarrow

$$a = 6cm$$

$$b = \frac{4}{3}a$$

$$= \frac{4}{3} \times 6 = 8cm$$

Area of the equilateral triangle

$$= \frac{\sqrt{3}}{4}a^2$$

$$= \frac{\sqrt{3}}{4} \times (8)^2$$

$$= \frac{\sqrt{3}}{4} \times 64 = 16\sqrt{3}cm^2$$

Hence (b) is the correct option.

- 14.** The height of a conical tent at the centre is 5m. The distance of any point on its circular base from the top of the tent is 13 m. The area of the slant surface is $156\pi sq.m$

Hence (c) is the correct option.

- 15.** Curved surface area of a cone

$$= \pi r \sqrt{r^2 + h^2} \quad d = 14cm$$

$$550 = \frac{22}{7} \times 7 \left(\sqrt{7^2 + h^2} \right) \quad r = 7cm$$

$$\frac{550}{22} = \sqrt{h^2 + 7^2}$$

$$\frac{50}{2} = \sqrt{49 + h^2}$$

$$25 = \sqrt{49 + h^2}$$

$$\Rightarrow 625 = 49 + h^2$$

$$\Rightarrow h^2 = 576$$

$$h = 24\text{cm}$$

Hence (d) is the correct option.

16. Volume of the right pyramid

$$= \frac{1}{3}(\text{area of the base}) \times (\text{height})$$

$$= \frac{1}{3} \cdot \left(6 \times \frac{\sqrt{3}}{4} \times 10^2 \right) \times 60$$

$$= \frac{100\sqrt{3} \times \cancel{60}^{30}}{\cancel{2}} = 3000\sqrt{3}$$

$$= 3000 \times 1.73 = 5196\text{m}^2$$

Hence (a) is the correct option.

17. Height = 15 cm

radius = 6 cm

Volume of the pyramid

$$= \frac{1}{3} \times \text{Area of the base} \times \text{height}$$

$$= \frac{1}{3} \times \frac{\sqrt{3}}{4} \times 6^2 \times 15 = 331\text{cm}^3$$

Hence (d) is the correct option.

18. $r_1 = r$

$$A_1 = A = \pi r^2$$

$$r_2 = 2r$$

$$A_2 = \pi(2r)^2$$

$$= 4\pi r^2$$

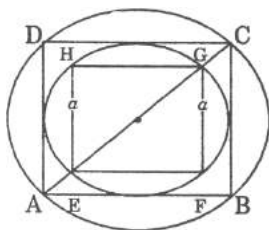
$$= 4A_1$$

The percentage of increase in Area

$$= \frac{4A_1 - A_1}{A_1} \times 100 = 300\%$$

Hence (c) is the correct option.

19.



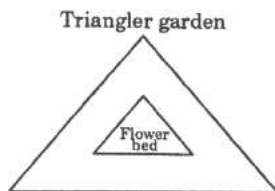
The diameter of outer circle = diagonal of A B C D
 $= 2a$

\Rightarrow Length of the side of E F G H

$$= \frac{\sqrt{2}a}{\sqrt{2}} = a$$

Hence (a) is the correct option.

20.



The ratio areas of the path and flower bed are in the ratio = 3 : 1
 Hence (d) is the correct option.

21.

If a solid right circular cylinder made of iron is heated to increase its radius and height 1 E C each then the volume of the solid increased to 2.01 PC

Hence (c) is the correct option.

- 22.** The radius of a piece of wire decreased to one-half. If volume remains same, its length will increase 4 times.
Hence (c) is the correct option.

- 23.** A wire bent into the shape of an equilateral triangle encloses an area 5 sq.cm. If the same wire is bent to form a circle, the area of the circle will

$$be = \frac{3\sqrt{3}s}{\pi}$$

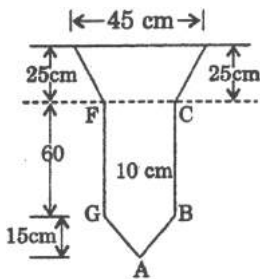
Hence (d) is the correct option.

- 24.** The length and breadth of a room are in the ratio 3 : 2. If the height is equal to half of its length. If the cost of carpetting the floor at ₹ 4.00 per m^2 is ₹ 216.00. Then the area of the four walls is $135m^2$.

$$\begin{aligned} \text{Since area of the four walls} \\ = 2h(1+b) \end{aligned}$$

Hence (a) is the correct option-

25.



Area of the Trapezium F C D E

$$= \frac{1}{2} \times (10 + 45) \times 25$$

Area of the triangle G A B

$$= \frac{1}{2} \times 15 \times 10$$

Area of the rectangle G B C F
 $= 60 \times 10$

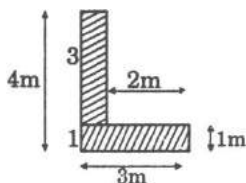
\therefore Total Area

$$= \frac{1}{2} \times 55 \times 25 + \frac{1}{2} \times 15 \times 10 + 60 \times 10$$

$$= 1175 \text{ cm}^2$$

Hence (a) is the correct option.

26.

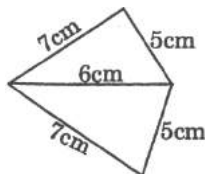


Area of the shaded region

$$= 3 \times 4 + 3 \times 1 = 6m^2$$

Hence (b) is the correct option.

27.

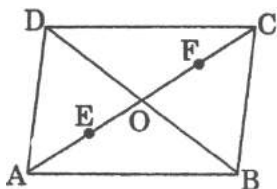


Area of the Quadrilateral $= 12\sqrt{6}$

Length of the other diagonal $= 4\sqrt{6}$

Hence (a) is the correct option.

28.



E is the centroid of $\triangle ABD$

F is the centroid of $\triangle BCD$

$$AO = OC$$

(\because ABCD is a parallelogram)

$$\frac{1}{3}OA = \frac{1}{3}OC$$

$$\Rightarrow OE = OF \Rightarrow EF = 2OE$$

$$= 2 \cdot \left(\frac{1}{3}OA \right)$$

$$= \frac{2}{3} \cdot OA$$

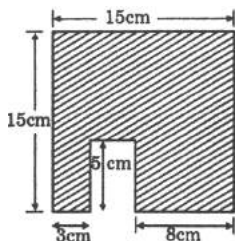
$$= \frac{2}{3} \left(\frac{1}{2}AC \right)$$

$$= \frac{1}{3}AC$$

$$= AE$$

\Rightarrow Hence (a) is the correct option.

29.



Area of the shaded region

$$= 15 \times 15 - 4 \times 5$$

$$= 225 - 20 = 205 \text{ cm}^2$$

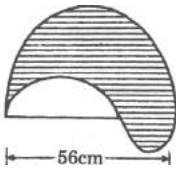
Hence (c) is the correct option.

30.

The area of the curved surface of cylinder is $= 4\pi r^2$

Hence (b) is the correct option.

31.



Diameter of semi circle = 56 mm

Radius of the semi circle = 28 mm

⇒

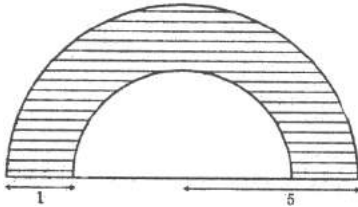
The area of the shaded region

$$= \frac{22}{7} \times \frac{28 \times 28}{2}$$

$$= 11 \times 4 \times 28 = 176 \text{ mm}$$

Hence (d) is the correct option.

32.



$$R = 5$$

$$r = 4$$

Area of the shaded region

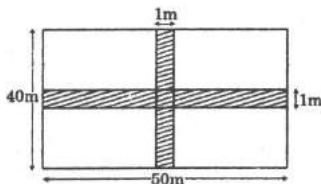
$$= \frac{1}{2} \pi (R^2 - r^2)$$

$$= \frac{1}{2} \times \frac{22}{7} (5^2 - 4^2)$$

$$= 11 \times 4 \times 28 = 176 \text{ mm}$$

Hence (d) is the correct option.

33.



Area of the shaded region

$$= 50 \times 1 + 40 \times 1 - 1 \times 1$$

$$= 90 - 1 = 89m^2$$

Hence (d) is the correct option.

SECTION - II

Assertion - Reason Questions

34. The radii of the bases of two cones are r_1 and r_2 slant height are s_1 and s_2 then the ratio of their I.S.A are $r_1 s_1 : r_2 s_2$ Since if the heights of two cones are equal then Their volumes are in the ratio of squares of their radii.
Hence (d) is the correct option.

35. Slant height of a cone $l^2 = r^2 + h^2$
Area of the base of cone $= \pi r^2$
Hence (c) is the correct option.

36. Volume of the sphere $= \frac{4}{3} \pi r^3$
Area of the ring $= \pi (R^2 - r^2)$
Where R is radius of outer circle r is the radius of inner circle
Hence (b) is the correct option.

37. Area of the ring edge of hollow hemisphere
 $= \pi (R^2 - r^2)$
Surface area of the hollow sphere

$$= \pi(3R^2 + r^2)$$

Hence (a) is the correct option.

38. Lateral surface area of a cube $= 4a^2$

Total surface area of cube

$$= 6a^2 = 4a^2 + 4a^2$$

Hence (a) is the correct option.

39. Volume of the cuboid $= lbh$

Total surface area $= 2(lh + bh + lb)$

Hence (b) is the correct option.

40. L.S.A of triangular prism $= ph$

Area of the base of the triangular prism is $\sqrt{s(s-a)(s-b)(s-c)}$

Hence (b) is the correct option.

41. The volume of the prism

$$= \frac{1}{3} \times \left(\frac{1}{2} \times 28 \times 96 \right) \times 32$$

$$= 43008 \text{ cm}^3$$

Volume of the prism $V = A \times h$

Hence (a) is the correct option.

42. Volume of the Masonry $= \text{Area of the cross section} \times \text{length}$

Hence (a) is the correct option.

43. Diagonals k of a cuboid $= \sqrt{l^2 + b^2 + h^2}$

Sum of the edges of a cuboid

$$= 4(l + b + h)$$

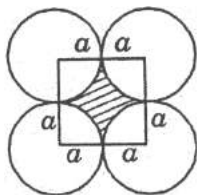
Hence (b) is the correct option.

- 44.** L.S.A. of Triangular prism of sides 15 cm, 20 cm, 25 cm with height 40 cm is 2400 sq.cm.
Perimeter of the base of prism is 60 cm
Hence (a) is the correct option.
- 45.** Volume of a regular hexagonal prism of side 30 cm and height 6 cm is 14029.2cc
Volume = Area of base x height
Hence (b) is the correct option.

SECTION - III

Linked Comprehension Type

46.



Area of the shaded

Portion = Area of the square

$- 4 \times \text{Area of the Quadrant}$

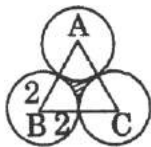
$$= (2a)^2 - 4 \times \frac{1}{4} \times \pi \times a^2$$

$$= 4a^2 - \pi a^2$$

$$= \left(4 - \frac{22}{7} \right) a^2 = \frac{6}{7} a^2$$

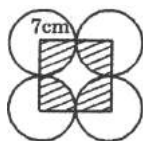
Hence (a) is the correct option.

47.



Area of the shaded portion
 = Area of the equilateral triangle
 $- 3 \times \text{area of the Quadrant}$
 $= \frac{\sqrt{3}}{4} \times (2)^2 - 3 \cdot \frac{1}{4} \times \pi (2^2)$
 $= \sqrt{3} - 3\pi = 0.642 \text{ cm}^2$
 Hence (b) is the correct option.

48.

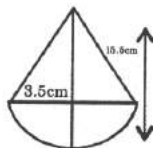


Area of the shaded portion
 = $4 \times \text{Area of the Quadrant}$
 $= 4 \times \frac{1}{4} \times \pi \times 7^2$
 $= 49\pi = 49 \times \frac{22}{7}$
 $= 7 \times 22 = 154 \text{ cm}^2$
 Hence (a) is the correct option.

49. Slant height of the cone = 7.5 mts
 Hence (a) is the correct option.

50. Canvas required for conical portion of the tent is 106.71 m
 Hence (b) is the correct option.

51.



Canvas required for the cylindrical part of the tent is 246.24 cm^2
 Hence (b) is the correct option.

52. Curved surface area is 137cm^2
Hence (a) is the correct option.
53. Curved surface area of the hemisphere = 77cm^2
Hence (c) is the correct option.
54. Total surface area of the top 214.5cm^2
Hence (c) is the correct option.
55. Slant height of the pyramid = 13 cm
Hence (a) is the correct option.
56. Lateral surface area of the pyramid is 260cm^2
Hence (a) is the correct option.
57. Volume of the pyramid is 200 c.c
Hence (b) is the correct option.

SECTION - IV

Matrix - Match Type

58.

	p	q	r	s
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C	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
D	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>

59.

	p	q	r	s
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60.

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61.

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62.

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63.

	p	q	r	s
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