

Basic Concepts in Rotating Electrical Machines

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Introduction

Electromagnetic torque

- Also called interaction torque.

$$T_e \propto (\text{Stator field strength}) (\text{Rotor field strength}) \sin \delta$$

where, δ = Torque angle

Electrical and Mechanical degrees

$$\theta_{\text{elec}} = \frac{P}{2} \theta_{\text{mech}}$$

where, θ_{elec} = angle in electrical degree

θ_{mech} = angle in mechanical degree

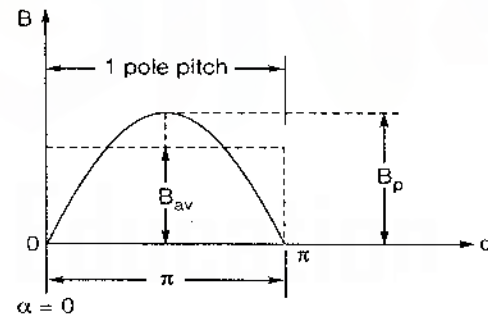
P = number of poles

Pole pitch

The peripheral distance between adjacent poles is called pole pitch. is always equal to 180 electrical degree.

Average value of flux density wave over one pole-pitch

$$B_{\text{av}} = \frac{2}{\pi} B_p$$



where, B_p = Maximum flux density

Total flux per pole

$$\phi = \frac{4}{P} B_p r l$$

where, l = Axial length of the armature core

r = Radius of armature core

Generated emf in a full-pitched coil

$$e = N \omega_r \phi \sin \omega_r t$$

where, N = Number of turns in single full pitched coil

ϕ = flux per pole

ω_r = relative velocity between field flux wave and armature coil

Rms value of generated emf in a full-pitched coil

$$E = 4.44 f_r N \phi$$

where, f_r = rotational or speed frequency

Rotational frequency

$$f_r = \frac{P n_r}{2} \text{ Hz}$$

where, n_r = relative speed between armature coil and flux-density wave in rps.

Generated emf in a short-pitched coil

$$E = 4.44 k_p f_r N \phi$$

where, k_p = coil pitch factor or coil-span factor or pitch factor

Pitch factor

$$k_p = \cos \frac{\epsilon}{2}$$

where, ϵ = Angle of chording (or pitching) for fundamental flux wave.

Note:

For n^{th} space field harmonic, chording angle becomes $n\epsilon^\circ$ electrical.

$$k_{pn} = \cos \frac{n\epsilon}{2}$$

Distribution factor

$$k_d = \frac{\sin \left(\frac{q\gamma}{2} \right)}{q \sin \left(\frac{\gamma}{2} \right)}$$

where, q = No. of slots per pole per phase
 γ = Angular slot pitch

$$\gamma = \frac{180 P}{\text{Total no. of slots}} \text{ electrical degree}$$

❑ Distribution factor for n^{th} harmonic

$$k_{dn} = \frac{\sin\left(\frac{qn\gamma}{2}\right)}{q \sin\left(\frac{n\gamma}{2}\right)}$$

❑ Winding factor

$$k_w = k_p \times k_d$$

❑ Phase spread

$$\sigma = q\gamma \text{ ... in electrical space degrees}$$

❑ Synchronous speed

Speed at which rotating magnetic field revolves is called synchronous speed

$$n_s = \frac{120f}{p} \text{ r.p.m.}$$

