

Topics : Inverse Trigonometric Function, Set & Relation, Fundamentals of Mathematics, Matrices & Determinants, Quadratic Equation

Type of Questions

M.M., Min.

Single choice Objective (no negative marking) Q.1 to Q. 7 (3 marks, 3 min.)

[21, 21]

Subjective Questions (no negative marking) Q. 8 (4 marks, 5 min.)

[4, 5]

1. Number of solutions of the equation

$$\tan^{-1}\left(\frac{1}{a-1}\right) = \tan^{-1}\left(\frac{1}{x}\right) + \tan^{-1}\left(\frac{1}{a^2 - x + 1}\right)$$

- (A) one (B) Two (C) Three (D) Zero

2. Let the matrix A and B be defined as $A = \begin{bmatrix} 3 & 2 \\ 2 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} 3 & 1 \\ 7 & 3 \end{bmatrix}$, then the value of $\text{Det.}(2A^9B^{-1})$ is

- (A) 2 (B) 1 (C) -1 (D) -2

3. If the quadratic equations, $ax^2 + 2cx + b = 0$ and $ax^2 + 2bx + c = 0$ ($b \neq c$) have a common root, then $a + 4b + 4c$ is equal to :

- (A) -2 (B) -2 (C) 0 (D) 1

4. Number of triplets (x, y, z) satisfying $\sin^{-1}x + \cos^{-1}y + \sin^{-1}z = 2\pi$, is

- (A) 0 (B) 2 (C) 1 (D) infinite

5. The matrix X for which $\begin{bmatrix} 1 & -4 \\ 3 & -2 \end{bmatrix} X = \begin{bmatrix} -16 & -6 \\ 7 & 2 \end{bmatrix}$

- (A) $\begin{bmatrix} -2 & 4 \\ -3 & 1 \end{bmatrix}$ (B) $\begin{bmatrix} -\frac{1}{5} & \frac{2}{5} \\ -\frac{3}{10} & \frac{1}{5} \end{bmatrix}$ (C) $\begin{bmatrix} 6 & 2 \\ 11 & 2 \end{bmatrix}$ (D) $\begin{bmatrix} -16 & -6 \\ 7 & 2 \end{bmatrix}$

6. Let $R = \{(3, 3), (6, 6), (9, 9), (12, 12), (6, 12), (3, 9), (3, 12), (3, 6)\}$ be relation on the set $A = \{3, 6, 9, 12\}$. The relation is-

- (A) reflexive and transitive only (B) reflexive only
(C) an equivalence relation (D) reflexive and symmetric only

7. Let $A = \{1, 2\}$, $B = \{0\}$ then which of the following is correct

- (A) number of possible relations from A to B is $2^0 = 1$
(B) number of void relations from A to B is not possible
(C) number of possible relations from A to B are 4
(D) number of possible relations are equal to $2^{n(A) + n(B)}$

8. Find out the values of 'a' for which any solution of the inequality, $\frac{\log_3(x^2 - 3x + 7)}{\log_3(3x + 2)} < 1$ is also a solution of the inequality, $x^2 + (5 - 2a)x \leq 10a$.

Answers Key

1. (B) 2. (D) 3. (C) 4. (C)

5. (C) 6. (1) 7. (C)

8. $a \geq \frac{5}{2}$