

CBSE Board
Class IX Mathematics

Time: 3 hrs

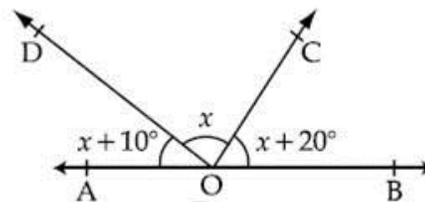
Total Marks: 80

General Instructions:

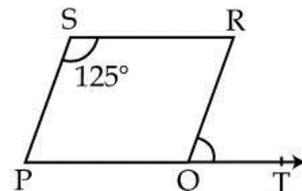
1. All questions are **compulsory**.
2. The question paper consists of **30** questions divided into **four sections** A, B, C, and D. **Section A** comprises of **6** questions of 1 mark each, **Section B** comprises of **6** questions of 2 marks each, **Section C** comprises of **10** questions of 3 marks each and **Section D** comprises of **8** questions of 4 marks each.
3. Question numbers **1 to 6** in **Section A** are multiple choice questions where you are to select **one** correct option out of the given four.
4. Use of calculator is **not** permitted.

Section A
(Questions 1 to 6 carry 1 mark each)

1. What is the decimal form of $\frac{11}{1000}$?
2. $x + y = 2$ and $x - y = 4$. Find the values of x and y .
3. In the given figure, find the value of x ?



4. If for one of the solutions of the equation $ax + by + c = 0$, x is negative and y is positive, then a portion of the above line will lie in which Quadrant?
5. The Class marks of a distribution are 47, 52, 57, 62, 67, 72, 77, 82, 87, 92, 97, and 102. Determine the Class size?
6. PQRS is a parallelogram in which $\angle PSR = 125^\circ$. Find $\angle RQT$.



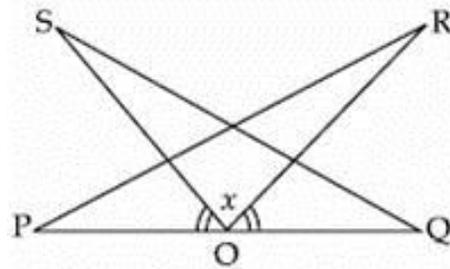
Section B
(Questions 7 to 12 carry 2 marks each)

7. If $a = 2 + \sqrt{3}$, find the value of $a + \frac{1}{a}$.
8. The perpendicular distance of a point from the x-axis is 2 units and the perpendicular distance from the y-axis is 5 units. Write the coordinates of such a point if it lies in one of the following quadrants:
(i) I Quadrant (ii) II Quadrant (iii) III Quadrant (iv) IV Quadrant
9. The total surface area of a cube is 294 cm^2 . Find its volume.
10. Check which of the following are solutions of the equation $7x - 5y = -3$.
i. $(-1, -2)$
ii. $(-4, -5)$
11. Find the area of an isosceles triangle with base 10 cm and perimeter 36 cm.
12. Simplify: $(-2x + 5y - 3z)^2$.

Section C
(Questions 13 to 22 carry 3 marks each)

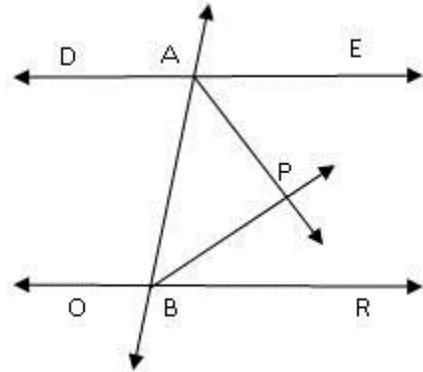
13. Express $\overline{0.001}$ as a fraction in the simplest form.
14. Find the value of $x^3 - 8y^3 - 36xy - 216$ when $x = 2y + 6$.
15. In the figure, PQ is a line segment and O is the mid-point of PQ. R and S are on the same side of PQ such that $\angle PQS = \angle QPR$ and $\angle POS = \angle QOR$. Prove that

- (i) $\triangle PQR \cong \triangle QOS$
(ii) $PR = QS$



16. If the polynomials $az^3 + 4z^2 + 3z - 4$ and $z^3 - 4z + a$ leave the same remainder when divided by $z - 3$, then find the value of a.

17. In the given figure, $DE \parallel OR$ and AP and BP are bisectors of $\angle EAB$ and $\angle RBA$, respectively. Find $\angle APB$.



18. The following frequency distribution table gives the weights of 38 students of a class.

Weight in kg	Number of students
30 - 35	10
35 - 40	5
40 - 45	15
45 - 50	5
50 - 55	1
55 - 60	2
Total	38

Find the probability that the weight of students is

- i. more than or equal to 45 Kg
 - ii. less than 30 kg
 - iii. more than or equal to 30 Kg but less than 60 Kg
19. Find the area of the triangle formed by $A(0, 4)$, $O(0, 0)$ and $B(3, 0)$.
20. If $x = 1 + \sqrt{2}$, find the value of $\left(x - \frac{1}{x}\right)^3$.
21. A wooden article was made by scooping out a hemisphere from each end of a solid cylinder. If the height of the cylinder is 10 cm and its base is 7 cm, find the total surface area of the article.

22. The length of 40 leaves of a plant are measured correct to one millimeter, and the data obtained is represented in the following table:

Length (in mm)	Number of leaves
118 – 126	3
127 – 135	5
136 – 144	9
145 – 153	12
154 – 162	5
163 – 171	4
172 – 180	2

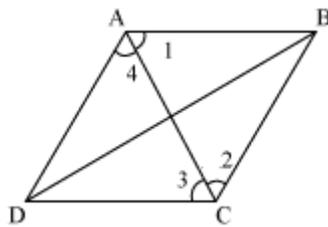
- Draw a histogram to represent the given data.
- Is there any other suitable graphical representation for the same data?
- Is it correct to conclude that maximum leaves are 153 mm long? Why?

Section D

(Questions 23 to 30 carry 4 marks each)

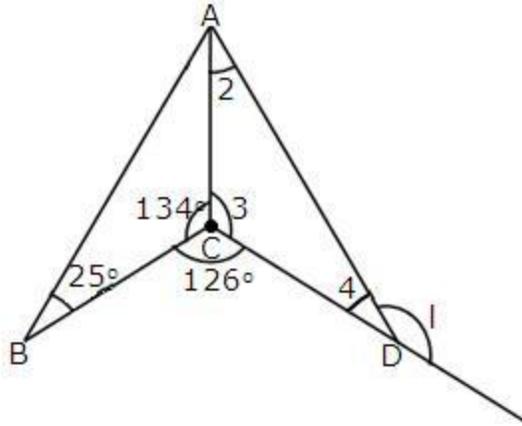
23. Simplify: $\frac{3\sqrt{2} - 2\sqrt{3}}{3\sqrt{2} + 2\sqrt{3}} + \frac{\sqrt{12}}{\sqrt{3} - \sqrt{2}}$

24. ABCD is a rhombus. Show that the diagonal AC bisects $\angle A$ as well as $\angle C$ and diagonal BD bisects $\angle B$ as well as $\angle D$.

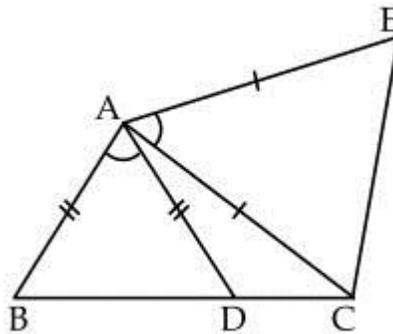


25. If the polynomial $x^4 + mx^3 - 25x^2 - 16x + n$ is exactly divisible by $x^2 - 4$, then what are the values of m and n ?

26. In the given figure, AC is the bisector of $\triangle BAD$. Find the measures of $\angle 1$, $\angle 2$, $\angle 3$ and $\angle 4$.



27. A cube and cuboid have the same volume. The dimensions of the cuboid are in the ratio $1 : 2 : 4$. If the difference between the cost of polishing the cube and cuboid at the rate of Rs. 5 per m^2 is Rs. 80, find their volumes.
28. If O is point lying inside $\triangle XYZ$, then show that $(OX + OY + OZ)$ cannot be less than the semi-perimeter of $\triangle XYZ$.
29. In the given figure, $AC = AE$, $AB = AD$ and $\angle BAD = \angle EAC$. Prove that $BC = DE$.



30. If $m = \frac{1}{2 - \sqrt{3}}$ and $n = \frac{1}{2 + \sqrt{3}}$, then what is the value of $7m^2 + 11mn - 7n^2$?

CBSE Board
Class IX Mathematics
Solution

Time: 3 hrs

Total Marks: 80

Section A

1. $\frac{11}{1000} = 0.011$

2. $x + y = 2$ (i)
and $x - y = 4$ (ii)
Adding (i) and (ii), we get
 $x = 3$
Putting $x = 3$ in the equation (i), we get
 $y = -1$
 $\therefore x = 3$ and $y = -1$

3. Since AOB is a Straight Line,
 $\therefore \angle AOB = 180^\circ$
 $\therefore \angle AOD + \angle COD + \angle COB = 180^\circ$
 $\therefore x + 10^\circ + x + x + 20^\circ = 180^\circ$
 $\therefore 3x = 150^\circ$
 $\therefore x = 50^\circ$

4. If for one of the solutions of the equation $ax + by + c = 0$, x is negative and y is positive, then a portion of the above line definitely lies in the II Quadrant.
As in the II Quadrant the x -axis contains only negative numbers and y -axis contains only positive numbers.

5. Here the class marks are uniformly spaced,
Therefore,
Class size is the difference between any two consecutive class marks.
 \therefore Class Size = $52 - 47 = 5$

6. $\angle PSR = \angle RQP = 125^\circ$ (since PQRS is a parallelogram, then the opposite angles will be equal)
 $\therefore \angle PQT = 180^\circ$ (PQT is a straight line)
 $\therefore \angle PQR + \angle RQT = 180^\circ$
 $\therefore 125^\circ + \angle RQT = 180^\circ$
 $\therefore \angle RQT = 55^\circ$

Section B

7. $a = 2 + \sqrt{3}$

$$\Rightarrow \frac{1}{a} = \frac{1}{2 + \sqrt{3}}$$

$$= \frac{1}{2 + \sqrt{3}} \times \frac{2 - \sqrt{3}}{2 - \sqrt{3}}$$

$$= \frac{2 - \sqrt{3}}{2^2 - (\sqrt{3})^2}$$

$$= 2 - \sqrt{3}$$

So, $a + \frac{1}{a} = (2 + \sqrt{3}) + (2 - \sqrt{3}) = 4$

8. (i) I quadrant: (5, 2)

(ii) II quadrant: (-5, 2)

(iii) III quadrant: (-5, -2)

(iv) IV quadrant: (5, -2)

9. Let 'l' be the length of the cube.

Now, T.S.A. of the cube = 294 cm^2 ...(given)

$$\therefore 6l^2 = 294$$

$$\therefore \text{Side, } l = 7 \text{ cm}$$

$$\text{Volume of cube} = l \times l \times l = 7 \times 7 \times 7 = 343 \text{ cm}^3$$

10. Given equation is $7x - 5y = -3$

i. (-1, -2)

Putting $x = -1$ and $y = -2$ in the L.H.S. of the given equation, we get

$$7x - 5y = 7(-1) - 5(-2) = -7 + 10 = 3 \neq \text{R.H.S.}$$

$\therefore \text{L.H.S.} \neq \text{R.H.S.}$

Hence, (-1, -2) is not a solution of this equation.

ii. (-4, -5)

Putting $x = -4$ and $y = -5$ in the L.H.S. of the given equation, we get

$$7x - 5y = 7(-4) - 5(-5) = -28 + 25 = -3 = \text{R.H.S.}$$

$\therefore \text{L.H.S.} = \text{R.H.S.}$

Hence, (-4, -5) is a solution of this equation.

11. Perimeter = 36 cm = 10 cm + 2(Length of an equal side)
 \Rightarrow Length of an equal side = 13 cm

Here, $s = \frac{36}{2} = 18$, and the sides are 10, 13 and 13.

By Heron's formula,

$$\text{Area} = \sqrt{18 \times 8 \times 5 \times 5} = 60 \text{ sq. cm}$$

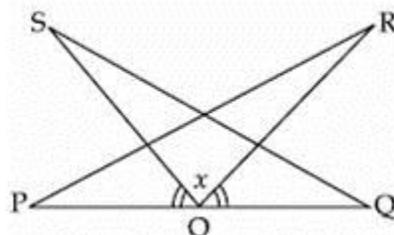
12. $(-2x + 5y - 3z)^2$
 $= (-2x)^2 + (5y)^2 + (-3z)^2 + 2(-2x)(5y) + 2(5y)(-3z) + 2(-2x)(-3z)$
 $= 4x^2 + 25y^2 + 9z^2 - 20xy - 30yz + 12zx$

Section C

13. Let $x = 0.\overline{001}$
 Then, $x = 0.001001001\dots\dots\dots$ (i)
 Therefore, $1000x = 1.001001001\dots\dots\dots$ (ii)
 Subtracting (i) from (ii), we get,
 $999x = 1 \Rightarrow x = \frac{1}{999}$
 Hence, $0.\overline{001} = \frac{1}{999}$

14. Given: $x = 2y + 6$ or $x - 2y - 6 = 0$
 We know that if $a + b + c = 0$, then $a^3 + b^3 + c^3 = 3xyz$
 Therefore, we have:
 $(x)^3 + (-2y)^3 + (-6)^3 = 3x(-2y)(-6)$
 Or, $x^3 - 8y^3 - 36xy - 216 = 0$

15. In ΔPOR and ΔQOS
 $\angle QPR = \angle PQS$ (given)
 $OP = OQ$ (O is the mid-point of PQ)
 $\angle POS = \angle QOR$ (given)
 $\angle POS + x^\circ = \angle QOR + x^\circ$
 $\angle POR = \angle QOS$
 By ASA congruence rule,
 $\Delta PQR \cong \Delta QOS$
 $\Rightarrow PR = QS$ (By CPCT)



16. Let $p(z) = az^3 + 4z^2 + 3z - 4$ and $q(z) = z^3 - 4z + a$
 When $p(z)$ is divided by $z - 3$, the remainder is given by

$$\begin{aligned} p(3) &= a \times 3^3 + 4 \times 3^2 + 3 \times 3 - 4 \\ &= 27a + 36 + 9 - 4 \\ &= 27a + 41 \quad \dots(i) \end{aligned}$$

When $q(z)$ is divided by $z - 3$, the remainder is given by

$$\begin{aligned} q(3) &= 3^3 - 4 \times 3 + a \\ &= 27 - 12 + a \\ &= 15 + a \quad \dots(ii) \end{aligned}$$

Given that $p(3) = q(3)$.

So, from (i) and (ii), we have

$$\begin{aligned} 27a + 41 &= 15 + a \\ 27a - a &= -41 + 15 \\ 26a &= -26 \\ a &= -1 \end{aligned}$$

17. Since interior angles on the same side of transversal are supplementary.

Therefore, $\angle EAB + \angle RBA = 180^\circ$

$$\frac{1}{2} \angle EAB + \frac{1}{2} \angle RBA = \frac{1}{2} \times 180^\circ \quad \dots(i)$$

As AP and BP are bisectors of $\angle EAB$ and $\angle RBA$ respectively,

$$\angle PAB = \frac{1}{2} \angle EAB \text{ and } \angle PBA = \frac{1}{2} \angle RBA \quad \dots(ii)$$

From (i) and (ii), we get

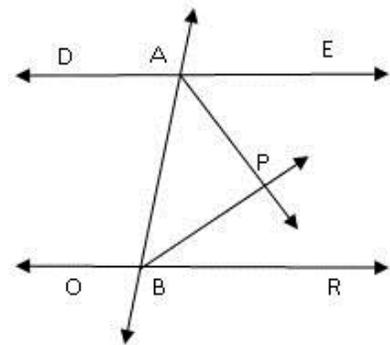
$$\angle PAB + \angle PBA = 90^\circ$$

In $\triangle APB$, we have

$$\angle PAB + \angle PBA + \angle APB = 180^\circ$$

$$\Rightarrow 90^\circ + \angle APB = 180^\circ$$

$$\Rightarrow \angle APB = 180^\circ - 90^\circ = 90^\circ$$



18. Total number of students = 38

i. Number of students weighing more than or equal to 45 kg = 5 + 1 + 2 = 8

$$\therefore P(\text{a student weighing more than or equal to 45 kg}) = \frac{8}{38} = \frac{4}{19}$$

ii. Number of students weighing less than 30 kg = 0

$$\therefore P(\text{a student weighing less than 30 kg}) = \frac{0}{38} = 0$$

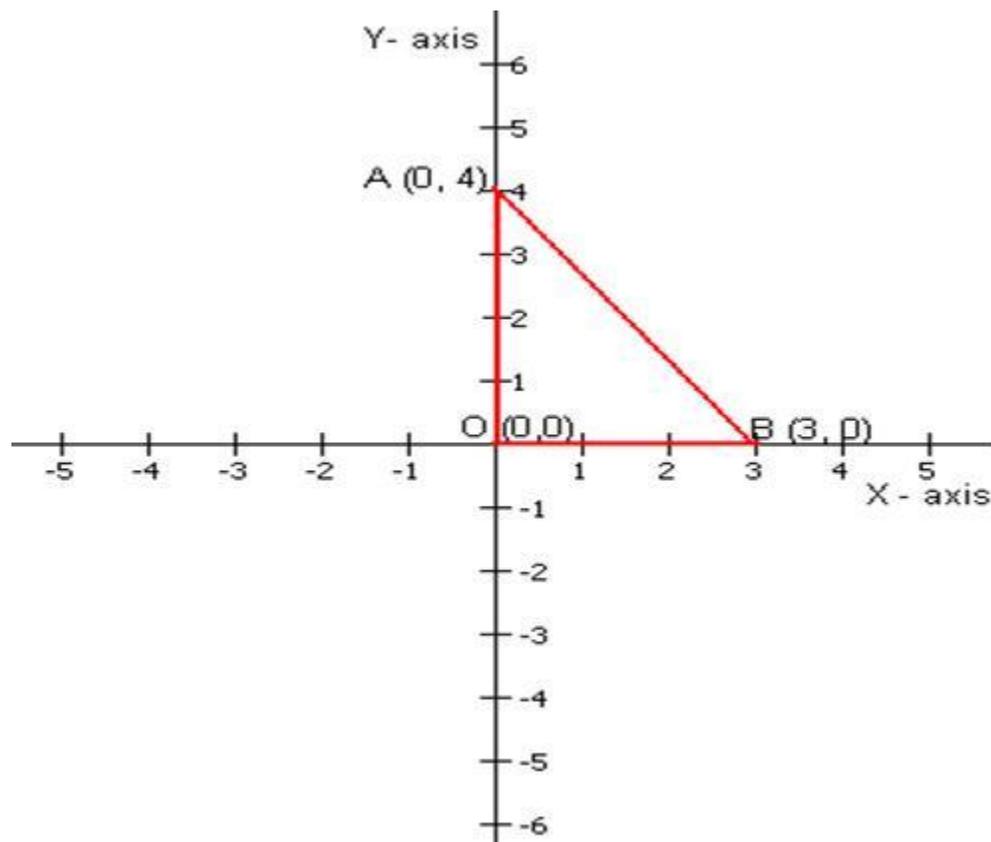
iii. Number of students weighing more than or equal to 30 kg but less than 60 kg

$$= 10 + 5 + 15 + 5 + 1 + 2$$

$$= 38$$

$$\therefore \text{Required probability} = \frac{38}{38} = 1$$

19. The given points A(0, 4), O(0, 0), B(3, 0) can be plotted as follows:



Clearly, AOB is a right-angled triangle.

OA = 4 units, OB = 3 units.

$$\text{Area of } \triangle AOB = \frac{1}{2} \times \text{Base} \times \text{Height} = \frac{1}{2} \times 3 \times 4 = 6 \text{ square units}$$

20. Given, $x = 1 + \sqrt{2}$

$$\begin{aligned}\text{And, } \frac{1}{x} &= \frac{1}{1 + \sqrt{2}} \\ &= \frac{1}{1 + \sqrt{2}} \times \frac{1 - \sqrt{2}}{1 - \sqrt{2}} \\ &= \frac{1 - \sqrt{2}}{1^2 - (\sqrt{2})^2} \\ &= -1 + \sqrt{2}\end{aligned}$$

$$\text{Now, } \left(x - \frac{1}{x}\right) = \sqrt{2} + 1 - (\sqrt{2} - 1) = 2$$

$$\therefore \left(x - \frac{1}{x}\right)^3 = 2^3 = 8$$

21. Base radius, $r = \frac{7}{2} = 3.5$ cm

Height of the cylinder, $h = 10$ cm

$$\begin{aligned}\text{Curved surface area of cylinder} &= 2\pi rh \\ &= 2 \times \pi \times 3.5 \times 10 \\ &= 70\pi \text{ cm}^2\end{aligned}$$

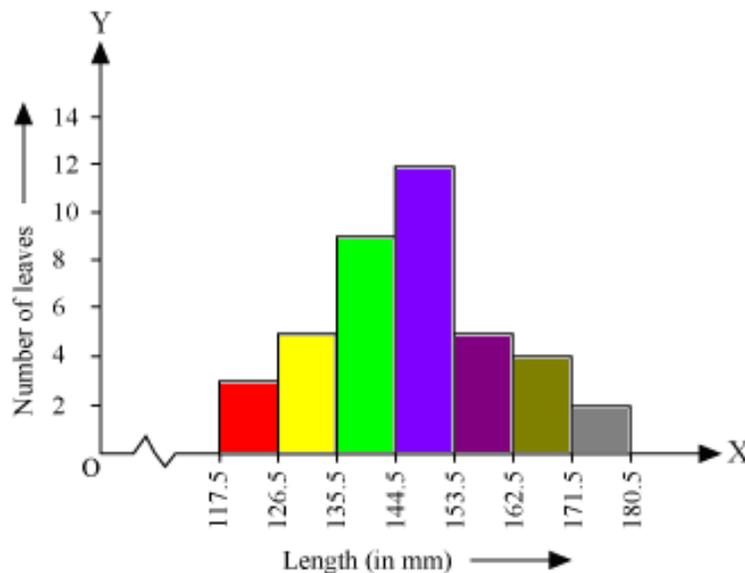
$$\begin{aligned}\text{Curved surface area of two hemisphere} &= 2 \times 2\pi r^2 \\ &= 4 \times \pi \times 3.5^2 \\ &= 49\pi \text{ cm}^2\end{aligned}$$

$$\therefore \text{Total surface area} = 70\pi + 49\pi = 119\pi \text{ cm}^2$$

22. Lengths of the leaves are represented in discontinuous class intervals. Hence we have to add 0.5 mm to each upper class limit and also have to subtract 0.5 mm from the lower class limits so as to make our class intervals continuous.

Length (in mm)	Number of leaves
117.5 - 126.5	3
126.5 - 135.5	5
135.5 - 144.5	9
144.5 - 153.5	12
153.5 - 162.5	5
162.5 - 171.5	4
171.5 - 180.5	2

- i. Now taking the length of leaves on the x-axis and number of leaves on the y-axis we can draw the histogram of this information as below:



Here 1 unit on the y-axis represents 2 leaves.

- ii. Other suitable graphical representation of this data could be a frequency polygon.
- iii. No, as maximum numbers of leaves (i.e. 12) have their length in between of 144.5 mm and 153.5 mm. It is not necessary that all have a length of 153 mm.

Section D

23.

We have,

$$\begin{aligned} & \frac{3\sqrt{2} - 2\sqrt{3}}{3\sqrt{2} + 2\sqrt{3}} + \frac{\sqrt{12}}{\sqrt{3} - \sqrt{2}} \\ &= \frac{3\sqrt{2} - 2\sqrt{3}}{3\sqrt{2} + 2\sqrt{3}} \times \frac{3\sqrt{2} - 2\sqrt{3}}{3\sqrt{2} - 2\sqrt{3}} + \frac{\sqrt{12}}{\sqrt{3} - \sqrt{2}} \times \frac{\sqrt{3} + \sqrt{2}}{\sqrt{3} + \sqrt{2}} \\ &= \frac{(3\sqrt{2} - 2\sqrt{3})^2}{(3\sqrt{2} + 2\sqrt{3})(3\sqrt{2} - 2\sqrt{3})} + \frac{\sqrt{12}(\sqrt{3} + \sqrt{2})}{(\sqrt{3} - \sqrt{2})(\sqrt{3} + \sqrt{2})} \\ &= \frac{(3\sqrt{2})^2 + (2\sqrt{3})^2 - 2 \times 3\sqrt{2} \times 2\sqrt{3}}{(3\sqrt{2})^2 - (2\sqrt{3})^2} + \frac{2\sqrt{3}(\sqrt{3} + \sqrt{2})}{(\sqrt{3})^2 - (\sqrt{2})^2} \\ &= \frac{18 + 12 - 12\sqrt{6}}{18 - 12} + \frac{6 + 2\sqrt{6}}{3 - 2} \\ &= \frac{30 - 12\sqrt{6}}{6} + 6 + 2\sqrt{6} \\ &= \frac{6(5 - 2\sqrt{6})}{6} + 6 + 2\sqrt{6} \\ &= 5 - 2\sqrt{6} + 6 + 2\sqrt{6} \\ &= 11 \\ \therefore \quad & \frac{3\sqrt{2} - 2\sqrt{3}}{3\sqrt{2} + 2\sqrt{3}} + \frac{\sqrt{12}}{\sqrt{3} - \sqrt{2}} = 11 \end{aligned}$$

24. Let us join AC.

In $\triangle ABC$

$BC = AB$ (sides of a rhombus)

$\therefore \angle 1 = \angle 2$ (angles opposite to equal sides of a triangle are equal)

But $\angle 1 = \angle 3$ (alternate interior angles)

$\Rightarrow \angle 2 = \angle 3$

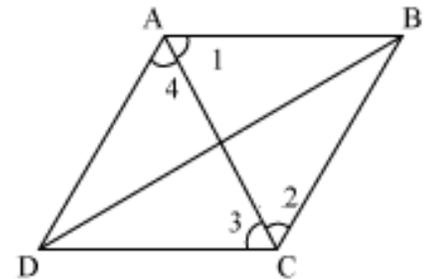
So, AC bisects $\angle C$.

Also, $\angle 2 = \angle 4$ (alternate interior angles)

$\Rightarrow \angle 1 = \angle 4$

So, AC bisects $\angle A$

Similarly, we can prove that BD bisects $\angle B$ and $\angle D$ as well.



25. Let $p(x) = x^4 + mx^3 - 25x^2 - 16x + n$ and $g(x) = x^2 - 4 = (x + 2)(x - 2)$

Since $p(x)$ is exactly divisible by $g(x)$, $p(x)$ is divisible by both $(x + 2)$ and $(x - 2)$.

Using factor theorem, we have

$$p(-2) = 0$$

$$\Rightarrow (-2)^4 + m(-2)^3 - 25(-2)^2 - 16(-2) + n = 0$$

$$\Rightarrow 16 - 8m - 100 + 32 + n = 0$$

$$\Rightarrow n - 8m - 52 = 0 \quad \dots(1)$$

Also, $p(2) = 0$

$$\Rightarrow (2)^4 + m(2)^3 - 25(2)^2 - 16(2) + n = 0$$

$$\Rightarrow 16 + 8m - 100 - 32 + n = 0$$

$$\Rightarrow n + 8m - 116 = 0 \quad \dots(2)$$

From equation (1) and (2), we get

$$n - 8m - 52 = n + 8m - 116 \quad (\text{Each is } 0)$$

$$\Rightarrow -8m - 52 = 8m - 116$$

$$\Rightarrow 116 - 52 = 16m$$

$$\Rightarrow m = \frac{64}{16} = 4$$

Substituting the value of m in equation (1),

$$n - 8(4) - 52 = 0$$

$$\Rightarrow n - 32 - 52 = 0$$

$$\Rightarrow n - 84 = 0$$

$$\Rightarrow n = 84$$

Thus, the values of m and n are 4 and 84 respectively.

26. Applying angle sum property in ΔABC , we have

$$\angle ABC + \angle BCA + \angle BAC = 180^\circ$$

$$\Rightarrow 25^\circ + 134^\circ + \angle BAC = 180^\circ$$

$$\Rightarrow \angle BAC = 180^\circ - 159^\circ = 21^\circ$$

Now, AC is the bisector of $\angle BAD$.

$$\therefore \angle BAC = \angle CAD$$

$$\Rightarrow \angle 2 = 21^\circ \quad (\because \angle BAC = 21^\circ)$$

We know that the measure of one complete angle is 360° .

$$\therefore \angle BCD + \angle BCA + \angle ACD = 360^\circ$$

$$\Rightarrow 126^\circ + 134^\circ + \angle 3 = 360^\circ$$

$$\Rightarrow \angle 3 = 360^\circ - 260^\circ = 100^\circ$$

By exterior angle property of triangles, we have

$$\angle 1 = \angle 2 + \angle 3$$

$$\Rightarrow \angle 1 = 21^\circ + 100^\circ = 121^\circ$$

By applying angle sum property in ΔACD , we have:

$$\angle ACD + \angle CDA + \angle CAD = 180^\circ$$

$$\Rightarrow 100^\circ + \angle 4 + 21^\circ = 180^\circ$$

$$\Rightarrow \angle 4 = 180^\circ - 121^\circ = 59^\circ$$

27. Let the dimensions of the cuboid are x , $2x$ and $4x$.

$$\text{Hence, volume of cuboid} = x \times 2x \times 4x = 8x^3$$

Volume of cube = Volume of cuboid

$$\therefore \text{Volume of cube} = 8x^3 = \text{side}^3$$

$$\therefore \text{Side of cube} = 2x$$

$$\text{Total Surface Area of cuboid} = 2(lb + bh + hl) = 2(2x^2 + 8x^2 + 4x^2) = 28x^2$$

$$\text{Cost of polishing the cuboid} = \text{Rs. } 5 \times 28x^2 = 140x^2$$

$$\text{Total Surface Area of cube} = 6(\text{side})^2 = 6(2x)^2 = 24x^2$$

$$\text{Cost of polishing the cube} = \text{Rs. } 5 \times 24x^2 = 120x^2$$

The difference between cost of polishing the cube and the cuboid is Rs. 80.

$$\text{Hence, } 140x^2 - 120x^2 = 80$$

$$\Rightarrow 20x^2 = 80$$

$$\Rightarrow x^2 = 4$$

$$\Rightarrow x = 2$$

$$\text{Volume of cuboid} = \text{Volume of cube} = 8 \times (2)^3 \text{ m}^3 = 64 \text{ m}^3.$$

28. The sum of any two sides of a triangle is always greater than the third side.

$$\text{In } \triangle OXY, OX + OY > XY \dots(1)$$

$$\text{In } \triangle OYZ, OY + OZ > YZ \dots(2)$$

$$\text{In } \triangle OXZ, OX + OZ > XZ \dots(3)$$

Adding equations (1), (2) and (3),

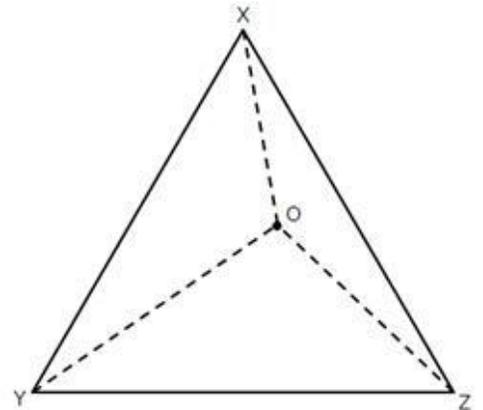
$$(OX + OY) + (OY + OZ) + (OX + OZ) > XY + YZ + ZX$$

$$2(OX + OY + OZ) > XY + YZ + ZX$$

$$OX + OY + OZ > \frac{1}{2} (XY + YZ + ZX)$$

$$OX + OY + OZ > \text{Semi-perimeter of } \triangle XYZ.$$

Hence, $(OX + OY + OZ)$ cannot be less than the semi-perimeter of $\triangle XYZ$.



29. Join DE.

$$\angle BAD = \angle EAC$$

$$\angle BAD + \angle DAC = \angle EAC + \angle DAC$$

$$\angle BAC = \angle DAE \dots\dots\dots (i)$$

In $\triangle ABC$ & $\triangle ADE$

$$AB = AD \text{ (Given)}$$

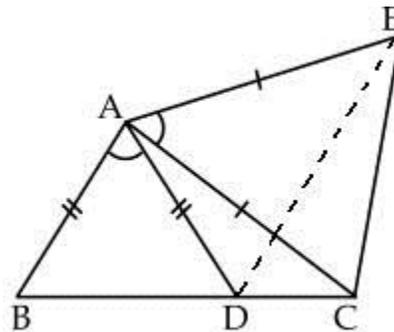
$$\angle BAC = \angle DAE \text{ (from (i))}$$

$$AC = AE$$

So, By SAS congruence criteria

$$\triangle ABC \cong \triangle ADE$$

$$BC = DE \text{ (CPCT)}$$



30.

$$m = \frac{1}{2-\sqrt{3}} \text{ and } n = \frac{1}{2+\sqrt{3}}$$

$$\therefore 7m^2 + 11mn - 7n^2$$

$$= 7 \times \left(\frac{1}{2-\sqrt{3}} \right)^2 + 11 \left(\frac{1}{2-\sqrt{3}} \right) \left(\frac{1}{2+\sqrt{3}} \right) - 7 \left(\frac{1}{2+\sqrt{3}} \right)^2$$

$$= \frac{7}{4+3-4\sqrt{3}} + \frac{11}{4-3} - \frac{7}{4+3+4\sqrt{3}}$$

$$= \frac{7}{7-4\sqrt{3}} + 11 - \frac{7}{7+4\sqrt{3}}$$

$$= \frac{7}{7-4\sqrt{3}} \times \frac{7+4\sqrt{3}}{7+4\sqrt{3}} + 11 - \frac{7}{7+4\sqrt{3}} \times \frac{7-4\sqrt{3}}{7-4\sqrt{3}}$$

$$= \frac{7(7+4\sqrt{3})}{(7)^2 - (4\sqrt{3})^2} + 11 - \frac{7(7-4\sqrt{3})}{(7)^2 - (4\sqrt{3})^2}$$

$$= \frac{7(7+4\sqrt{3})}{49-48} + 11 - \frac{7(7-4\sqrt{3})}{49-48}$$

$$= 49 + 28\sqrt{3} + 11 - 49 + 28\sqrt{3}$$

$$= 11 + 56\sqrt{3}$$