

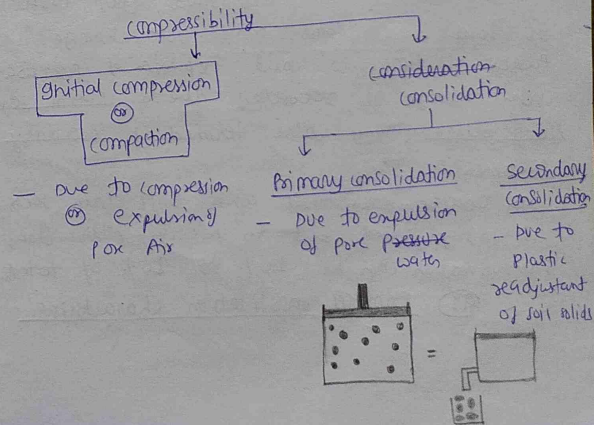
Lecture 8
12/11/18

CHAPTER-6

compressibility and consolidation

1) compressibility

- 1) It is the gradual $\downarrow$ in volume of soil due to application of load on soil mass and under consideration.



① Initial compression ② compaction :-

1) It is an instantaneous process which occurs immediately after loading and is due to compression and expulsion of pore air

② Primary consolidation

- 1) It begins when soil reaches to full saturation (after the completion of pore air) and remains saturated during entire process of primary consolidation.
- 2) It takes place due to expulsion of pore water and it completes when expulsion of pore water stop
- 3) It is time taking phenomenon. Rate of consolidation depend upon
 - ① permeability of soil
 - ② length of drainage path
 - ③ loading σ_v

③ Secondary consolidation (2°)

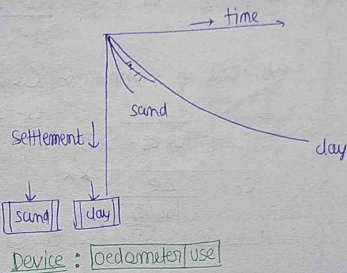
completion of
It start after 1° Primary consolidation.

It load is constant and vol^m change is recorded with passes of time, without expulsion of pore water then vol^m change is recorded due to Plastic readjustment of soil solids. It is also termed as Secondary consolidation settlement

In coarse grain soil and stiff clays secondary consolidation is insignificant but in highly plastic clay secondary consolidation can be 10% to 20% of total settlement.

②.1 Primary consolidation characteristic

②.2 Settlement V/s time

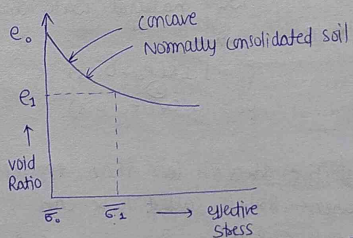


- The rate of consolidation in sand is more due to its high permeability but total settlement of clay is much greater than that of sand, at same loading rate & having same thickness of samples of both the soil
- This settlement of clay is higher beco^e of its high void ratio and porosity thus for practical purposes settlement of sand is neglected in comparison of clay.

②.3 Void Ratio V/s effective stress

(Normally consolidated soils and normal compression curve)

- Normally consolidated soils are those which are subjected to 1st time in the history to the present applied effective stress (Present > Past)



$$\text{slope of } e \text{ vs } \sigma_v = \frac{e_0 - e_1}{\sigma_{v0} - \sigma_{v1}}$$

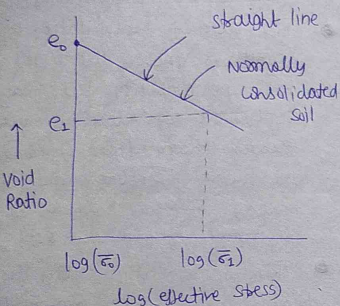
$$\text{① Coefficient of compressibility} \\ (a_v) = \left| \frac{e_0 - e_1}{\sigma_{v0} - \sigma_{v1}} \right|$$

$$a_v = \frac{\Delta e}{\Delta \sigma} \quad \text{--- ① formula}$$

Since a_v is not constant for whole curve, it is not widely used. But when we draw this curve in semi-log graph paper straight line is obtained

③ Void Ratio Vs log(effective stress)

Important



$$\text{Slope of } e \text{ vs } \log(\bar{\sigma}) = \frac{e_0 - e_1}{\log \bar{\sigma}_0 - \log \bar{\sigma}_1}$$

Coefficient of Compression (C_c)

$$= \left| \frac{e_0 - e_1}{\log \bar{\sigma}_0 - \log \bar{\sigma}_1} \right| = \frac{e_0 - e_1}{\log \bar{\sigma}_1 - \log \bar{\sigma}_0}$$

$$C_c = \frac{\Delta e}{\log \left(\frac{\bar{\sigma}_1}{\bar{\sigma}_0} \right)} \quad \text{--- (2)}$$

Empirical Relation of determination of C_c

1) For undisturbed soil (clay)

$$C_c = 0.009 (W_L - 10) \quad \text{--- (3)}$$

2) For Remoulded clay

$$C_c = 0.007 (W_L - 7)$$

W_L = liquid limit in %

3) for organic clay

$$C_c = 0.015 (W_n)$$

W_n = natural water content

4) When initial void ratio (e_0) is known

$$C_c = 1.15 (e_0 - 0.35)$$

$$C_c = 0.54 (e_0 - 0.3)$$

④ over consolidation stage /
Pre consolidation stage

1) If Presently applied effective stress is less than applied effective stress in the past when soil is called to be an over consolidation stage (Present < Past)

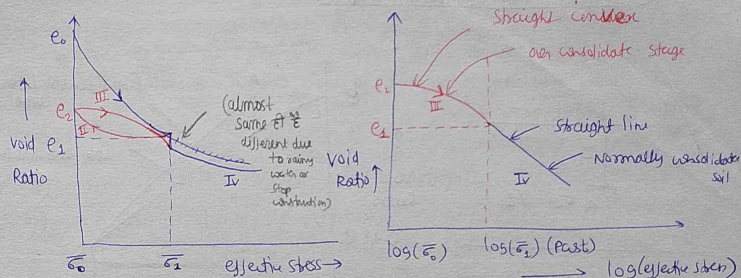
2) Over consolidated soils show less volume change and highly over consolidated clay behave like dense sand

① Normally consolidated stage (concave) ② virgin compression curve

③ Swelling / Rebound curve

④ over consolidation curve (convex)

⑤ Normally consolidated curve (concave)



Coefficient of Reconsolidation

$$\left\{ \text{Slope of } e \text{ vs } \log \bar{\sigma} \right\}_{\text{in overconsolidated soil stage}} = \left\{ \frac{e_2 - e_1}{\log \bar{\sigma}_2 - \log \bar{\sigma}_1} \right\}$$

$$= \left| \frac{e_2 - e_1}{\log \bar{\sigma}_2 - \log \bar{\sigma}_1} \right| = \frac{e_2 - e_1}{\log \bar{\sigma}_1 - \log \bar{\sigma}_2}$$

$$C_R = \frac{\Delta e}{\log \left(\frac{\bar{\sigma}_1}{\bar{\sigma}_2} \right)} \quad \text{--- (3)}$$

Generally,

$$C_R = \frac{1}{5} \text{ to } \frac{1}{10} \text{ of } C_c$$

* over consolidated Ratio

$$O.C.R. = \frac{\text{Maxm applied eff. stress in Past}}{\text{Maxm applied eff stress in Present}}$$

for o.c stage $O.C.R. > 1$

for N.C stage $O.C.R. = 1$

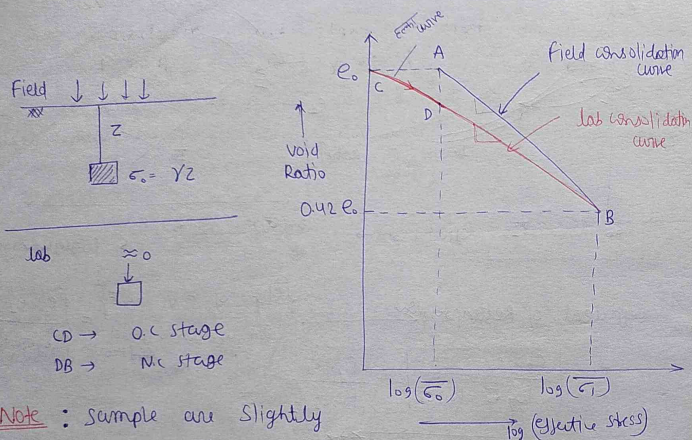
for under consolidated stage

$$O.C.R. < 1$$

Note

Melting of glaciers, Removal of construction load, Rising of water table, Dissipation of clay are some eg of over consolidation

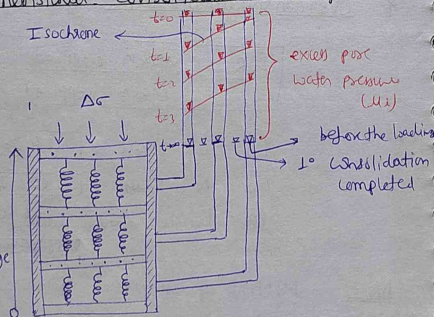
V) ⑤ Field consolidation curve



Note: Sample are slightly disturbed when these are taken out from the ground. the disturbance cause a slight decrease in the slope of laboratory consolidation curve

* Terzaghi's 1 dimensional consolidation theory

Spring analogy



1) Application of total stress

2) At $t=0$

(Excess pore water pressure developed) drainage path

$$\Delta \sigma = \Delta \sigma_v^0 + u_i$$

3) At any time (t) (Excess pore pressure decreases, eff stress $\uparrow$)

$$\Delta \sigma = \Delta \sigma_v^0 + u_i$$

4) At $t=\infty$ (Excess pore water pressure reduces to zero, 1st consolidation completed)

$$\Delta \sigma = \Delta \sigma_v^0 + u_i^0$$

- (Consolidation depends on effective stress not total stress)
- (Isochrone $\rightarrow$ different level of piezometric at same time)

Assumptions

- 1) Soil is Homogeneous and isotropic
- 2) Darcy's law is valid
- 3) The consolidation is 1 dimensional it means flow of seeping water is uni-directional (In vertical) and there is no change in areal volume change is due to change in depth only)
- 4) Soil is fully saturated and remains saturated throughout the process of consolidation it means initial compression is not considered, s
- 5) Strain coming on soil solids is small and negligible it means solids are incompressible Hence 2nd secondary consolidation is not considered
- 6) The hydrodynamic lag is considered whereas plastic lag is ignored. However plastic lag is found to exist it means time required for plastic readjustment of soil solids is neglected Hence secondary consolidation is not considered
- 7) Coefficient of consolidation and compressibility are constant

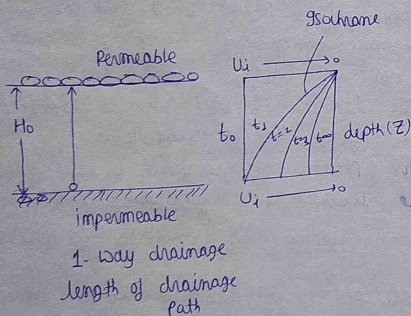
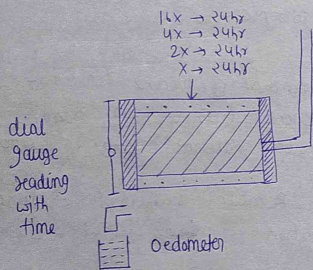
• In order to develop field cond in the lab consolidation test is being performed on soil mass in consolidometer

① oedometer there are two type of consolidometers

- ① Fixed Ring cell (Only top plate is allowed to move)
- ② Floating Ring cell (both top and bottom plate are allowed to move.)

* In consolidation test pressure on the soil specimen is doubled in each stage so that significant change in void ratio can be obtained in small time.

* In oedometer load increment ratio is 2



2-Way drainage
length of drainage path $d = \frac{H_0}{2}$

Note Isochrones are the curve which represents the time which pore water leaves at same time and at different depth.

Terzaghi's 1D consolidation Eqn

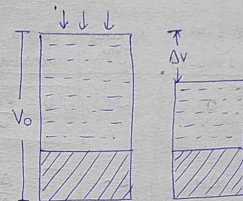
$$\frac{\partial v}{\partial t} = C_v \frac{\partial^2 v}{\partial z^2}$$

C_v = coefficient of consolidation

$$C_v = \frac{k}{m_v \gamma_w}$$

coefficient

k = coefficient of permeability
 m_v = coefficient of volm compressibility of modulus of volm change



$$m_v = \frac{-\Delta v}{V_0} = \frac{-\Delta e}{1+e_0} = \frac{-\Delta e}{\Delta e} \left(\frac{1}{1+e_0} \right)$$

$$m_v = \frac{q_v}{1+e_0} \quad \text{--- (5)}$$

C_v = Coeff. of compressibility
 e_0 = initial void ratio

coefficient	Symbol	formula	Unit
① Coefficient of Permeability	q_v	$q_v = \frac{\Delta e}{\Delta t}$	$\frac{m^2}{KN}$
② Coefficient of compressibility	C_c	$\frac{\Delta e}{\log \left(\frac{\sigma_1}{\sigma_0} \right)}$	—
③ Volume compressibility	C_R	$\frac{\Delta e}{\log \left(\frac{\sigma_1}{\sigma_0} \right)}$	—
④ Volm compressibility	m_v	$\frac{q_v}{1+e_0}$	$\frac{m^2}{KN}$
⑤ Consolidation	C_v	$\frac{k}{m_v \gamma_w}$	$\frac{m^2}{sec} = \frac{m^2}{KN \cdot m^3}$

Solution of terzaghi eqn

① Degree of consolidation (%)

- It is the fraction of ultimate consolidation which is completed at any time (t) during the consolidation
- It is defined only for primary consolidation.

- When excess pore pressure is known
- When settlement is known
- When void ratio is known

At $t=0$ ($\%U=0$)	At $t=\infty$ ($\%U=100$)	At any time t	Degree of consolidation
U_i	0	U	$\%U = \frac{U_i - U}{U_i} \times 100$
0	ΔH	Δh	$\%U = \frac{\Delta H - \Delta h}{\Delta H} \times 100$
e_0	e_{100}	e	$\%U = \frac{e_0 - e}{e_0 - e_{100}} \times 100$

② Time factor

gt is the Parameter which relates to the degree of consolidation and time required for that consolidation

$$T_v = \frac{C_v t}{d^2} \quad C_v = \text{coefficient of consolidation}$$

$$C_v = \frac{K}{m_v \gamma_w} = \frac{K}{\frac{q_v \gamma_w}{1+e_0}} = \frac{K}{\Delta e \frac{\gamma_w}{\Delta \sigma (1+e_0)}} = \frac{K \Delta \sigma}{\Delta e \gamma_w (1+e_0)}$$

$d \rightarrow$ length of drainage path

for 2way drainage

$$d = \frac{H_0}{2}$$

for 1way drainage

$$d = H_0$$

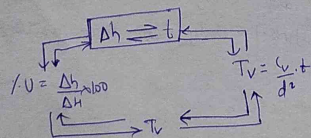
$t \rightarrow$ time at which time factor is required

$T_v =$ time factor

$$T_v = \frac{\pi}{4} U^2 = \frac{\pi}{4} \left(\frac{\%U}{100} \right)^2 \quad \%U \leq 60\%$$

$$T_v = 1.71 - 0.933 \log_{10} (100 - \%U) \quad \%U > 60\%$$

Rule



50% $U \rightarrow 2 \text{ year}$

$\%U$	50%	90%	100%	60%
T_v	0.196	0.848	∞	0.283

Note

theoretically 100% consolidation takes ∞ time but consolidation is assumed to be completed when $\%U \geq 90\%$.

Determination of C_v

1) C_v depends upon type of soil and loading consolidation generally, it has been observe that liquid limit $\uparrow$ ($v \downarrow$)

$w_L \uparrow \rightarrow$ compressibility $\uparrow \rightarrow q_v \uparrow \rightarrow m_v \uparrow \rightarrow C_v \downarrow$

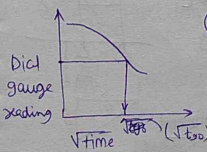
$$C_v = \frac{K}{m_v \gamma_w}$$

$$C_v \uparrow = 0.009 (w_L - 10)$$

There are two method to find C_v

(A) Square Root of the fitting Method

Given by Taylor $\%U = 90\%$



$$(T_v)_{90} = \frac{C_v t}{d^2}$$

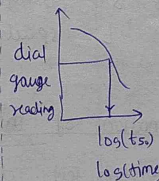
$$0.848 = \frac{C_v t_{90}}{d^2}$$

$$C_v = 0.848 \times \frac{d^2}{t_{90}}$$

* Square root of time fitting Method is better

(B) logarithmic of time fitting method

Given by Casagrande $\%U = 50\%$



$$(T_v)_{50} = \frac{C_v t}{d^2}$$

$$0.196 = \frac{C_v t_{50}}{d^2}$$

$$C_v = \frac{0.196 d^2}{t_{50}}$$

Settlement analysis

① total settlement is the sum of initial/immediate settlement, Primary consolidation settlement and secondary consolidation settlement.

$$S = S_i + S_c + S_s$$

IS CODE GUIDELINES :

1) Total Permissible settlement

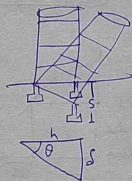
	For steel structure	For R.C.C. structure (mm)
for isolated footing on sand	50	50
for isolated footing on clay	50	75
for Raft footing on sand	75	75
for Raft footing on clay	100	100

2) Permissible Angular settlement

	For steel structure	For R.C.C. structure
for isolated footing	1/300	1/500
for Raft footing	1/300	1/600

3) Permissible differential settlement (s)

$s =$ angular settlement $\times L$
 $L =$ spacing b/w the footing



Not imp

Determination of Initial / immediate settlement

cone penetration test data can be used to determine the initial settlement due to expulsion of pore air.

$$S_i = \frac{H_0 \bar{\sigma}_0}{1.5 q_c} \log \left(\frac{\bar{\sigma}_0 + \Delta \bar{\sigma}}{\bar{\sigma}_0} \right)$$

$q_c =$ Static cone penetration resistance

$H_0 =$ thickness of compressible layers

$\bar{\sigma}_0 =$ Initial of stress at C/C of compressible layers

$\Delta \bar{\sigma} =$ change in " " " " " "

③ Elastic settlement Important

Small elastic settlement can occur due to squeezing of soil particles निचोड़ना

$$S_i = \frac{q B (1 - \mu^2) I_f}{E_s} \quad **$$

$q =$ uniform pressure on the footing

$B =$ width of footing

$\mu =$ Poisson's ratio of soil (0.35 to 0.5)

$E_s =$ Young's modulus of soil.

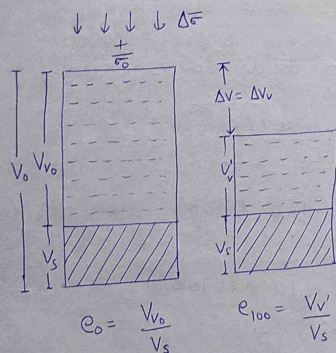
$I_f =$ influence factor $\odot$ shape factor which depends upon type of soil

Flexible footing

	centre	corner	avg	Rigid footing
① Circular	1.00	0.64	0.85	0.8
② square	1.12	0.56	0.95	0.82
③ Rectangular	1.3			
④ $\frac{L}{B} = 1.5$	1.36	0.68	1.20	1.09
$\frac{L}{B} = 2$	1.52	0.76	1.31	1.22

Determination of Primary consolidation settlement

A) When change in void ratio is known



$$\Rightarrow \frac{\Delta V}{V_0} = \frac{\Delta H \cdot B^2}{H_0 \cdot B^2} = \frac{\Delta H}{H_0} \quad \text{--- (A)}$$

{ Terzaghi's 1-D consolidation

$$\Rightarrow \frac{\Delta V}{V_0} = \frac{\Delta V_v}{V_0 + V_s} = \frac{\Delta V_v}{V_s \left[1 + \frac{V_{v0}}{V_s} \right]}$$

$$= \frac{\Delta V_v}{V_s} \cdot \frac{1}{1 + \frac{V_{v0}}{V_s}}$$

$$\frac{\Delta V}{V_0} = \frac{\Delta e}{1 + e_0} \quad \text{--- (B)}$$

from (A) and (B) $\left\{ \begin{array}{l} \therefore \frac{\Delta V_v}{V_s} = \Delta e \\ \therefore \frac{V_{v0}}{V_s} = e_0 \end{array} \right.$

$$\frac{\Delta H}{H_0} = \frac{\Delta e}{1 + e_0} \quad \text{--- (1)}$$

ΔH = Ultimate consolidation settlement

H_0 = Initial thickness of compressible layer

$\Delta e = e_0 - e_{100}$ = change in void ratio

e_0 = initial void ratio

(B) When coefficient of vol^m compressibility (m_v) is known

$$\frac{\Delta H}{H_0} = \frac{\Delta e}{1 + e_0} = \frac{\Delta e}{1 + e_0} \cdot \frac{\Delta \bar{\sigma}}{\Delta \bar{\sigma}} = \left(\frac{\Delta e}{\Delta \bar{\sigma}} \right) \cdot \frac{\Delta \bar{\sigma}}{1 + e_0} = \left(\frac{q_v}{1 + e_0} \right) \Delta \bar{\sigma} = m_v \Delta \bar{\sigma}$$

$$\Delta H = H_0 m_v \Delta \bar{\sigma} \quad \text{--- (2)}$$

(C) When coefficient of compression (C_c) is known

$$\frac{\Delta H}{H_0} = \frac{\Delta e}{1 + e_0} = \frac{\Delta e}{1 + e_0} \cdot \frac{\log \left(\frac{\bar{\sigma}_1}{\bar{\sigma}_0} \right)}{\log \left(\frac{\bar{\sigma}_1}{\bar{\sigma}_0} \right)} = \left(\frac{\Delta e}{\log \left(\frac{\bar{\sigma}_1}{\bar{\sigma}_0} \right)} \right) \cdot \frac{\log \left(\frac{\bar{\sigma}_1}{\bar{\sigma}_0} \right)}{1 + e_0} = \frac{C_c}{1 + e_0} \log \left(\frac{\bar{\sigma}_1}{\bar{\sigma}_0} \right)$$

$$\Delta H = \frac{H_0 C_c}{1 + e_0} \log \left(\frac{\bar{\sigma}_1}{\bar{\sigma}_0} \right)$$

$$\Delta H = \frac{H_0 C_c}{1 + e_0} \log \left(\frac{\bar{\sigma}_0 + \Delta \bar{\sigma}}{\bar{\sigma}_0} \right)$$

Note ①

If soil is in N.C stage $\rightarrow$ use C_c

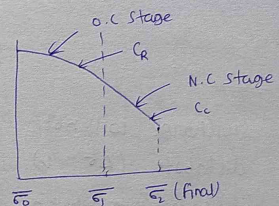
If soil is in o.c stage $\rightarrow$ use C_r

1) Past ($\bar{\sigma}_1$)

2) Present ($\bar{\sigma}_0$)

3) change ($\Delta \bar{\sigma}$)

4) final ($\bar{\sigma}_1$)



$$\Delta H = \frac{H_0 C_r}{1 + e_0} \log \left(\frac{\bar{\sigma}_1}{\bar{\sigma}_0} \right) + \frac{H_0 C_c}{1 + e_0} \log \left(\frac{\bar{\sigma}_1}{\bar{\sigma}_0} \right)$$

Very important

Note ②

four step method

Step ① H_0

Step ② $\bar{\sigma}_0$ at CLC of compressible layer

Step ③ load distribution 1:n

$$\Delta \bar{\sigma} = \frac{q(B+L)}{(B+2nz)(L+2nz)}$$

$$\frac{q}{(B+2nz)(L+2nz)}$$

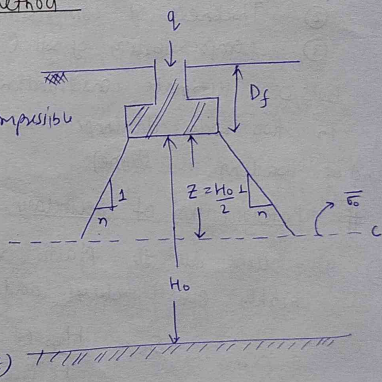
$$\frac{q}{(B+2nz)(L+2nz)}$$

load = force area
force = load area
= q(B+L)

NOT

if load distribution is not given then assume

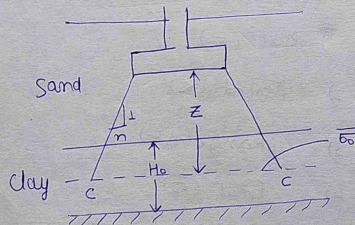
$\Delta V : \Delta H$



Step ④ Ultimate consolidation settlement

$$\Delta H = \frac{H_0 C_c}{1+e_0} \log \left(\frac{\bar{\sigma}_0 + \Delta \bar{\sigma}}{\bar{\sigma}_0} \right)$$

Note ③ Determine settlement of clay layer



Note ④

surcharge will not distribute ($\Delta \bar{\sigma} = q$)
(surcharge will distribute in large area)

Note ⑤ Ultimate consolidation settlement depends upon

- ① change in effective stress
- ② Thickness of compressible layer
- ③ compressibility of soil (q_v, m_v, C_c)

Note ⑥ Ultimate consolidation settlement will be same in two way drainage and one way drainage (if soil and loading is same)

Determination of secondary consolidation

- ① It occurs due to plastic rearrangement of soil solid in highly plastic clays and in organic clays

(Not too much imp)

$$S_s = \frac{H_{100} C_s}{1+e_{100}} \log \left(\frac{t}{t_{100}} \right)$$

C_s = secondary compressive index it is the slope of e vs $\log(\text{time})$ curve after primary consolidation obtained from laboratory

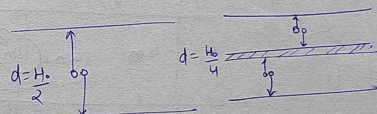
H_{100} = thickness after primary consolidation

e_{100} = Void ratio after primary consolidation

t_{100} = time required for primary consolidation approximately (90%) (t_{90})

t = time at which secondary consolidation is required.

⑥ solution Page ③7



$$T_v = \left(c_v \cdot \frac{t}{d^2} \right)$$

$$\frac{T_v}{c_v} = \frac{t}{d^2} = \text{constant}$$

$$\frac{q}{\left(\frac{H_0}{2} \right)^2} = \frac{t_1}{\left(\frac{H_0}{4} \right)^2}, \quad t_1 = \frac{9}{4} \text{ year} + 2 \text{ years 3 months}$$

W.B ④7 Page ④3

I# 60% $\rightarrow$ 1 year ($d = H_0$) 1 way

II# 39% $\rightarrow$ 6K, 3H₀ ($d = \frac{3H_0}{2}$) 2 way

$$\text{I\#} \quad T_v = \frac{c_v t}{d^2} = \frac{K}{m_v \alpha_v d^2} = \frac{K}{\alpha_v \cdot \gamma_w \cdot (H_0)^2} \cdot \frac{12 \text{ years}}{1+e_0}$$

$$\text{II\#} \quad T_v = \frac{612 \cdot t}{39 \gamma_w \cdot \left(\frac{3H_0}{2} \right)^2}$$

% U same $\rightarrow$ (T_v - same)

$$(t = 135 \text{ year})$$

Solution (48) Page (43)

Four step method

Step 1

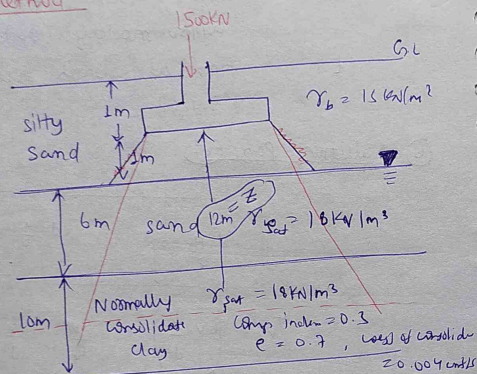
$$H_0 = 10m$$

Step 2

$$\bar{\sigma}_0 = \sigma - U$$

$$= (2 \times 1 + 6 \times 2 + 5 \times 2) - 11 \times 0$$

$$= 2 \times (15) + 6 \times (18) + 5 \times 18 - 11 \times 0 = 118$$

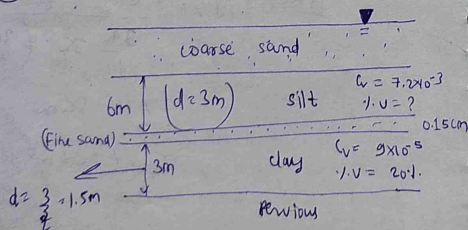


$$\text{Step 3 } \Delta \bar{\sigma} = \frac{\text{force}}{\text{area}} = \frac{Q}{\frac{\pi}{4} (D+2mz)^2} = \frac{1500 kN}{\frac{\pi}{4} (3+2 \times \frac{1}{2} \times 2)^2}$$

$$\Delta \bar{\sigma} = 8.48$$

$$\text{Step 4 } \Delta H = \frac{H_0 C_c}{1+e_0} \log \left(\frac{\bar{\sigma}_0 + \Delta \bar{\sigma}}{\bar{\sigma}_0} \right) = \frac{10 \times 0.3}{1+0.7} \log \left(\frac{118 + 8.48}{118} \right) = 0.0538m = 53.8mm$$

Solution (31) Page (41)



$$\text{1) } 1.0 \leq 60\%$$

$$\text{For clay } T_v = \frac{\pi}{4} \left(\frac{U}{100} \right)^2 = \frac{\pi}{4} \left(\frac{60}{100} \right)^2 = 0.282$$

$$T_v = \frac{C_v \times t}{d^2}$$

$$0.282 \times (d)^2 = \frac{9 \times 10^{-3} \times 7.2 \times 10^3 \times t}{7.2 \times 10^3 \times t}$$

$$0.282 (1.5)^2 = \frac{9 \times 10^{-3}}{7.2 \times 10^3} t$$

$$t =$$

For silt

$$T_v = \frac{C_v t}{d^2} = \frac{7.2 \times 10^{-3}}{(3m)^2} \times \left(\frac{\pi}{4} \frac{(0.2)^2}{5 \times 10^{-5}} \times (1.5)^2 \right)$$

$$T_v = 0.628$$

$$(> 60\% \Rightarrow (T_v)_{60} = 0.283)$$

$$T_v = 1.781 - 0.933 \log_{10} (100 - 1.0) = 0.68$$

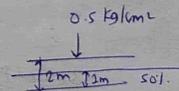
$$\text{doubt } 1.0 = 82.73\%$$

Solution (9) Page (39)

logic

Solution (40)

$$K = 3mm/year$$



$$(T_v)_s = \frac{C_v t}{d^2} = \frac{K}{m_v \gamma_w} \frac{t}{d^2}$$

$$0.196 = \frac{3mm \times 10^{-3}m \times 1.45}{m_v \times 9.81 \frac{kN}{m^3} \times (1m)^2}$$

$$m_v = 1.56 \times 10^{-3} m^2/kN$$

$$\Delta H = H_0 m_v \Delta F$$

$$= 2 \times 1.56 \times 10^{-3} \times 49.05 = 0.1535 = 15.35mm$$

After 1 years $\%U = \frac{\Delta h}{\Delta H} \times 100 = 50\%$

$\Delta h = \frac{\Delta H}{2} = \frac{153.5}{2} = 76.6 \text{ mm}$

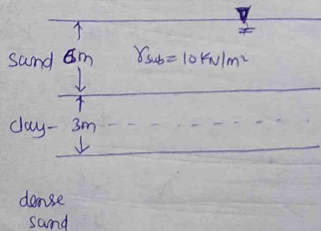
Solution (29)

Compression index

$= 0.35$

$w = 40\%$

$G_c = 2.7$



Step ④

$H_0 = 3\text{m}$

Step ① $\bar{\sigma} = \sigma - U$

$= 50 - \frac{1.5 \times 20}{10} + 6 \times 18 - 7.5 \times 10$

$= 30 + 6 \times (10) - 7.5 \times (10)$

$= 30 + 60 - 75$

$= 90 - 75 = 15 \text{ kN/m}^2$

$= 3 \times (18) + 6 \times 18 - 7.5 \times 10$

$\bar{\sigma}_0 = 1.5 \times (10) + 6 \times (10) = 75 \text{ kN/m}^2$

$\Delta H = \frac{H_0 C_c}{1 + e_0} \log \left(\frac{\bar{\sigma} + \Delta \bar{\sigma}}{\bar{\sigma}_0} \right)$

$= \frac{3 \times 0.35}{1 + 0.9} \log \left(\frac{72.01 + 120}{72.01} \right)$

$= 0.2149 \text{ m}$

$21.49 \text{ cm} \approx 22 \text{ cm}$

③ In 2 months $\rightarrow 4.4 \text{ cm}$

$\%U = \frac{\Delta h}{\Delta H} \times 100 = \frac{4.4}{22} \times 100 = 20\%$

$(T_v)_{20} = \frac{\Delta v^2}{4} = \frac{C_v \cdot t}{d^2}$

$\frac{\Delta v^2}{4} (0.2)^2 = \left(\frac{C_v}{d^2} \right) \cdot 2 \text{ months}$

for soil consolidation

$(T_v)_{10} = \frac{C_v \cdot t}{d^2}$

$0.196 = \frac{\Delta v^2}{4} \frac{(0.2)^2}{(2 \text{ months})} \times t$

$t = 12.5 \text{ months}$

$e = \frac{w}{S}$

$= \frac{0.4 \times 2.2}{1}$

$= 1.08$

$\gamma' = \frac{K - 1}{1 + e} \gamma_w$

$= 8.9 \text{ kN/m}^3$

Solution (51)

$C_r = 0.05$

$H_0 = 3\text{m}$

$\bar{\sigma}_1 = 60 \text{ kPa}$

$w = 25\%$

Percent ($\bar{\sigma}_0$)

$= 0.5 \times \gamma_{\text{sat}}$

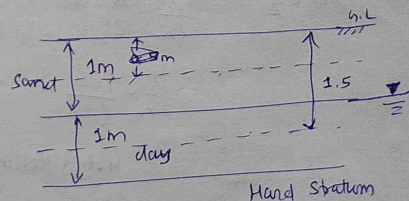
$+ 1 \times \gamma_{\text{bur}} - 1.5 \times \gamma_w$

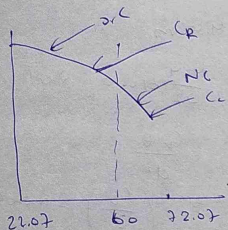
$= 0.5 \times (20.15) + 17 - 0.5 \times (10)$

$= 22.07 \text{ kN/m}^2$

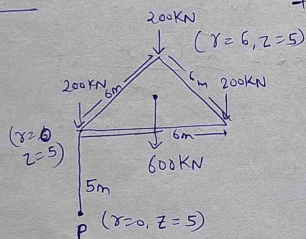
③ change ($\Delta \bar{\sigma}$) = $2.5 \times 20 = 50 \text{ kPa}$

④ final ($\bar{\sigma}_2$) = $\bar{\sigma}_0 + \Delta \bar{\sigma} = 22.07 + 50 = 72.07$





$$\begin{aligned}\Delta H &= \frac{H_0(R)}{1+e_0} \log\left(\frac{\sigma}{\sigma_0}\right) \\ &+ \frac{H_0(C_c)}{1+e_0} \log\left(\frac{\sigma_v}{\sigma_v'}\right) \\ &= \frac{1 \times 0.05}{1+0.675} \log\left(\frac{60}{21.07}\right) \\ &+ \frac{1.05}{1+0.675} \log\left(\frac{72.07}{60}\right) \\ &= 0.0367 \text{ m} \\ &= 36.7 \text{ mm}\end{aligned}$$



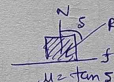
$$\begin{aligned}\sigma_z &= \frac{3}{2\pi} \cdot \frac{Q}{z^2} + 2 \times \frac{3}{2\pi} \left(\frac{1}{1+\frac{z^2}{r^2}} \right)^{\frac{3}{2}} \cdot \frac{Q}{z^2} \\ &= \frac{3}{2\pi} \times \frac{200}{(5)^2} + 2 \times \frac{3}{2\pi} \left(\frac{1}{1+\left(\frac{6}{5}\right)^2} \right)^{\frac{3}{2}} \cdot \left(\frac{200}{5^2} \right) \\ &= 4.64 \text{ kN/m}^2\end{aligned}$$

CHAPTER-8

Shear strength of soil

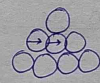
SSS of a resistance offered by the soil grain against shear deformation. Soil may derive its shear strength from following parameters

- ① Friction b/w Particle of sliding and rolling (sand, gravel, silt)
- ② Interlocking b/w Particles (Gravel and dense sand)
- ③ Intermolecular attraction due to cohesion and adhesion (silt and clay)



$$\begin{aligned}f &= \mu N \\ &= \sigma_v \tan \phi\end{aligned}$$

friction



Interlocking